

CROSS-DOMAIN ACTIVITY RECOGNITION VIA SUBSTRUCTURAL OPTIMAL TRANSPORT

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ABSTRACT

It is expensive and time-consuming to collect sufficient labeled data for human activity recognition (HAR). Recently, lots of work solves the problem via domain adaptation which leverages the labeled samples from the source domain to annotate the target domain. Existing domain adaptation methods mainly focus on adapting cross-domain representations via domain-level, class-level, or sample-level distribution matching. However, the domain- and class-level matching are too coarse that may result in under-adaptation, while sample-level matching may be affected by the noise seriously and eventually cause over-adaptation. In this paper, we propose substructure-level matching for domain adaptation (SSDA) to utilize the internal substructures of the domain to perform accurate and efficient knowledge transfer. Based on SSDA, we propose an optimal transport-based implementation, Substructural Optimal Transport (SOT), for cross-domain HAR. We obtain the substructures of activities via clustering methods and seeks the coupling of the weighted substructures between different domains. We conduct comprehensive experiments on four large public activity recognition datasets (i.e. UCI-DSADS, UCI-HAR, USC-HAD, PAMAP2), which demonstrates that SOT significantly outperforms other state-of-the-art methods w.r.t classification accuracy (10%+ improvement). In addition, SOT is much faster than comparison methods.

1 INTRODUCTION

Human activity recognition (HAR) plays an important role in ubiquitous computing. Through collected raw signals from sensors, it can easily learn high-level knowledge about human activity via a machine learning model. HAR has been applied to many fields, including gait analysis Zhao et al. (2018a), gesture recognition Jia et al. (2020) and sleep stage detection Zhao et al. (2017). A robust machine learning model is the key to a successful HAR application. However, a robust model always acquires sufficient labeled data which is time-consuming and expensive. A possible way to cope with the problem is to exploit the labeled activity data from an auxiliary dataset. The new problem is referred to as the cross-domain activity recognition (CDAR) Wang et al. (2018a).

It is not appropriate to use labeled activity data from an auxiliary dataset directly, due to different distributions between the auxiliary data and the target data. Domain adaptation (DA) Pan & Yang (2009) is a usual way to transfer knowledge from an auxiliary dataset (i.e. source domain) to an unlabeled domain (i.e. target domain). Domain adaptation tries to reduce the distribution gap between the source domain and the target domain and makes use of the knowledge from the source domain to help annotate the target domain.

A lot of work Ding et al. (2019); Khan et al. (2018); Rokni & Ghasemzadeh (2018) on domain adaptation based HAR has achieved great success. According to matching methods, we divide the work into two categories. The first category is rough matching which includes the domain-level matching methods Fernando et al. (2013); Sun et al. (2015), the class-level matching methods Zhu et al. (2020); Wang et al. (2018a) and both domain- and class-level matching methods Wang et al.

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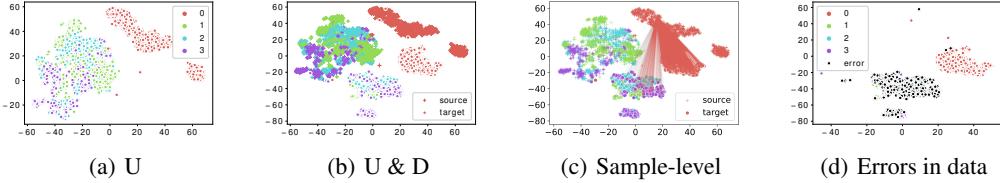


Figure 1: (Best zoom in) Different colors mean different classes while black means error predictions. The boundaries of different colors correspond to the boundaries of different classes.

(2018b); Long et al. (2014). The other category is sample-level matching methods such as Optimal Transport for Domain Adaptation (OTDA) Courty et al. (2016) and Hypergraph Matching based Domain Adaptation Das & Lee (2018b;a).

Despite the progress made by domain-, class-, or sample-level matching, these methods still suffer from the *under-adaptation* and *over-adaptation* issues. We use a real example to illustrate this issue. The four classes ($0 \sim 3$ in the figure) of USC-HAD Zhang & Sawchuk (2012) dataset in Figure 1(a) clearly have different substructures (i.e., clusters). As shown in Figure 1(b), we can see that the different substructures are not aligned, which means only performing rough matching may result in under-adaptation. On the other hand, when performing DA using sample-level methods in Figure 1(c), one data point in the source domain corresponds to too many data points in the target domain, which is notoriously time-consuming. Moreover, Figure 1(d) shows that errors can happen in the boundaries and the overlap parts, resulting in over-adaptation. Other than these empirical evidences, we also theoretically show that the domain-, class-, or sample-level matching for DA is not sufficient to ensure accurate and robust knowledge transfer performance.

In this paper, we take a different perspective on domain adaptation, and hence propose **Substructural Domain Adaptation (SSDA)** for accurate and robust domain adaptation. SSDA mainly performs *substructure-level* matching. Compared with the domain- and class-level methods, SSDA utilizes more fine-grained substructures to overcome under-adaptation. In contrast to sample-level methods that can be easily affected by noise or outliers, SSDA utilizes the substructure of the data that can prevent over-adaptation. Based on SSDA, we propose an optimal transport-based implementation, namely, *Substructural Optimal Transport (SOT)*, for the cross-domain HAR problems. OT has a solid theoretical background and allows a flexible mapping without being restricted to a particular hypothesis class Redko et al. (2017), hence it has no restriction on the numbers of substructures in different domains. Specifically, SOT first obtains the internal substructures by a clustering method (we use Gaussian Mixture Model in this paper, but SOT is agnostic to the clustering method). Then, the activity substructure weights of the source domain are given via partial optimal transport according to its distance from the target domain. Finally, two representations of substructures are used to learn a transportation plan matching both substructures' probability distribution functions (PDFs). We conduct experiments on four public activity recognition datasets (UCI DSADS Barshan & Yüksek (2014), UCI-HAR Anguita et al. (2012), USC-HAD Zhang & Sawchuk (2012), and PAMAP2 Reiss & Stricker (2012)) to evaluate the performance of SOT and the results demonstrate that our method outperforms other state-of-the-art methods with a significant improvement of over 10% w.r.t classification accuracy, while remaining more efficient to train.

Our contributions are mainly three-fold:

1. We propose SSDA for accurate and robust domain adaptation. SSDA can overcome the under-adaptation and over-adaptation issues in existing domain-, class-, or sample-level matching methods.
2. Based on SSDA, we propose an optimal transport-based implementation, SOT, to perform cross-domain activity recognition.
3. Comprehensive experiments on four public activity recognition datasets demonstrate the superiority of SOT (10%+ improvement in accuracy). In addition, SOT is much faster than other methods.

The remainder of this paper is organized as follows. Section 2 surveys the related work. Section 3 introduces the problem formulation and SOT. In Sections 4, experimental settings and results are discussed. Finally, Section 5 concludes the paper and indicates possible research directions in the future.

