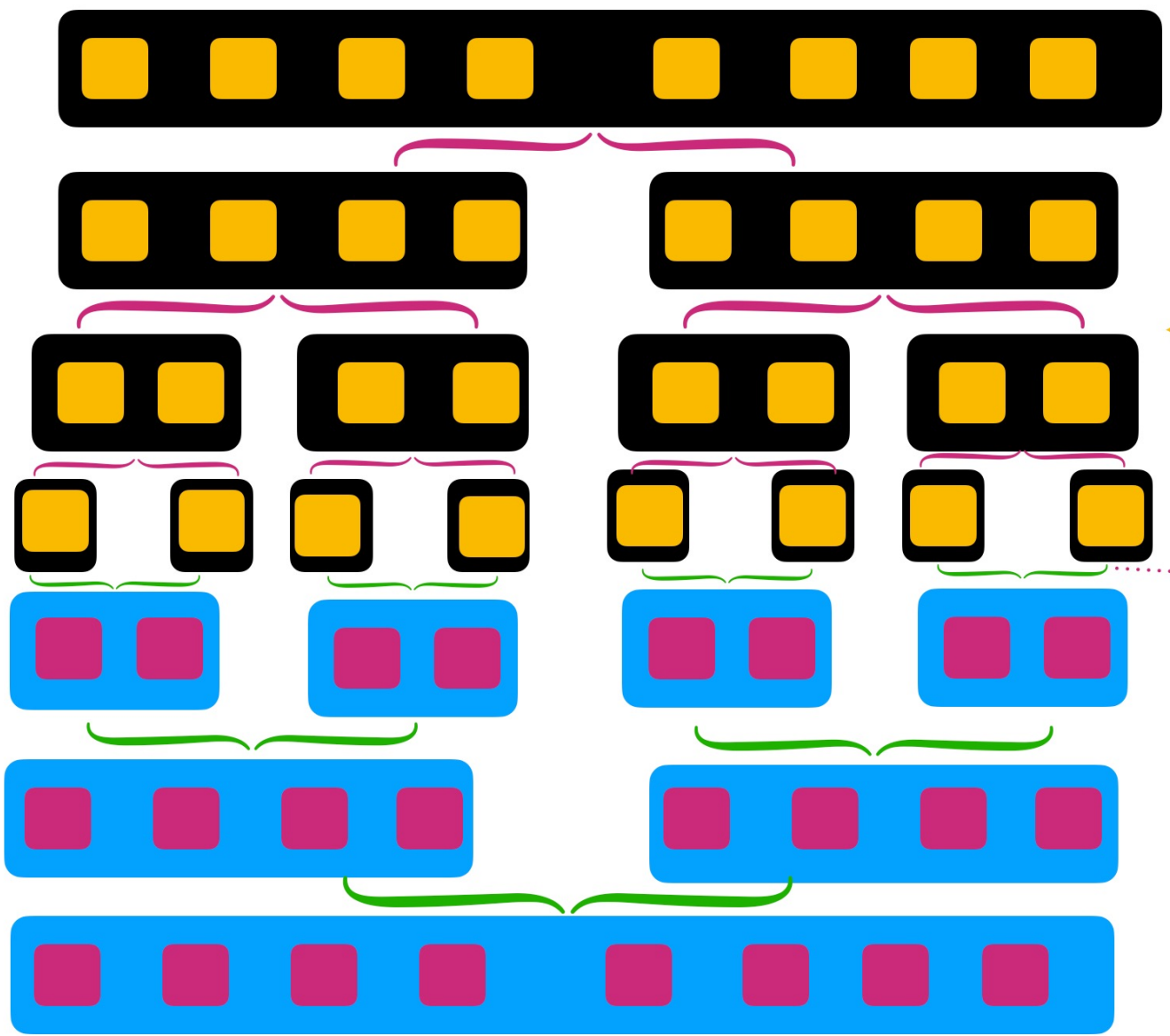


Merge Sort uses divide and conquer pattern.

Merge sort divides the problem into possible small problems then applies sorting recursively.

