

### **COMP 9517 Computer Vision**

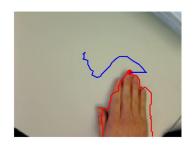
**Tracking** 

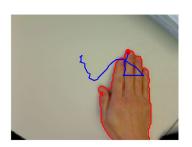
### **Motion Tracking**

 Tracking is the problem of generating an inference about the motion of an object given a sequence of images









### **Applications**

#### Motion capture

- Record motion of people to control cartoon characters in animations
- Modify the motion record to obtain slightly different behaviours

#### Recognition from motion

- Determine the identity of a moving object
- Assess what the object is doing

#### Surveillance

- Detect and track objects in a scene for security
- Monitor their activities and warn if anything suspicious happens

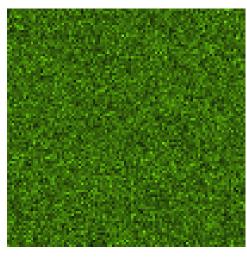
### Targeting

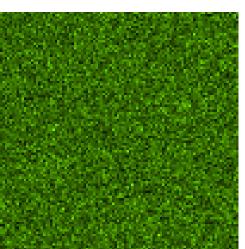
- Decide which objects to shoot in scene
- Make sure the objects get hit

### Difficulties in Tracking

- Loss of information caused by projection of the 3D world on a 2D image
- Noise in images
- Complex object motion
- Non-rigid or articulated nature of objects
- Partial and full object occlusions
- Complex object shapes
- Scene illumination changes
- Real-time processing requirements

### **Example Tracking Problem**





#### Single moving microscopic particle

Imaged with signal-to-noise ratio (SNR) of 1.5

#### **Human visual motion perception**

- Not so accurate and reproducible in quantification
- Good at integrating spatial and temporal information
- Powerful in making associations and predictions

#### **Computer vision challenges**

- Integration of spatial and temporal information
- Modeling and incorporation of prior knowledge
- Probabilistic rather than deterministic approach

#### Bayesian estimation methods...

### **Motion Assumptions**

- When moving objects do not have unique texture or colour, the characteristics of the motion itself must be used to connect detected points into trajectories
- Assumptions about each moving object:
  - Location changes smoothly over time
  - Velocity (speed and direction) changes smoothly over time
  - Can be at only one location in space at any given time
  - Not in same location as another object at the same time

### **Topics**

Bayesian inference

Using probabilistic models to perform tracking

Kalman filtering

Using linear model assumptions for tracking

Particle filtering

Using nonlinear models for tracking

## **Bayesian Inference**

### **Problem Definition**

A moving object has a state which evolves over time

Random variable:  $X_i$ 

Specific value:  $X_i$ 

can contain any quantities of interest (position, velocity, acceleration, shape, intensity, colour, ...)

The state is measured at each time point

Random variable:  $Y_i$ 

Specific value:  $y_i$ 

in computer vision the measurements are typically features computed from the images

Measurements are combined to estimate the state

### Three Main Steps

• **Prediction**: use the measurements  $(y_0, y_1, ..., y_{i-1})$  up to time i-1 to predict the state at time i

$$P(X_i | Y_0 = y_0, Y_1 = y_1, ..., Y_{i-1} = y_{i-1})$$

- Association: select the measurements at time i
  that are related to the object state
- Correction: use the incoming measurement  $y_i$  to update the state prediction

$$P(X_i | Y_0 = y_0, Y_1 = y_1, ..., Y_{i-1} = y_{i-1}, Y_i = y_i)$$

### Independence Assumptions

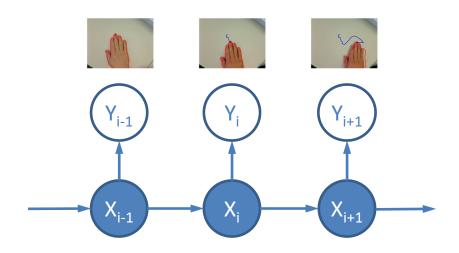
Current state depends only on the immediate past

$$P(X_i | X_0, X_1, ..., X_{i-1}) = P(X_i | X_{i-1})$$

Measurements depend only on the current state

$$P(Y_i, Y_j, ..., Y_k \mid X_i) = P(Y_i \mid X_i)P(Y_j, ..., Y_k \mid X_i)$$

These assumptions imply the tracking problem has the structure of inference on a hidden Markov model



