COMP 9517 Computer Vision

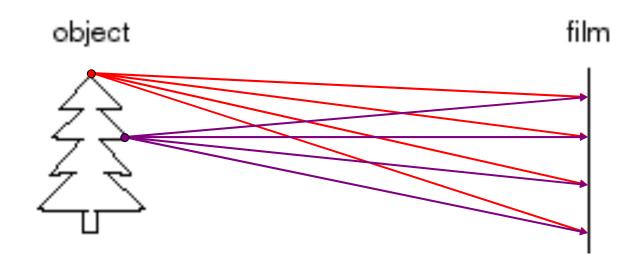
Image Formation

Geometry of Image Formation

Mapping between image and world coordinates

- Pinhole camera model
- Projective geometry
 - Vanishing points and lines
- Projection matrix

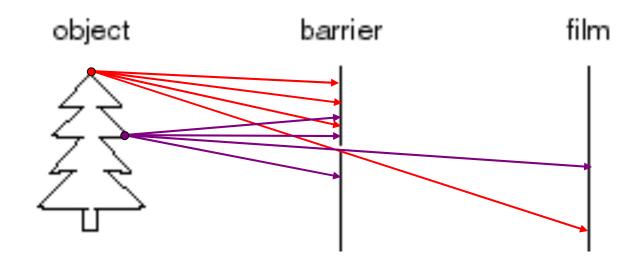
Image formation



Let us design a camera

- Idea 1: put a piece of film in front of an object
- Do we get a reasonable image?

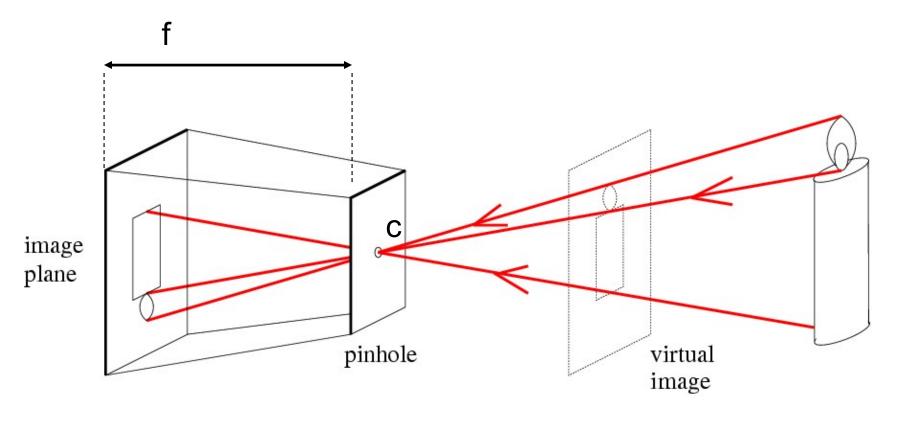
Pinhole camera



Idea 2: add a barrier to block off most of the rays

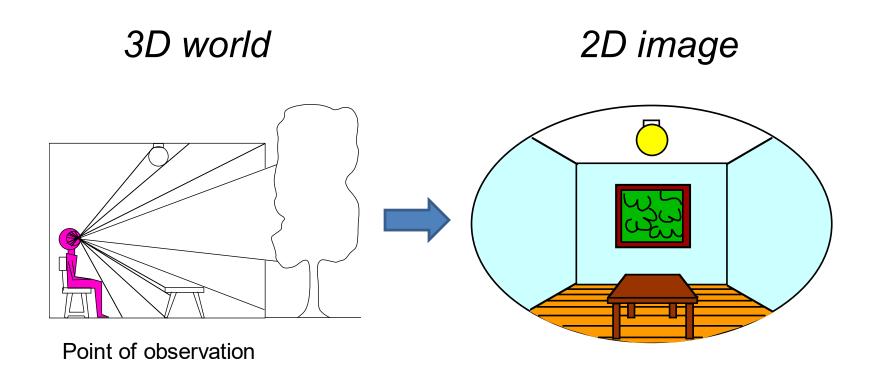
- This reduces blurring
- The opening known as the aperture

Pinhole camera



f = focal length
c = centre of the camera

Dimensionality Reduction Machine (3D to 2D)



