



## Memoization (Top-down)

Is the subproblem  
solved earlier?

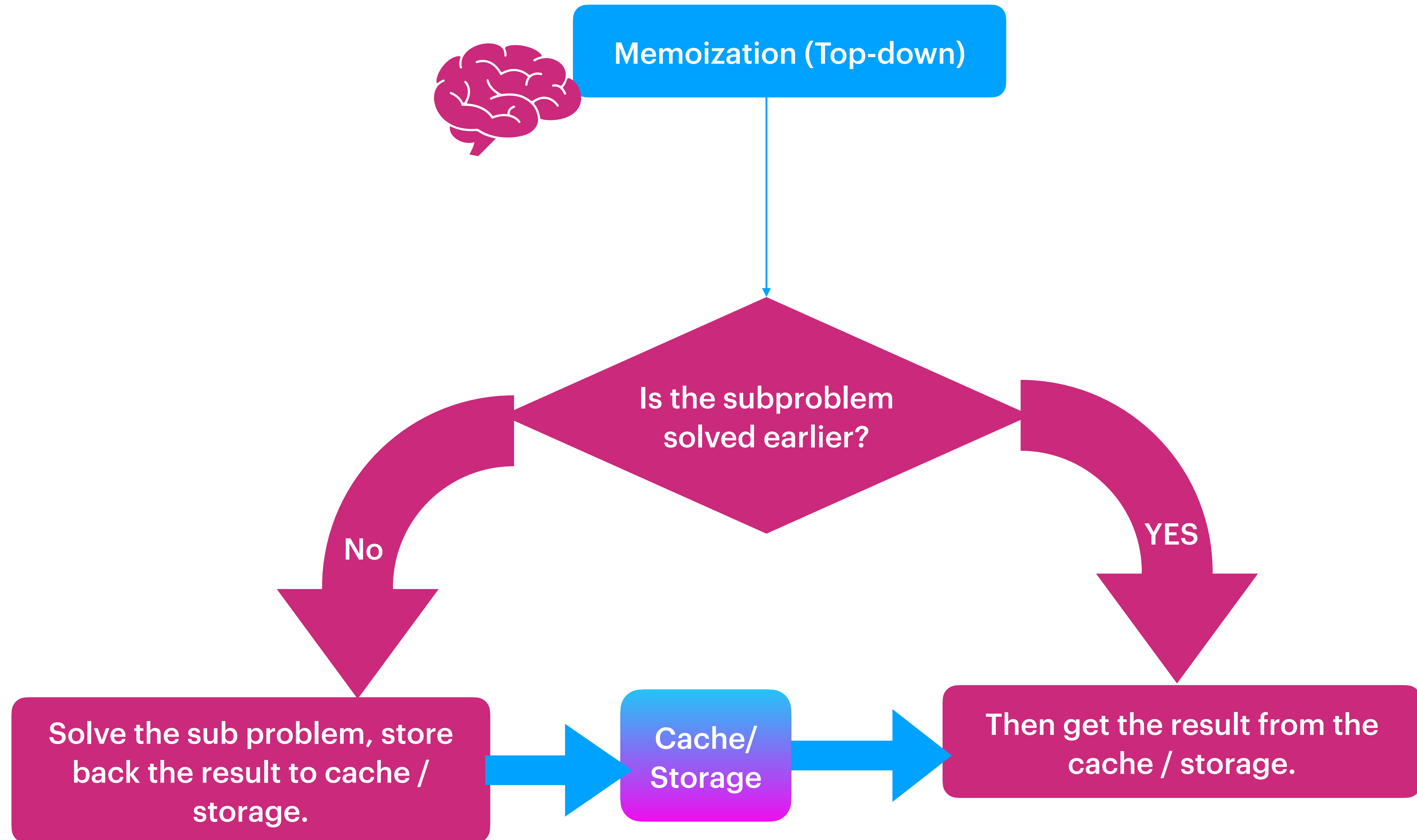
No

YES

Solve the sub problem, store  
back the result to cache /  
storage.

Cache/  
Storage

Then get the result from the  
cache / storage.





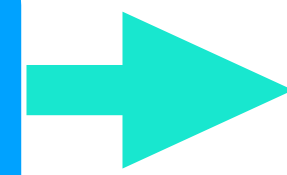
## Memoization (Top-down)

How to identify  
the sub problems for caching  
/ storing?

Have a proper knowledge on the data structure design, observe what are the parameters are being changed & encouraging us to move to all possible sub problems.

Hint : In simple what ever parameters we use in base condition of recursion, can be used to identify the caching / storing.

