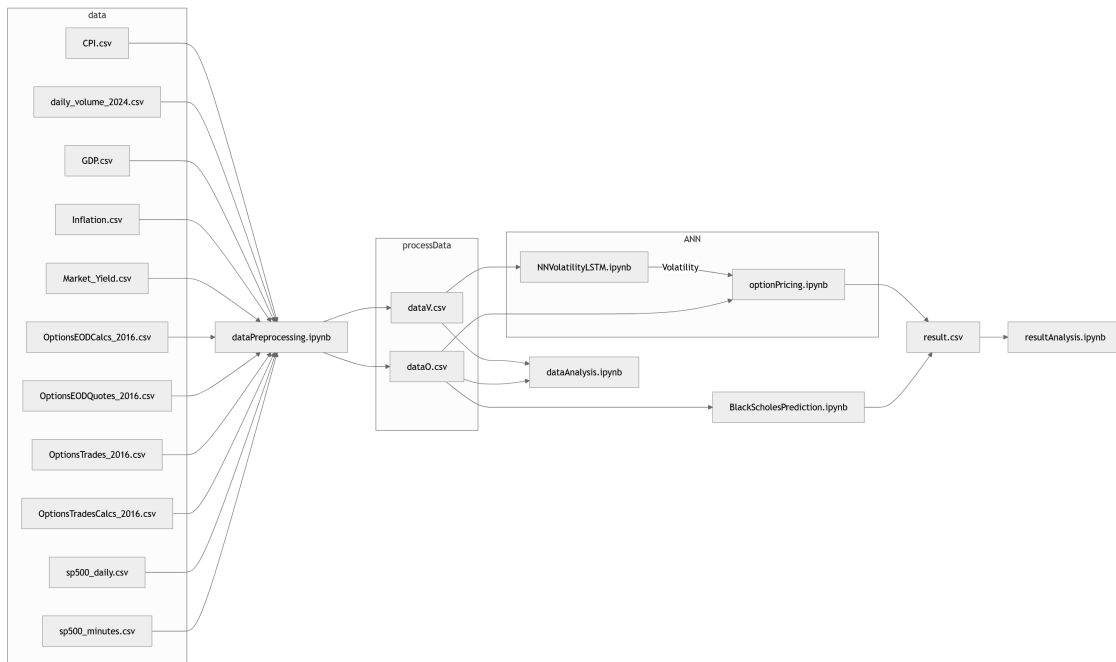


Research Project Report

April 15, 2025

1 Introduction

This document will clearly outline the advancement of the research project. Based on the Scrum and sprint methodology, I will update the document every week, including what is new and what is next.

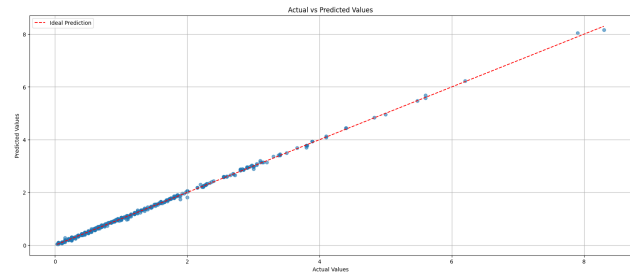
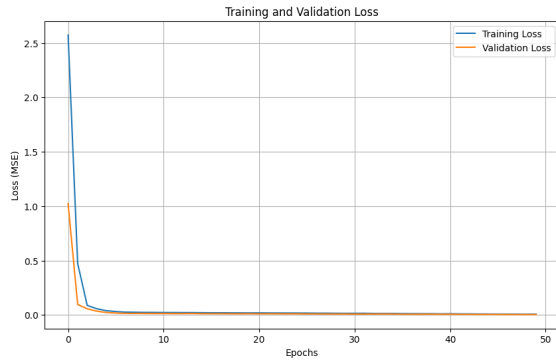


