Basic Derivatives

$$\frac{d}{dx}e^{f(x)} = f'(x)e^{f(x)}$$

$$\frac{d}{dx}\sin f(x) = \cos f(x) \cdot f'(x)$$

$$\frac{d}{dx}\cos f(x) = -\sin f(x) \cdot f'(x)$$

$$\frac{d}{dx}\tan f(x) = \sec^2 f(x) \cdot f'(x)$$

$$\frac{d}{dx}\cot f(x) = -\csc^2 f(x) \cdot f'(x)$$

$$\frac{d}{dx}\sec f(x) = \sec f(x)\tan f(x) \cdot f'(x)$$

$$\frac{d}{dx}\csc f(x) = -\csc f(x)\cot f(x) \cdot f'(x)$$

$$\frac{d}{dx}\log_a f(x) = \frac{f'(x)}{f(x)}$$

$$\frac{d}{dx}(f(x))^n = n(f(x))^{n-1}f'(x)$$

$$\frac{d}{dx}\sqrt{f(x)} = \frac{f'(x)}{2\sqrt{f(x)}}$$

$$\frac{d}{dx}a^x = a^x \ln a$$

$$\frac{d}{dx}b^{g(x)} = b^{g(x)}\ln b \cdot g'(x)$$

Chain Rule

$$\frac{d}{dx}f(g(x)) = f'(g(x)) \cdot g'(x)$$

Higher-Order Derivatives

$$\frac{d^2}{dx^2}e^x = e^x$$

$$\frac{d^3}{dx^3}\sin x = -\cos x$$

$$\frac{d^4}{dx^4}\cos x = \cos x$$

Inverse Trigonometric

$$\frac{d}{dx}\arcsin f(x) = \frac{f'(x)}{\sqrt{1 - (f(x))^2}}$$

$$\frac{d}{dx}\arccos f(x) = -\frac{f'(x)}{\sqrt{1 - (f(x))^2}}$$

$$\frac{d}{dx}\arctan f(x) = \frac{f'(x)}{1 + (f(x))^2}$$

$$\frac{d}{dx}\operatorname{arccot} f(x) = -\frac{f'(x)}{1 + (f(x))^2}$$

$$\frac{d}{dx}\operatorname{arcsec} f(x) = \frac{f'(x)}{|f(x)|\sqrt{(f(x))^2 - 1}}$$

$$\frac{d}{dx}\operatorname{arccsc} f(x) = -\frac{f'(x)}{|f(x)|\sqrt{(f(x))^2 - 1}}$$

Hyperbolic Function

$$\frac{d}{dx}\sinh f(x) = \cosh f(x) \cdot f'(x)$$

$$\frac{d}{dx}\cosh f(x) = \sinh f(x) \cdot f'(x)$$

$$\frac{d}{dx}\tanh f(x) = \operatorname{sech}^2 f(x) \cdot f'(x)$$

$$\frac{d}{dx}\coth f(x) = -\operatorname{csch}^2 f(x) \cdot f'(x)$$

$$\frac{d}{dx}\operatorname{sech} f(x) = -\operatorname{sech} f(x)\tanh f(x) \cdot f'(x)$$

$$\frac{d}{dx}\operatorname{csch} f(x) = -\operatorname{csch} f(x)\coth f(x) \cdot f'(x)$$

Product and Quotient

$$\frac{d}{dx}[u \cdot v] = \qquad \qquad u' \cdot v + u \cdot v'$$

$$\frac{d}{dx}\left(\frac{u}{v}\right) = \qquad \qquad \frac{u' \cdot v - u \cdot v'}{v^2}$$

Integration

Trigonometric Integrals

$$\int \sin x \, dx = -\cos x + C$$

$$\int \cos x \, dx = \sin x + C$$

$$\int \sin^2 x = \frac{1}{2}(x - \sin x \cos x) + C$$

$$\int \cos^2 x = \frac{1}{2}(x + \sin x \cos x) + C$$

$$\int \tan x \, dx = -\ln|\cos x| + C$$

$$\int \cot x \, dx = \ln|\sin x| + C$$

$$\int \sec x \, dx = \ln|\sec x + \tan x| + C$$

$$\int \csc x \, dx = -\ln|\csc x + \cot x| + C$$

$$\int \sec^2 x \, dx = -\cot x + C$$

$$\int \sec^2 x \, dx = -\cot x + C$$

$$\int \csc x \cot x \, dx = -\csc x + C$$

Reduction Formulas for Sine and Cosine

$$\int \sin^n x \, dx = -\frac{1}{n} \sin^{n-1} x \cos x + \frac{n-1}{n} \int \sin^{n-2} x \, dx$$
$$\int \cos^n x \, dx = \frac{1}{n} \cos^{n-1} x \sin x + \frac{n-1}{n} \int \cos^{n-2} x \, dx$$