2 RELATED WORK

2.1 HUMAN ACTIVITY RECOGNITION

Human activity recognition has been a popular research topic in ubiquitous computing for its important role in human daily life. HAR attempts to identify and analyze human activities using learned high-level knowledge from raw data of various types of sensors. Several surveys have summarized recent progress in HAR. Bux et al. (2017); Beddiar et al. (2020) summed up vision-based HAR and Wang et al. (2019); Dang et al. (2020) summarized recent work from a different point. In this paper, we focus on work about sensor-based HAR.

Conventional machine learning approaches often treat HAR as a standard time series classification problem. After getting raw data from sensors, they first preprocess the raw data which includes denoising Castro et al. (2016); Wang et al. (2016) and segmentation Triboan et al. (2019). Then feature extraction Jan et al. (2017) and feature selection Dawn & Shaikh (2016) are implemented to extract useful features from the pre-processed data. In the following, different models, such as random forest (RF) Hu et al. (2018), Bayesian networks Xiao & Song (2018), and support vector machine (SVM) Abidine et al. (2018); Chen & Wang (2018), are built with selected features. Finally, we can use these learned models to make activity inferences. Deep learning based HAR Ignatov (2018); Zhao et al. (2018b); Khan & Taati (2017); Hassan et al. (2018a;b) automatically extracts abstract features through several hidden layers and reduces the effort of choosing the right features.

However, most of the methods mentioned before assume that the training and testing data are in the same distribution, which is not suitable for CDAR problems. As for CDAR problems, source and target data are usually from a different distribution, which results in weak generalization of the aforementioned methods. Therefore, approaches to the CDAR are needed. And in this paper, we mainly focus on the traditional approaches for CDAR problems.

2.2 TRANSFER LEARNING AND DOMAIN ADAPTATION

Transfer learning tries to leverage source domain knowledge to help learn models in the target domain, which mitigates the problem that the target domain has no label or few labels. Pan & Yang (2009); Weiss et al. (2016) concluded the traditional transfer learning methods and Tan et al. (2018) introduced the deep transfer learning methods. Domain adaptation, as a branch of the transfer learning, solves the problem that a distribution shift exists between different domains and has been successfully applied in many applications, such as visual image classification Wang & Deng (2018), natural language processing Wilson & Cook (2020), sentiment classification Dai et al. (2020), etc. We roughly divide domain adaptation into two categories: 1) rough matching which includes domain-level matching, class-level matching, and both domain- and class-level matching; 2) sample-level matching which is a meticulous matching way.

Domain adaptation has developed for many years and most of those methods exploit rough matching between two domains. Pan et al. (2010) proposed a method, named Transfer Component Analysis (TCA), which learns a kernel in the reproducing kernel Hilbert space (RKHS) to minimize the maximum mean discrepancy (MMD) between domains. Long et al. (2014) extended TCA. It matches the marginal distribution and selected the samples of the source domain at the same time. Wang et al. (2018a) proposed stratified transfer learning (STL) and achieved the goal of intra-class transfer. Joint distribution adaptation (JDA) Long et al. (2013) is based on minimizing joint distribution between domains. Wang et al. (2017) extended it and proposed Balanced Distribution Adaptation (BDA) which adaptively adjusts the importance of marginal distribution and conditional distribution. Zhao et al. (2020) proposed a method, named Local Domain Adaptation (LDA), which takes a compromise between domain- and class-level matching and utilizes high-level abstract clusters to organize data.

Sample-level matching is the other way to match distribution between domains and the representative work is Courty et al. (2016). Nicolas Courty et al. utilized the theory of optimal transport to learn the coupling between two probability density functions. Through the barycentric mapping Villani (2008), the images of the source samples in the target domain are obtained, and then a simple classification model can be used to classify the target samples. Kerdoncuff et al. (2020) extended it which designs a metric learning optimal transport (MLOT) algorithm to optimizes a mahalanobis distance. Besides optimal transport based methods, Das & Lee (2018b;a) used hypergraph matching to match the samples between two domains.

SSDA is different from these methods. It takes advantage of the substructure of domains and utilizes the substructure-level matching to seek the balance of rough matching and sample-level matching.

2.3 HUMAN ACTIVITY RECOGNITION WITH TRANSFER LEARNING

There is much prior work focusing on HAR with transfer learning and a detailed survey can be found in Cook et al. (2013).

Zhao et al. (2011) proposed an algorithm known as transfer learning embedded decision tree (TransEMDT) which integrates a decision tree and the k-means clustering algorithm to solve the cross-people activity recognition problem. Lin et al. Lin et al. (2016) identified a compact joint subspace for each class and then measured the distance between classes using principal angle. Wang et al. (2018a) tried to learn more reliable pseudo labels using the majority voting technique on both domains. Rey & Lukowicz (2017) considered a special case that the new domain just contains the old one and Feuz & Cook (2017) proposed a heterogeneous transfer learning method for HAR. Recently, Qin et al. Qin et al. (2019) proposed an adaptive spatial-temporal transfer learning (ASTTL) approach to select the most similar source domain to the target domain and accurately transfer activity. Despite many approaches have been designed to solve the CDAR problem and some of them attempted to use clustering methods, little work is substructure-based. SOT tries to complete substructure-level matching through joint Gaussian Mixture Model and optimal transport. The number of substructures may be different from the number of the classes.

3 METHOD

3.1 PROBLEM FORMULATION

In a CDAR problem, a labeled source domain $\mathcal{D}_s = \{(\mathbf{x}_i, y_i)\}_{i=1}^{n_s}$ and an unlabeled target domain $\mathcal{D}_t = \{\mathbf{x}_j\}_{j=1}^{n_t}$ are given. In our problem, \mathcal{D}_s and \mathcal{D}_t have the same feature spaces and label spaces, i.e. $\mathbf{x}_i, \mathbf{x}_j \in \mathbb{R}^d$ and $\mathcal{Y}_s = \mathcal{Y}_t$. n_s and n_t are the number of source and target samples respectively and d is the dimension of the feature space. $y_s \in \{1, \dots, C\}$ and C is the number of classes. The goal of cross-domain learning is to obtain the labels y_t for the target domain with the help of the source domain \mathcal{D}_s .

3.2 MOTIVATION

In a CDAR problem, labeled source data often has a different distribution with target data. For example, source data may be collected from the sensor tied on the front right hip while target data may contain waist-mounted smartphone data. When we perform rough distribution matching which aligns whole data or aligns data based on classes, we may not be able to match data perfectly since different people have their styles even performing the same activity.

