

# Who Needs These Operators Anyway: Top Quality Planning with Operator Subset Criteria

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## Introduction: Classical Planning and Beyond

An FDR **Planning task** is 5-tuple  $\Pi = \langle V, A, cost, I, G \rangle$ :

- $V$ : finite set of multi-valued (finite-domain) **state variables**
- $A$ : finite set of **actions** of form  $\langle pre, eff \rangle$  (preconditions/effects; partial variable assignments)
- $cost : A \mapsto \mathbb{R}^{0+}$  captures **action cost**
- $I$ : **initial state** (variable assignment)
- $G$ : **goal description** (partial variable assignment)

$\mathcal{P}_\Pi$  is the set of all plans for  $\Pi$

**Cost-optimal**: find one single plan  $\pi \in \mathcal{P}_\Pi$  minimizing summed action cost

**Top-quality planning** [Katz et al., AAAI 2020]:

**Given**: planning task  $\Pi$ , natural number  $q$

**Find**: the set of plans  $P = \{\pi \in \mathcal{P}_\Pi \mid cost(\pi) \leq q\}$ .

**Quotient top-quality planning** [Katz et al., AAAI 2020]:

**Given**: planning task  $\Pi$ , **equiv. relation**  $N$  over its set of plans  $\mathcal{P}_\Pi$ , natural number  $q$

**Find**:  $P \subseteq \mathcal{P}_\Pi$  such that  $\bigcup_{\pi \in P} N[\pi]$  is the solution to the top-quality planning.

**Unordered Top-quality Planning**:

$$\mathbf{U}_\Pi = \{(\pi, \pi') \mid \pi, \pi' \in \mathcal{P}_\Pi, \mathbf{MS}(\pi) = \mathbf{MS}(\pi')\}.$$

## Challenges in Top-quality Planning

- Top-quality set of plans can be quite large, sometimes infinite
- Unordered top-quality does not help in cases of infinite solution sizes
- Even in unordered top-quality planning, plans can be unnecessarily long

## Contributions

- Novel computational problem *subset top-quality planning*
- Solution (plan sets) are provably finite
- Planner based on task reformulation: extending ForbidIterative framework
- Theoretically stricter reformulation, forbidding more plans
  - Simpler and easier to solve: more tasks where solution is found
  - Solution set sizes are mostly the same

## Subset Top-quality Planning

### Subset Top-quality Planning Problem

**Given**: planning task  $\Pi$  and a natural number  $q$

**Find**: a set of plans  $P \subseteq \mathcal{P}_\Pi$  such that  $\forall \pi \in P, cost(\pi) \leq q$ , and  $\forall \pi' \in \mathcal{P}_\Pi \setminus P$  with  $cost(\pi') \leq q$ ,  $\exists \pi \in P$  such that

$$\mathbf{MS}(\pi) \subset \mathbf{MS}(\pi')$$

### Theorem (Finite Solution Size)

Given a planning task  $\Pi$  and a natural number  $q$ , a smallest subset top-quality planning problem solution  $P$  is of finite size.

**Proof hint**: cycle-free plans

## Subset Top-quality Planners

### ForbidIterative Subset Top-quality Planning Algorithm

**Input**:

Planning task  $\Pi$ ,  
quality bound  $q$

$P \leftarrow \emptyset$

$\Pi' \leftarrow \Pi$

$\pi \leftarrow$  shortest cost-optimal plan of  $\Pi'$

**while**  $cost(\pi) \leq q$  **do**

$\bar{\pi} \leftarrow \text{MAPPLANBACK}(\pi)$

$P \leftarrow P \cup \{\bar{\pi}\} \cup \{\pi' \mid \pi' \sim \bar{\pi}, \mathbf{MS}(\pi') \neq \mathbf{MS}(\bar{\pi})\}$

$\Pi' \leftarrow \Pi_{\mathcal{M}^+}^-$ , where  $\mathcal{M} = \{\mathbf{MS}(\pi') \mid \pi' \in P\}$