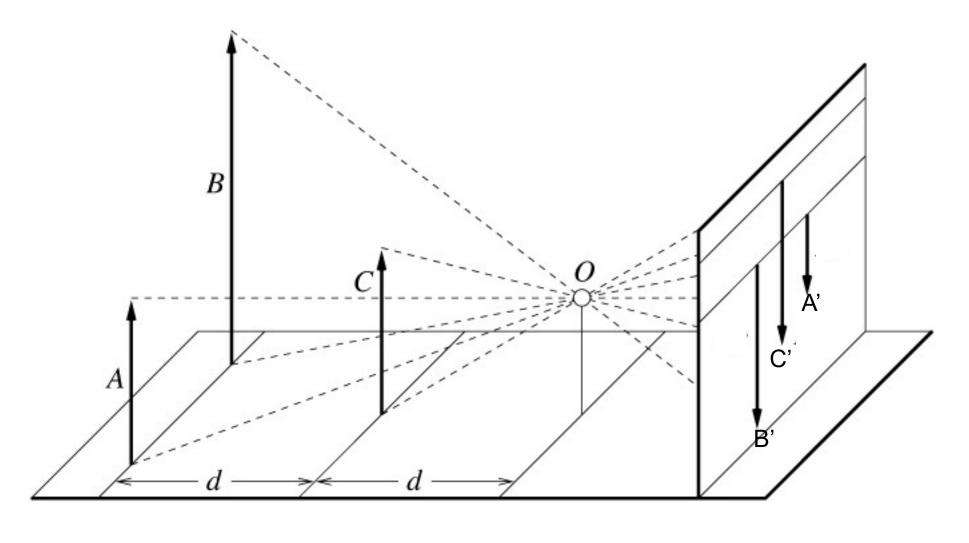
Projection can be tricky...



Projection can be tricky...



Length and area are not preserved



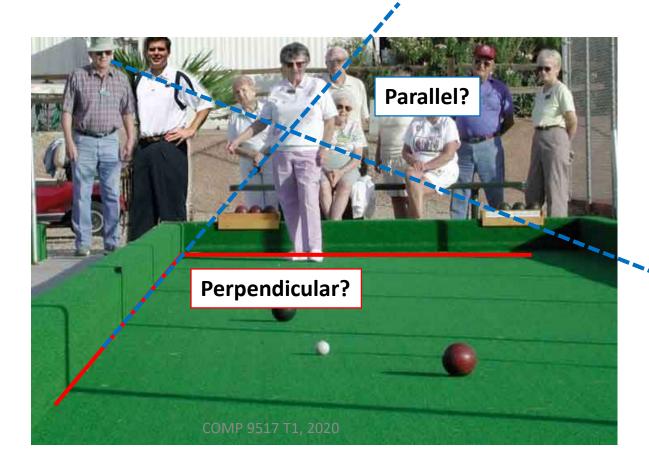
19/02/2020 COMP 9517 T1, 2020 9
Figure by David Forsyth

Projective Geometry

What is lost?

Length

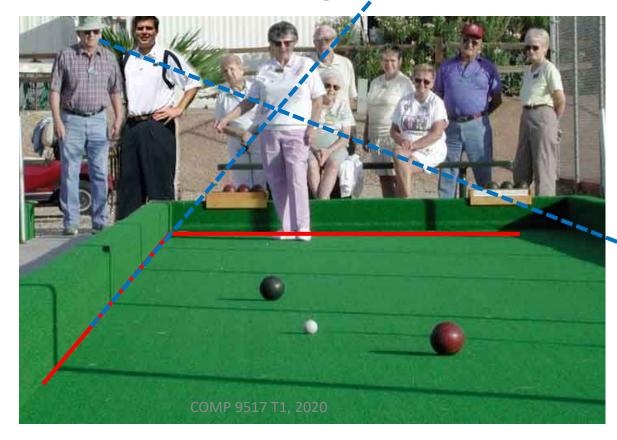
Angles



Projective Geometry

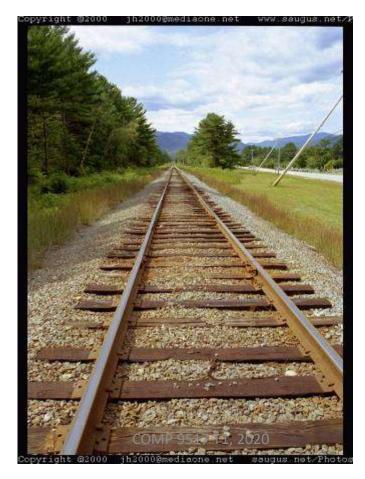
What is preserved?

