# Inferring Probabilistic Reward Machines from Non-Markovian Reward Signals for Reinforcement Learning

- T. Dohmen<sup>1</sup>, N. Topper<sup>2</sup>, G. Atia<sup>2</sup>, A. Beckus<sup>3</sup>, A. Trivedi<sup>1</sup>, A. Velasquez<sup>3</sup>
- <sup>1</sup> University of Colorado Boulder, <sup>2</sup> University of Central Florida, <sup>3</sup>Air Force Research Laboratory

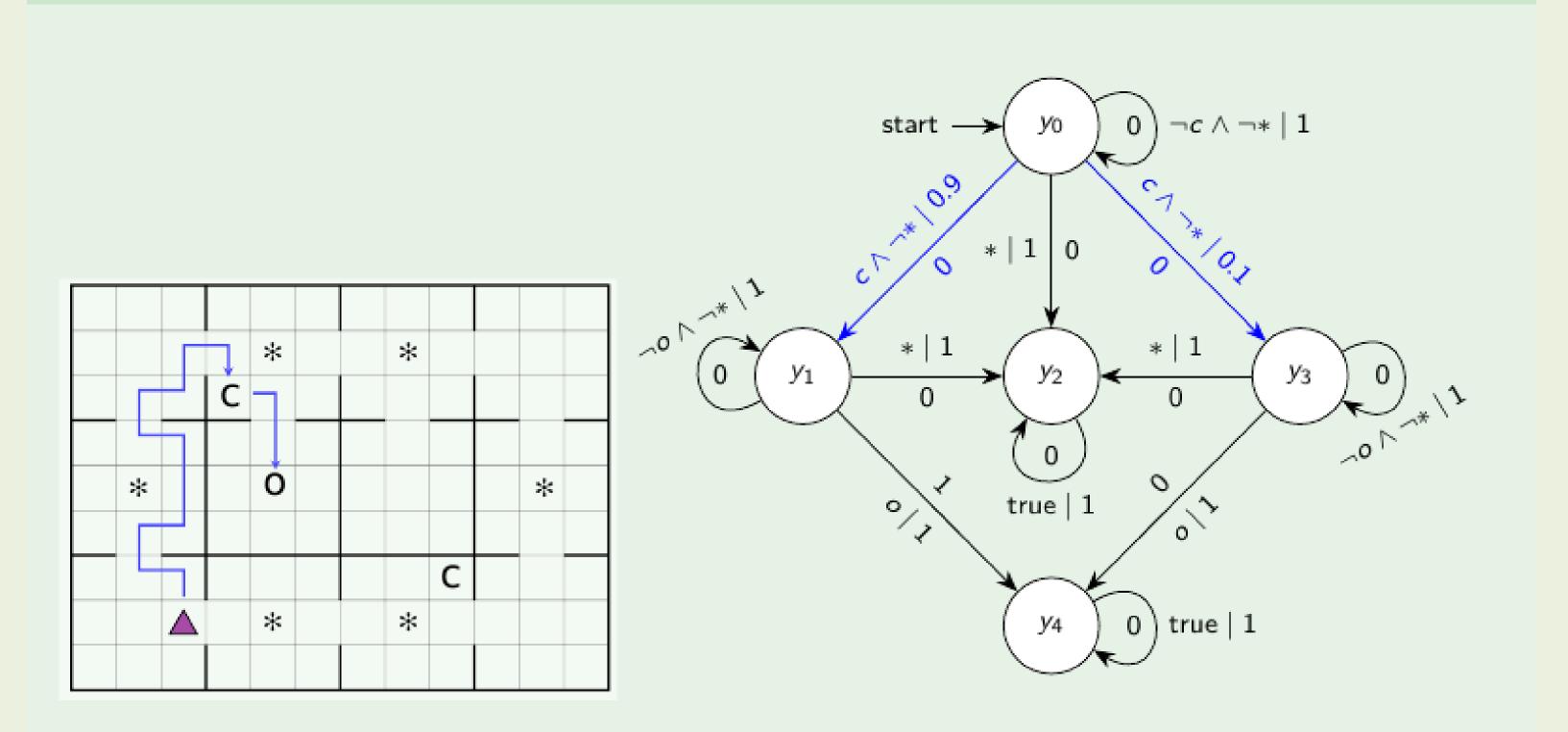
## Summary

- Reinforcement learning (RL) is typically predicated on the assumption that the reward signal is Markovian, i.e. depends only on the current state and action.
- •Reward machines have emerged as a structured representation based on the theory of finite automata of non-Markovian reward signals.
- We introduce and study probabilistic reward machines (PRMs) as representations of non-Markovian stochastic reward signals.

### Results

- •We prove that the product of a decision process and a PRM is a decision process with Markovian reward (MDP).
- •We formulate an inference procedure for learning PRMs that combines a sampling based variant of the L\* algorithm with an RL-driven sampling tehcnique.
- •We show that the algorithm coverges to a PRM encoding of the target reward function, assuming the reward function is sufficiently regular.
- •We prove an exponential upper bound on the state-space blowup for simulating a product MDP T x H of a decision process T and a PRM H by a product MDP U x J where the randomness of H is embedded in U and the non-Markovian dynamics of H preserved in J a deterministic reward machine.

## Example (Office gridworld and probabilistic reward machine)



#### Combining $L^*$ and RL for Learning PRMs Teacher reward frequency data Membership Agent Query $T \times H_w$ Sampling closed and RL Engine Observation consistent? Table $T \times H$ hypothesis H data Counterexample v Equivalence Query counterexample? NO $\longrightarrow$ return H