Iteration 1

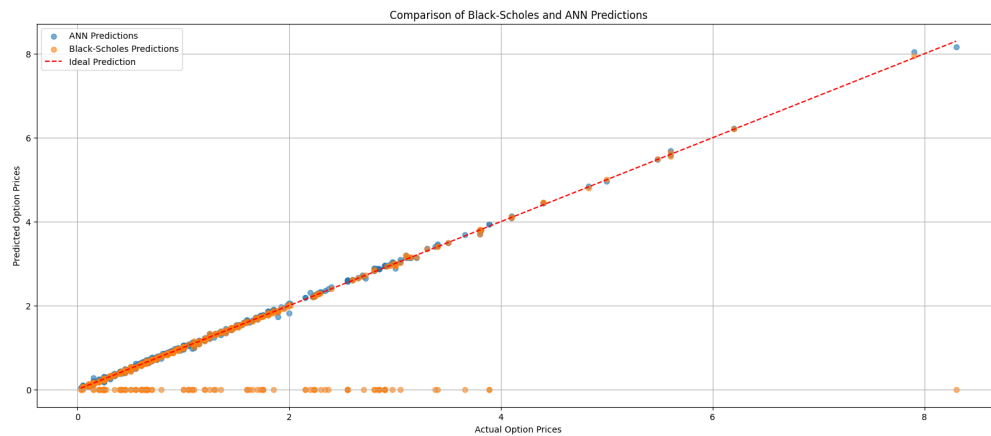
February 3, 2025

What Is New?

- Created and trained a ANN MLP model for option pricing, using Black-Scholes parameters to target option prices.



- Compared the model's performance against Black-Scholes models:



- Started to build a custom LSTM model with NumPy. For now, I think Python allows better flexibility and development time than C++, while still maintaining decent performance using only NumPy. I want the model to be compatible with TensorFlow formatting for easier use.

What Is Next?

- Finish the custom MLP model.
- Outliers suppression

Iteration 2

February 10, 2025

What Is New?

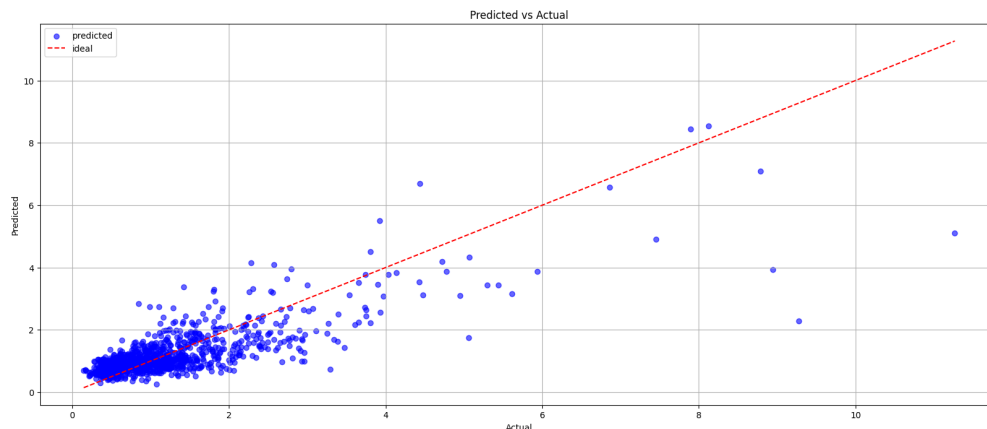
- First principle implementation of artificial neural network **multilayer perceptron**. Can be found here : `/code_/models/annModels.py`

- ```
mlp = am.MLP(n_input=22, n_hidden1=64, n_hidden2=32, n_output=1)
epochs = 5000
learning_rate = 0.001
```

```
#Training
history = mlp.train(X_train_normalized, y_train, epochs, learning_rate)
```

```
Predict
train_preds = mlp.forward(X_train_normalized)
y_pred = mlp.forward(X_test_normalized)
```

```
#---
Final Training Loss: 0.41194406219492513
Final Test Loss: 0.41460153925356924
```



### What Is Next?

- Parameter optimization for custom model implementation ?
- Would a Transformer work better ? - Wiki Transformer
  - Very likely, However, to get a working transformer model, the data volume is much more advanced than we currently use.