Straight lines are still straight,

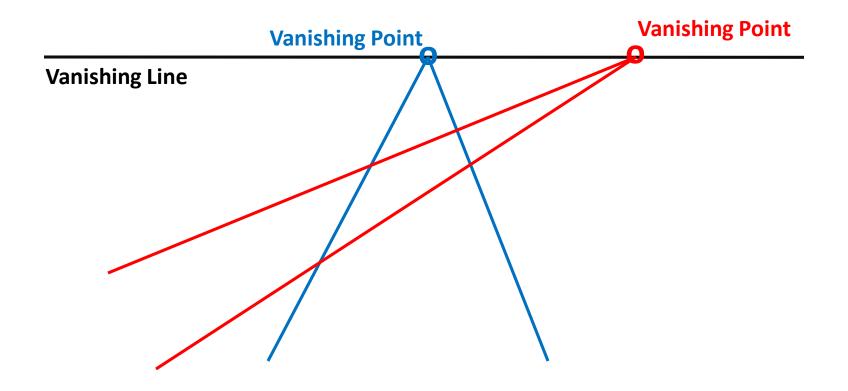


Vanishing points and lines

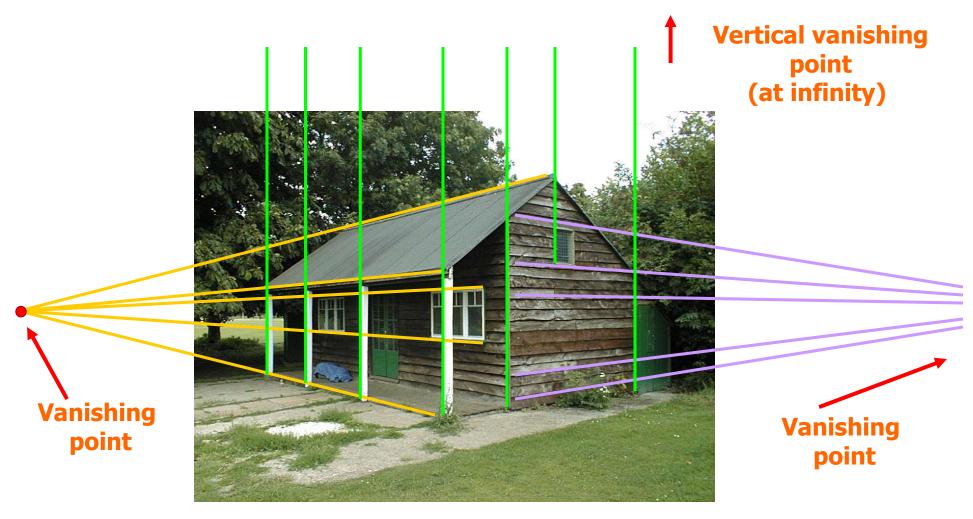
Parallel lines in the world intersect in the image at a "vanishing point"



