

CSCE
496/896
Lecture 5:
Autoencoders
Stephen Scott

Introduction
Basic Idea
Stacked AE
Denoising AE
Sparse AE
Contractive AE
Variational AE
GAN

CSCE 496/896 Lecture 5: Autoencoders

Stephen Scott

(Adapted from Paul Quint and Ian Goodfellow)

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Introduction

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- **Autoencoding** is training a network to replicate its input to its output
- Applications:
 - Unlabeled pre-training for semi-supervised learning
 - Learning **embeddings** to support information retrieval
 - Generation of new instances similar to those in the training set
 - Data compression

Outline

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- Basic idea
- Stacking
- Types of autoencoders
 - Denoising
 - Sparse
 - Contractive
 - Variational
 - Generative adversarial networks

Basic Idea

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Basic Idea

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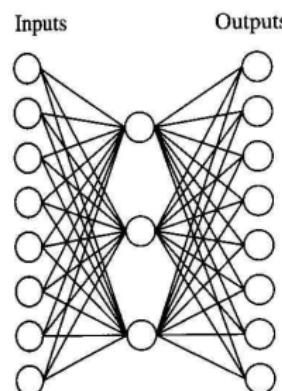
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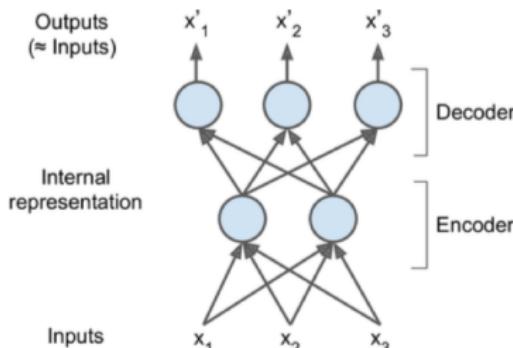
GAN



Input	Hidden Values			Output
10000000	→ .89	.04	.08	→ 10000000
01000000	→ .15	.99	.99	→ 01000000
00100000	→ .01	.97	.27	→ 00100000
00010000	→ .99	.97	.71	→ 00010000
00001000	→ .03	.05	.02	→ 00001000
00000100	→ .01	.11	.88	→ 00000100
00000010	→ .80	.01	.98	→ 00000010
00000001	→ .60	.94	.01	→ 00000001

- Sigmoid activation functions, 5000 training epochs, square loss, no regularization
- What's special about the hidden layer outputs?

Basic Idea



- An **autoencoder** is a network trained to learn the **identity function**: $\text{output} = \text{input}$

- Subnetwork called **encoder** $f(\cdot)$ maps input to an **embedded representation**
- Subnetwork called **decoder** $g(\cdot)$ maps back to input space

- Can be thought of as **lossy compression** of input
- Need to identify the important attributes of inputs to reproduce faithfully

Basic Idea

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- General types of autoencoders based on size of hidden layer
 - **Undercomplete** autoencoders have hidden layer size smaller than input layer size
 - ⇒ Dimension of embedded space lower than that of input space
 - ⇒ Cannot simply memorize training instances
 - **Overcomplete** autoencoders have much larger hidden layer sizes
 - ⇒ Regularize to avoid overfitting, e.g., enforce a **sparsity** constraint

Basic Idea

Example: Principal Component Analysis

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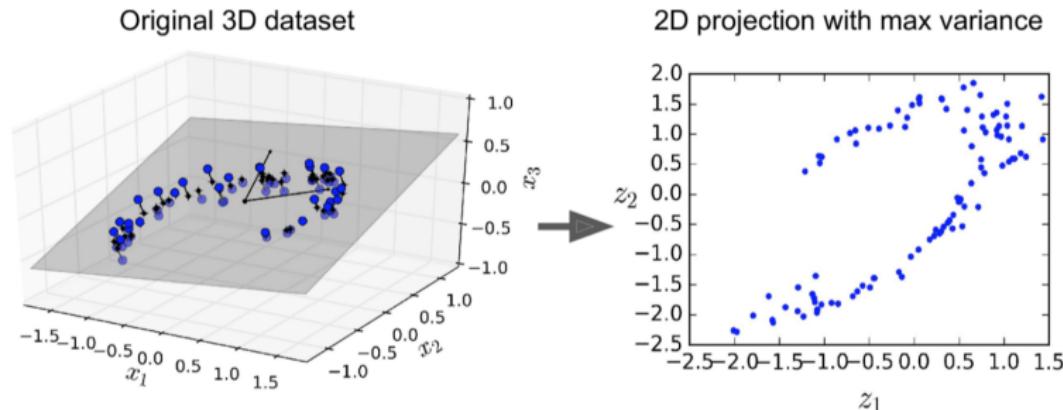
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- A 3-2-3 autoencoder with linear units and square loss performs **principal component analysis**: Find linear transformation of data to maximize variance