The raw activity data can be represented as $\mathbf{x} = \mathbf{z} + \boldsymbol{\delta}$, where $\mathbf{z} \in \mathbb{R}^d$ represents the activity prototype which contains the data collected from the person's standard activity in an ideal situation and $\boldsymbol{\delta}$ corresponds to the noise when performing the action. Therefore, sample-level matching that aligns \mathbf{x} directly may introduce noise, and performing sample-level matching might have no practical meaning. Overall, a compromise between rough matching and sample-level matching is needed to obtain more fine-grained alignments and avoid noise influence.

$$p(\mathbf{x}) = \sum_y p(\mathbf{x}|y)p(y) \quad (1a)$$

$$\begin{aligned} &= \sum_y (\sum_o p(\mathbf{x}, o|y))p(y) \\ &= \sum_y \sum_o p(\mathbf{x}|y, o)p(y, o) \end{aligned} \quad (1b)$$

$$\begin{aligned} &= \sum_o \sum_y p(\mathbf{x}|y, o)p(y|o)p(o) \\ &= \sum_o p(\mathbf{x}|o)p(o). \end{aligned} \quad (1c)$$

Apart from empirical analysis, we analyze our motivation theoretically in the following. Corresponding to Equation 1a, we know domain-level matching tries to match $p(\mathbf{x})$ while class-level matching tries to match $p(\mathbf{x}|y)$. From the previous analysis, we know that one class may include more than one substructure, which means class-level matching may not be enough. Therefore, a deeper decomposition of \mathbf{x} is needed. We introduce o and each y contains multiple o . As shown in Equation 1b, we can divide the source domain into more fine-grained groups since we have known the labels of data in the source domain. Due to no information offered about the target domain's labels, further conversion is performed and Equation 1c shows we can divide the target domain into finer substructures.

In fact, Equation 1b and Equation 1c express the same meaning. We know that

$$p(y|o) = \begin{cases} 1 & o \text{ is part of } y \\ 0 & \text{o.w.} \end{cases} \quad (2)$$

We denote the class of o as y_o . We can get $\sum_y \sum_o p(\mathbf{x}|y, o)p(y, o) = \sum_o p(\mathbf{x}, y_o|o)p(o)$, which is like as Equation 1c. Now, we can match $p(\mathbf{x}|o)$. Obviously, SSDA uses a more fine-grained matching, which considers more detailed invariant features, compared with domain- and class-level matching while it avoids the influence of noise via the use of substructures compared with sample-level matching.

From Table 1, we can see the main characters of the different matching methods.

Table 1: Comparison between different matching schemes

Type	Assumption	Formulation	Limitations
Domain-level	domain-invariant features	$p(\mathbf{x}_s) \leftrightarrow p(\mathbf{x}_t)$	too coarse matching
Class-level	class-invariant features	$p(\mathbf{x}_s y_s) \leftrightarrow p(\mathbf{x}_t y_t)$	coarse matching
Substructure-level	substructure-invariant features	$p(\mathbf{x}_s, y_s c_s) \leftrightarrow p(\mathbf{x}_t c_t)$	
Sample-level	no strict restrictions	$(\mathbf{x}_s, y_s) \leftrightarrow \mathbf{x}_t$	affected by noise, low-efficiency

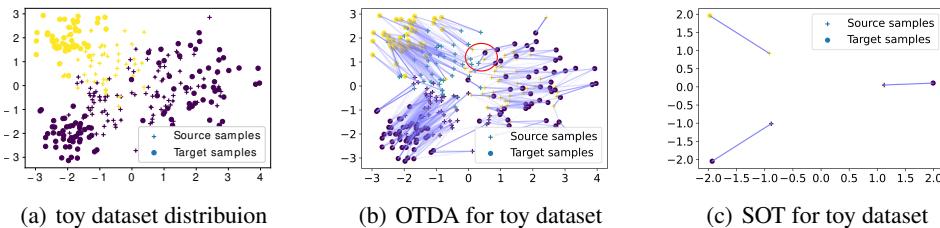


Figure 2: Toy example to show the effectiveness of substructure-level matching

To explain the necessity of using the substructures more clearly, we give a toy example. As we can see from Figure 2(a), the source has three clusters that are sampled from a GMM and the target also

has three clusters sampled from a slightly different GMM. Both of the domains have two classes while the different colors respond to the different classes. It is obvious that one of the classes has two components, which means rough matching may not be suitable. Next, we consider the sample-level matching. The concrete data can be treated as the noisy version of the prototypes, i.e. the cluster centers adding perturbation. As Figure 2(b) shows, if we directly match two domains with concrete data points, miss matching may come into being. The red circle in Figure 2(b) points one miss matching. Intuitively speaking, the matching of noise points to noise points has no practical meaning. And Figure 2(c) demonstrates SSDA is a possible solution.

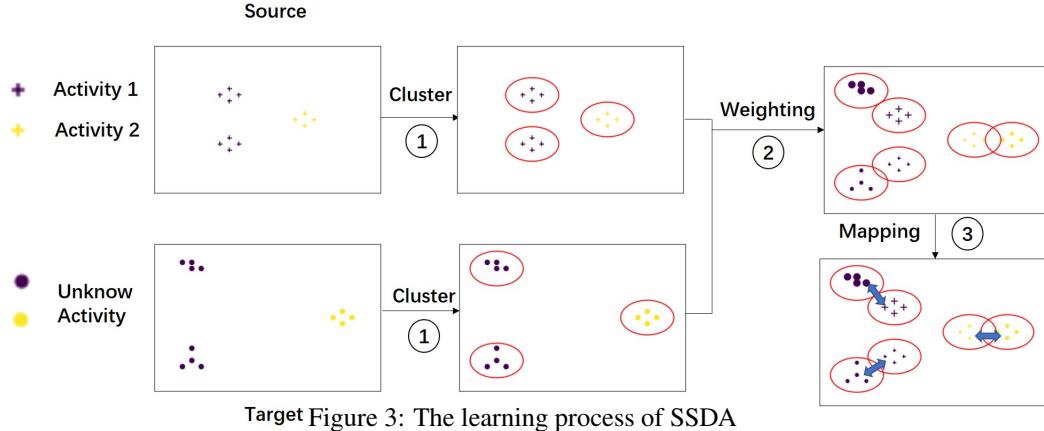


Figure 3: The learning process of SSDA

3.3 SSDA: A GENERAL FRAMEWORK FOR DOMAIN ADAPTATION

In this paper, we propose a general **Substructural Domain Adaptation (SSDA)** method. SSDA designs a general framework consistent with the substructure and Figure 3 illustrates the main process of SSDA which mainly contains three steps. Firstly, SSDA clusters the data and obtains the substructures of activities. As a general framework, we can choose a suitable clustering algorithm to customize our own method. Then, it gives weights to the source substructures according to priors or adaptive methods. Weight represents the importance of substructures and different substructures often play different roles. For example, some substructures far away from most data should play small roles with small weights. For simplicity, we usually give uniform weights to all structures without priors. Finally, mapping is performed on the substructures of different domains. We can extend some traditional method, such as CORrelation alignment (CORAL) Sun et al. (2015), to perform substructure-level matching, which is really commendable.

3.4 SOT: AN OT IMPLEMENTATION OF SSDA

In this section, we propose an OT implementation of SSDA, named SOT. SOT utilizes GMM to get substructures while it uses OT to perform weighting and mapping. According to the substructures' representation, we introduce SOT_c with center representation and SOT_g with distribution representation.

