

# Errata from *The Stationary Tower*.

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- On page 4, in Exercise 1.1.7, replace ‘(i.e., preserving the  $\in$ -relation)’ with ‘(i.e., preserving formulas whose quantifiers are bounded)’.
- On page 6, add to the hypothesis of Lemma 1.1.13 that  $\kappa \setminus \alpha$  is in  $U$  for each  $\alpha < \kappa$ .
- On page 8, add to the hypothesis of Lemma 1.1.18 that  $M$  satisfies ‘ $V_\alpha$  exists for every ordinal  $\alpha$ .’
- On page 13, in the statement of Lemma 1.1.27, insert ‘on  $\kappa$ ’ after the first occurrence of  $\mu$ .
- On page 18, line -7, put ‘when  $\lambda \geq 2^\omega$ .’ after ‘under the Axiom of Choice’.
- On page 23, in the third bulleted point at the top of the page, the tower should concentrate on  $T_x$ .
- On page 24, in the last sentence of the statement of Lemma 1.3.13, insert ‘if  $\sigma$  contains a nonprincipal measure then’ after ‘in particular’.
- On page 25, the key point in the proof of Lemma 1.3.14 doesn’t follow from the Lemma 1.1.25, but it does follow easily from the fact that  $\bar{\pi}$  in the proof of Lemma 1.1.25 is a bijection.
- On page 29,  $M$  should be  $N$  in the sentence beginning with ‘Then  $E_j$  is a function’ in the second to last paragraph.
- On page 37,  $V$  should be  $M$  on the third-to-last line.
- On page 43, line -14,  $s^{<\omega}$  should be  $2^{<\omega}$ .
- On page 43, in the sentence in the second-to-last paragraph starting with ‘Assuming that we have’, ‘ $\sigma_t$  for all  $t$  in  $2^{G(i-1)}$ ’ should be ‘ $\sigma_t$  in  $2^{G(i-1)}$  for all  $t$  in  $2^i$ ’.
- On page 46, in the last line of the proof of lemma 1.6.26,  $b_S$  should be  $b_T$ .

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- On page 47, switch the order of the first two sentences of the proof of Lemma 1.7.3.
- On page 62, in the last line of Definition 2.5.1, replace ‘is club in’ with ‘contains a club in’.
- On page 62, in the hint for Exercise 2.5.3, the ‘D’ at the end of the second-to-last sentence should be a ‘d’.
- On page 63, in the hint for Exercise 2.5.5, instead of letting  $\langle a_\alpha : \alpha < \delta \rangle$  be an enumeration of  $\mathbb{P}_{<\delta}$ , let  $a_\alpha$  be the set of ordinals of cardinality  $\aleph_\alpha$ .
- On page 67, in lines 15-16, remove ‘ $b \in \mathcal{P}_{<\delta}$ , i.e.,’.
- On page 68, in Definition 2.5.12, insert ‘strongly inaccessible’ in between ‘A’ and ‘cardinal’.
- On page 82, in the second line of the statement of Lemma 2.7.14, ‘ $V_{\delta_1}$ ’ should be ‘ $V_{\delta_1+1}$ ’.
- On page 95, line -3, ‘in’ should be ‘for.’
- I probably should have included an appendix on sharps. A note on this topic can be found at <http://www.logic.univie.ac.at/~caicedo/sharps.pdf>

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