Memoization (Top-down)



0/1 Knapsack Problems

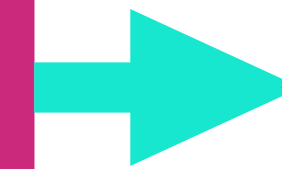


For the 0/1 Knapsack problems, there are two parameters, can encourage us to move forward with possible sub problems.

1. currentIndex (moving from index 0 to n-1)
2. capacity (Moving from capacity value "c" to 0)



So finally we can have a storage/caching on these two variable for all possible combinations.



All possible combinations?  
How ?

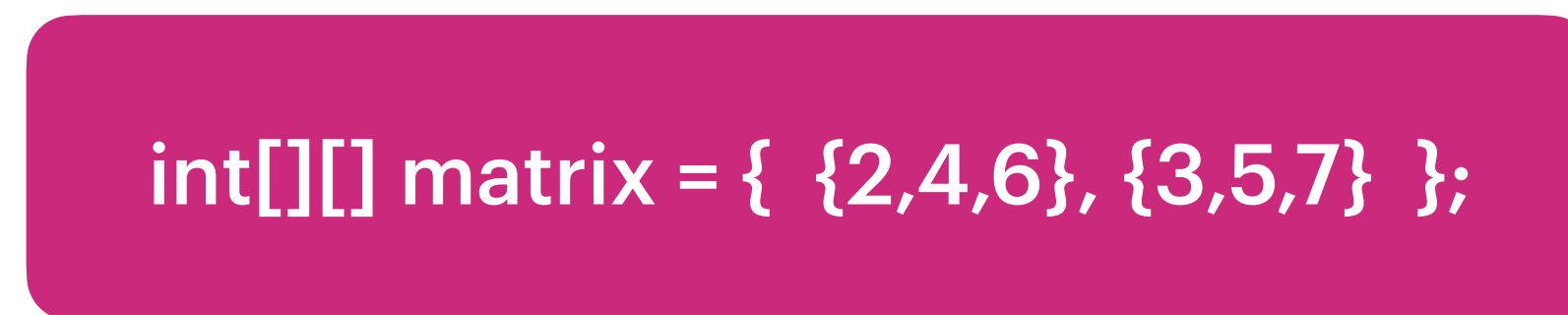
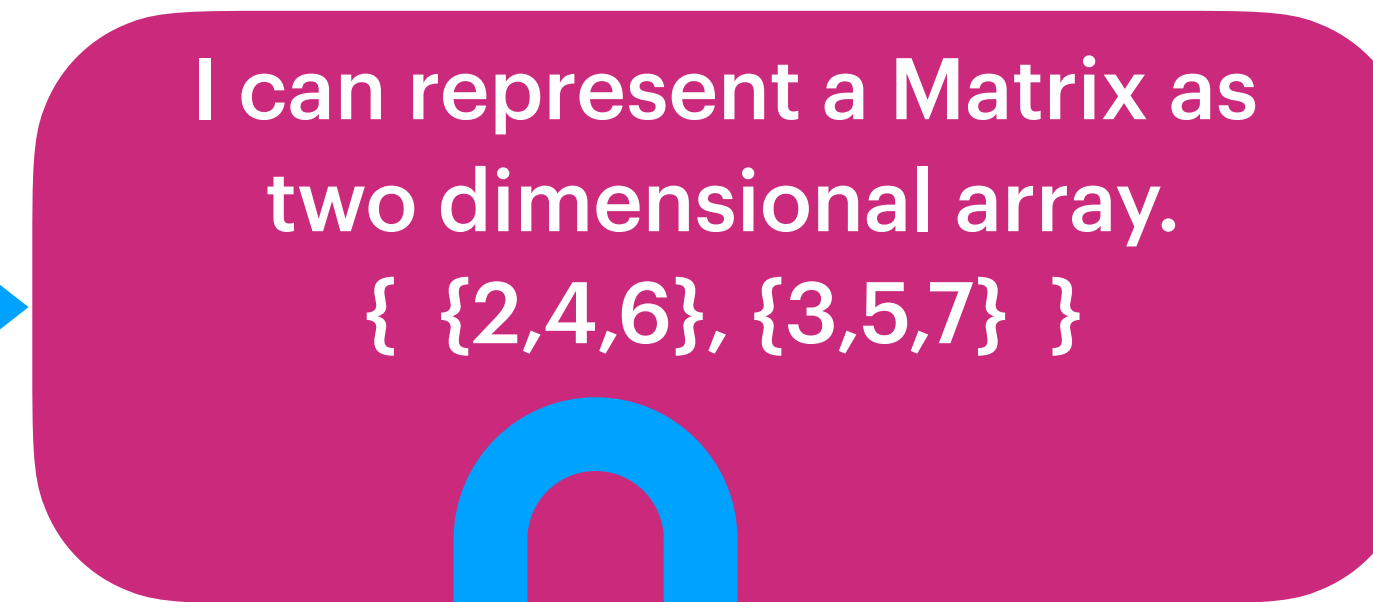
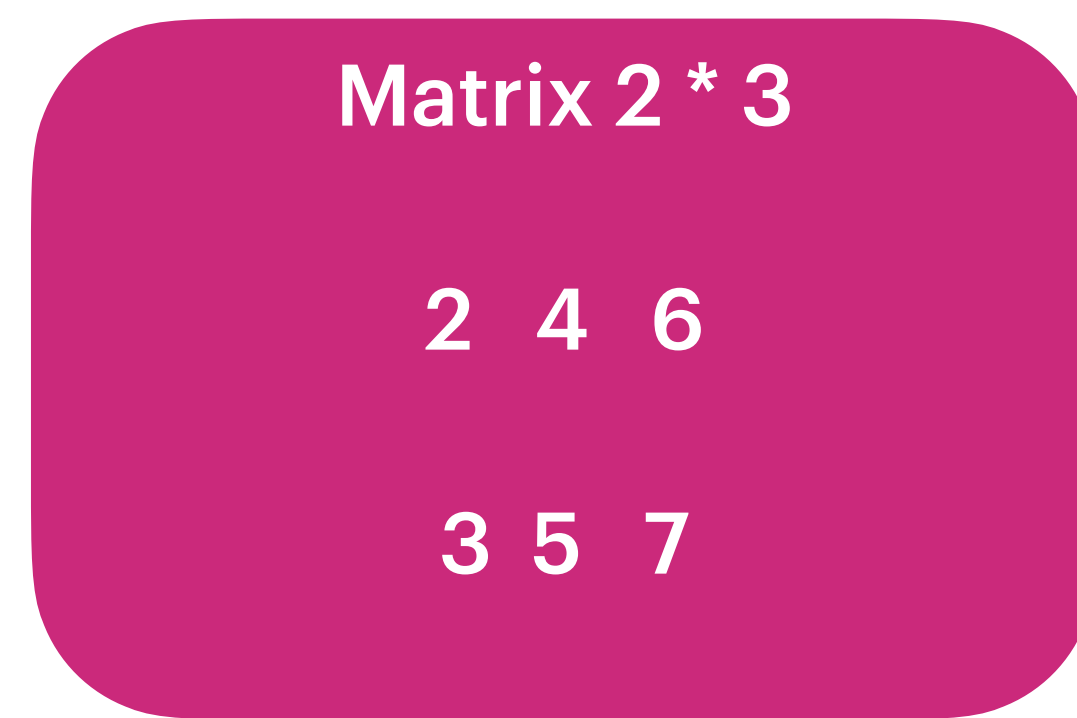