3.4.1 SUBSTRUCTURES GENERATION AND REPRESENTATIONS

As we know, $\delta \sim \mathcal{N}(0; \sigma^2)$ and \mathbf{X} represents all feature data. Equivalently, \mathbf{X}^k conforms to another Gaussian distribution whose center is the corresponding prototypes, i.e. $\mathbf{X}^k \sim \mathcal{N}(\mathbf{z}^k, \sigma^k)$. \mathbf{z}^k means the k th center's value, σ^k means the k th covariance, and \mathbf{X}^k means the data belong to the k th cluster. Now, we have data \mathbf{X} and our goal is to get \mathbf{z}^k and σ^k . It is easy to use Expectation Maximum (EM) Dempster et al. (1977) algorithm to obtain the parameters of the Gaussian Mixture Models.

To maintain label consistency in the source domain, we treat the source domains as a mixture distribution of C Gaussian mixture models and each Gaussian Mixture Model corresponds to one class in the source domain. The number of components is determined by the Bayesian Information Criterion

(BIC) Schwarz et al. (1978), i.e.

$$BIC = -2 \ln(L) + k \ln(m). \quad (3)$$

L represents the maximized value of the likelihood function for the estimated model, k represents the number of free parameters to be estimated, and m is the sample size. We seek K which minimizes BIC. Due to the lack of labels in the target domain, we have to perform clustering on the entire target domain and the number of clusters is up to the specific dataset.

After getting the clusters in the source domain and the target domain, we design two different ways to represent the substructures which correspond to SOT_c and SOT_g respectively. SOT_c with center representation utilizes only cluster centers' information, and it is simple and computationally efficient while SOT_g with distribution considers more information on clusters, but it needs some approximations when computing.

SOT_c : After clustering, two domains are expressed as the cluster centers, i.e. $\mu_s^c = \sum_{i=1}^{k_s} w_i^s \delta_{\mathbf{z}_i^s}$, $\mu_t^c = \sum_{i=1}^{k_t} w_i^t \delta_{\mathbf{z}_i^t}$. $\mathbf{z} \in \mathbb{R}^D$ represents the cluster centers and $\delta_{\mathbf{z}}$ is a Dirac function at location \mathbf{z} . μ_s^c, μ_t^c are distributions of the source domain and the target domain respectively and w are probability masses associated to the \mathbf{z} . Obviously, $\sum_{i=1}^{k_s} w_i^s = 1$, $\sum_{i=1}^{k_t} w_i^t = 1$. In addition, the squared Euclidean distance can be chosen as the cost between \mathbf{z}_i^s and \mathbf{z}_j^t , i.e.

$$c(\mathbf{z}_i^s, \mathbf{z}_j^t) = \|\mathbf{z}_i^s - \mathbf{z}_j^t\|_2^2. \quad (4)$$

SOT_g : This one utilizes the cluster distributions to represent the substructures, and the covariance of the clusters can be understood as the difficulty of the activity for the person. Therefore, the source domain can be expressed as $\mu_s^g = \sum_{i=1}^{k_s} w_i^s \mathcal{N}(\mathbf{z}_i^s, \boldsymbol{\sigma}_i^s)$ and the target domain can be expressed as $\mu_t^g = \sum_{i=1}^{k_t} w_i^t \mathcal{N}(\mathbf{z}_i^t, \boldsymbol{\sigma}_i^t)$. The meanings of the symbols are similar to the first way. The only difference is that we use a Gaussian distribution $\mathcal{N}(\mathbf{z}, \boldsymbol{\sigma})$ instead of a Dirac function $\delta_{\mathbf{z}}$. In this situation, the squared wasserstein distance Peyré et al. (2019) takes places of the squared Euclidean distance and serves as the cost function, i.e.

$$\begin{aligned} c(\mathcal{N}(\mathbf{z}_i^s, \boldsymbol{\sigma}_i^s), \mathcal{N}(\mathbf{z}_j^t, \boldsymbol{\sigma}_j^t)) &= W_2^2(\mathcal{N}(\mathbf{z}_i^s, \boldsymbol{\sigma}_i^s), \mathcal{N}(\mathbf{z}_j^t, \boldsymbol{\sigma}_j^t)) \\ &= \|\mathbf{z}_i^s - \mathbf{z}_j^t\|^2 + B(\boldsymbol{\sigma}_i^s, \boldsymbol{\sigma}_j^t)^2. \end{aligned}$$

B is the Bures metric Bhatia et al. (2019) between positive definite matrices and can be calculated as follows,

$$B(\boldsymbol{\sigma}_i^s, \boldsymbol{\sigma}_j^t)^2 = \text{tr}(\boldsymbol{\sigma}_i^s + \boldsymbol{\sigma}_j^t - 2(\boldsymbol{\sigma}_i^{s1/2} \boldsymbol{\sigma}_j^t \boldsymbol{\sigma}_i^{s1/2})^{1/2}), \quad (5)$$

where $\text{tr}(\cdot)$ denotes the trace of a matrix, $\boldsymbol{\sigma}^{1/2}$ is the matrix square root. For simplicity, we force the covariance matrix to be a diagonal matrix, i.e. $\boldsymbol{\sigma} = \text{diag}(r_i)_{i=1}^d$. In this case, the Bures metric is the Hellinger distance $B(\boldsymbol{\sigma}_i^s, \boldsymbol{\sigma}_j^t) = \|\sqrt{\mathbf{r}_i^s} - \sqrt{\mathbf{r}_j^t}\|$. Overall, the cost function is

$$\begin{aligned} c(\mathcal{N}(\mathbf{z}_i^s, \boldsymbol{\sigma}_i^s), \mathcal{N}(\mathbf{z}_j^t, \boldsymbol{\sigma}_j^t)) &= \|\mathbf{z}_i^s - \mathbf{z}_j^t\|^2 + \|\sqrt{\mathbf{r}_i^s} - \sqrt{\mathbf{r}_j^t}\|_2^2 \\ &= \|(\mathbf{z}_i^s, \sqrt{\mathbf{r}_i^s}) - (\mathbf{z}_j^t, \sqrt{\mathbf{r}_j^t})\|_2^2. \end{aligned} \quad (6)$$

\mathbf{r}_i^s and \mathbf{r}_j^t represent diagonals of the i th source domain cluster's covariance and the j th target domain cluster's covariance respectively. $(\mathbf{z}, \sqrt{\mathbf{r}})$ concatenates the \mathbf{z} and $\sqrt{\mathbf{r}}$ and serves as the new feature of the substructure.

3.4.2 WEIGHTING SOURCE SUBSTRUCTURES

For unity, we denote the source domain as $P_s = \sum_{i=1}^{k_s} w_i^s p_i^s$ and denotes the target domain as $P_t = \sum_{i=1}^{k_t} w_i^t p_i^t$. Due to little information about the target domain, we treat p_i^t equally and fix w_i^t to $1/k_t$. Now, we compute the w_i^s adaptively.