## Iteration 3

February 17, 2025

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### What Is New?

- Finnish data gathering with script `:/code_/tools/getData.ipynb`, all the assets data are gathered in `/data/stocks` (around 200 symbols)
- Transformer implementation in progress
- Benchmark against LSTM model
- Parameter optimization for custom model implementation ?

### What Is Next?

- Document on maths behind models (`models.pdf`)

## Iteration 4

February 24, 2025

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### What Is New?

- LSTM implementaiton in progress
- FFNN MLP and LSTM mathematics models

### What Is Next?

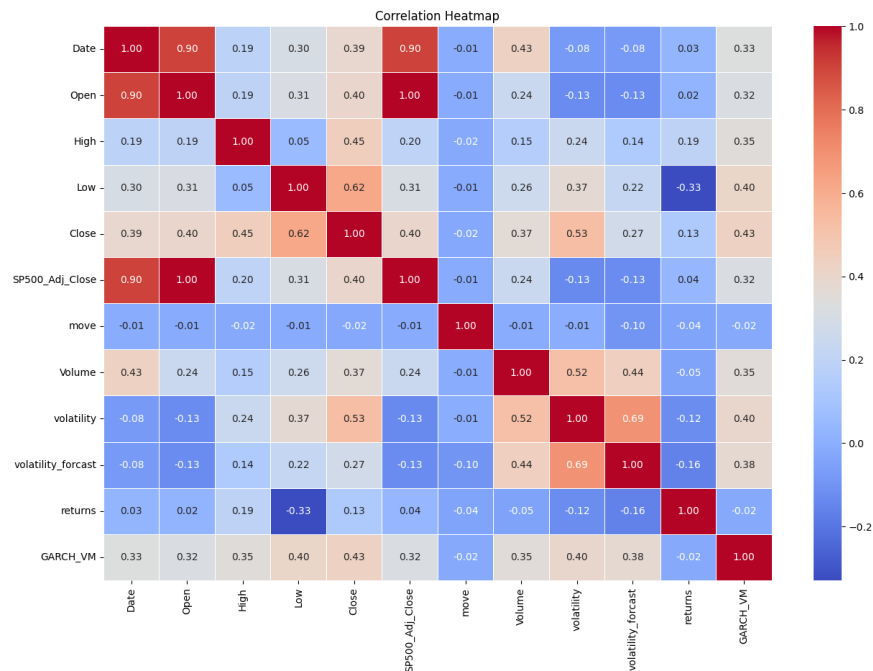
- Identifies specific aspect of volatility time series (mean reversion, volatility clustering, heavy tail)
- identifies drawback in LSTM architecture for specific financial time series
- Optimize model for financial time series
- identify best loss function for volatility time series

## Iteration 5

March 3, 2025

### What Is New?

- Data Work
  - Compare to litterature
  - Normalize data to improve models performances
  - Select relevant feature to work with the model (clean confusion matrix)
- Litterature about new/modify LSTM model for financial time series prediction
- Document on volatility model updated



### What Is Next?

- Improve mathematical relationship of LSTM models with litterature and financial time series properties.

### What Is New?

- The volatility time series have some properties as for exemple **volatility clustering**. It implied that huge amplitude volatility periode are follow by small volatility changes and back to huge periode. The default LSTM network isn't aware of that so we can try to implement this in the forget gate to keep this informaiton inside the network. For instance we can propose a solution like this

$$F_t = \sigma(W_f \cdot [H_{t-1}, X_t] + b_f - k\sigma_t)$$

Where the new term  $k\sigma_t$  represente the a contante  $k$  that is a leanring parameter to scale the impact on the network and  $\sigma_t$  that is the volatility estimation value.

