Maharishi University of Management Computer science Department CS 435: Algorithms

MIDTERM EXAM - NOV-2018

Student Name:	Student Id:
Instructor: Sami Taha	

Question #	1 (12)	2 (16)	3 (12)	4 (5)	Total Grade
Grade (45)					

Instructions

- 1. Allotted exam duration is 2 hours.
- 2. Closed book/notes.
- 3. No personal items including electronic devices (cell phones, computers, calculators, PDAs).
- 4. Cell phones must be turned in to your proctor before beginning exam.
- 5. No additional papers are allowed. Sufficient blank paper is included in the exam packet.
- 6. Exams are copyrighted and may not be copied or transferred.
- 7. Restroom and other personal breaks are not permitted.
- 8. Total exam including questions and scratch paper must be returned to the proctor.

Information you might need.

1. Master Formula

Suppose T(n) satisfies

$$T(n) = \begin{cases} d & \text{if } n = 1\\ aT(\left\lceil \frac{n}{b} \right\rceil) + cn^k & \text{otherwise} \end{cases}$$

Where k is none negative integer and a, b, c, d are constants with a>0, b>1, c>0, d>=0 then

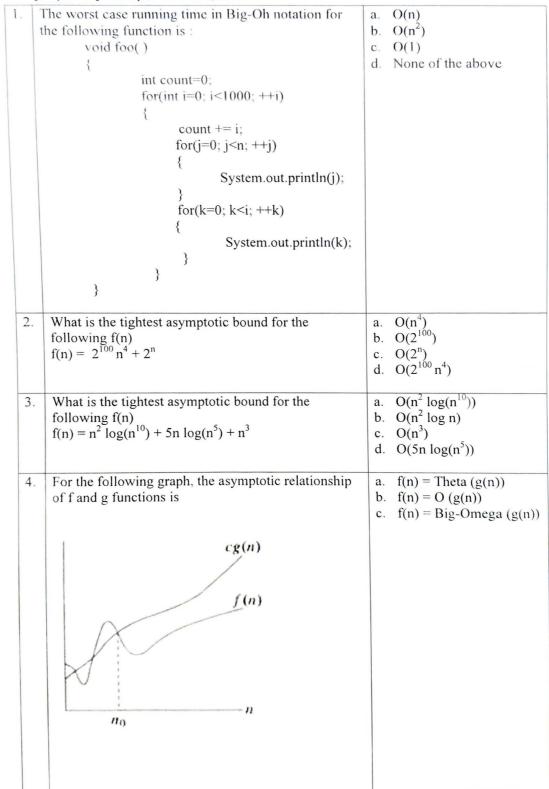
$$T(n) = \begin{cases} \Theta(n^k) & \text{if } a < b^k \\ \Theta(n^k \log n) & \text{if } a = b^k \\ \Theta(n^{\log_b^a}) & \text{if } a > b^k \end{cases}$$

$$2. \quad x = b^y = > Log_b x = y$$

3.
$$\sum_{i=0}^{n-1} i = \frac{n(n-1)}{2}$$

Q1) (12 points) Complexity Analysis

1. [12 points] Multiple Choice Question:



5	Given the function $f(n) = 2n + \log n$ and the two statements 1. $f(n) = \Theta(n)$ 11. $f(n) = \Theta(\log n)$	b.	Only statement I is true Only statement II is true Statement I and II are true Both statements are false
6	The order of 2n is	b. c.	$O(n)$ $O(n^2)$ $O(n^2)$ A and B B and C

Q2) (16 points) Analysis

1. [4 points] Give tight asymptotic bound for the following recurrences.

a.
$$T(n)=3T(n/9)+2$$
 n

b.
$$T(n) = 16T(n/4) + 100 n^2$$

2. [2 points] Discuss whether the statement "Amortization makes an algorithm more efficient" is true or false. Justify your answer.

- 3. [3 points] An algorithm solves a problem by dividing it into 4 sub-problems. Each recursive call divides the problem into one-third of the size of the problem. After solving all sub-problems it combines the solutions in quadratic time.
 - a. Give a recurrence formula for this algorithm.

b. Give the tightest asymptotic bound for the proposed recurrence in part a.

4. [2 points] Express the complexity of the following algorithm as a recurrence relation procedure

```
void foo(int n)
{
  if(n <=0) return;
  System.out.println(n);
  foo(n/3)+foo(n/2);
}</pre>
```

5. [5 points] Given an array A with n integers and there may be duplicate elements. We want to find which element has the most duplicates in A. Propose an algorithm to solve this problem in O(n) worst-case time or better. Example: [1 2 2 3 1 4 2 2 3] the entry with most duplicate is 2

Q3) (12 points) Sorting algorithms:

- 1. [5 points] Answer the following questions by True or False. Fill your answers in the following table.
 - a. For the binary search algorithm, the successful search requires only O(log n) comparisons, but the unsuccessful search requires n comparisons.
 - b. The best time complexity of Bubble Sort is O(n log n).
 - c. Selection-Sort makes less swap operations than Merge Sort.
 - d. Any comparison based sorting algorithm can be made stable by using position as a criteria when two elements are compared.
 - e. Bubble-Sort is stable sorting algorithm.

A	В	С	D	Е

- 2. [7 points] Considering Quick Sort Algorithm.
 - a. [1 point] What is the worst running time for Quick Sort?

b. [2 points] What can you do to avoid the worst case running time?

c. [4 point] Sort the following array using Quick-Sort Algorithm. Assume that the first element is the pivot in every iteration. Show all your work in each step. You do not need to write the algorithm

ı								
	48	33	31	60	1	49	30	70

Q4) (5 points) SCI Question:

Write a short essay that connects one of the studied topics to the Science of Creative Intelligence (SCI). You can pick any topic.