

```
function [v, omega] = lqr control(x, y, theta, x ref, y ref)
%#codegen
robotState = [x; y; theta];
targetPoint = [x ref; y ref];
[v, omega] = LQRController(robotState, targetPoint);
function [v, omega] = LQRController(robotState, targetPoint)
   % Inputs:
   % robotState = [x; y; theta]
   % targetPoint = [x target; y target]
   x = robotState(1);
   y = robotState(2);
   theta = robotState(3);
   x target = targetPoint(1);
   y target = targetPoint(2);
   % LQR Gain matrix (2x3)
   K = [1.5, 0.0, 0.0;
         0.0, 1.5, 2.0];
   % Global error
   dx = x target - x;
   dy = y target - y;
   error global = [dx; dy];
   % Rotation matrix to robot frame
   c = cos(theta);
   s = sin(theta);
   R = [c, s; -s, c];
   error robot = R * error global;
   % Theta error
   angle to target = atan2(dy, dx);
   theta error = atan2(sin(angle to target - theta), cos(angle to target - theta));
   % Form error state
   error state = [error robot; theta error];
   % Control input via LQR gains
   v r = K(1, :) * error state;
   v l = K(2, :) * error state;
   % Convert to unicycle model control inputs
   v = (v r + v 1) / 2;
   omega = (v r - v l) / 0.2; % 0.2m wheel base
   % Saturation
   v = max(0.2, min(v, 5.0));
   omega = min(max(omega, -pi), pi);
end
end
```

```
function [v, omega, updated v, updated omega] = fast mpc control(x, y, theta, x ref, y ref, dt, data, last v, last omega)
%#codegen
robotState = [x; y; theta];
targetPoint = [x ref; y ref];
[v, omega, updated v, updated omega] = FastMPCController(robotState, targetPoint, dt, last v, last omega);
function [best v, best omega, last v, last omega] = FastMPCController(robotState, targetPoint, dt, last v, last omega)
    % Unpack current state
    x = robotState(1);
    y = robotState(2);
    theta = robotState(3);
    x target = targetPoint(1);
    y target = targetPoint(2);
   % MPC parameters
    N = 20; % Prediction horizon
    % Cost weights (speed-prioritized)
    w pos = 0.5;
    w theta = 1.0;
    w^{-}v = 0.05;
    w omega = 0.1;
    velocity bias = 0.3; % Reward for high velocity
    % Control limits
    v \min = 0.0;
    v^{-}max = 5.0;
    \overline{omega} min = -pi;
    omega max = pi;
    % Control search ranges (favoring acceleration)
    v range min = max(v min, last v - 0.3);
    v range max = min(v max, last v + 0.7);
    v options = linspace(v range min, v range max, 5);
    omega options = linspace (max (omega min, last omega - 0.5), min (omega max, last omega + 0.5), 7);
    % Initialize best control
    best cost = inf;
    best_v = last_v;
    best_omega = last omega;
    for vi = 1:length(v options)
        for wi = 1:length(omega options)
            v = v \text{ options}(vi);
            omega = omega options(wi);
            pred x = x;
            pred_y = y;
            pred theta = theta;
            tota\overline{l} cost = 0;
            for i = 0:N-1
                % Predict next state
                pred x = pred x + v * cos(pred theta) * dt;
                pred y = pred y + v * sin(pred theta) * dt;
                pred theta = pred theta + omega * dt;
```

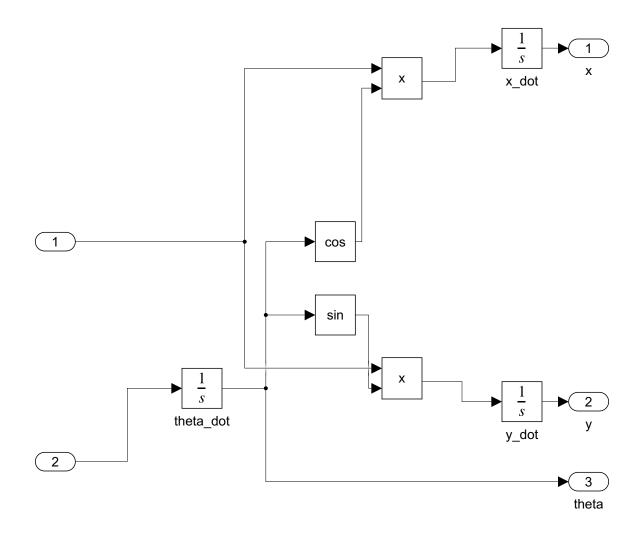
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% Errors
                pos error = sqrt((x target - pred x)^2 + (y target - pred y)^2);
                desired theta = atan2 (y target - pred y, x target - pred x);
                theta error = atan2(sin(desired theta - pred theta), cos(desired theta - pred theta));