### What Is Next?

- Implementaiton
- Benchmark against default LSTM and Black-Scholes
- Litterature

## Litterature review

1. AT-LSTM: An Attention-based LSTM Model for Financial Time Series Prediction

*Adding and attention layer to LSTM model. Applying weight to input feature thanks to an attention layer. Then, in a second stage, the attention model select all relevant features for LSTM input model.*

| MAPE on DJIA |         |
|--------------|---------|
| LSTM         | 0.00625 |
| AT-LSTM      | 0.00486 |

2. Improved Financial Predicting Method Based on Time Series Long Short-Term Memory Algorithm

*Automated capital prediction strategy, first by analysing the fluctuation and tail risk. Then by use ARIMA and Prophet models. Finally time series modeleing of the wavelet LSTM for a two part analysis of the linear separated wavelet and non-linear embedded wavelet to predict volatility.*

| Model          | Redeem         |        | Purchase       |        | Yield          |        |
|----------------|----------------|--------|----------------|--------|----------------|--------|
|                | R <sup>2</sup> | RMSE   | R <sup>2</sup> | RMSE   | R <sup>2</sup> | RMSE   |
| ARIMA          | 0.6290         | 0.5222 | 0.6091         | 0.5801 | 0.4183         | 1.3628 |
| Prophet        | 0.7677         | 0.3497 | 0.7494         | 0.3959 | 0.4105         | 1.4210 |
| Proposed model | 0.8539         | 0.2406 | 0.8692         | 0.2318 | 0.8281         | 0.3002 |

3. Prediction of Financial Time Series Based on LSTM Using Wavelet Transform and Singular Spectrum Analysis

*Imporove LSTM prediction capabilities by using data denoising methods including wavelet transformation (WT) and singular spectrum analysis (SSA) on the closing DJIA, divided in short, meduim and long term time periode. The LSTM data denoising performe better than raw data for data prediciton on all tree time periodes.*

TABLE 5: 6-hour DJIA closing price forecast results.

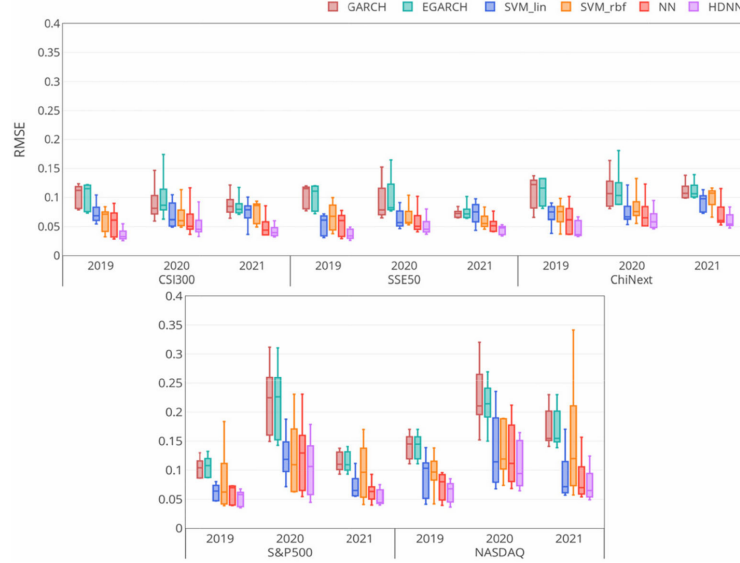
|              | RMSE      | MAE       | MAPE      | SDAPE     |
|--------------|-----------|-----------|-----------|-----------|
| LSTM         | 6.1655946 | 4.5780000 | 0.0001503 | 0.0001356 |
| RNN-dropout  | 5.3630017 | 4.3020694 | 0.0001413 | 0.0001053 |
| LSTM-dropout | 4.5014469 | 3.2249583 | 0.0001059 | 0.0001032 |
| SSA-LSTM     | 1.1753464 | 0.9942363 | 0.0000326 | 0.0000206 |
| WT-LSTM      | 1.9164739 | 1.4123594 | 0.0000464 | 0.0000426 |