Vanishing points and lines

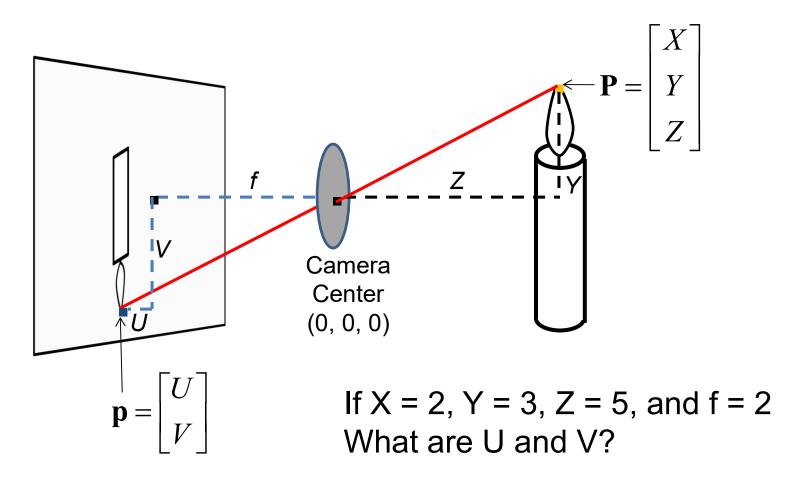


Vanishing points and lines

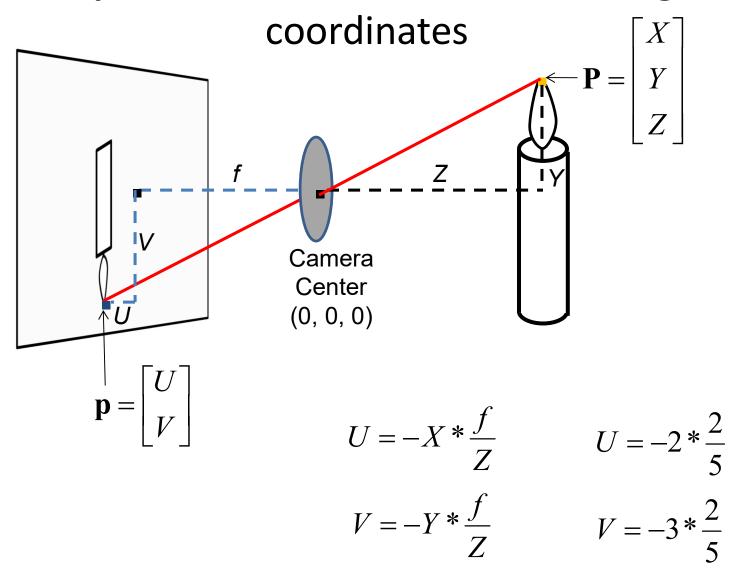


19/02/2020 COMP 9517 T1, 2020 14

Projection: world coordinates \rightarrow image coordinates



Projection: world coordinates -> image



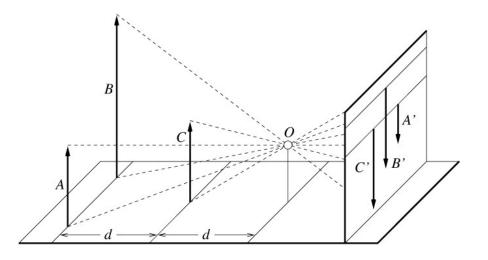
Perspective Projection

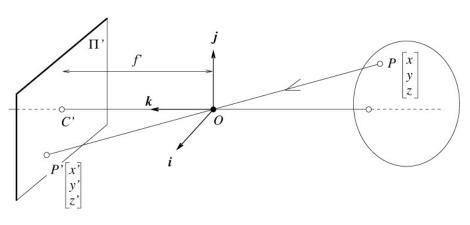
- Apparent size of object depends on its distance: far objects appear smaller
- By similar triangles

$$(x', y', z') \rightarrow (f\frac{x}{z}, f\frac{y}{z}, -f)$$

 Ignore the third coordinate, and get

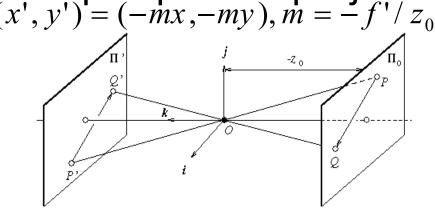
$$(x', y') \rightarrow (f\frac{x}{z}, f\frac{y}{z})$$





Affine Projection

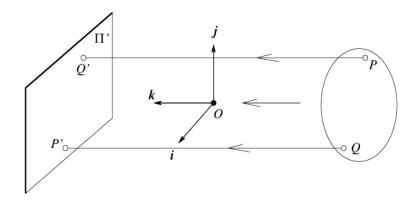
- Suitable when scene depth is small relative to the average distance from the camera
- Let magnification $m = -f'/z_0$ be positive constant, since z_0 is negative, i.e. treat all points in the scene as at constant distance from camera
- Leads to weak perspective projection $(x', y') = (-mx, -my), m = -f'/z_0$



Affine Projection-ctd

- Camera always remains at roughly constant distance from the scene
- Orthographic projection when m normalised to -1