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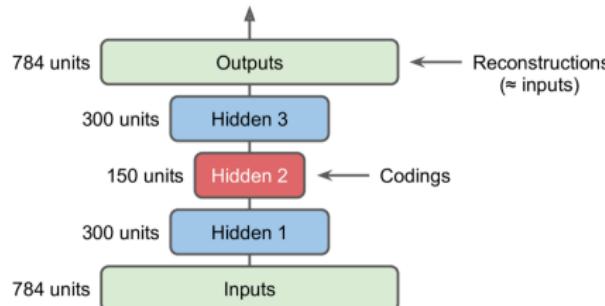
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- A stacked autoencoder has multiple hidden layers

- Can share parameters to reduce their number by exploiting symmetry: $W_4 = W_1^\top$ and $W_3 = W_2^\top$

```
weights1 = tf.Variable(weights1_init, dtype=tf.float32, name="weights1")
weights2 = tf.Variable(weights2_init, dtype=tf.float32, name="weights2")
weights3 = tf.transpose(weights2, name="weights3")           # shared weights
weights4 = tf.transpose(weights1, name="weights4")           # shared weights
```

Stacked Autoencoders

Incremental Training

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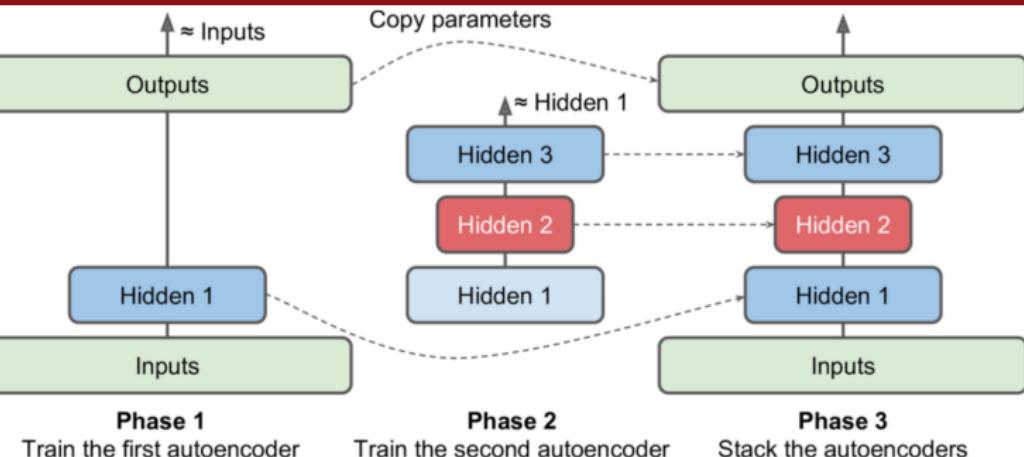
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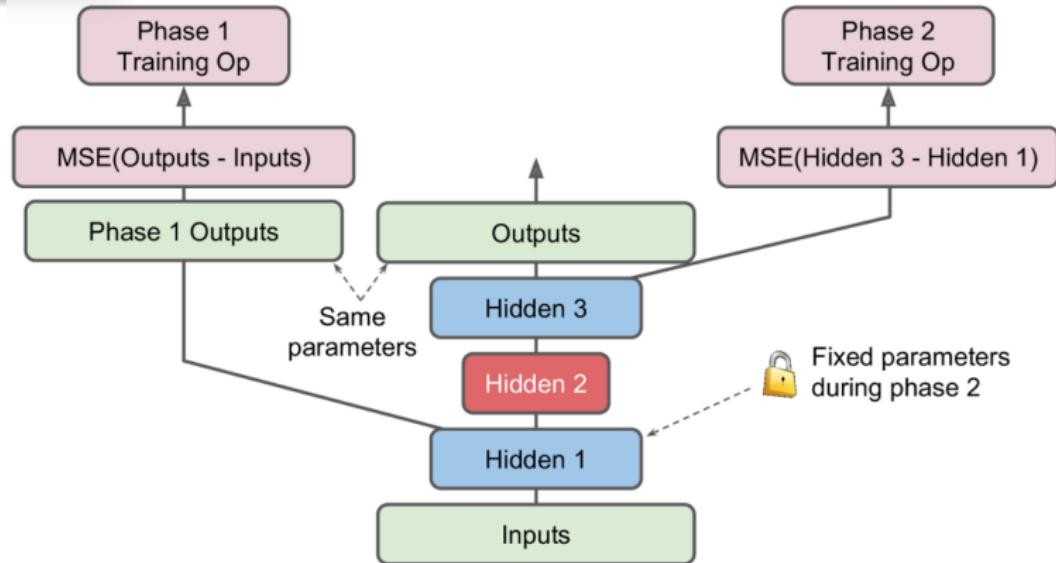
- Can simplify training by starting with single hidden layer H_1
- Then, train a second AE to mimic the output of H_1
- Insert this into first network
- Can build by using H_1 's output as training set for Phase 2

Stacked Autoencoders

Incremental Training (Single TF Graph)

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- Previous approach requires multiple TensorFlow graphs
- Can instead train both phases in a single graph: First left side, then right

Stacked Autoencoders

Visualization

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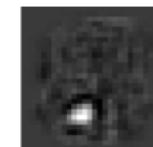
Input MNIST Digit