Since we only know $\sum_{i=1}^{k_s} w_i^s = 1$, it can be seen as a partial optimal transport problem, and the upper bounds of w_i^s are all 1. Obviously, the total cost of the partial optimal transport is $\langle \pi, \mathbf{C} \rangle_F$, where $\langle \cdot, \cdot \rangle_F$ is the Frobenius dot product, \mathbf{C} is the cost matrix, and π is the coupling matrix between

two PDFs. For calculation convenience, an entropy item, i.e. $H(\boldsymbol{\pi}) = \sum_{ij} \pi_{ij} \log \pi_{ij}$, is added. Now, our goal is to obtain the optimal transport.

$$\begin{aligned}\boldsymbol{\pi}_1^* &= \arg \min_{\boldsymbol{\pi}} \langle \boldsymbol{\pi}, \mathbf{C} \rangle_F + \lambda_1 H(\boldsymbol{\pi}) \\ s.t \quad &\boldsymbol{\pi}^T \mathbf{1}_{k_s} = \mathbf{w}^t \\ &\boldsymbol{\pi} \mathbf{1}_{k_t} \leq \mathbf{1}_{k_s} \\ &\mathbf{1}_{k_t}^T \boldsymbol{\pi}^T \mathbf{1}_{k_s} = 1.\end{aligned}\tag{7}$$

$\mathbf{1}_k$ is k-dimensional vector of ones and λ_1 is a hyper-parameter that balances the calculation speed and accuracy. $H(\boldsymbol{\pi})$ requires $\boldsymbol{\pi} \geq 0$. When $\boldsymbol{\pi} \geq 0$ and $\mathbf{1}_{k_t}^T \boldsymbol{\pi}^T \mathbf{1}_{k_s} = 1$, it is obvious that $\boldsymbol{\pi} \mathbf{1}_{k_t} \leq \mathbf{1}_{k_s}$ always holds. In addition, $\mathbf{1}_{k_t}^T \mathbf{w}^t = 1$ holds, which means $\mathbf{1}_{k_t}^T \boldsymbol{\pi}^T \mathbf{1}_{k_s} = 1$ also always holds. Therefore, Equation 7 can be simplified as the following.

$$\begin{aligned}\boldsymbol{\pi}_1^* &= \arg \min_{\boldsymbol{\pi}} \langle \boldsymbol{\pi}, \mathbf{C} \rangle_F + \lambda_1 H(\boldsymbol{\pi}) \\ s.t \quad &\boldsymbol{\pi}^T \mathbf{1}_{k_s} = \mathbf{w}^t.\end{aligned}\tag{8}$$

We denote the feasible solution set of $\boldsymbol{\pi}^T \mathbf{1}_{k_s} = \mathbf{w}^t$ as C_1 . Obviously, the C_1 is a convex set. The optimization goal of Equation 8 is also convex. And, it is easy to get the closed form of this problem. In the following, the Lagrange method is adopted to solve the problem.

We denote ϕ as the Lagrange multiplier, then our goal can be derived as

$$L = \langle \boldsymbol{\pi}, \mathbf{C} \rangle_F + \lambda_1 H(\boldsymbol{\pi}) + \phi^T (\boldsymbol{\pi}^T \mathbf{1}_{k_s} - \mathbf{w}^t).$$

To get the optimal point, the following equations must hold.

$$\begin{cases} \frac{\partial L}{\partial \boldsymbol{\pi}} = 0 \\ \boldsymbol{\pi}^T \mathbf{1}_{k_s} - \mathbf{w}^t = \mathbf{0}. \end{cases}\tag{9a}$$

$$\boldsymbol{\pi}^T \mathbf{1}_{k_s} - \mathbf{w}^t = \mathbf{0}.\tag{9b}$$

According to Equation 9a, we can get $\mathbf{C} + \lambda_1(1 + \log \boldsymbol{\pi}) + \mathbf{1}_{k_s} \phi^T = \mathbf{0}$, which means

$$\boldsymbol{\pi} = e^{-\frac{\mathbf{1}_{k_s} \phi^T - \mathbf{C}}{\lambda_1} - 1}.\tag{10}$$

Then, we substitute Equation 10 into Equation 9b and get

$$e^{\frac{-\mathbf{1}_{k_s} \phi^T - \mathbf{C}}{\lambda_1} - 1} \mathbf{1}_{k_s} = \mathbf{w}_t.$$

Therefore, we get

$$e^{\frac{-\mathbf{C}}{\lambda_1} - 1} \odot e^{\frac{-\mathbf{1}_{k_s} \phi^T}{\lambda_1} - 1} \mathbf{1}_{k_s} = \mathbf{w}_t,$$

where \odot means element-wise product. Obviously, each element in the same row of $\exp(\frac{-\mathbf{1}_{k_s} \phi^T}{\lambda_1})$ is the same number, and we can easily get the optimal $\boldsymbol{\pi}^*$. We initialize $\boldsymbol{\pi}_0 = \exp(-\frac{\mathbf{C}}{\lambda_1} - 1)$ and get

$$\boldsymbol{\pi}_1^* = \boldsymbol{\pi}_0 \text{diag}(\mathbf{w}^t \oslash \boldsymbol{\pi}_0^T \mathbf{1}_{k_s}),\tag{11}$$

where \oslash denotes element-wise divide. Once the optimal coupling matrix $\boldsymbol{\pi}_1^*$ is obtained, the source weight can be easily calculated as $\mathbf{w}^s = \boldsymbol{\pi}_1^* \mathbf{1}_{k_t}$.

3.4.3 OT-BASED MAPPING OF THE SUBSTRUCTURES

Through the previous steps, the source domain distribution is $P_s = \sum_{i=1}^{k_s} w_i^s p_i^s$ while the target domain distribution is $P_t = \sum_{i=1}^{k_t} w_i^t p_i^t$. And the label corresponding to p_i^s is the label of the data belongs to i th cluster in the source domain, i.e. \bar{y}_i^s . According to Equation 4 or Equation 6, we can easily get the cost matrix \mathbf{C} . Following Courty et al. (2016), the objective for SOT is

$$\begin{aligned}\boldsymbol{\pi}^* &= \arg \min_{\boldsymbol{\pi}} \langle \boldsymbol{\pi}, \mathbf{C} \rangle_F + \lambda H(\boldsymbol{\pi}) + \eta \Omega(\boldsymbol{\pi}) \\ s.t \quad &\boldsymbol{\pi}^T \mathbf{1}_{k_s} = \mathbf{w}^t \\ &\boldsymbol{\pi} \mathbf{1}_{k_t} = \mathbf{w}^s.\end{aligned}\tag{12}$$

Algorithm 1 SOT: Substructural Optimal Transport

Input: source dataset $\mathcal{D}_s = \{(\mathbf{x}_i^s, y_i^s)\}_{i=1}^{n_s}$, target dataset $\mathcal{D}_t = \{(\mathbf{x}_i^t)\}_{i=1}^{n_t}$, hyper-parameters $\lambda_1, \lambda, \eta, k_t$