                % Smoothness
                v change = abs(v - last v);
                omega change = abs(omega - last omega);
                % Reward for speed
                velocity reward = -velocity bias * v / v max;
                % Step cost
                step cost = w pos * pos error + w theta * abs(theta error) + w v * v change + w omega * omega change + velocity re
                discount = 0.\overline{9} ^ i;
                total cost = total cost + discount * step cost;
            end
            % Update best control
            if total cost < best cost
                best cost = total_cost;
                best v = v;
                best omega = omega;
            end
        end
    end
    % Update memory for next call
    last v = best v;
    last omega = best omega;
end
end
```

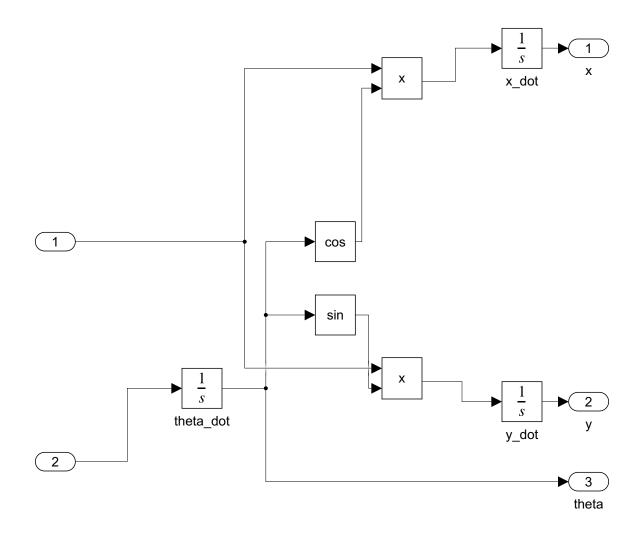
```
function [v, omega, updatedError] = pd control(x, y, theta, x ref, y ref, dt, prevError)
%#codegen
robotState = [x; y; theta];
targetPoint = [x ref; y ref];
[v, omega, updatedError] = PD Controller(robotState, targetPoint, dt, prevError);
    function [v, omega, updatedPrevAngleError] = PD Controller(robotState, targetPoint, dt, prevAngleError)
    x = robotState(1); y = robotState(2); theta = robotState(3);
    x target = targetPoint(1); y target = targetPoint(2);
    dx = x target - x;
    dy = y target - y;
    dist to target = sqrt(dx^2 + dy^2);
    angle to target = atan2(dy, dx);
    angle error = atan2(sin(angle to target - theta), cos(angle to target - theta));
    angle error deriv = (angle error - prevAngleError) / dt;
    updatedPrevAngleError = angle error;
    % PD Gains
    kp v = 1.5;
    kp omega = 2.0;
    kd omega = 1.0;
    v = min(max(kp v * dist to target, 0.2), 5.0);
    omega = min(max(kp omega * angle error + kd omega * angle error deriv, -pi), pi);
end
end
```

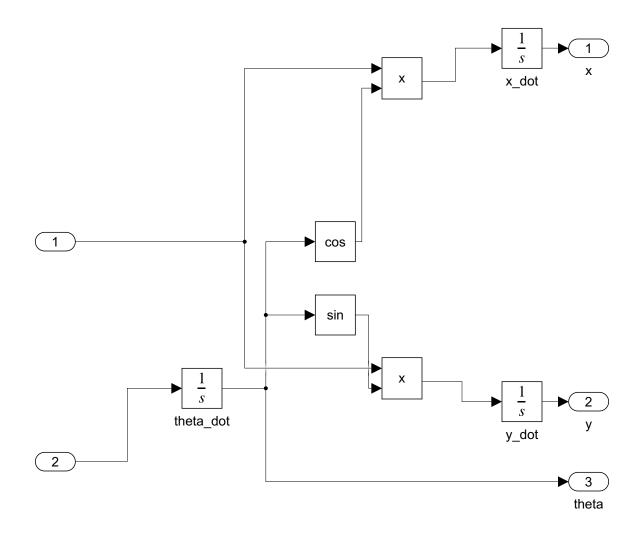
```
function [v, omega, updatedLastV, updatedLastOmega] = mpc control(x, y, theta, x ref, y ref, dt, last v, last omega)
%#codegen
robotState = [x; y; theta];
targetPoint = [x ref; y ref];
[v, omega, updatedLastV, updatedLastOmega] = MPCController(robotState, targetPoint, dt, last v, last omega);
function [best v, best omega, last v, last omega] = MPCController(robotState, targetPoint, dt, last v, last omega)
   % Unpack state
   x = robotState(1);
   y = robotState(2);
   theta = robotState(3);
   x target = targetPoint(1);
   y target = targetPoint(2);
   % MPC Parameters
   N = 10; % Prediction horizon
   % Weights
   w pos = 1.0;
   w theta = 1.5;
   w v = 0.1;
   w \text{ omega} = 0.2;
   % Control limits
   v \min = 0.2; v \max = 5.0;
   omega min = -pi; omega max = pi;
   % Discretized control space
   v options = linspace(max(v min, last v - 0.5), min(v max, last v + 0.5), 5);
   omega options = linspace(max(omega min, last omega - 0.5), min(omega max, last omega + 0.5), 7);
   % Initialize best control
   best cost = inf;
   best_v = last_v;
   best omega = last omega;
   % Evaluate control sequences
   for vi = 1:length(v options)
        for wi = 1:length(omega options)
            v = v \text{ options}(vi);
            omega = omega options(wi);
            pred x = x;
            pred y = y;
            pred theta = theta;
            total cost = 0;
            for i = 0:N-1
                % Predict next state
                pred x = pred x + v * cos(pred theta) * dt;