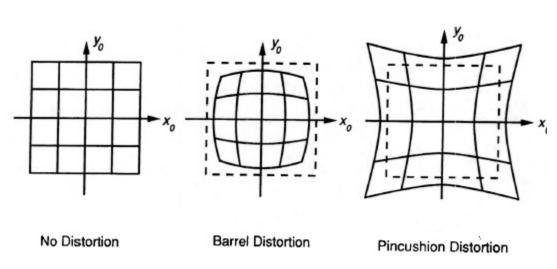
$$(x', y') = (x, y), m = -1$$



Other Projections

- Scaled orthographic projection
 - special case of perspective projection
 - Object dimensions are small compared to distance to camera

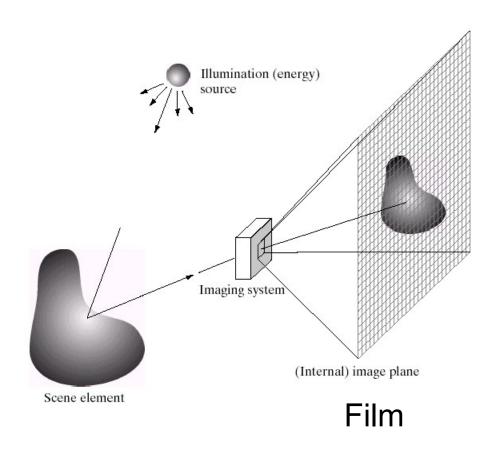
Beyond Pinholes: Radial Distortion

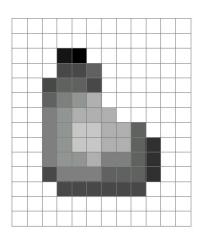




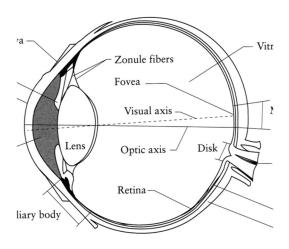
Corrected Barrel Distortion

Image Formation





Digital Camera

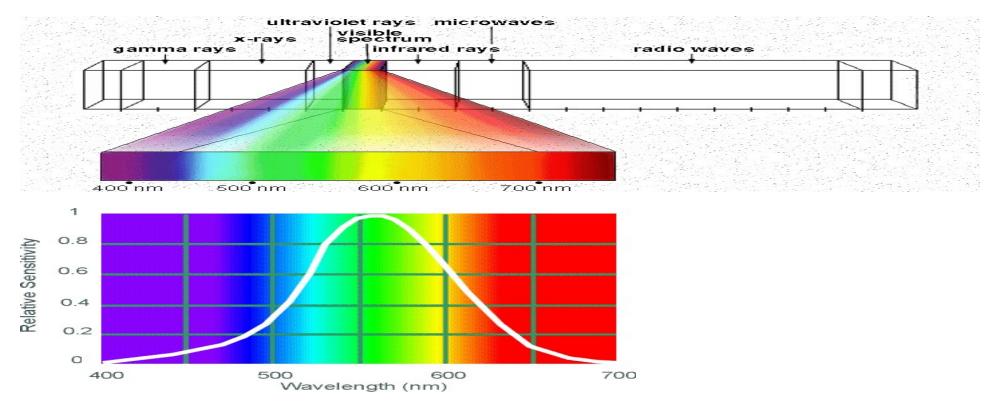


The Eye

Why do we care about human vision?

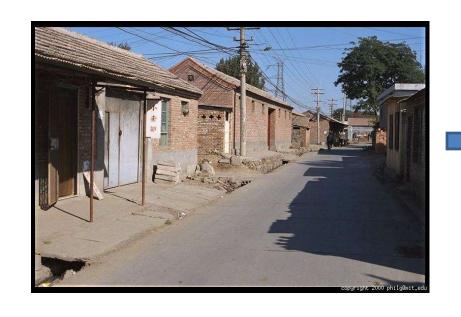
- Cameras necessarily imitate the frequency response of the human eye, so we should know that much.
- Computer vision probably would not get as much attention if biological vision (especially human vision) had not proved that it was possible to make important judgements from 2D images.