Output: target labels $\{y_i^t\}_{i=1}^{n_t}$

- 1: Use EM for GMM, cluster each class data in the source domain to obtain $\{(\mathbf{p}_i^s, \tilde{y}_i^s)\}_{i=1}^{k_s}$. The number of clusters is determined by Equation 3.
 - 2: Use EM for GMM to obtain $\{(\mathbf{p}_i^t)\}_{i=1}^{k_t}$
 - 3: Compute cost matrix \mathbf{C} according Equation 4 (SOT_c) or Equation 6 (SOT_g)
 - 4: Use Equation 11 to compute the source substructures' weights \mathbf{w}^s . Set $\mathbf{w}^t = \frac{\mathbf{1}_{k_t}}{k_t}$
 - 5: Use GCG to compute the optimal coupling matrix $\boldsymbol{\pi}^*$
 - 6: According to Equation 13, compute the transformation of the source substructures and obtain $\hat{\mathbf{P}}^s$
 - 7: Use $\hat{\mathbf{P}}^s$ and $\tilde{\mathbf{Y}}^s$ to build the model and predict the \mathbf{P}^t . The predictions are noted as $\tilde{\mathbf{Y}}^t$
 - 8: Assign \tilde{y}_i^t to the data belonging to p_i^t in the target domain
-

$\Omega(\boldsymbol{\pi})$ is group-sparse regularizer, and it expects that each target sample receives masses only from source samples that have the same label. And following Courty et al. (2016), we define the regularizer as $\Omega(\boldsymbol{\pi}) = \sum_j \sum_{cl} \|\boldsymbol{\pi}(I_{cl}, j)\|_2$, where $\|\cdot\|_2$ denotes the l_2 norm and I_{cl} contains the indices of rows in $\boldsymbol{\pi}$ related to source domain samples of class cl . $\boldsymbol{\pi}(I_{cl}, j)$ is a vector containing coefficients of the j th column of $\boldsymbol{\pi}$ associated to class cl , and it induces the desired sparse representation in the target samples. λ and η are hyper-parameters. We use generalized conditional gradient (GCG) following Courty et al. (2016) to solve the optimization problem.

Once the optimal coupling matrix $\boldsymbol{\pi}^*$ is obtained, we can compute the transformation of \mathbf{p}_i^s according to the barycentric mapping, i.e. $\hat{\mathbf{P}}^s = \arg \min_{\mathbf{P}} \sum_j \boldsymbol{\pi}^*(i, j) c(\mathbf{p}, \mathbf{p}_j^t)$. When the cost function is the squared l_2 distance, this barycentric mapping can be expressed as:

$$\hat{\mathbf{P}}^s = \text{diag}(\boldsymbol{\pi}^* \mathbf{1}_{k_t})^{-1} \boldsymbol{\pi}^* \mathbf{P}^t, \quad (13)$$

where \mathbf{P}^t represents the target representation and $\hat{\mathbf{P}}^s$ represents the source mapping representation. Now, any traditional machine learning model, such as 1-Nearest Neighbor (1NN), can be used to learn the predictions with help of $\hat{\mathbf{P}}^s$ and \tilde{y}_i^s . After getting the label \tilde{y}_i^t corresponding to p_i^t , we assign the same label, \tilde{y}_i^t , to the data belonging to p_i^t in the target domain.

The overall process of SOT is described in Algorithm 1.

4 EXPERIMENTAL EVALUATION

In this section, we evaluate the performance of SOT via extensive experiments on cross-domain activity recognition.

4.1 DATASET AND PREPROCESSING

We adopt four common public datasets. Table 2 describes the information of the four public datasets and demonstrates the selected data volume. In the following, we briefly introduce the basic information of each dataset, and more information can be found in their original papers.

UCI daily and sports dataset (DSADS, D) Barshan & Yiuksek (2014) consists of 19 activities collected from 8 subjects wearing body-worn sensors on 5 body parts. UCI human activity recognition using smartphones data set (UCI-HAR, H) Anguita et al. (2012) is collected by 30 subjects performing 6 daily living activities with a waist-mounted smartphone. USC-SIPI human activity dataset (USC-HAD, U) Zhang & Sawchuk (2012) composes of 9 subjects executing 12 activities with a sensor tied on the front right hip. PAMAP2 physical activity monitoring dataset (PAMAP2, P) Reiss & Stricker (2012) contains data of 18 different physical activities, performed by 9 subjects wearing 3 sensors.

The cross-domain activity recognition experimental setup is in the following ways. Since different datasets use different sensors and contain different classes of activities, we need to unify our experi-

Table 2: Information of four datasets. Num means the select data volume.

Dataset	Subject	Activity	Sample	Location	Num
DSADS	8	19	1.14M	Tarso, Right Arm, Left Arm, Right Leg, Left Leg	2400
UCI-HAR	30	6	1.31M	Waist	6616
USC-HAD	14	12	2.81M	Front Right Hip	4187
PAMAP	9	18	2.84M	Wrist, Chest, Ankle	1688

mental setup for datasets first, and we choose the common parts of the sensors and four common categories of activities. Specifically, we utilize the accelerometer and gyroscope, and each sensor provides 3-axial data (x-, y- and z-axis). For convenience, we combine them by $\alpha = \sqrt{x^2 + y^2 + z^2}$. Then, according to Wang et al. (2018a), we exploit the sliding window technique to extract features, and 19 features from both time and frequency domains are extracted for a single sensor. We extract 38 features from one position since two sensors are selected. We choose data from Right Arm, Waist, Front Right Hip, and Right Wrist from these four datasets respectively, and choose four categories, including lying, walking, ascending, descending. In experiments, we perform unsupervised domain adaptation on the target domain.

4.2 COMPARISON METHODS AND IMPLEMENTATION DETAILS

We adopt eight comparison methods:

1. Baseline models
 - 1NN: 1-Nearest Neighbor.
 - LMNN: Large margin nearest neighbor Weinberger & Saul (2009).
2. Rough matching
 - TCA:Transfer component analysis Pan et al. (2010).
 - SA:Subspace alignment Fernando et al. (2013).
 - CORAL:CORrelation alignment Sun et al. (2015).
3. Sample-level matching
 - OT:Optimal transport Cuturi (2013).
 - OTDA: Optimal transport for domain adaptation Courty et al. (2016).
 - MLOT: Metric learning optimal transport Kerdoncuff et al. (2020).

1NN and LMNN serve as baseline models and TCA, SA, and CORAL perform the rough matching while OT, OTDA, and MLOT belong to sample-level matching methods. And all of these methods use a 1NN classifier for the classification tasks. We conduct experiments in every pair of four datasets and construct 12 tasks in total.

For a particular hyper-parameter configuration, we follow the similar protocol used in Courty et al. (2016). The target domain is partitioned in validation and test sets. The validation set is used to obtain the best accuracy in the range of the possible hyper-parameters. The hyper-parameter range used follows Kerdoncuff et al. (2020) and we slightly reduce the range to fit our task. With the best selected hyper-parameters, we evaluate the performance on the testing set. Classification accuracy on the target domain is adopted as the evaluation metric.