Network Output



Weights (features selected) for five nodes from H_1 :



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Semi-Supervised Learning

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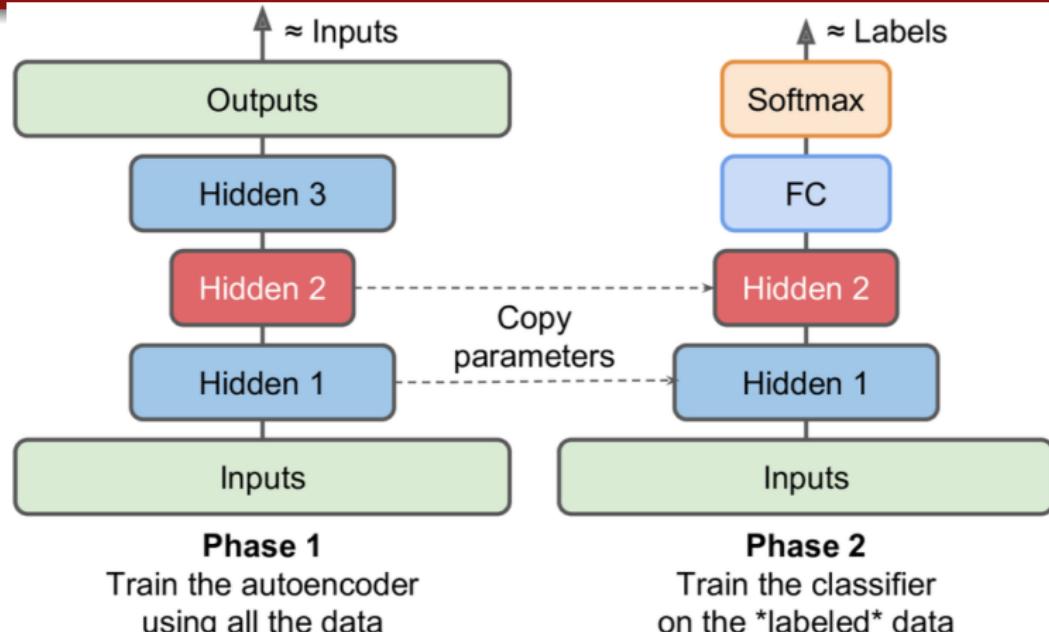
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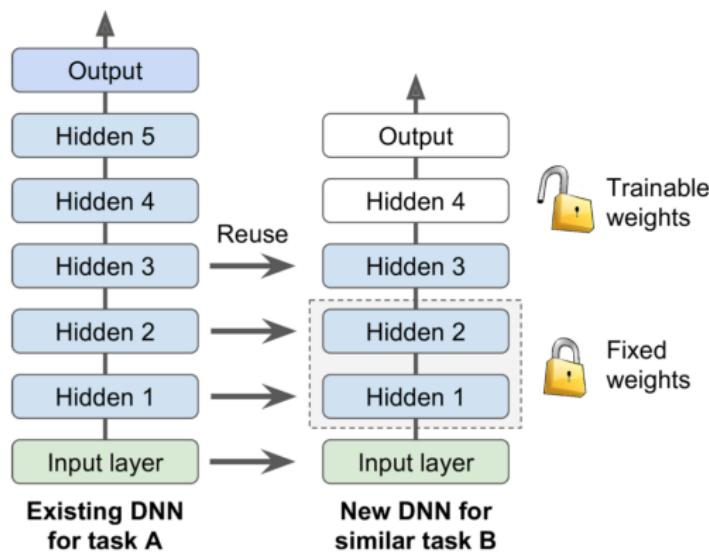
- Can **pre-train** network with unlabeled data
- ⇒ learn useful features and then train “logic” of dense layer with labeled data

Transfer Learning from Trained Classifier

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- Can also transfer from a classifier trained on different task, e.g., transfer a GoogleNet architecture to ultrasound classification



- Often choose existing one from a **model zoo**

Denoising Autoencoders

Vincent et al. (2010)

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- Can train an autoencoder to learn to **denoise** input by giving input **corrupted** instance \tilde{x} and targeting **uncorrupted** instance x
- Example noise models:
 - **Gaussian noise:** $\tilde{x} = x + z$, where $z \sim \mathcal{N}(\mathbf{0}, \sigma^2 I)$
 - **Masking noise:** zero out some fraction ν of components of x
 - **Salt-and-pepper noise:** choose some fraction ν of components of x and set each to its min or max value (equally likely)