                pred y = pred y + v * sin(pred theta) * dt;
                pred theta = pred theta + omega * dt;
                % Compute errors
                pos error = sqrt((x target - pred x)^2 + (y target - pred y)^2);
                desired theta = atan2(y target - pred y, x target - pred x);
                theta error = atan2(sin(desired theta - pred theta), cos(desired theta - pred theta));
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% Control smoothness
                v change = abs(v - last v);
                omega change = abs(omega - last omega);
                % Cost with discount
                step_cost = w_pos * pos_error + w_theta * abs(theta_error) + w_v * v_change + w_omega * omega_change;
                discount = 0.\overline{9} ^ i;
                total cost = total cost + discount * step cost;
            end
            % Update best control
            if total cost < best cost
                best cost = total cost;
                best_v = v;
                best omega = omega;
            end
        end
    end
    % Update memory for next step
    last v = best v;
    last omega = best omega;
end
end
```

```
function [v, omega, paOut, aSumOut, pvOut, vSumOut, pdOut] = pid controller block(x, y, theta, x ref, y ref, dt, paIn, aSumIn, pvI
%#codegen
robotState = [x; y; theta];
targetPoint = [x ref; y ref];
[v, omega, paOut, aSumOut, pvOut, vSumOut, pdOut] = PIDController(robotState, targetPoint, dt, paIn, aSumIn, pvIn, vSumIn, pdIn);
    function [v, omega, prevAngleError, angleErrorSum, prevVError, vErrorSum, prevDistance] = PIDController(robotState, targetPoin
    % Unpack robot state
    x = robotState(1);
    y = robotState(2);
    theta = robotState(3);
    x target = targetPoint(1);
    y target = targetPoint(2);
    % Desired forward velocity
    v desired = 5.0;
    %% --- Angular control (omega) ---
    angle to target = atan2(y target - y, x target - x);
    angle error = atan2(sin(angle to target - theta), cos(angle to target - theta));
    angle error deriv = (angle error - prevAngleError) / dt;
    angleErrorSum = angleErrorSum + angle error * dt;
    angleErrorSum = min(max(angleErrorSum, -1.0), 1.0); % Anti-windup
    prevAngleError = angle error;
    % PID gains for angular velocity
    kp omega = 2.0;
    ki omega = 1.0;
    kd omega = 0.6;
    omega = kp omega * angle error + ki omega * angleErrorSum + kd omega * angle error deriv;
    omega = min(max(omega, -pi), pi);
    %% --- Linear velocity control ---
    dist to target = sqrt((x target - x)^2 + (y target - y)^2);
    v current = (prevDistance - dist to target) / dt;
    prevDistance = dist to target;
    v error = v desired - v current;
    v error deriv = (v error - prevVError) / dt;
    \overline{vErrorSum} = \overline{vErrorSum} + \overline{v} = \overline{verror} * dt;
    vErrorSum = min(max(vErrorSum, -2.0), 2.0); % Anti-windup
    prevVError = v error;
    % PID gains for linear velocity
    kp v = 1.0;
    ki^{v} = 0.5;
    kd v = 0.2;
    v = kp v * v error + ki v * vErrorSum + kd v * v error deriv;
    % Reduce speed when not aligned with target
    v = v * cos(angle error);
    % Clamp final velocity
    v = min(max(v, 0.2), 5.0);
end
```







```
function [x_ref, y_ref, theta_ref] = trajectoryGen(t)
    radius = 5;
    omega_ref = 0.2;
    x_ref = radius * cos(omega_ref * t);
    y_ref = radius * sin(omega_ref * t);
    theta_ref = omega_ref * t + pi/2;
end
```