$\pi \leftarrow$  shortest cost-optimal plan to  $\Pi'$

**return**  $P$

- Solution, initially empty
- Current task
- Current plan

- Remove aux operators
- Extend with symmetries
- Reformulate

### Reformulation: MSQ

#### Variables

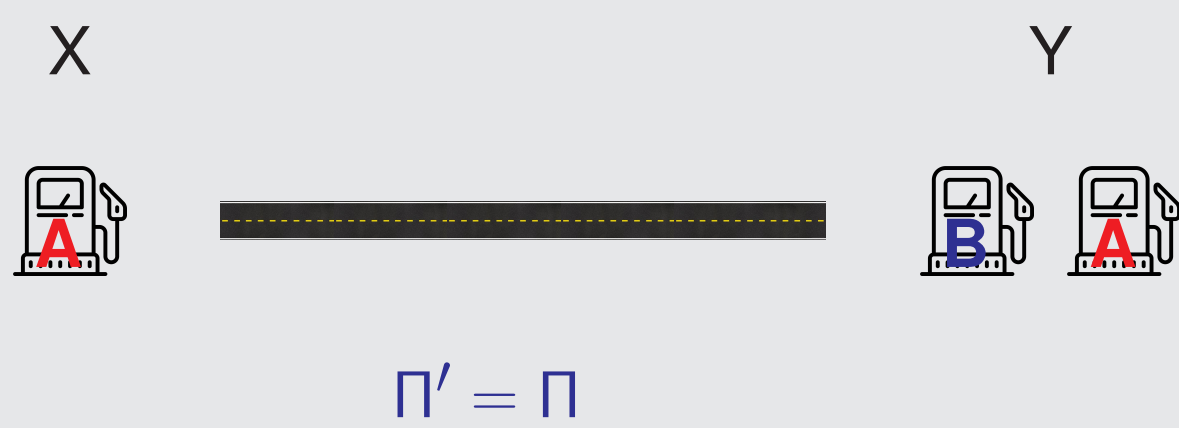
- additional variable  $\bar{v}$  checking off multisets in  $\mathcal{M}$
- additional counting variables  $\bar{v}_o$  per operator in multisets

#### Init & Goal

- $\bar{v}$  variable: initially 0, in goal  $|\mathcal{M}|$
- $\bar{v}_o$  variables: initially 0, not in goal

#### Operators

- per original operator: copies with additional pre and effects counting the number of appearances (up to max value in  $\mathcal{M}$ ), **while**  $\bar{v}$  is at its initial value
- additional operators: checking off multisets **once original goal is reached**



✓ Fuel A, move X Y, Fuel A  
 $\mapsto \Pi' = \Pi_{\mathcal{M}^+}^-$

✓ Fuel A, move X Y, Fuel B  
✗ Fuel A, move X Y, Fuel A  
✗ Fuel A, move X Y, Fuel A, Fuel B  
✗ Fuel A, move X Y, Fuel B, Fuel A

### Reformulation: SQ

#### Variables

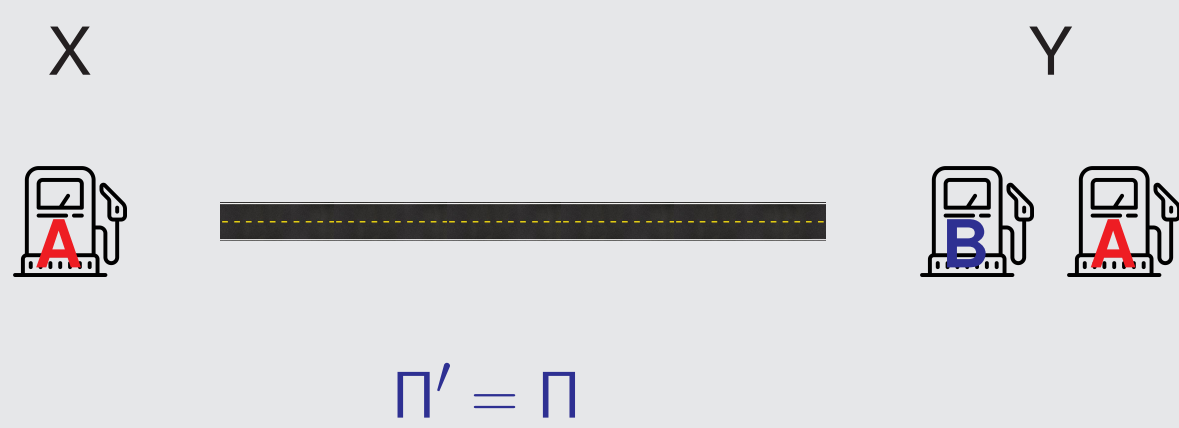
- additional variable  $\bar{v}$  checking off sets in  $\mathcal{M}$  ( $|\mathcal{M}| + 1$  values)
- additional binary variables  $\bar{v}_o$  per operator in sets

#### Init & Goal

- $\bar{v}$  variable: initially 0, in goal  $|\mathcal{M}|$
- $\bar{v}_o$  variables: initially 0, not in goal

#### Operators

- per original operator: additional pre and effects, setting  $\bar{v}_o = 1$  if in  $\mathcal{M}$ , **while**  $\bar{v}$  is at its initial value
- additional operators: checking off sets **once original goal is reached**