### Tracking by Bayesian Inference

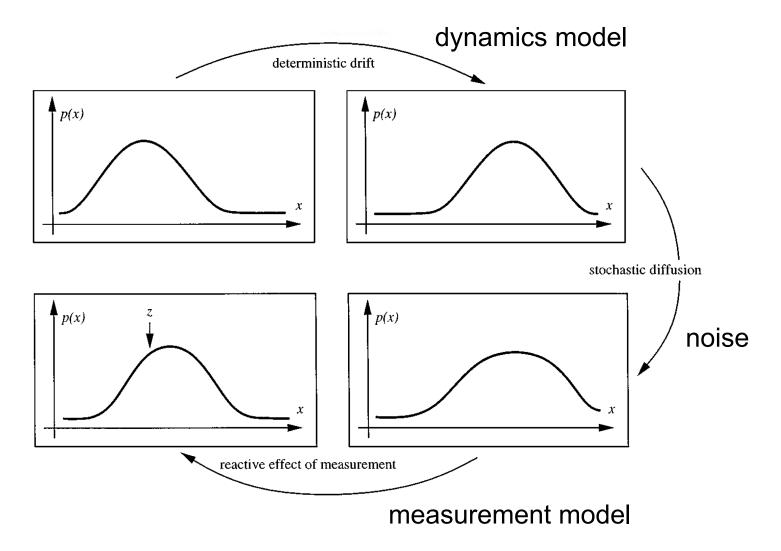
#### Prediction

### Tracking by Bayesian Inference

#### Correction

# Kalman Filtering

### **Probability Density Propagation**



### Linear / Gaussian Assumption

If we assume the dynamics (state transition) model and the measurement model to be linear, and the noise to be additive Gaussian, then all the probability densities will be Gaussians

$$x \sim N(\mu, \Sigma)$$

 The state is advanced by multiplying with some known matrix and then adding a zero-mean normal random variable

$$x_i \sim N(D_i x_{i-1}, \sum_{d_i})$$
  $x_i = D_i x_{i-1} + w_{i-1}$ 

• The measurement is obtained by multiplying the state by some matrix and then adding a zero-mean normal random variable

