

Class 2: Algebraic Data Types

January 30

Q: difference between : operator and ++ operator?

A: the first is “cons”, the second is “append”

$(:)\ ::\ \text{Int} \rightarrow [\text{Int}] \rightarrow [\text{Int}]$

e.g. $1\ :\ [2,\ 3]$

$(++)\ ::\ [\text{Int}] \rightarrow [\text{Int}] \rightarrow [\text{Int}]$

e.g. $[1,\ 2]\ ++\ [3,\ 4]$

Q: can we pattern match on whether an input is negative?

A: yes, using *guards*

see week 1 reading for more details!

```
func :: Int -> Int
func n
  | n < 0 = something
  | otherwise = something else
```

questions from homework

Q: how does indentation work?

A: most of what we will write is single line, and thus left-aligned.
most **multiline things** need to be indented.

Q: why is it hard to pattern match on the end of the list?

A: because we pattern match on the *constructors* of a data type, and the list constructors are “nil” and “cons”

data types by example

note: the weather example is inspired by the video
“Algebraic Data Types (ADT) in Scala | Rock the JVM”

name of the type being defined

```
data Weather
  = Sunny
  | Cloudy
  | Windy
  | Rainy
  | Snowy
```

constructors for values of that type

enumeration types

name of the type being defined

```
data Weather
  = Sunny
  | Cloudy
  | Windy
  | Rainy
  | Snowy
```

the only constructors for values of that type

enumeration types

```
w :: Weather  
w = Sunny
```

```
ws :: [Weather]  
ws = [Sunny, Rainy, Snowy]
```

enumeration types

(example: deriving)

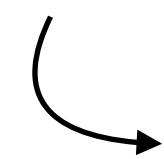
```
isGray :: Weather -> Bool
isGray Sunny    = True
isGray Cloudy   = False
isGray Windy    = True
isGray Rainy    = False
isGray Snowy    = True
```

enumeration types

```
isGray :: Weather -> Bool
isGray Cloudy = True
isGray Rainy   = True
isGray w       = False
```

enumeration types

```
isGray :: Weather -> Bool
isGray Cloudy = True
isGray Rainy   = True
isGray _       = False
```



“wildcard” pattern

enumeration types


```
data Bool = False  
          | True
```

enumeration types

```
or :: Bool -> Bool -> Bool
or True  True   = True
or True  False  = True
or False True   = True
or False False  = False
```

enumeration types

```
or :: Bool -> Bool -> Bool
or False False = False
or _          _ = True
```

enumeration types

```
or :: Bool -> Bool -> Bool
or True  _   = True
or False b   = b
```

enumeration types

```
data WeatherRequest  
  = ByLocation String  
  | ByCoordinate Int Int
```



constructors that take arguments

more data types

please follow along!

```
predict :: WeatherRequest -> Weather  
predict (ByLocation "Philly") = Sunny  
predict (ByCoordinate 90 _)    = Snowy
```

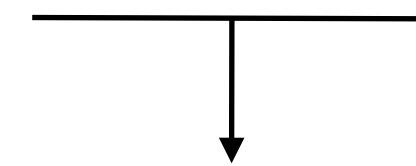


pattern matching can use *literals*

more data types

please follow along!

```
predict :: WeatherRequest -> Weather  
predict (ByLocation "Philly") = Sunny  
predict (ByCoordinate 90 _)    = Snowy
```



pattern matching can also be *nested*

more data types

```
data WeatherForecast
  = Forecast Weather
  | Unknown
```

more data types

please follow along!

```
predict :: WeatherRequest -> WeatherForecast
predict (ByLocation "Philly") = Forecast Sunny
predict (ByCoordinate 90 _)   = Forecast Snowy
predict _                     = Unknown
```