Inverse Trigonometric Integrals

$$\int \frac{1}{\sqrt{a^2 - x^2}} dx = \arcsin\left(\frac{x}{a}\right) + C$$

$$\int \frac{1}{a^2 + x^2} dx = \frac{1}{a} \arctan\left(\frac{x}{a}\right) + C$$

$$\int \frac{1}{x\sqrt{x^2 - a^2}} dx = \frac{1}{a} \operatorname{arcsec}\left(\frac{x}{a}\right) + C$$

Regular Integrals and e

$$\int x^n dx = \frac{1}{n+1} x^{n+1} + C$$

$$\int \frac{1}{x} dx = \ln|x| + C$$

$$\int e^x dx = e^x + C$$

$$\int e^{ax} dx = \frac{1}{a} e^{ax} + C$$

$$\int e^{f(x)} f'(x) dx = e^{f(x)} + C$$

Common Definite Integrals Exponetials

$$\int_0^b e^x dx = e^b - 1$$

$$\int_0^b e^{-x} dx = 1 - e^{-b}$$

$$\int_0^\infty e^{-x} dx = 1$$

$$\int_0^\infty x^n e^{-x} dx = n!$$

Sines and Cosines

n	$\int_0^{\pi/2} \sin^n x dx$	$\int_0^{\pi/2} \cos^n x dx$	$\int_0^\pi \sin^n x dx$	$\int_0^\pi \cos^n x dx$	$\int_0^{2\pi} \sin^n x dx$	$\int_0^{2\pi} \cos^n x dx$
1	1	1	2	0	0	0
2	$\pi/4$	$\pi/4$	$\pi/2$	$\pi/2$	π	π
3	2/3	2/3	4/3	0	0	0
4	$3\pi/16$	$3\pi/16$	$3\pi/8$	$3\pi/8$	$3\pi/4$	$3\pi/4$
5	8/15	8/15	16/15	0	0	0
6	$5\pi/32$	$5\pi/32$	$5\pi/16$	$5\pi/16$	$5\pi/8$	$5\pi/8$

θ	Radians	$\sin(\theta)$	$\cos(\theta)$	$\tan(\theta)$
0°	0	0	1	0
30°	$\pi/6$	1/2	$\sqrt{3}/2$	$\sqrt{3}/3$
45°	$\pi/4$	$\sqrt{2}/2$	$\sqrt{2}/2$	1
60°	$\pi/3$	$\sqrt{3}/2$	1/2	$\sqrt{3}$
90°	$\pi/2$	1	0	-
180°	π	0	-1	0
270°	$3\pi/2$	-1	0	_

Table 1: Important Trigonometric Angles

Trigonometric Identities

Pythagorean

$\sin^2 \theta + \cos^2 \theta = 1$ $\tan^2 \theta + 1 = \sec^2 \theta$ $1 + \cot^2 \theta = \csc^2 \theta$

Even and Odd

$$\sin(-x) = -\sin x$$

$$\cos(-x) = \cos x$$

$$\tan(-x) = -\tan x$$

Product to Sum

$$\sin x \sin y = \frac{1}{2} [\cos(x-y) - \cos(x+y)]$$

$$\cos x \cos y = \frac{1}{2} [\cos(x-y) + \cos(x+y)]$$

$$\sin x \cos y = \frac{1}{2} [\sin(x+y) + \sin(x-y)]$$

$$\cos x \sin y = \frac{1}{2} [\sin(x+y) - \sin(x-y)]$$

Sum to Product

$$\sin x + \sin y = 2 \sin \left(\frac{x+y}{2}\right) \cos \left(\frac{x-y}{2}\right)$$

$$\sin x - \sin y = 2 \cos \left(\frac{x+y}{2}\right) \sin \left(\frac{x-y}{2}\right)$$

$$\cos x + \cos y = 2 \cos \left(\frac{x+y}{2}\right) \cos \left(\frac{x-y}{2}\right)$$

$$\cos x - \cos y = -2 \sin \left(\frac{x+y}{2}\right) \sin \left(\frac{x-y}{2}\right)$$

Half Angle

$$\sin^{2}(x) = \frac{1 - \cos(2x)}{2}$$

$$\cos^{2}(x) = \frac{1 + \cos(2x)}{2}$$

Double Angle

$$\sin 2x = 2 \sin x \cos x$$

$$\cos 2x = \cos^2 x - \sin^2 x$$

$$2 \cos^2 x - 1$$

$$1 - 2 \sin^2 x$$

$$\frac{2 \tan x}{1 - \tan^2 x}$$