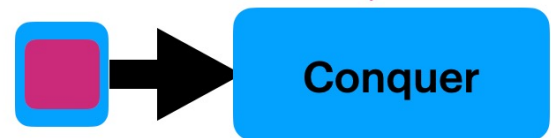
Divide => divides source collection into possible $n/2$ sub problems recursively.

Conquer=> Applies the sorting at subproblem level (compare, swap & merge) then repeats recursively.



Divide=> Break up the problem into smallest possible sub problems.

Compare, Swap & Merge

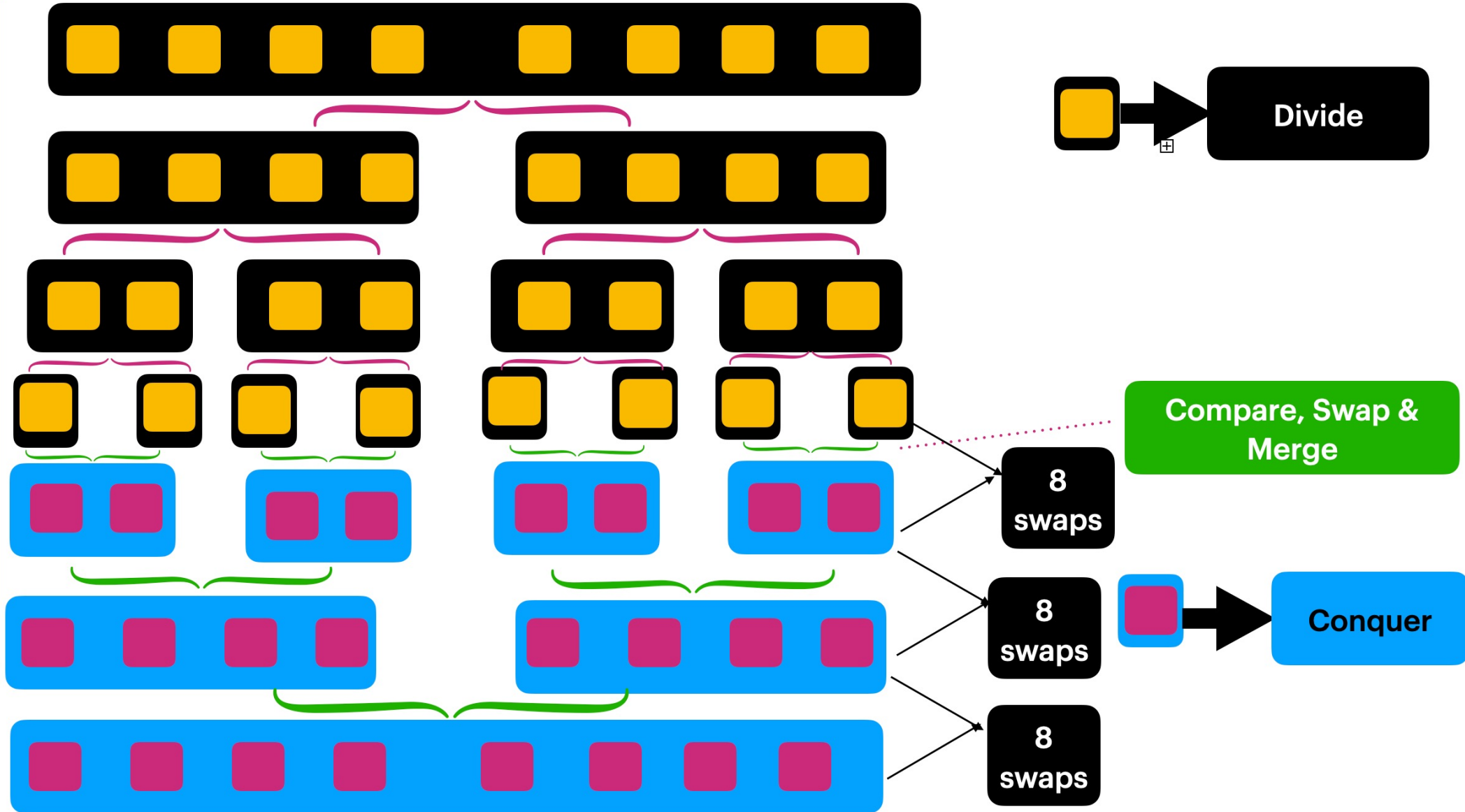


Conquer=> Figure out the solution for the smallest sub problem, then apply the same technique to solve larger problems recursively .