Denoising Autoencoders

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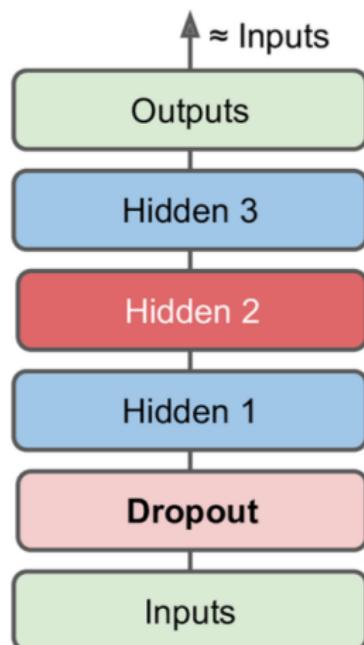
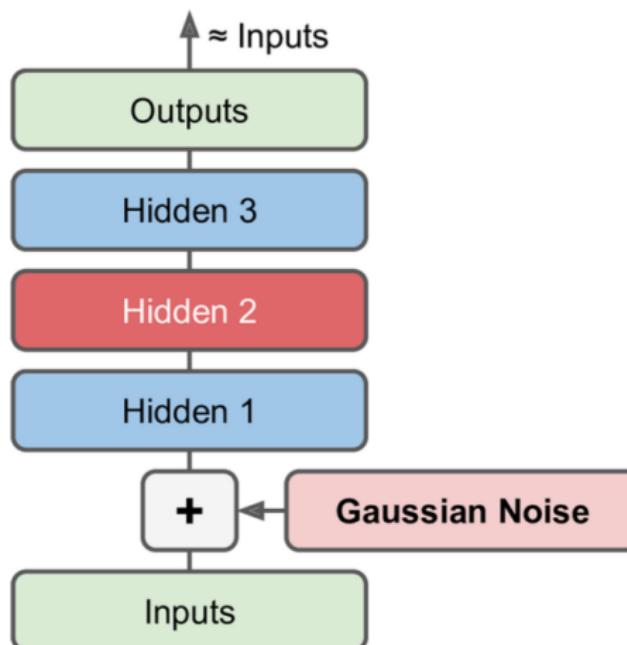
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Denoising Autoencoders

Example

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Original Images



Noisy Input



Autoencoder Output



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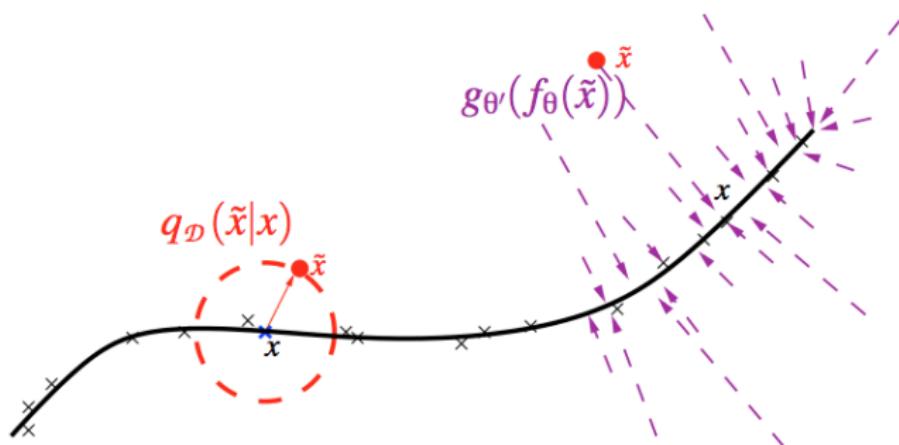
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- How does it work?
- Even though, e.g., MNIST data are in a 784-dimensional space, they lie on a low-dimensional **manifold** that captures their most important features
- **Corruption process** moves instance x off of manifold
- Encoder f_θ and decoder g_θ' are trained to project \tilde{x} back onto manifold



Sparse Autoencoders

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- An overcomplete architecture
- Regularize outputs of hidden layer to enforce **sparsity**:

$$\tilde{\mathcal{J}}(\mathbf{x}) = \mathcal{J}(\mathbf{x}, g(f(\mathbf{x}))) + \alpha \Omega(\mathbf{h}) ,$$

where \mathcal{J} is loss function, f is encoder, g is decoder, $\mathbf{h} = f(\mathbf{x})$, and Ω penalizes non-sparsity of \mathbf{h}

- E.g., can use $\Omega(\mathbf{h}) = \sum_i |h_i|$ and ReLU activation to force many zero outputs in hidden layer
- Can also measure average activation of h_i across mini-batch and compare it to user-specified **target sparsity** value p (e.g., 0.1) via square error or **Kullback-Leibler divergence**:

$$p \log \frac{p}{q} + (1 - p) \log \frac{1 - p}{1 - q} ,$$

where q is average activation of h_i over mini-batch

Contractive Autoencoders

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- Similar to sparse autoencoder, but use

$$\Omega(\mathbf{h}) = \sum_{j=1}^m \sum_{i=1}^n \left(\frac{\partial h_i}{\partial x_j} \right)^2$$

- I.e., penalize large partial derivatives of encoder outputs wrt input values
- This **contracts** the output space by mapping input points in a neighborhood near x to a smaller output neighborhood near $f(x)$
 - ⇒ Resists perturbations of input x
- If \mathbf{h} has sigmoid activation, encoding near binary and a CE pushes embeddings to corners of a hypercube

