## Multivariable Calculus Practice Set III

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- 1. (3 points) Determine the absolute extrema for the function  $f(x,y) = x^2 + 3y^2 2x y xy$  on the triangular region with vertices (0,0), (2,0), and (0,1).
- 2. (1 point each) Convert each as indicated; leave each answer as exact:
  - (a) Convert the rectangular point (-5,1) to polar coordinates.
  - (b) Convert the cylindrical point  $(5, \frac{7\pi}{6}, 2)$  to rectangular.
  - (c) Convert the rectangular point (-2, 4, -1) to spherical.
  - (d) Convert the spherical point  $(4, \frac{11\pi}{6}, \frac{3\pi}{4})$  to cylindrical.
- 3. (3 points) Determine the value of each given integral. You need to do the work here by hand, but of course can check any answers with technology.
- 4. (3 points) Find the volume of the solid described by  $x^2 + y^2 \le 1$ ,  $x \ge 0$ ,  $0 \le z \le 4 y$ .
- 5. (3 points) Find the average value of the function  $f(x,y) = x \sin(y)$  over the region enclosed by y = 0,  $y = x^2$ , and x = 1.
- 6. (3 points) Find the volume of the solid that lives within both the cylinder  $x^2 + y^2 = 1$  and sphere  $x^2 + y^2 + z^2 = 9$ .