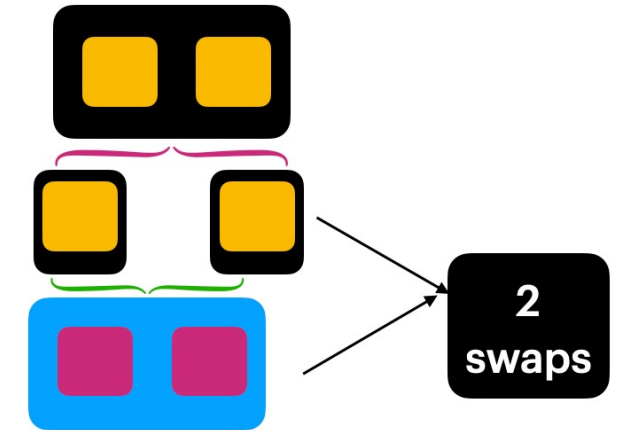
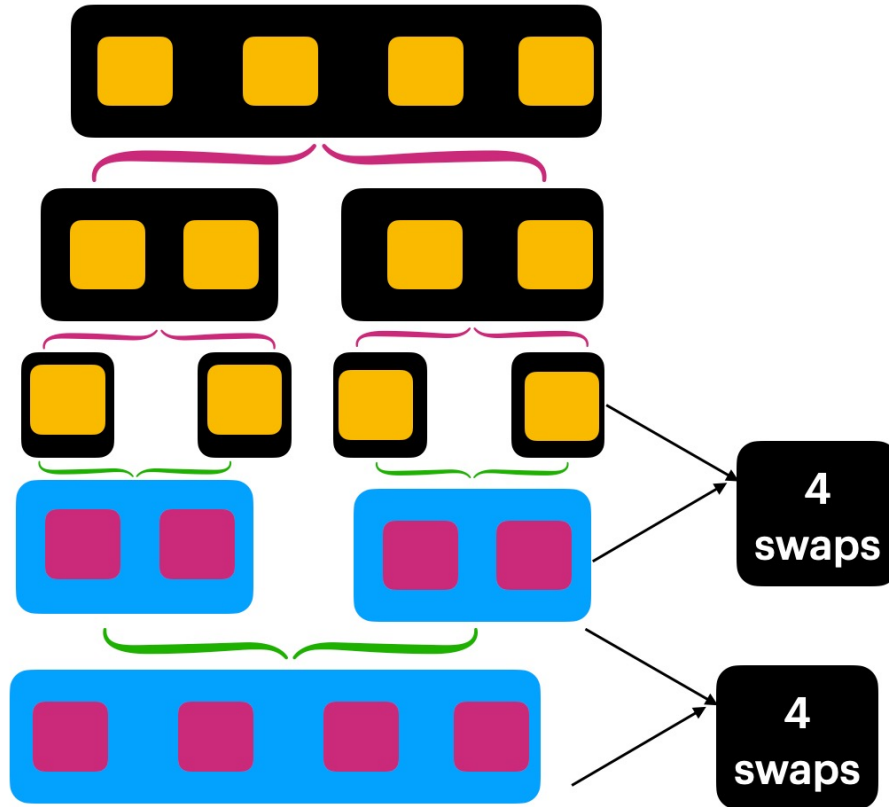
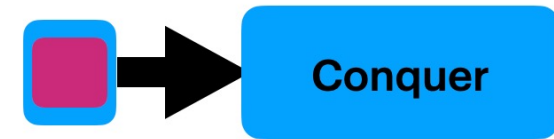
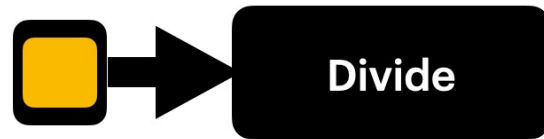
Let's figure out the Time Complexity.