4.3 CLASSIFICATION RESULTS

The results of classification are shown in Table 3 and Figure 4. From these results, we can have the following observations: 1) Both SOT_c and SOT_g achieve the best classification accuracy on all tasks. It is obvious that SOT significantly outperforms other methods with a remarkable improvement (over 10% on the average). 2) Compared to baseline methods, rough matching methods almost have no improvements, which may be caused by the details neglected, while sample-level matching methods only have slight improvements due to too much noise. Thus, being too rough or too delicate is not suitable for cross-dataset activity recognition. 3) Lying is easy to identify correctly while walking, ascending and descending are difficult to classify, which is in line with the intuition and is

Table 3: Results on 12 tasks

methods	D→H	D→U	D→P	H→D	H→U	H→P	U→D	U→H	U→P	P→D	P→H	P→U	AVG
NA	62.70	56.40	66.03	65.16	55.03	60.81	71.30	61.38	60.37	60.99	55.26	51.63	60.59
LMNN	55.24	65.74	48.38	64.27	56.55	65.00	64.58	65.46	67.13	59.53	39.11	41.21	57.68
TCA	60.79	51.98	65.66	62.50	41.87	52.06	69.06	53.43	60.88	57.81	46.38	51.45	56.16
SA	63.61	57.36	65.44	66.35	55.60	60.88	70.62	59.64	61.18	62.60	55.45	50.58	60.78
CORAL	64.23	52.25	64.85	64.48	53.03	64.41	68.75	61.93	60.15	60.21	56.20	54.46	60.41
OT	62.13	65.86	65.66	68.91	58.58	67.50	69.90	59.49	63.75	66.77	51.71	57.59	63.15
OTDA	59.36	54.97	65.52	68.91	59.45	67.50	70.26	62.25	63.09	67.19	53.41	59.09	62.58
MLOT	62.53	53.33	64.85	68.12	58.10	62.13	69.53	59.68	61.25	65.99	63.30	49.24	61.51
SOT _c	67.74	79.74	73.31	73.39	70.87	73.23	80.99	78.04	74.41	76.46	72.82	76.51	74.79
SOT _g	74.84	79.74	68.68	73.39	71.26	73.23	79.90	72.82	72.28	74.48	72.82	76.51	74.16

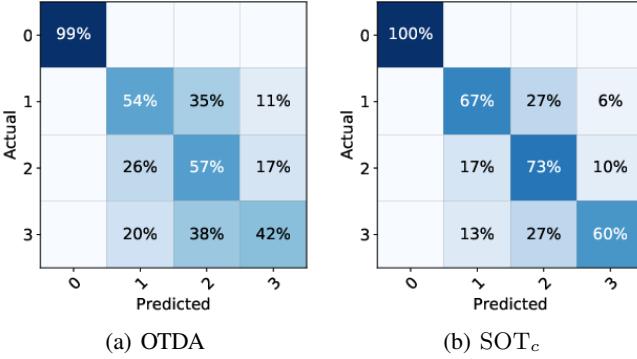


Figure 4: Confusion matrices for $U \rightarrow D$

consistent with Figure 1(a). 4) SOT_g is slightly worse than SOT_c. Maybe because SOT_g uses more approximations when computing. In the following experiments, we use SOT_c by default if there is no special instruction.

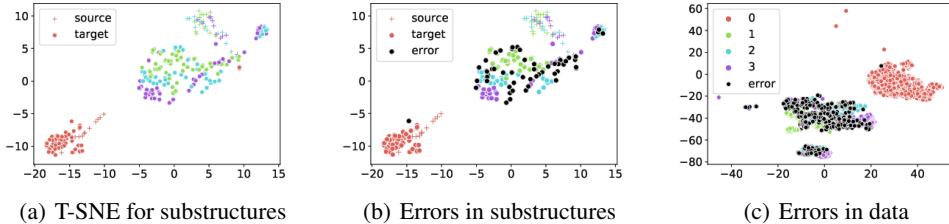


Figure 5: Visualization for $U \rightarrow D$ using SOT. Different colors mean different classes while black means error predictions. The boundaries of different colors correspond to the boundaries of different classes.

4.4 VISUALIZATION STUDY

As we can see in Figure 5(a), the number of points is much smaller after clustering, which can bring high efficiency, and the margins between points are bigger. The class of the substructures in the target domain is temporarily determined by most of the data in the corresponding cluster. In Figure 5(b), we can see that it is easy to misclassify the points which are near the margins or intersected with other classes' points. Due to the bigger margins and the fewer intersecting points, the accuracy on the substructures is 73% while the accuracy on raw data using OTDA is 70.375%. Figure 5(c) shows the misclassified data using SOT_c and the accuracy is improved over 10% due to the exploitation of the substructures.

4.5 ABLATION STUDY

We first demonstrate SSDA is not limited to its OT implementation (i.e., SOT), but a general framework, and then evaluate the importance and robustness of three important parts of SOT, namely, substructures generation, weighting source substructures and OT-based mapping of substructures.

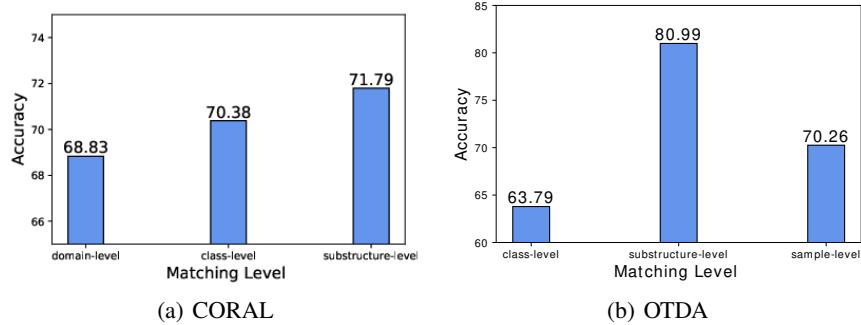


Figure 6: Accuracy of different matching levels with different methods for task $U \rightarrow D$

4.5.1 SSDA

We implement CORAL with domain-, class- and substructure-level matching and Figure 6(a) shows that class-level matching CORAL gets better accuracy than domain-level matching while substructure-level matching CORAL achieves the best accuracy, which demonstrates finer matching gets better results. In addition, we implement OTDA with class-, substructure- and sample-level matching, and Figure 6(b) illustrates that substructure-level matching OTDA gets a better accuracy than the sample-level matching OTDA, which may be substructure-level matching is robust to noise. Overall, Figure 6 demonstrates SSDA is a general framework and can achieve commendable results.

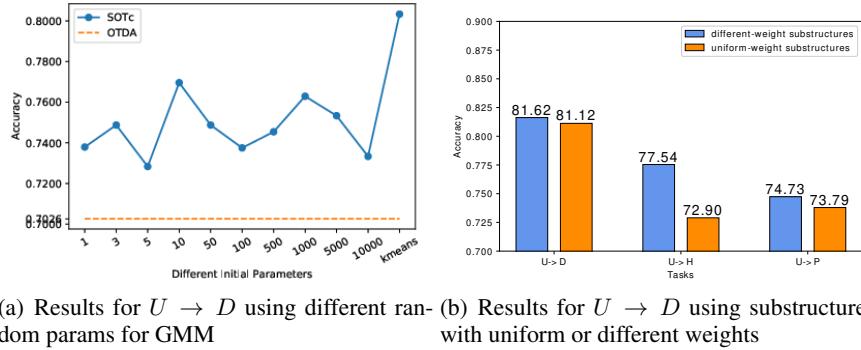


Figure 7: Ablation study of substructures generation and weighting source substructures

4.5.2 SUBSTRUCTURES GENERATION

We generate substructures with GMM using different initial parameters and the results are in Figure 7(a). The x-axis shows the different initial states. Obviously, SOT performs better than OTDA on any random initial states. The initial parameters obtained from k-means get the best accuracy, which indicates that good clustering results bring high accuracy.