Electromagnetic Spectrum



Human Luminance Sensitivity Function

Colour Image





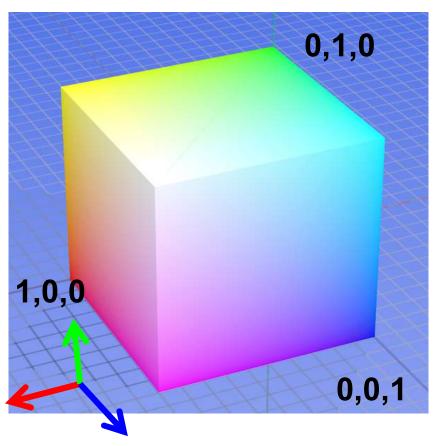
Images represented as a matrix

		col	um	n -									\Rightarrow				
ro	W	0.92	0.93	0.94	0.97	0.62	0.37	0.85	0.97	0.93	0.92	0.99	R				
		0.95	0.89	0.82	0.89	0.56	0.31	0.75	0.92	0.81	0.95	0.91					
		0.89	0.72	0.51	0.55	0.51	0.42	0.57	0.41	0.49	0.91	0.92	0.92	0.99	ı G		
		0.96	0.95	0.88	0.94	0.56	0.46	0.91	0.87	0.90	0.97	0.95	0.95	0.91			
		0.71	0.81	0.81	0.87	0.57	0.37	0.80	0.88	0.89	0.79	0.85	0.91	0.92			B
		0.49	0.62	0.60	0.58	0.50	0.60	0.58	0.50	0.61	0.45	0.33	0.97	0.95	0.92	0.99	
		0.86	0.84	0.74	0.58	0.51	0.39	0.73	0.92	0.91	0.49	0.74	0.79	0.85	0.95	0.91	
		0.96	0.67	0.54	0.85	0.48	0.37	0.88	0.90	0.94	0.82	0.93	0.45	0.33	0.91	0.92	
		0.69	0.49	0.56	0.66	0.43	0.42	0.77	0.73	0.71	0.90	0.99	0.49	0.74	0.97	0.95	
		0.79	0.73	0.90	0.67	0.33	0.61	0.69	0.79	0.73	0.93	0.97	0.82	0.93	0.79	0.85	
		0.91	0.94	0.89	0.49	0.41	0.78	0.78	0.77	0.89	0.99	0.93	0.90	0.99	0.45	0.33	
				0.79	0.73	0.90	0.67	0.33	0.61	0.69	0.79	0.73	0.93	0.97	0.49	0.74	
				0.73	0.73	0.89	0.49	0.33	0.78	0.03	0.73	0.73	0.99	0.93	0.82	0.93	
				0.91	0.94	0.03	0.49	0.41	0.78	0.78	0.77	0.89	0.99	0.93	0.90	0.99	
						0.79	0.73	0.90	0.67	0.33	0.61	0.69	0.79	0.73	0.93	0.97	
						0.91	0.94	0.89	0.49	0.41	0.78	0.78	0.77	0.89	0.99	0.93	

Colour spaces: RGB

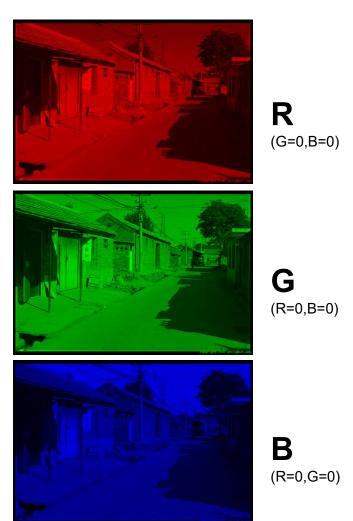
Default colour space





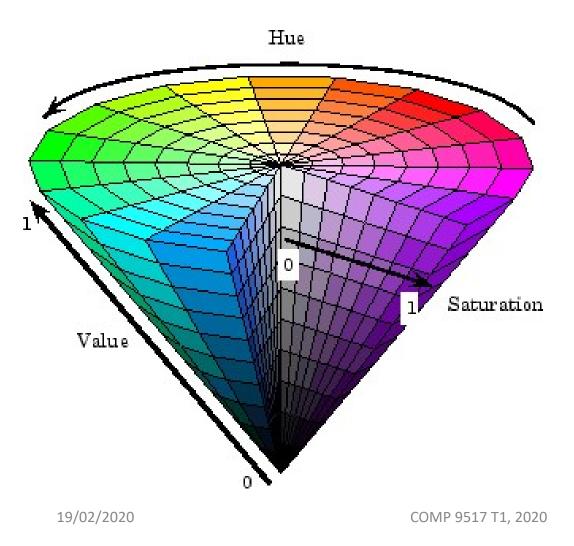


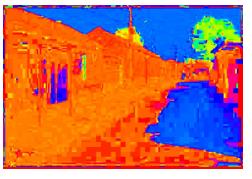
- Strongly correlated channels
- Non-perceptual