For a merge sort the complex operations happens while swapping (Conquer logic).

Let's find out solution for time complexity by considering swap count.



Merge Sort taken 24 swaps If the size of the array is 8.
 $\text{SizeOf}(8) \Rightarrow 8\text{swaps in } 3\text{steps} = 8 \times 3 = 24 \text{ swaps}$



For SizeOf(2) $\Rightarrow 2 \times 1$
 $= 2$ swaps

Merge Sort taken 8 swaps If the size of the array is 4.
SizeOf(4) $\Rightarrow 4$ swaps in 2steps $= 4 \times 2 = 8$ swaps

MergeSort :

For Size Of (2) = 2 swaps $\Rightarrow 2 * 1 = 2 * \log_2^1$

For Size Of (4) = 8 swaps $\Rightarrow 4 * 2 = 4 * \log_2^2$

For Size Of (8) = 24 swaps $\Rightarrow 8 * 3 = 8 * \log_2^3$

Finally for a Merge Sort we can derive a time complexity as $n \log n$.

Time Complexity = $O(n \log n)$

Space Complexity = $O(n)$

Recursive / Non Recursive = Recursive

Stability = Stable

{4,1,4,3}

{4,1} {4,3}

{4} {1} {4} {3}

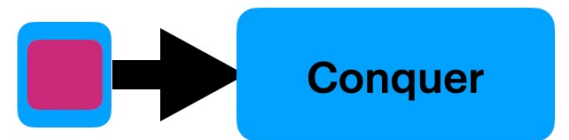
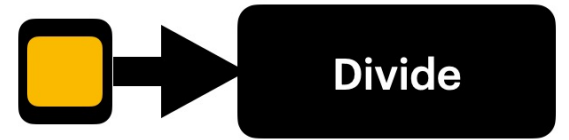
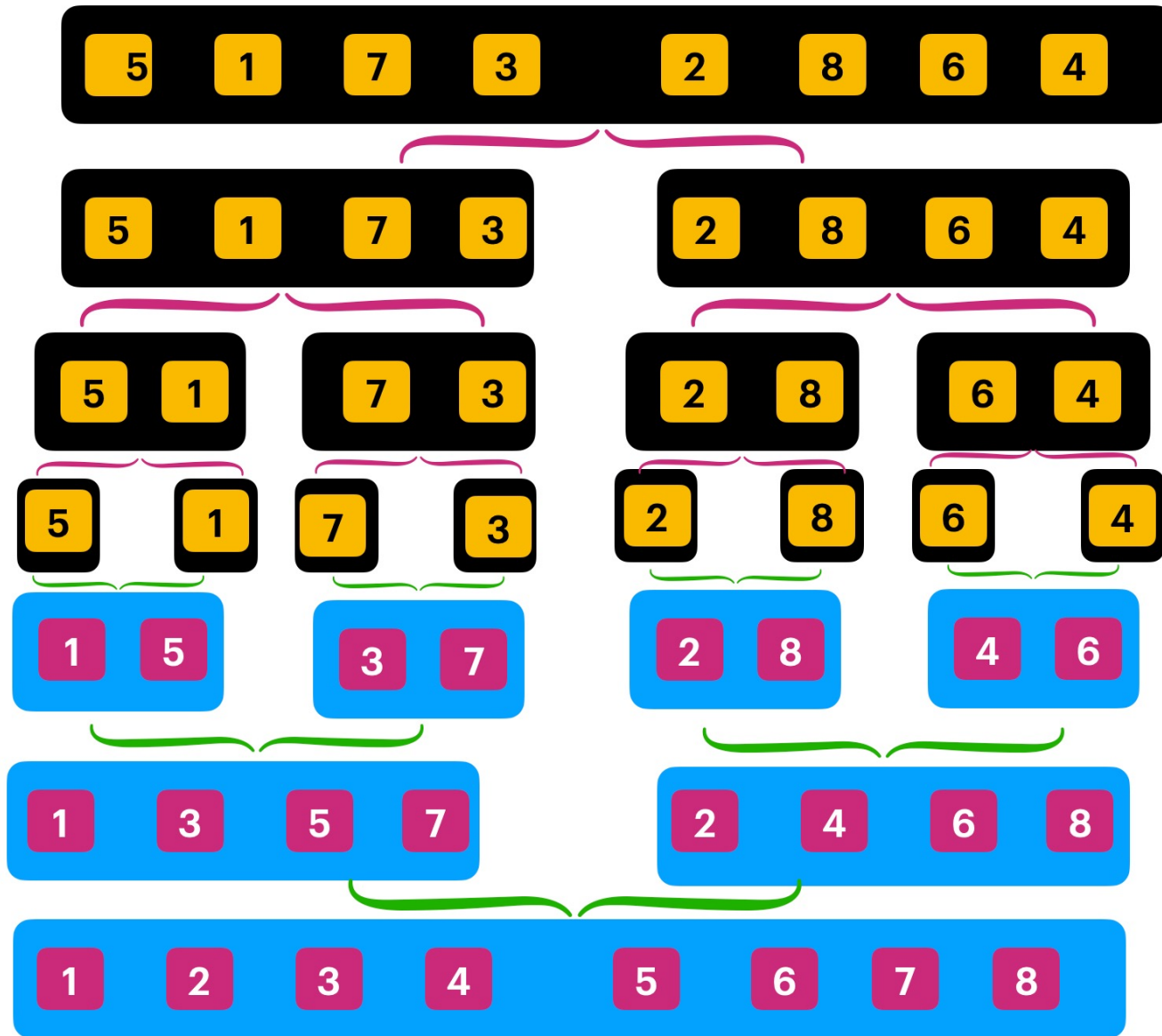
{1,4} {3,4}