4. Black-Scholes-Artificial Neural Network : A novel option princing model

*Comparaision of multiple option pricing model and intruduction of a new model call BSANN, a basic ANN MLP model in [11-15-1] performing better than tranditionnal methodes.*



5. Volatility forecasting using deep neural network with time-series feature embedding  
*Propose a hybrid deep neural network model (HDNN). Encoding one-dimensionnal time-series data into two-dimensionnal GAF images to use a CNN with 2D concolutions layers, then performe feature embedding and dense layers regression to predict the volatility*



6. Volatility forecasting using deep recurrent neural networks as GARCH models  
*Propose new method to predict volatility time series by using a combination of GARCH and and deep neural network. Also introduce a mehanisme to identify ideal sliding windows side for volatility. With evaluation of GRU, LSTM, BiLSTM*

**Table 6** Performance results for the Volatility prediction of the ASX200 Time Series using Recurrent Neural Networks

|          | Train dataset       |         |         | Test dataset         |         |         |
|----------|---------------------|---------|---------|----------------------|---------|---------|
|          | ALL-GARCH(1,1) with |         |         | ALL- GARCH(1,1) with |         |         |
|          | BILSTM              | LSTM    | GRU     | BILSTM               | LSTM    | GRU     |
| RMSE     | <b>0.1205</b>       | 0.2979  | 0.3391  | <b>0.2106</b>        | 0.2226  | 0.2594  |
| MAE      | <b>0.0934</b>       | 0.1952  | 0.2163  | <b>0.1382</b>        | 0.1737  | 0.2078  |
| MAPE(%)  | <b>7.7217</b>       | 9.49156 | 10.3561 | <b>8.5580</b>        | 10.9473 | 13.1652 |
| $R^2$    | <b>0.9725</b>       | 0.8321  | 0.7825  | <b>0.4968</b>        | 0.4380  | 0.2368  |
| Spearman | <b>0.9570</b>       | 0.8788  | 0.8711  | <b>0.7785</b>        | 0.6719  | 0.6788  |

7. Machine Learning for Options Pricing: Predicting Volatility and Optimizing Strategies – Explore how ML models can outperform traditional pricing models (like Black-Scholes), enhancing option traders’ decision-making.
8. NEURAL NETWORK LEARNING OF BLACK-SCHOLES EQUATION FOR OPTION PRICING
9. Option Pricing with Deep Learning  
*This paper propose a deep learning approach to option pricing with 3 models, 2 MLP(1&2)*

and a LSTM model. MPL1 as a MLP predicting the option price, while MLP2 predicting the bid & ask of the underlying price. Furthermore, LSTM model estimating volatility to feed its output to the MLP1 and then having a prediction of the option price.

|      | Model | train-MSE | MSE    | Bias  | AAPE  | MAPE  | PE5   | PE10  | PE20  |
|------|-------|-----------|--------|-------|-------|-------|-------|-------|-------|
| Call | BS    | 322.95    | 321.37 | -0.05 | 78.79 | 4.81  | 50.52 | 59.33 | 67.43 |
|      | MLP1  | 23.71     | 24.00  | 0.01  | 24.49 | 2.12  | 61.04 | 68.39 | 74.33 |
|      | MLP2  | 7.70      | 15.21  | 0.09  | 23.45 | 1.73  | 63.03 | 70.10 | 75.54 |
|      | LSTM  | 30.61     | 30.97  | 0.13  | 26.58 | 2.33  | 58.94 | 66.35 | 72.42 |
| Put  | BS    | 543.48    | 533.25 | 97.37 | 68.00 | 97.46 | 12.87 | 18.22 | 23.58 |
|      | MLP1  | 15.65     | 15.66  | 5.03  | 43.73 | 18.48 | 30.46 | 40.51 | 51.13 |
|      | MLP2  | 2.03      | 8.84   | 3.85  | 39.59 | 14.32 | 33.74 | 44.25 | 55.01 |
|      | LSTM  | 22.81     | 23.15  | 6.01  | 48.32 | 26.05 | 27.45 | 36.24 | 46.17 |

Table 1: Error metrics comparing MLP1 price and MLP2 equilibrium price with Black-Scholes prices. Note all metrics beside MSE are percentages.