Colour spaces: HSV

Intuitive colour space









S (H=1,V=1)

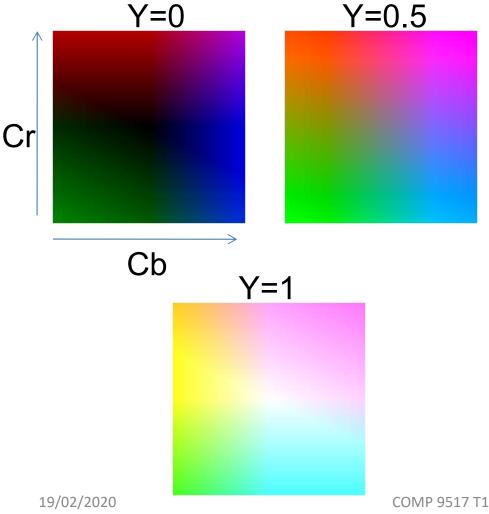


V (H=1,S=0)

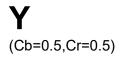
28

Colour spaces: YCbCr

Fast to compute, good for compression, used by TV









Cb (Y=0.5,Cr=0.5)



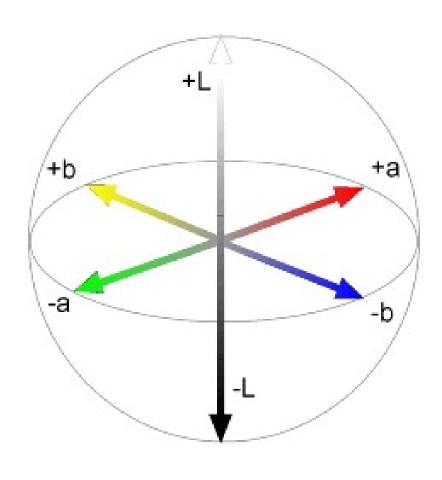
Cr (Y=0.5,Cb=05)

COMP 9517 T1, 2020

29

Colour spaces: L*a*b* "Perceptually uniform"* colour space











a (L=65,b=0)



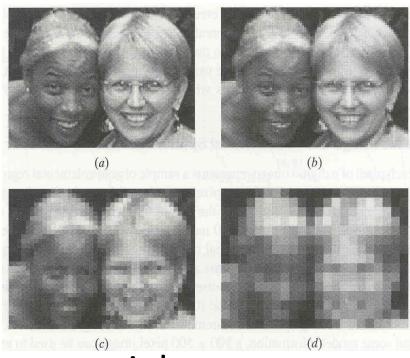
b (L=65,a=0)

Digitisation and Sampling

- Digitisation: converts analog image to digital image
- Sampling digitises the coordinates x and y:
 - spatial discretisation of picture function F (x,y)
 - use a grid of sampling points, normally rectangular: image sampled at points $x = j \Delta x$, $y = k \Delta y$, j = 1...M, k = 1...N.
 - $-\Delta x$, Δy called the **sampling intervals**.

Spatial Resolution

- Spatial Resolution: number of pixels per unit of length
- Resolution decreases by one half- see right
- Human faces can be recognized at 64 x 64 pixels per face



- Appropriate resolution is essential:
 - too little resolution, poor recognition
 - too much resolution, slow and wastes memory

Quantisation

- Quantisation digitises the intensity or amplitude values, ie F (x, y)
 - called intensity or gray level quantisation
 - Gray-level resolution:
 - usually has 16, 32, 64,, 128, 256 levels
 - number of levels should be high enough for human perception of shading details - human visual system requires about 100 levels for a realistic image.

For Reading

- Szeliski, Chapter 2
- Shapiro and Stockman, Chapter 2

Acknowledgement

- Slides from Derek Hoiem, Alexei Efros, Steve Seitz, and David Forsyth
- Image sources credited where possible
- Some material, including images and tables, were drawn from the referenced textbooks and associated online resources.