{1,3,4,4}

Internal / External Sort = Can be used for both.

Comparison Sort = Yes

Swap = $O(n \log n)$



First we apply divide and conquer on left array then on right array recursively.

This occurs recursively
So that at any given point in time the number of active StackFrame count is $\log n$

The flow is based on StepNumber please observe .



mergeSort(arr)

divide(arr) $n = 4$
{5,1,7,3}

Step6 : leftArr output {1,5}
rightArr output {3,7}
Here conquer at $n=4$
final output {1,3,5,7}

Step4 : As divide of leftArr & rightArr completed we do the conquer .i.e {1,5}

divide(leftArr) $n = 2$
{5,1}

divide(righter) $n = 2$
{7,3}

Step5 : now recursion start at rightArr. Process is exactly same,
(follow leftArr recursion)
final output {3,7}

divide(leftArr)
{5} $n=1$

divide(rightArr)
) $n=1$ {1}

Step1 : StackFrame
Count : 1

Represents divide logic

Represent conquer logic

divide(leftArr)
r) $n=1$

Step2 : $n == 1$ this
stackframe will terminate

divide(rightArr)
rr) $n=1$

Step3 : As $n == 1$ this
stackframe will terminate

Finally About Merge Sort :

Merge Sort follows the divide & conquer pattern. Which divides array into possible sub problems then do the conquering .

As the merge sort does the sorting using Out-Place algorithm it takes $O(n)$ Space complexity.

MergeSort is good for External Sorting.

Time Complexity = $O(n \log n)$

Space Complexity = $O(n)$

Recursive / Non Recursive = Recursive

Stability = Stable

$\{4, 1, 4, 3\}$
 $\{4, 1\} \quad \{4, 3\}$
 $\{4\} \{1\} \quad \{4\} \{3\}$
 $\{1, 4\} \{3, 4\}$
 $\{1, 3, 4, 4\}$

Internal / External Sort = Can be used for both.

Comparison Sort = Yes

Swap = $O(n \log n)$