## Paul Gustafson Math 644

## **HW** 1

- ${f 1}$  Given a (left) R-module show:
  - i. The covariant functor  $\operatorname{Hom}_R(M,-)$  is a left-exact functor.

*Proof.* Let  $0\to A\xrightarrow{f} B\xrightarrow{g} C\to 0$  be a short exact sequence. Application of the functor gives a complex

ii. This functor is right-exact iff M is a projective R-module.

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