$$y_i \sim N(M_i x_i, \sum_{m_i})$$
  $y_i = M_i x_i + v_i$ 

$$x_i \sim N(Ax_{i-1}, Q)$$

$$y_i \sim N(Hx_i, R)$$

### Kalman Filtering

#### **Prediction**

1. Predict state

$$x_i^- = Ax_{i-1}$$

2. Predict covariance

$$P_i^- = AP_{i-1}A^T + Q$$

#### Correction

1. Compute Kalman gain

$$K_i = P_i^- H^T (H P_i^- H^T + R)^{-1}$$

2. Correct state with measurement

$$x_{i} = x_{i}^{-} + K_{i}(y_{i} - Hx_{i}^{-})$$

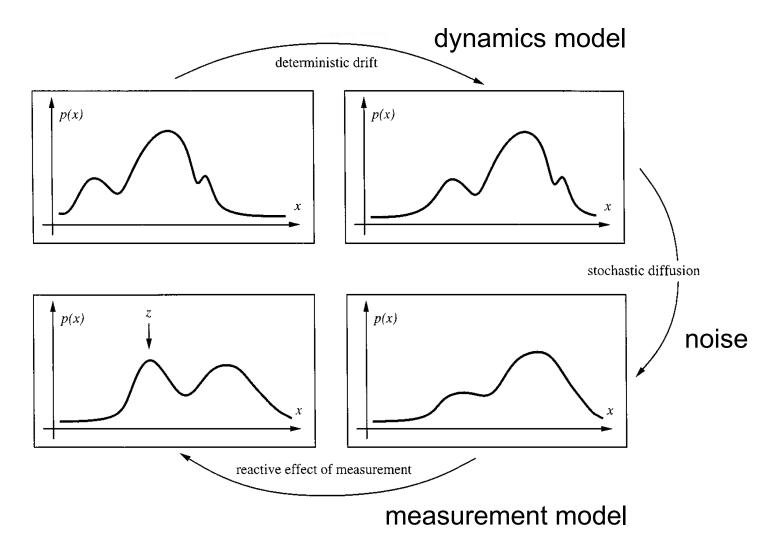
3. Correct covariance

$$P_i = (I - K_i H) P_i^-$$

$$i \rightarrow i+1$$

# Particle Filtering

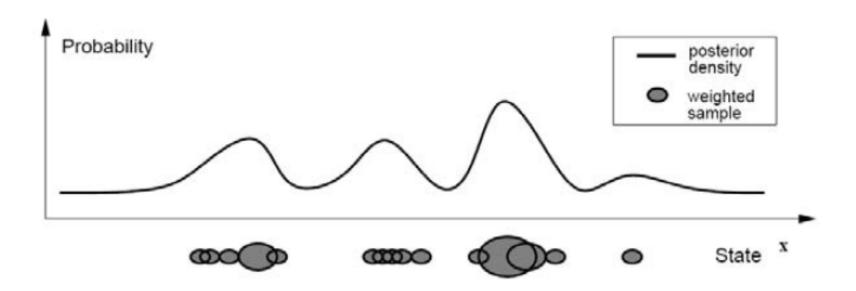
### **Probability Density Propagation**



### Non-Linear / Non-Gaussian Case

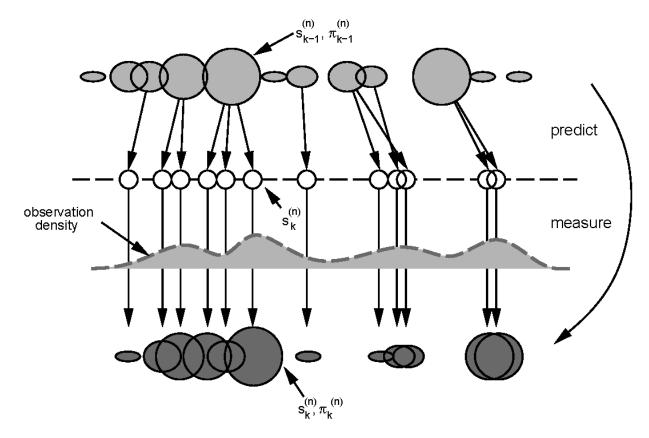
 Represent the conditional state density by a set of samples (particles) with corresponding weights (importance)

$$P(X_i \mid y_0, y_1, ..., y_i) \rightarrow \{s_i^{(n)}, \pi_i^{(n)}\}_{n=1}^N$$



### Particle Filtering

 Propagate each sample using the dynamics model and obtain its new weight using the measurement model



### Particle Filtering Algorithm

#### Iterate

From the "old" sample set  $\{\mathbf{s}_{k-1}^{(n)}, \pi_{k-1}^{(n)}, c_{k-1}^{(n)}, n = 1, \dots, N\}$  at time-step  $t_{k-1}$ , construct a "new" sample set  $\{\mathbf{s}_{k}^{(n)}, \pi_{k}^{(n)}, c_{k}^{(n)}, n = 1, \dots, N\}$  for time  $t_{k}$ .