## 10. Volatility forecast using hybrid Neural Network models

## Iteration 8

March 31, 2025

### LSTM implementation

Model architecture : [8-16-1]

### Data work

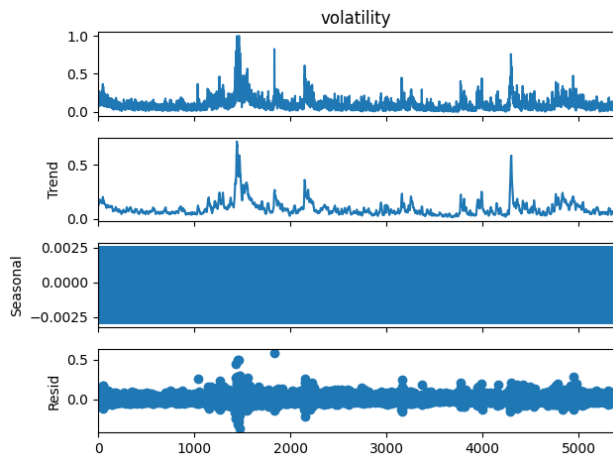
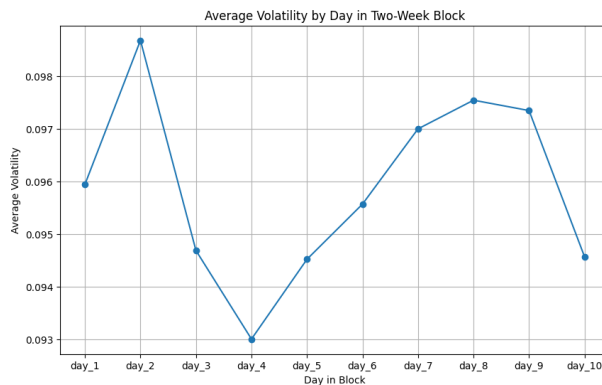
- **Re-sizing of the data** - Data work

In the file dataResize.csv the size of the data have been resize to 2 weeks per exemple.

|   | day_1  | day_2  | day_3  | day_4  | day_5  | day_6  | day_7  | day_8  | day_9  | day_10 |
|---|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
| 0 | 0.0668 | 0.2115 | 0.0912 | 0.1286 | 0.1648 | 0.1331 | 0.1111 | 0.0820 | 0.1396 | 0.1226 |
| 1 | 0.1395 | 0.1692 | 0.1084 | 0.1211 | 0.2697 | 0.1923 | 0.1249 | 0.2248 | 0.2137 | 0.1754 |
| 2 | 0.0790 | 0.1978 | 0.1910 | 0.1030 | 0.1896 | 0.1327 | 0.1782 | 0.1336 | 0.1503 | 0.2014 |
| 3 | 0.1765 | 0.1169 | 0.1218 | 0.2071 | 0.1563 | 0.2128 | 0.1299 | 0.1427 | 0.0892 | 0.1941 |
| 4 | 0.1313 | 0.1039 | 0.0944 | 0.1857 | 0.2305 | 0.1404 | 0.1576 | 0.2914 | 0.1265 | 0.3658 |