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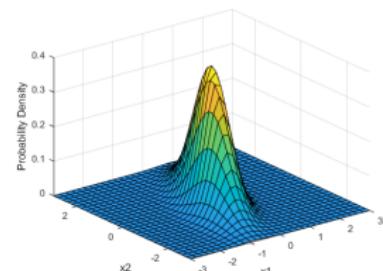
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- VAE is an autoencoder that is also **generative model**
 - ⇒ Can generate new instances according to a probability distribution
 - E.g., hidden Markov models, Bayesian networks
 - Contrast with **discriminative models**, which predict classifications
- Encoder f outputs $[\mu, \sigma]^\top$
 - Pair (μ_i, σ_i) parameterizes Gaussian distribution for dimension $i = 1, \dots, n$
 - Draw $z_i \sim \mathcal{N}(\mu_i, \sigma_i)$
 - Decode this **latent variable** z to get $g(z)$



Variational Autoencoders

Latent Variables

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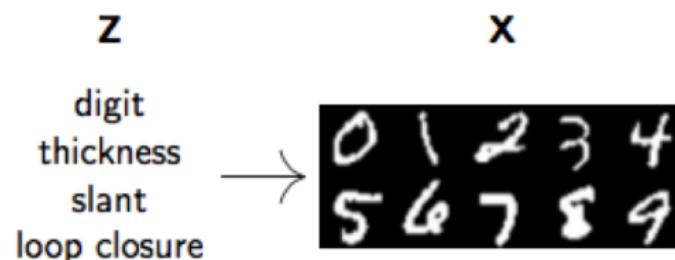
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- Independence of z dimensions makes it easy to generate instances wrt complex distributions via decoder g
- Latent variables can be thought of as values of attributes describing inputs
 - E.g., for MNIST, latent variables might represent “thickness”, “slant”, “loop closure”



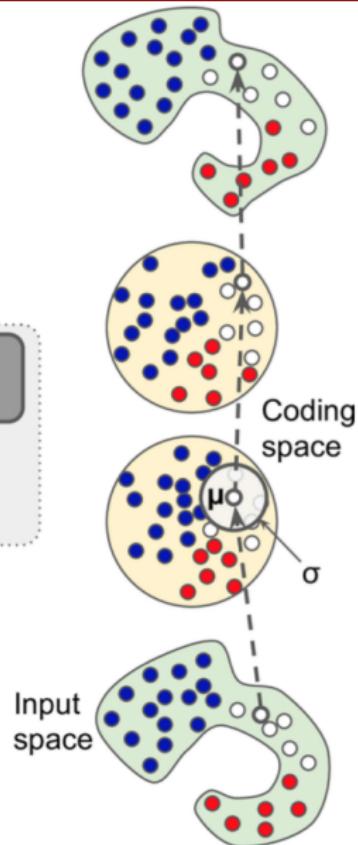
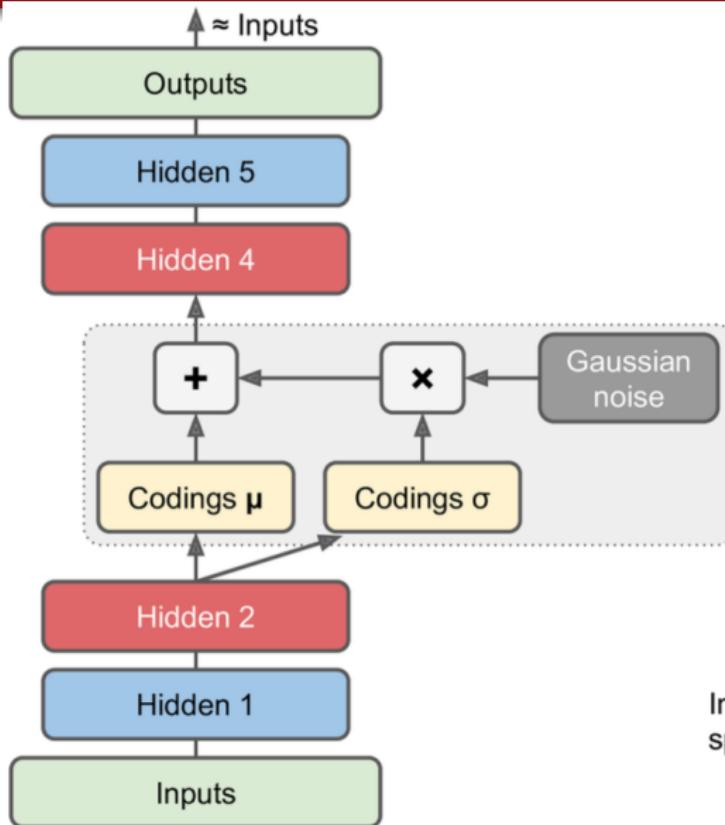
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Architecture