We can represent a matrix with two dimensional array.



Matrix is the place where we can design all possible combinations.





matrix

index

0

arr1  
addr

2

index

0

4

1

6

2

arr2  
addr

1

index

0

3

1

5

2

7

matrix[0] => arr1addr  
matrix[1] => arr2addr

matrix[0][0] = arr1addr[0] = 2  
matrix[0][1] = arr1addr[1] = 4

matrix[1][0] = arr2addr[0] = 3  
matrix[1][1] = arr2addr[1] = 5

# Algorithm For 0/1 Knapsack Memoization

design a matrix with  
currentIndex and  
capacity.

Base Condition in Recursion :

1. As we are moving from index 0 to n, the max possible valid value for currentIndex = n-1
2. As and when we add item to the knapsack, we reduce the capacity so the smallest possible value for capacity is '0'.

```
int[][] dp = new int[n][capacity+1];
```

Which is  
representing  
currentIndex.  
Index starts  
from 0 to n-1

Should be capacity+1  
as would like to have a  
combination storage on  
index & capacity .

Check in matrix, does this  
combination of (index, capacity) sub  
problem is already been solved?

YES

Just return the result from  
the matrix.

No

Current  
Item  
Weight

When currentItem weight is less  
than or equals to capacity.  
 $\text{weights}[\text{currentIndex}] \leq \text{capacity}$

When currentItem weight is greater  
than capacity.  
 $\text{weights}[\text{currentIndex}] > \text{capacity}$

Find profit1 with including item.  
Find profit2 without including item.  
Return max of profit1, profit2

Find profit without including item.  
return the profit.

Solve the sub  
problem for the  
current  
combination of  
index & capacity.  
Store back the  
result to Matrix.