

## Basic Derivatives

$$\frac{d}{dx} e^{f(x)} = f'(x) e^{f(x)}$$

$$\frac{d}{dx} \sin f(x) = \cos f(x) \cdot f'(x)$$

$$\frac{d}{dx} \cos f(x) = -\sin f(x) \cdot f'(x)$$

$$\frac{d}{dx} \tan f(x) = \sec^2 f(x) \cdot f'(x)$$

$$\frac{d}{dx} \cot f(x) = -\csc^2 f(x) \cdot f'(x)$$

$$\frac{d}{dx} \sec f(x) = \sec f(x) \tan f(x) \cdot f'(x)$$

$$\frac{d}{dx} \csc f(x) = -\csc f(x) \cot f(x) \cdot f'(x)$$

$$\frac{d}{dx} \ln f(x) = \frac{f'(x)}{f(x)}$$

$$\frac{d}{dx} \log_a f(x) = \frac{f'(x)}{f(x) \ln a}$$

$$\frac{d}{dx} (f(x))^n = n (f(x))^{n-1} f'(x)$$

$$\frac{d}{dx} \sqrt{f(x)} = \frac{f'(x)}{2\sqrt{f(x)}}$$

$$\frac{d}{dx} a^x = a^x \ln a$$

$$\frac{d}{dx} b^{g(x)} = b^{g(x)} \ln b \cdot g'(x)$$

## Chain Rule

$$\frac{d}{dx} f(g(x)) = f'(g(x)) \cdot g'(x)$$

## Higher-Order Derivatives

$$\frac{d^2}{dx^2} e^x = e^x$$

$$\frac{d^3}{dx^3} \sin x = -\cos x$$

$$\frac{d^4}{dx^4} \cos x = \cos x$$

## Inverse Trigonometric

$$\frac{d}{dx} \arcsin f(x) = \frac{f'(x)}{\sqrt{1 - (f(x))^2}}$$

$$\frac{d}{dx} \arccos f(x) = -\frac{f'(x)}{\sqrt{1 - (f(x))^2}}$$

$$\frac{d}{dx} \arctan f(x) = \frac{f'(x)}{1 + (f(x))^2}$$

$$\frac{d}{dx} \operatorname{arccot} f(x) = -\frac{f'(x)}{1 + (f(x))^2}$$

$$\frac{d}{dx} \operatorname{arcsec} f(x) = \frac{f'(x)}{|f(x)| \sqrt{(f(x))^2 - 1}}$$

$$\frac{d}{dx} \operatorname{arccsc} f(x) = -\frac{f'(x)}{|f(x)| \sqrt{(f(x))^2 - 1}}$$

## Hyperbolic Function

$$\frac{d}{dx} \sinh f(x) = \cosh f(x) \cdot f'(x)$$

$$\frac{d}{dx} \cosh f(x) = \sinh f(x) \cdot f'(x)$$

$$\frac{d}{dx} \tanh f(x) = \operatorname{sech}^2 f(x) \cdot f'(x)$$

$$\frac{d}{dx} \coth f(x) = -\operatorname{csch}^2 f(x) \cdot f'(x)$$

$$\frac{d}{dx} \operatorname{sech} f(x) = -\operatorname{sech} f(x) \tanh f(x) \cdot f'(x)$$

$$\frac{d}{dx} \operatorname{csch} f(x) = -\operatorname{csch} f(x) \coth f(x) \cdot f'(x)$$

## Product and Quotient

$$\frac{d}{dx} [u \cdot v] = u' \cdot v + u \cdot v'$$

$$\frac{d}{dx} \left( \frac{u}{v} \right) = \frac{u' \cdot v - u \cdot v'}{v^2}$$

$\theta$	Radians	$\sin(\theta)$	$\cos(\theta)$	$\tan(\theta)$
$0^\circ$	0	0	1	0
$30^\circ$	$\pi/6$	$1/2$	$\sqrt{3}/2$	$\sqrt{3}/3$
$45^\circ$	$\pi/4$	$\sqrt{2}/2$	$\sqrt{2}/2$	1
$60^\circ$	$\pi/3$	$\sqrt{3}/2$	$1/2$	$\sqrt{3}$
$90^\circ$	$\pi/2$	1	0	—
$180^\circ$	$\pi$	0	−1	0
$270^\circ$	$3\pi/2$	−1	0	—
$360^\circ$	$2\pi$	0	1	0

Table 1: Important Trigonometric Angles