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Optimization

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- **Maximum likelihood (ML)** approach for training generative models: find a model (θ) with maximum probability of generating the training set \mathcal{X}
- Achieve this by minimizing the sum of:
 - End-to-end AE loss (e.g., square, cross-entropy)
 - **Regularizer** measuring distance (K-L divergence) from latent distribution $q(z | x)$ and $\mathcal{N}(\mathbf{0}, I)$ (= standard multivariate Gaussian)
- $\mathcal{N}(\mathbf{0}, I)$ also considered the **prior distribution** over z (= distribution when no x is known)

```
eps = 1e-10
latent_loss = 0.5 * tf.reduce_sum(
    tf.square(hidden3_sigma) + tf.square(hidden3_mean)
    - 1 - tf.log(eps + tf.square(hidden3_sigma)))
```

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Reparameterization Trick

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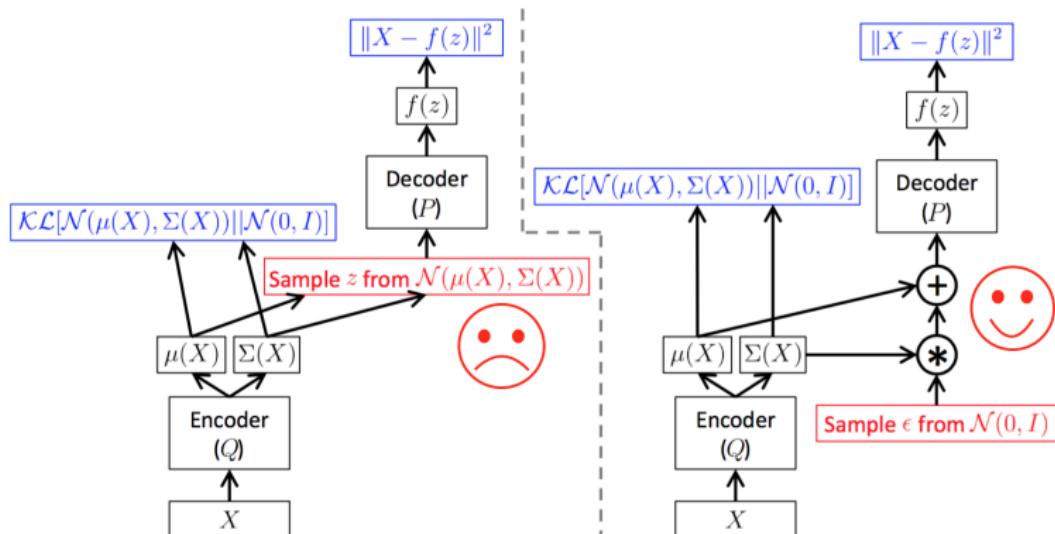
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- Cannot backprop error signal through random samples
- Reparameterization trick** emulates $z \sim \mathcal{N}(\mu, \sigma)$ with $\epsilon \sim \mathcal{N}(0, 1)$, $z = \epsilon\sigma + \mu$



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Example Generated Images: Random

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- Draw $z \sim \mathcal{N}(\mathbf{0}, I)$ and display $g(z)$



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Example Generated Images: Manifold

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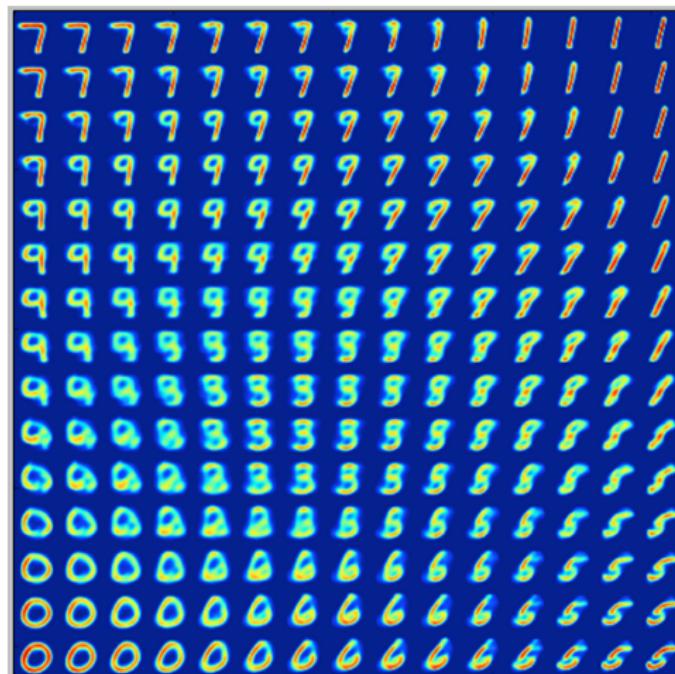
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- Uniformly sample points in z space and decode