✓ Fuel A, move X Y, Fuel A  
 $\mapsto \Pi' = \Pi_{\mathcal{M}^+}^-$

✗ Fuel A, move X Y, Fuel B

$\Pi' = \Pi$

✓ Fuel A, move X Y, Fuel B  
 $\mapsto \Pi' = \Pi_{\mathcal{M}^+}^-$

✓ Fuel A, move X Y, Fuel A

## Evaluation

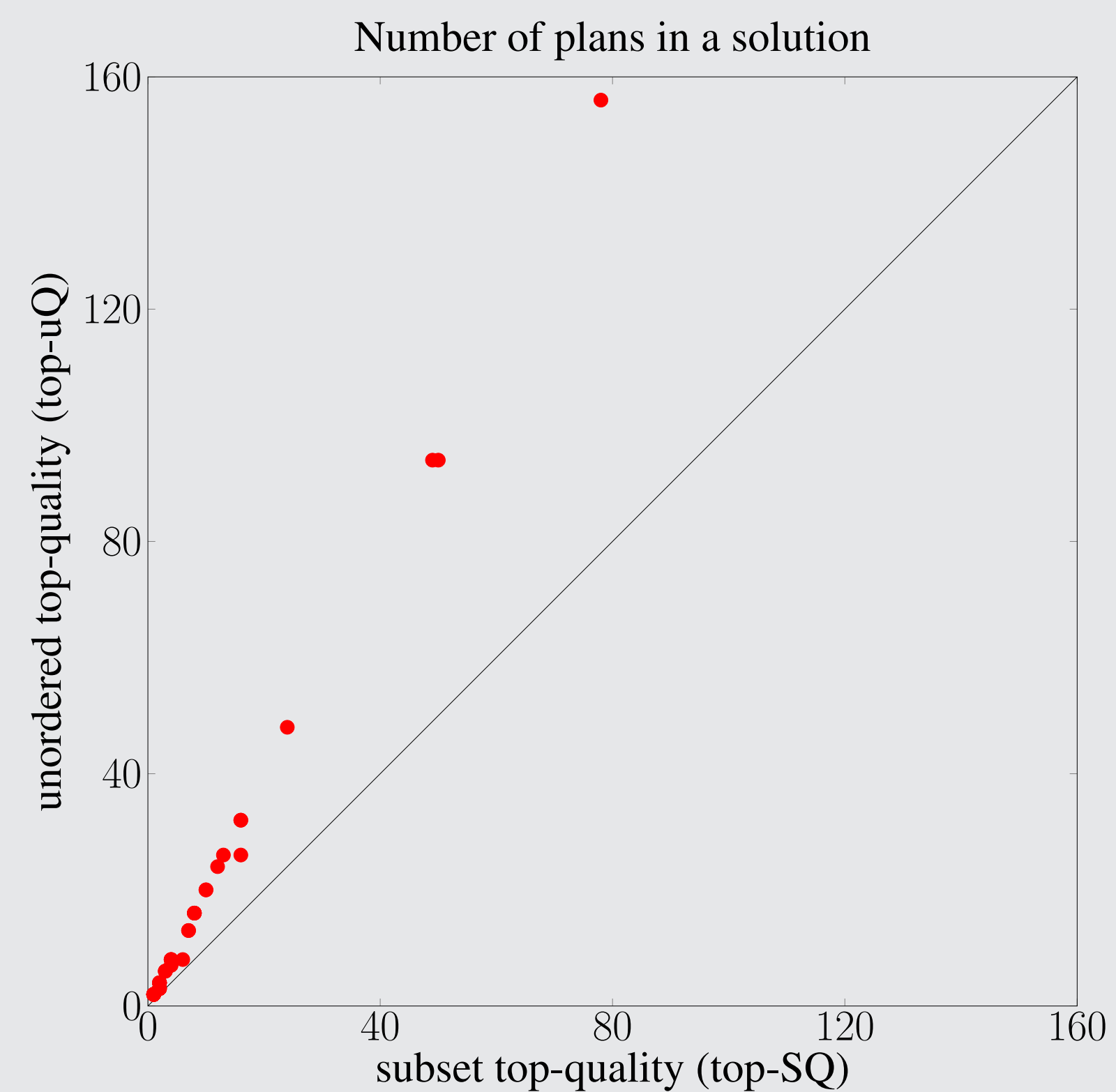
### Experimental Setting

- Comparing unordered top-quality planner to the suggested reformulations
- While they solve different problems, we compare in how many cases a solution could be found
- Compare solution size

### Coverage on IPC domains

Domain	top-uQ	top-MSQ	top-SQ
childsnaek14	0	<b>6</b>	<b>6</b>
data-network18	0	<b>4</b>	<b>4</b>
elevators08	0	<b>2</b>	<b>2</b>
gripper	5	<b>16</b>	<b>16</b>
miconic	15	<b>17</b>	16
movie	<b>1</b>	0	0
openstacks08	<b>2</b>	1	1
parcprinter08	<b>25</b>	24	24
parcprinter11	<b>18</b>	17	17
pipesworld-notankage	<b>8</b>	7	7
psr-small	45	45	<b>47</b>
satellite	2	<b>4</b>	<b>4</b>
scanalyzer08	4	<b>6</b>	<b>6</b>
scanalyzer11	1	<b>3</b>	<b>3</b>
sokoban08	0	0	<b>1</b>
storage	<b>11</b>	9	10
Sum	337	361	<b>364</b>

### Solution Size



## Summary and Future Work

- Introduced a new computational problem in top-quality planning
- Introduced planners based on planning task reformulation
- Shown the new planners to be more practical than existing (unordered) top-quality planners
- Future: improve the coverage of existing top-quality planners, for all computational problems