

Assignment 24

A loop with the double length of the edges needs twice more *msg.forward* blocks ■

Assignment 25

The reproduction of the *Chou-Reggia*-loop is basically identical to *Langton's loop*, except that in *Chou-Reggia*-loop all sheaths are removed. Instead of the extending arm, a *growth cap* is developed at the tip of the first *msg.forward* blocks. This *growth cap* provides a sense of orientation, replacing the function of the sheaths.

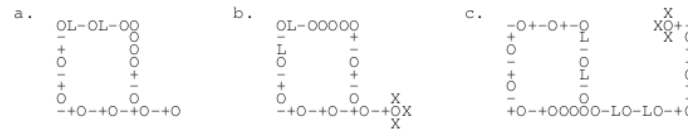


Figure 1: first three steps in replication of a *Chou-Reggia*-loop. From [01].

Assignment 27

Let "||" be the concatenation of words. Then we have the following recursion for the L-system from the example:

$$\begin{aligned} w_0 &= C, w_1 = A \\ w_n &= w_{n-2} | w_{n-1} \\ |w_n| &= |w_{n-2}| + |w_{n-1}| \end{aligned}$$

which is the recursion formula of the Fibonacci numbers ($|w_0| = |w_1| = 1$).

Proof of the recursion by induction:

Induction start: $n = 2$; $w_2 = w_0 | w_1 = C | A = CA$

Induction step: $n \rightarrow n + 1$; Using the induction hypothesis we conclude: $w_{n+1} = w_{(n+1)-2} | w_{(n+1)-1} = w_{n-1} | w_n$

Assignment 28

variables: R, S, T
axiom: R

rule 1: $R \rightarrow RS$
rule 2: $S \rightarrow ST$
rule 3: $T \rightarrow TR$

Assignment 29

- a) The $B \rightarrow BC$ rule adds one unit length per turn, thus controls the length of the segments. The $A \rightarrow A + BC + BC$ concatenates the turns of the spiral variables: A, B, C
 constants: +,-
 axiom: -A

rule 1: $A \rightarrow A + BC + BC$

rule 2: $B \rightarrow BC$

variables: B, C, D, E, F

constants: +,-

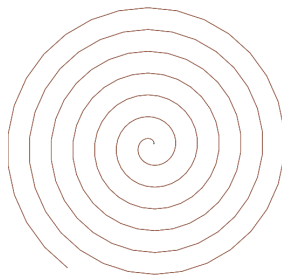
axiom: B

b)

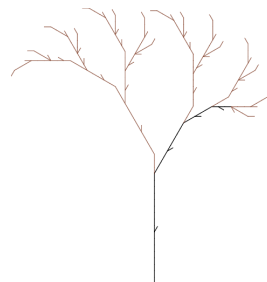
rule 1: $B \rightarrow C[-B]E[+B]$

rule 2: $C \rightarrow F[-D]F$

rule 3: $F \rightarrow FF$



(a) spiral for $\alpha = 12^\circ$, 100 iterations



(b) tree, for $\alpha = 30^\circ$, 5 iterations

■

References

- [01] Reggia, James A and Chou, Hui-Hsien and Lohn, Jason D: "Cellular automata models of self-replicating systems" published in "Advances in Computers", volume 47, pp. 141–183, *Elsevier*, 1998