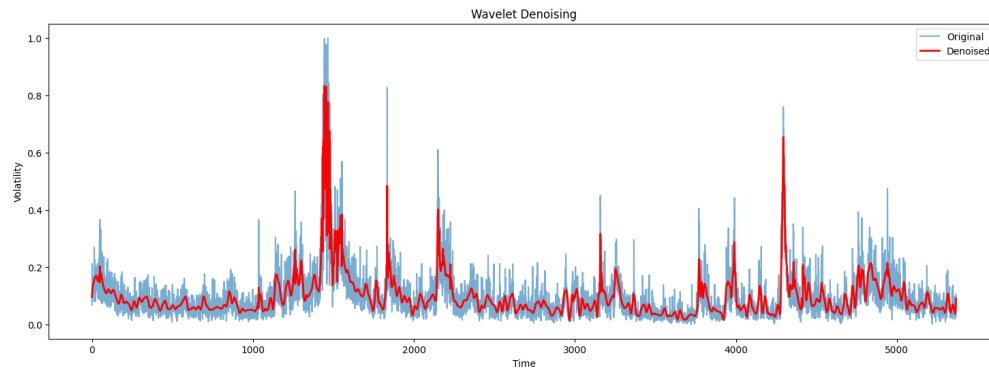
- **Data seasonality** - Analysis

Analysis reccurent pattern in dataResize to use the 10-days seasonnality.



- **De-noising (Wavelet)** - Data work

De-noising the raw data to better capture the trend in the time serie



- **Sliding windows - Analysis**  
Papers : Volatility forecasting using deep recurrent neural networks as GARCH models  
and Single-scale time-dependent window-sizes in sliding-window dynamic functional connectivity analysis

### Statistical models

- ARIMA
- GRU
- BiLSTM

## Iteration 9

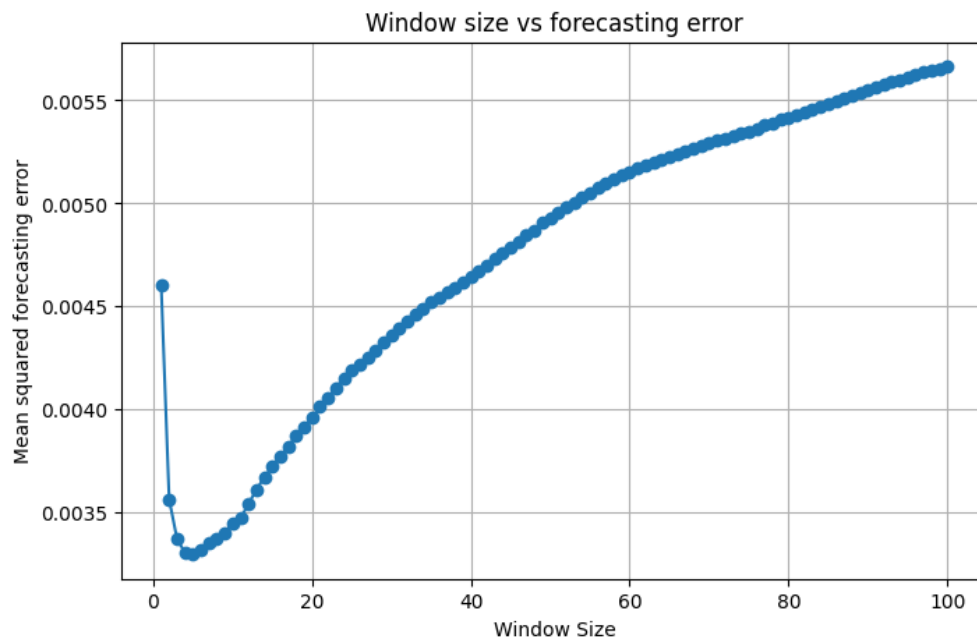
April 7, 2025

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### Sliding window

#### Implementation

Implementation of static sliding windows on the volatility time serie



Best window size given by the EMD is currently 5 days (a trading week) with MSE estimator.

#### Improvement - Dynamic sliding window

## Iteration 10

April 14, 2025

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### LSTM

Need to improve LSTM performance, not as good as TensorFlow implementation.

### Sliding Window

The dynamic sliding vector may cause a problem with the LSTM vectore size.