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2D Cluster Analysis

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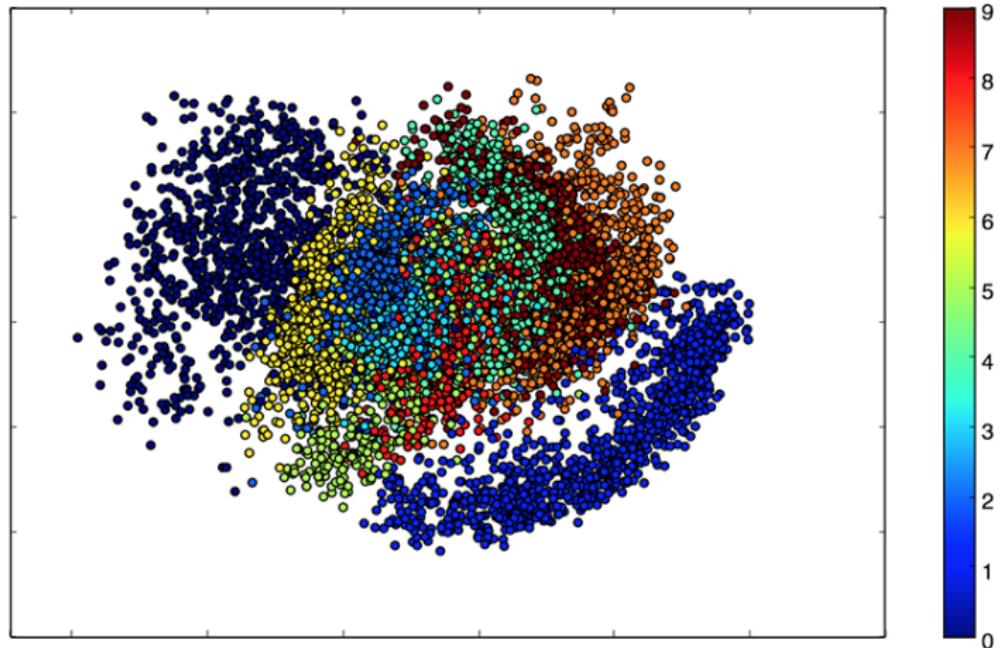
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● Cluster analysis by digit



Generative Adversarial Network

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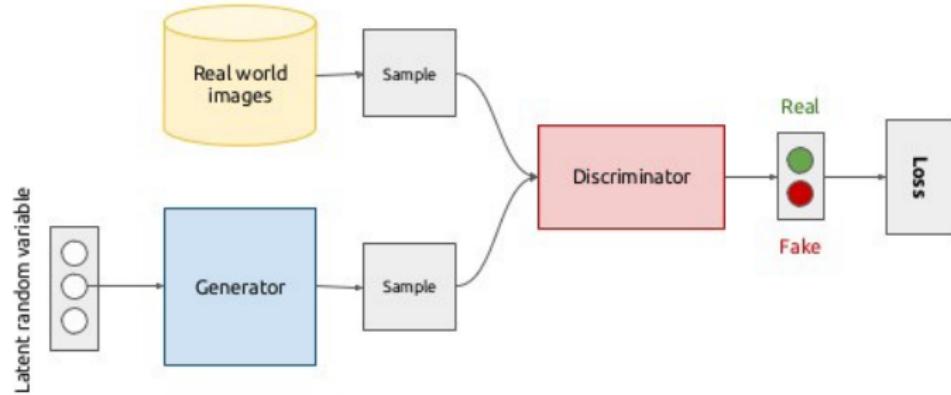
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- GANs are also generative models, like VAEs
- Models a game between two players
 - **Generator** creates samples intended to come from training distribution
 - **Discriminator** attempts to discern the “real” (original training) samples from the “fake” (generated) ones
- Discriminator trains as a binary classifier, generator trains to fool the discriminator



Generative Adversarial Network

How the Game Works

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- Let $D(x)$ be discriminator parameterized by $\theta^{(D)}$
 - Goal: Find $\theta^{(D)}$ minimizing $J^{(D)}(\theta^{(D)}, \theta^{(G)})$
- Let $G(z)$ be generator parameterized by $\theta^{(G)}$
 - Goal: Find $\theta^{(G)}$ minimizing $J^{(G)}(\theta^{(D)}, \theta^{(G)})$
- A **Nash equilibrium** of this game is $(\theta^{(D)}, \theta^{(G)})$ such that each $\theta^{(i)}$, $i \in \{D, G\}$ yields a local minimum of its corresponding J

Generative Adversarial Network

Training

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- Each training step:
 - Draw a minibatch of x values from dataset
 - Draw a minibatch of z values from prior (e.g., $\mathcal{N}(\mathbf{0}, I)$)
 - Simultaneously update $\theta^{(G)}$ to reduce $J^{(G)}$ and $\theta^{(D)}$ to reduce $J^{(D)}$, via, e.g., Adam
- For $J^{(D)}$, common to use cross-entropy where label is 1 for real and 0 for fake
- Since generator wants to trick discriminator, can use $J^{(G)} = -J^{(D)}$
 - Others exist that are generally better in practice, e.g., based on ML

