

Time: 1.30 hrs

Maximum: 30 Marks

PART - A (2 x 5 = 10 Marks)

Q.1. Answer ALL questions

- | | CO # | Blooms Level |
|---|------|--------------|
| a. Find the rank of the matrix $\begin{pmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 9 \end{pmatrix}$ | CO1 | K1 |
| b. Prove that the diagonal elements of a skew-symmetric matrix are zero | CO1 | K1 |
| c. Find the spectrum and spectral radius of the matrix $\begin{pmatrix} 1 & 1 \\ 2 & 2 \end{pmatrix}$ | CO1 | K2 |
| d. Find the total derivative of $z = e^x \sin y$ | CO2 | K1 |
| e. Find $\frac{dy}{dx}$ where $x \sin(x - y) - (x + y) = 0$ | CO2 | K2 |

PART - B (10 x 2 = 20 Marks)

Answer ALL Questions

- | | Marks | CO# | Blooms Level |
|--|-------|-----|--------------|
| 2.a. Solve the system of linear equations by Gauss Elimination method
$3x + 7y + 8z = -13,$
$2x + 9z = -5,$
$-4x + y - 26z = 2$ | 5 | COI | K2 |
| b. Find the Diagonalization of matrix $A = \begin{bmatrix} -19 & 7 \\ -42 & 16 \end{bmatrix}$
(OR) | 5 | COI | K2 |
| c. Find the eigenvectors of the matrix $\begin{pmatrix} 16 & 0 & 0 \\ 48 & -8 & 0 \\ 84 & -24 & 4 \end{pmatrix}$ | 5 | CO1 | K2 |
| d. Find out which type of conic section is represented by Quadratic function $41x_1^2 - 24x_1x_2 + 34x_2^2 = 0$ | 5 | CO1 | K2 |
| 3.a. If $z = xyf\left(\frac{y}{x}\right)$ show that $x \frac{\partial z}{\partial x} + y \frac{\partial z}{\partial y} = 2z$ and if z is constant
then $\frac{f'\left(\frac{y}{x}\right)}{f\left(\frac{y}{x}\right)} = \frac{x\left(y + x \frac{dy}{dx}\right)}{y\left(y - x \frac{dy}{dx}\right)}$ | 5 | CO2 | K2 |
| b. Expand $f(x, y) = \log(x + e^y)$ by Taylor's series in powers of $(x - 1)$ and y .
(OR) | 5 | CO2 | K2 |
| c. If $x^x y^y z^z = c$, show that at $x = y = z$ $\frac{\partial^2 z}{\partial x \partial y} = -(x \ln ex)^{-1}$ | 6 | CO2 | K2 |
| d. Discuss the maxima and minima of $f(x, y) = \sin x + \sin y + \sin(x + y)$ | 4 | CO2 | K2 |