more data types

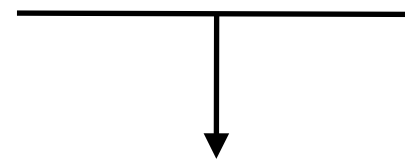
ByLocation :: String -> WeatherRequest

ByCoordinate :: Int -> Int -> WeatherRequest

more data types

(polls: types for WeatherForecast)

```
data Coord = Coord Int Int
```



idiom for single-constructor types

more data types

```
c :: Coord  
c = Coord 90 0
```

```
reflect :: Coord -> Coord  
reflect (Coord x y) = Coord y x
```

more data types

(exercises: add and incorporate)

important: see the reading for sections on
“Pattern Matching” and “Case Expressions”

interlude: why “algebraic”?


```
data Bool = False | True
```

```
data Color = Red | Green | Blue
```

`data Mix = Mix Bool Color Color`

number of values of this type: `2 x 3 x 3`

product types

```
data Unit = Unit
          1
```

product types

data Mix

= Black

| Single Color

| Double Color Color

| White

1
+
3
+
9
+
1

sum types

data Empty

0

sum types

```
data Shape
  = Rectangle Int Int
  | Circle Int
```

```
area :: Shape -> Double
area (Rectangle x y) = ...
area (Circle r) = ...
```

```
interface Shape
  double area();
```

```
class Rectangle implements Shape
  int x, y;
  double area() { ... }
```

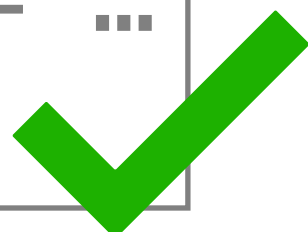
```
class Circle implements Shape
  int r;
  double area() { ... }
```

readiness for change

```
data Shape
  = Rectangle Int Int
  | Circle Int
```




```
area :: Shape -> Double
area (Rectangle x y) = ...
area (Circle r) = ...
```




```
perimeter :: Shape -> Int
```

```
interface Shape
  double area();
  int perimeter();
```

```
class Rectangle implements Shape
  int x, y;
  double area() { ... }
```



```
class Circle implements Shape
  int r;
  double area() { ... }
```



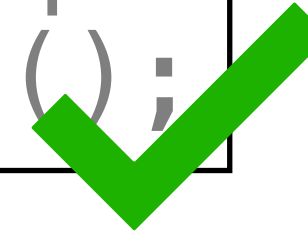
readiness for change

```
data Shape
  = Rectangle Int Int
  | Circle Int
  | Triangle Int Int Int
```

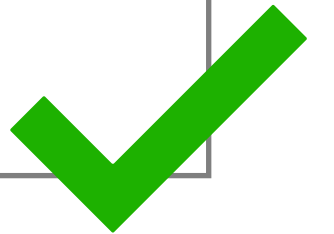
```
area :: Shape -> Double
area (Rectangle x y) = ...
area (Circle r) = ...
```



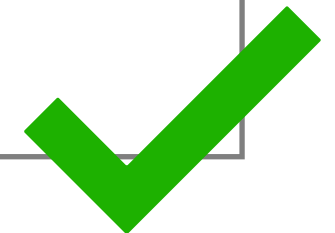
```
interface Shape
  double area();
```



```
class Rectangle implements Shape
  int x, y;
  double area() { ... }
```



```
class Circle implements Shape
  int r;
  double area() { ... }
```

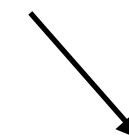


```
class Triangle implements Shape
```

readiness for change

recursive data types

```
data IntList
  = Nil
  | Cons Int IntList
```



data types can defined in terms of themselves!

recursive types

```
prod :: IntList -> Int
prod Nil = 1
prod (Cons x xs) = x * prod xs
```

recursive types

```
data Tree
  = Leaf
  | Node Tree Int Tree
```

recursive types

```
tree :: Tree  
tree = Node Leaf 1 (Node Leaf 2 Leaf)
```

recursive types

(exercises: size and add3)