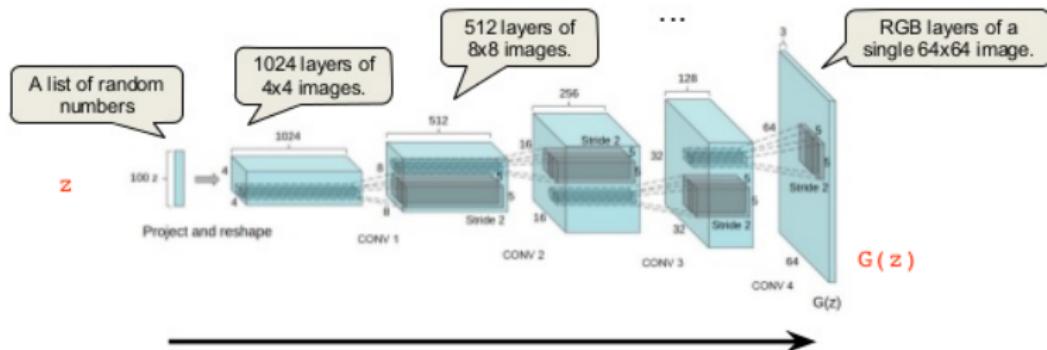
Generative Adversarial Network

DCGAN: Radford et al. (2015)

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- “Deep, convolution GAN”
- Generator uses **transposed convolutions** (e.g., `tf.layers.conv2d_transpose`) without pooling to upsample images for input to discriminator



Generative Adversarial Network

DCGAN Generated Images: Bedrooms

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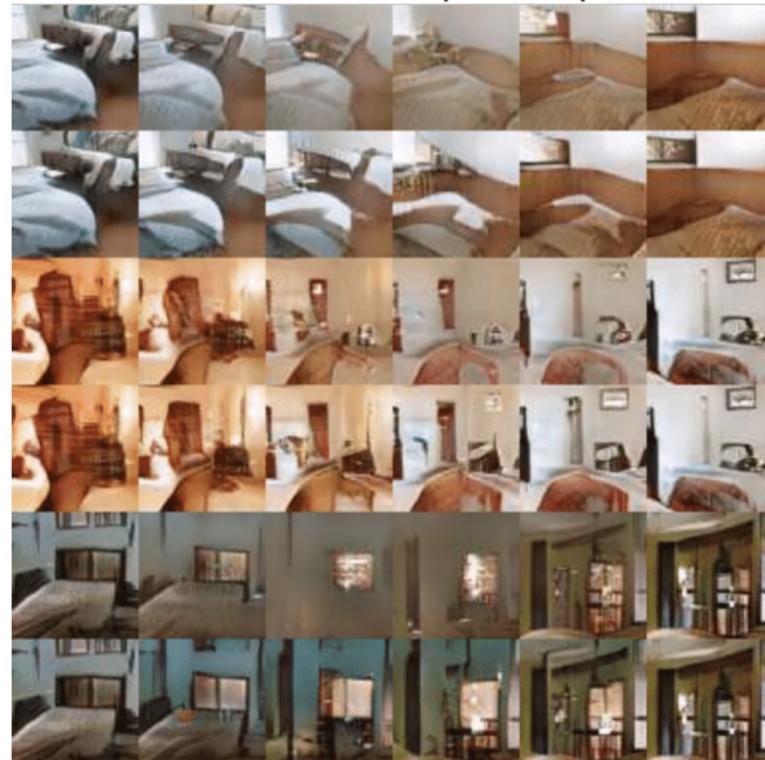
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Trained from LSUN dataset, sampled z space



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DCGAN Generated Images: Adele Facial Expressions

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Trained from frame grabs of interview, sampled z space



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DCGAN Generated Images: Latent Space Arithmetic

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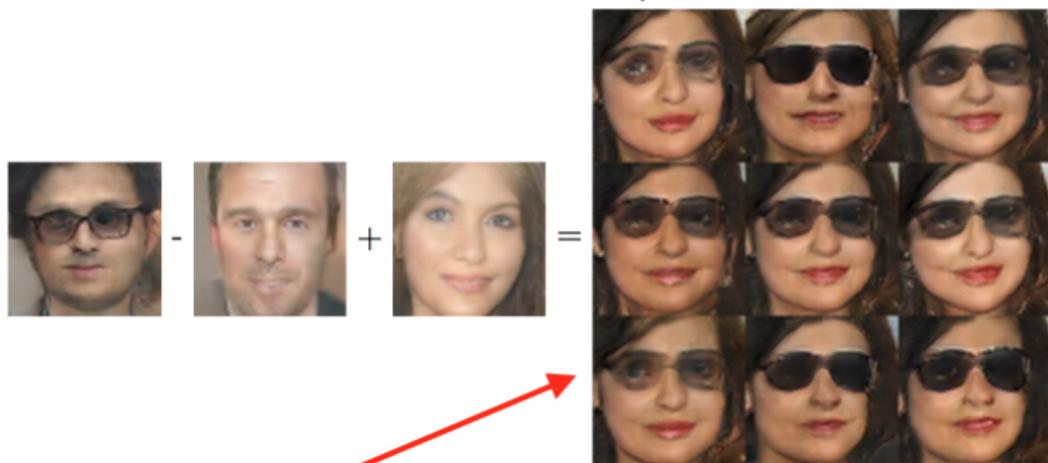
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Performed semantic arithmetic in z space!



(Non-center images have noise added in z space; center is noise-free)