Test 5: Ruin probability: Poisson / Exponential. (* Accuracy parameters *) K = 16; $R = 10^5$; numPoints = 25; (* Problem description *) c = 1; $\lambda = 4$; UDist = ExponentialDistribution[4]; UDist = GammaDistribution[2, 2]; (* Time grid *) tMax = 1;dt = tMax / numPoints; ts = Table[i, {i, dt, tMax, dt}]; (* Orthogonal polynomial method *) Verbosity = 0; **SLPs** = Table NDist = PoissonDistribution [λt]; $r = \lambda t \text{ Mean}[UDist]^2 / \text{Moment}[UDist, 2];$ m = Moment[UDist, 2] / Mean[UDist]; SeedRandom[1]; ps = PseudoGammaCoeffsIndirectly[NDist, UDist, r, m, K, Verbosity]; OrthogonalSLP = Sum[ps[[i+1]] (m (r+i) Γ u[r+i+1, m, ct] - ct Γ u[r+i, m, ct]), {i, 0, K}]; SeedRandom[1]; CrudeSLP = First@Last@ReferenceCMC[NDist, UDist, {}, {ct}, R]; svfStarI = Last@LaplaceInversionMethod[NDist, UDist]; LapInvSLP = Mean[NDist] Mean[UDist] svfStarI[ct]; {OrthogonalSLP, LapInvSLP, CrudeSLP}, {t, ts}];

RefRuins = Table[Median[AllRuins[[;;,i]]], {i, Length[ts]}] // GaussianFilter[#, 2] &;

RuinEst = ListPlot[WithT /@ Append[AllRuins, RefRuins], Joined → True, AspectRatio → 1 / 3];

RuinPlot = Legended[GraphicsColumn[{RuinEst, RuinAbsErr(*,RuinRelErr*)}],

8.0

8.0

RuinAbsErr = ListPlot[WithT[AbsErr[#, RefRuins]] & /@ AllRuins, Joined → True, AspectRatio → 1 / 3];

Crude MC (R = 1e5)

Orthogonal (K = 16)

Laplace Inversion

Smooth Median

(*RuinRelErr=ListPlot[WithA[RelErr[#,RefRuins]]&/@AllRuins,Joined→True,AspectRatio→1/3];*)

1.0

1.0

OrthoRuins = $\frac{1}{c t s}$ ($\lambda t s * Mean[UDist] - SLPs[[;;,1]]) // N;$ $LapInvRuins = <math>\frac{1}{c t s}$ ($\lambda t s * Mean[UDist] - SLPs[[;;,2]]) // N;$ $CrudeRuins = <math>\frac{1}{c t s}$ ($\lambda t s * Mean[UDist] - SLPs[[;;,3]]) // N;$

AllRuins = {CrudeRuins, OrthoRuins, LapInvRuins};

LineLegend[Colours, Append[EstNames, RefName]]]

Export["poisson exponential ruin.pdf", RuinPlot];

0.4

0.4

0.6

0.6

■ Test 6: Ruin probability: Poisson Pareto

(**** Make the plots ****)

"Laplace Inversion"};

RefName = "Smooth Median";

1.0

8.0

0.6

0.4

0.2

0.08

0.06

0.04

0.02

-0.02

-0.04

0.0

0.2

0.2

(* Accuracy parameters *)

(* Problem description *)

(* Time grid *)

Verbosity = 0;

SLPs = Table

tMax = 5;

K = 16; $R = 10^5$; numPoints = 25;

(* Orthogonal polynomial method *)

NDist = PoissonDistribution [λt];

"Laplace Inversion"};

RefName = "Smooth Median";

Memory problem...

1.0

0.8

0.6

0.4

0.2

0.015

0.010

0.005

-0.005

-0.010

0

GaussianFilter[#, 2] &;

WithT[Data_] := Transpose[{ts, Data}];

AllRuins = {CrudeRuins, OrthoRuins, LapInvRuins};

LineLegend[Colours, Append[EstNames, RefName]]]

Export["poisson_pareto_ruin.pdf", RuinPlot];

2

3

(* Orthogonal polynomial method *)

WithT[Data_] := Transpose[{ts, Data}];

```
c = 1; \lambda = 2; a = 5; b = 11; \theta = 0;

LTofU[\] = Expectation[E^{-\frac{1}{2}, \hat{1}{2}}, \hat{1}] \approx UDist];
```

 $dt = tMax / numPoints; ts = Table[i, {i, 10⁻¹, tMax, dt}];$

```
Tilt = 1;
    ThetaFracOfM = \frac{1}{2};
    mOrig = ThetaFracOfM ;
    r = Mean[UDist];
    m = \frac{mOrig}{1 - mOrig Tilt};
    (*Print["Want to take m > 1/2 Tilt i.e. ", mOrig, " > " ,1/(2 Tilt)];
    Print["Tilting by ", N@Tilt, " which gives a modified m of ", N@m];
    *)
    SeedRandom[1];
    ps = PseudoGammaCoeffsIndirectly[NDist, UDist, r, mOrig, K, Verbosity, LTofU, Tilt];
    OrthogonalSLP = Sum[ps[[i+1]] (m (r+i) \Gammau[r+i+1, m, ct] - ct \Gammau[r+i, m, ct]), {i, 0, K}];
    SeedRandom[1];
    CrudeSLP = First@Last@ReferenceCMC[NDist, UDist, {}, {ct}, R];
    svfStarI = Last@LaplaceInversionMethod[NDist, UDist, LTofU];
    (*LapInvSLP= Mean[NDist]Mean[UDist]svfStarI[c t];*)
    LapInvSLP = Quiet@Catch[Mean[NDist] Mean[UDist] svfStarI[ct], _SystemException];
    If [LapInvSLP === SystemException["MemoryAllocationFailure"], Print["Memory problem..."];
     LapInvSLP = Indeterminate];
    {OrthogonalSLP, LapInvSLP, CrudeSLP}, {t, ts}];
OrthoRuins = \frac{1}{c ts} (\lambda ts * Mean[UDist] - SLPs[[;;,1]]) // N;

LapInvRuins = <math>\frac{1}{c ts} (\lambda ts * Mean[UDist] - SLPs[[;;,2]]) // N;
CrudeRuins = \frac{1}{c ts} (\lambda ts * Mean[UDist] - SLPs[[;;, 3]]) // N;
(**** Make the plots *****)
EstNames = {"Crude MC (R = 1e" <> ToString[Log10[R]] <> ")", "Orthogonal (K = " <> ToString[K] <> ")",
```

RefRuins = Table[Median[DeleteCases[AllRuins[[;;,i]], Indeterminate]], {i, Length[ts]}] //

RuinEst = ListPlot[WithT /@ Append[AllRuins, RefRuins], Joined → True, AspectRatio → 1 / 3];

RuinPlot = Legended[GraphicsColumn[{RuinEst, RuinAbsErr(*,RuinRelErr*)}],

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RuinAbsErr = ListPlot[WithT[AbsErr[#, RefRuins]] & /@ AllRuins, Joined → True, AspectRatio → 1 / 3];

Crude MC (R = 1e5)

Orthogonal (K = 16)

Laplace Inversion

Smooth Median

(*RuinRelErr=ListPlot[WithA[RelErr[#,RefRuins]]&/@AllRuins,Joined→True,AspectRatio→1/3];*)

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