4.5.3 WEIGHTING SOURCE SUBSTRUCTURES

To demonstrate the effect of weighting source substructures, we compare the accuracy between the experiments with it and without it. Without weighting source substructures, we simply assign

the same weight to all the source substructures. Figure 7(b) shows there is an improvement with weighting source substructures.

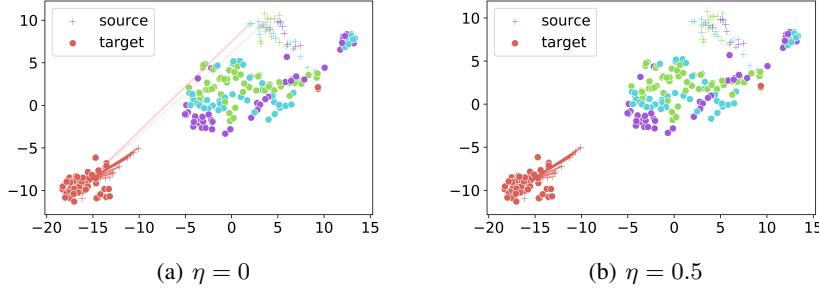


Figure 8: The group regularizer’s function

4.5.4 OT-BASED MAPPING OF SUBSTRUCTURES

In this part, we illustrate the function of the group regularizer. No group regularizer is used in Figure 8(a) while there is a group regularizer with $\eta = 0.5$ is used in Figure 8(b). In Figure 8(a), some points with different colors are linked with the red point while only red points are linked with the red point in Figure 8(b), which are caused by the group regularizer.

4.6 PARAMETER SENSITIVITY

In this section, we evaluate the parameter sensitivity of SOT. SOT involves four parameters: λ_1 , λ , η and k_t . We change one parameter and fix the other parameters to observe the performance of SOT. In Figure 9, the red points are the optimal points, and we observe the surrounding results. From 9(a)-9(d), we can see that the results with parameters around the red points are all better than OTDA. The results reveal that SOT is more effective and robust than other methods under different parameters near the optimal.

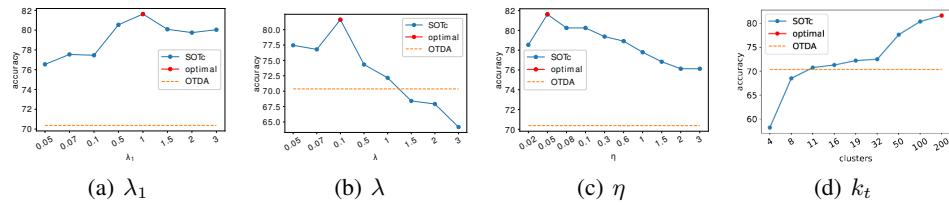


Figure 9: Influence of different hyper-parameters

4.7 CONVERGENCE AND TIME COMPLEXITY

In this section, we investigate the convergence and time complexity. In Figure 10(a), we can see SOT converges in the 10th epoch. And in the actual experiments, 20 epochs are enough for SOT. This means our SOT can reach fast convergence.

To compare the time complexity, we conduct each experiment 10 times and sum over the time. Figure 10(b) indicates that SOT gets the best accuracy while the time spent is much less than TCA and MLOT. When we slightly change the parameters of OTDA, the time used changes from 71.11s to 285.32s. From Figure 10(c), we can see that GMMs use most of the time in SOT. These two parts can be fixed in real experiments, which means we only need to pay attention to the parts of weighting and mapping. Obviously, the time used in the weighting part is negligible, and the time used in the

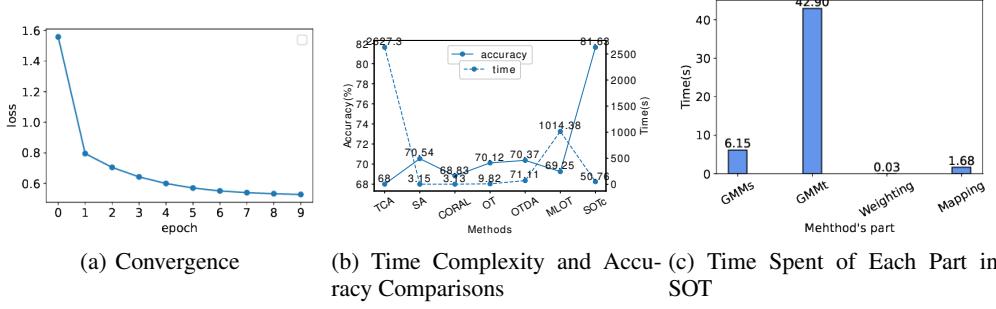


Figure 10: Convergence and Time Complexity

mapping part is smaller than all the other methods compared. In the following, we analyze the time complexity theoretically.

As we know, without the entropy regularizer, combinatorial algorithms, such as the simplex methods and its network variants, are used to solve the optimal transport. However, their computational complexity is shown to be $O((n_s + n_t)n_s n_t \log(n_s + n_t))$, which is impossible to handle large datasets. When handling the OT with the entropy regularizer, we can get an algorithm with the quadratic complexity, which is still below our expectations. The key problem is that n_s and n_t are too large to get the fast results. To deal with this problem, we use the substructures instead of initial data points. The numbers of the substructures are k_s and k_t respectively, and they are much smaller than n_s and n_t . To get the substructures, GMM, whose time complexity is $O(L_1 K N)$, is adopted. K is the number of clusters, N is the number of data, while L_1 is the number of iterations. We can get the weights of the substructures with one matrix operation and the time spent on this operation is negligible. To sum up, the time complexity of our method is about $O(L_1 K N + L_2 K^2)$, where L_1 and L_2 are the numbers of the iterations, and they are much smaller than N .

5 CONCLUSION AND FUTURE WORK

Leveraging labeled data from auxiliary domains is a usual way to deal with the label scarcity problem in Human Activity Recognition. In this paper, we propose SSDA to utilize substructures and propose an OT based implementation, SOT, for cross-domain activity recognition. Comparing to existing methods which perform rough matching or sample-level matching, SSDA obtains the internal substructures and completes substructures-level matching which considers more fine-grained structures of domains and is robust to noise in a certain degree. Comprehensive experiments on four large public datasets demonstrate the significant superiority of SOT over other state-of-the-art methods. In addition, SOT is much faster than other methods, which means it can be used in the larger datasets.

In the future, we plan to extend SOT using deep clustering, as well as applying SSDA to other fine-grained activity recognition problems.

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