Construct the  $n^{\text{th}}$  of N new samples as follows:

- 1. Select a sample  $\mathbf{s}_{k}^{\prime (n)}$  as follows:
  - (a) generate a random number  $r \in [0, 1]$ , uniformly distributed.
  - (b) find, by binary subdivision, the smallest j for which  $c_{k-1}^{(j)} \geq r$
  - (c) set  $\mathbf{s}'_k{}^{(n)} = \mathbf{s}_{k-1}^{(j)}$
- 2. Predict by sampling from

$$p(\mathcal{X}_k|\mathcal{X}_{k-1} = \mathbf{s'}_k^{(n)})$$

to choose each  $\mathbf{s}_k^{(n)}$ . For instance, in the case that the dynamics are governed by a linear AR process, the new sample value may be generated as:  $\mathbf{s}_k^{(n)} = A \mathbf{s}_k'^{(n)} + (I-A) \overline{\mathcal{X}} + B \mathbf{w}_k^{(n)}$  where  $\mathbf{w}_k^{(n)}$  is a vector of standard normal random variates, and  $BB^T$  is the process noise covariance.

3. Measure and weight the new position in terms of the measured features  $\mathbf{Z}_k$ :

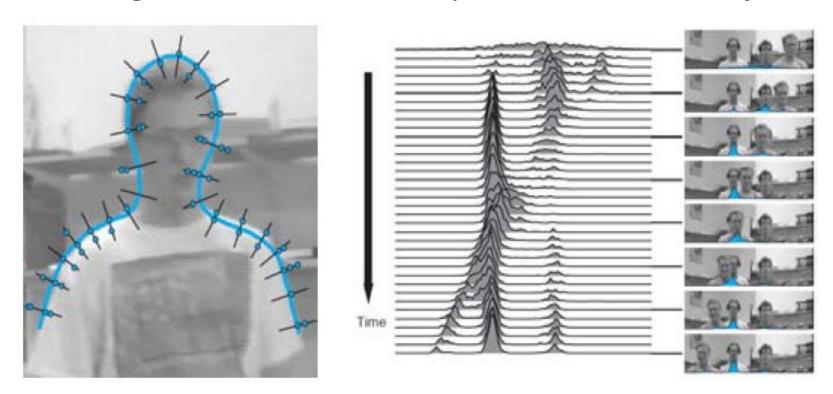
$$\pi_k^{(n)} = p(\mathbf{Z}_k | \mathcal{X}_k = \mathbf{s}_k^{(n)})$$

then normalise so that  $\sum_n \pi_k^{(n)} = 1$  and store together with cumulative probability as  $(\mathbf{s}_k^{(n)}, \pi_k^{(n)}, c_k^{(n)})$  where

$$c_k^{(0)} = 0,$$
  
 $c_k^{(n)} = c_k^{(n-1)} + \pi_k^{(n)} \text{ for } n = 1, \dots, N.$ 

### **Example Application**

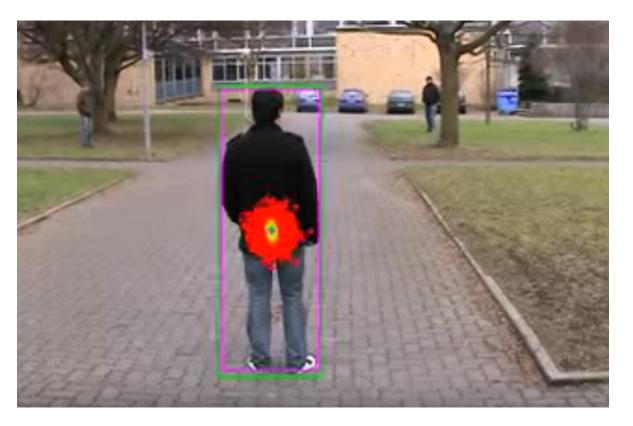
Tracking of active contour representations of objects



Particle filtering is also known variously as sequential Monte Carlo (SMC) filtering, bootstrap filtering, the condensation algorithm...

### **Example Application**

Tracking of object location in presence of clutter



https://www.youtube.com/watch?v=j-duyzShJ o

### References and Acknowledgements

- Shapiro and Stockman 2001
- Chapter 18 Forsyth and Ponce 2003
- Chapter 5 Szeliski 2010
- M. Isard and A. Blake 1998
- Images drawn from the above references unless otherwise mentioned