

Name:\_\_\_\_\_

Student ID:\_\_\_\_\_

Section:\_\_\_\_\_

Instructor: Paul Gustafson

# Math 131 (Principles of Calculus)

## Final Exam A

# RED

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Instructions:

- Simplify your answers.
- Calculators are allowed.
- Should you have need for more space than is allocated to answer a question, use the back of the exam.
- **Honor Code:**

An Aggie does not lie, cheat, or steal or tolerate those who do.

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Signature

**Multiple Choice (5 points each)** Mark the correct answer on the bubble sheet.

For questions 1-4, use the following graph of  $f(x)$ :

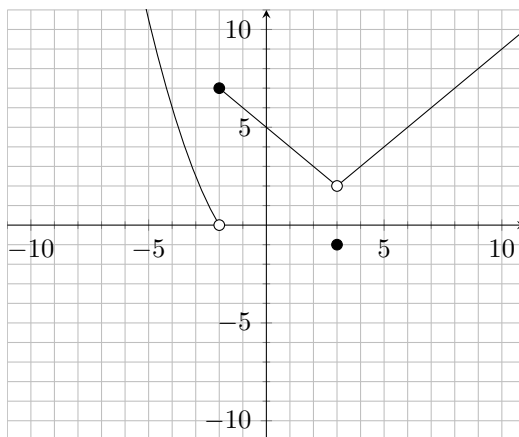


Figure 1:  $f(x)$

1. According to the graph of  $f(x)$ , the  $\lim_{x \rightarrow 3} f(x)$  equals which of the following.

- a)  $-3$                                       b)  $8$                                       c)  $-1$   
d)  $2$     e) The limit does not exist.

2. According to the graph of  $f(x)$ , the  $\lim_{x \rightarrow -2^-} f(x)$  equals which of the following.

- a)  $7$     b)  $0$                                       c)  $-2$   
d)  $-5$     e) The limit does not exist.

3. According to the graph of  $f(x)$ , the  $\lim_{x \rightarrow 5} f(x)$  equals which of the following.

- a)  $8$     b)  $4$                                       c)  $-1$   
d)  $0$     e) The limit does not exist.

4. According to the graph of  $f(x)$ , the function  $f(x)$  is not continuous at  $x = 3$  because

- a) there is a horizontal asymptote at  $x = 3$ .      b) there is a vertical asymptote at  $x = 3$ .      c)  $f(x)$  is not defined at  $x = 3$ .  
d)  $\lim_{x \rightarrow 3} f(x)$  does not exist.                      e) there is a removable discontinuity at  $x = 3$

5. The graph of  $g(x)$  is given below.

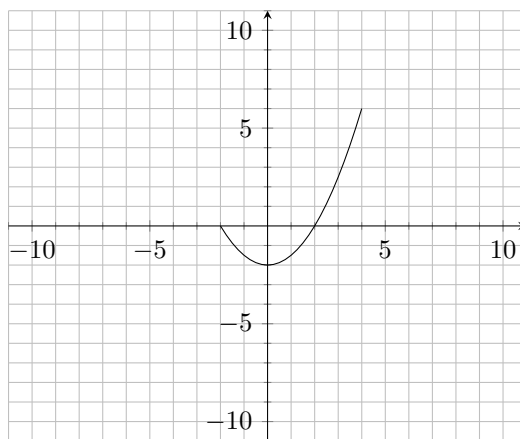


Figure 2:  $g(x)$

According to the graph above, the domain and range of  $g(x)$  are

- a) Domain:  $[-4, 4]$ , Range:  $[-6, 2]$
- b) Domain:  $[-2, -6]$ , Range:  $[-2, 4]$
- c) Domain:  $[-4, 4]$ , Range:  $[-4, 2]$
- d) Domain:  $[-6, 2]$ , Range:  $[-2, 4]$
- e) Domain:  $[-2, 4]$ , Range:  $[-2, 6]$

6. Find the domain of  $f(x) = \frac{1}{x^2 - 16}$ .

- a)  $(-2, 2) \cup (2, \infty)$
- b)  $(-\infty, -4) \cup (-4, 4) \cup (4, \infty)$
- c)  $(-\infty, -4) \cup (0, \infty)$
- d)  $(-\infty, -2) \cup (-2, 2) \cup (2, \infty)$
- e)  $[-2, 2)$

7. Let  $f(x) = \sqrt{4 - x^2}$  and  $g(x) = \ln(x)$ . What is the domain of  $f(x)g(x)$ ?

- a)  $(0, 2]$
- b)  $[-1, 2)$
- c)  $[-2, \infty)$
- d)  $(0, \infty)$
- e)  $[-2, 2]$

8. Evaluate  $\lim_{x \rightarrow 3} \frac{\sqrt{25 - x^2} - 4}{3 - x}$ .

a) 1

b)  $\frac{\sqrt{23} - 4}{2}$

c) -2

d)  $\frac{3}{4}$

e) 9

9. Given a function  $f(x)$ , then the graph of  $2f(3 - x)$  will be

a) the graph of  $f(x)$  shrunk horizontally by a factor of 2, shifted 4 units up, then reflected across the  $x$ -axis.

b) the graph of  $f(x)$  stretched vertically by a factor 3, shifted 2 units up, then reflected across the  $y$ -axis.

c) the graph of  $f(x)$  stretched vertically by a factor of 2, shifted 3 units to the right, then reflected across the  $y$ -axis.

d) the graph of  $f(x)$  stretched vertically by a factor of 2, shifted 3 units to the left, then reflected across the  $y$ -axis.

e) the graph of  $f(x)$  shrunk horizontally by a factor of 3, shifted 4 units to the right, then reflected across the  $x$ -axis.

10. A bacteria population doubles every 47 minutes. If the initial population is 1000 bacteria, how many bacteria will there be after 5 hours?

a)  $4.2 \times 10^4$

b)  $3.2 \times 10^3$

c)  $4.3 \times 10^3$

d)  $1.2 \times 10^3$

e)  $8.3 \times 10^3$

11. Find the derivative of the function  $f(x) = \frac{3}{x^3} - 4x^2 + 3$ .

a)  $-\frac{15}{x^2} - 8x$

b)  $-\frac{15}{x^2} + 3$

c)  $-\frac{9}{x^4} - 8x$

d)  $-\frac{9}{x^4} - 4$

e)  $-\frac{10}{x} - 3$



15. Find the linear approximation to  $\sqrt{x^2 + 8}$  at  $x = 1$

a)  $3x + \sqrt{8}$

b)  $\frac{2}{3}x + 3$

c)  $\frac{1}{3}x + \frac{8}{3}$

d)  $x + \sqrt{8}$

e)  $\frac{1}{3}x + 3$

16. We are given an unknown function  $f(x)$  such that  $f'(2) > 0$  and  $f''(2) < 0$ . We can conclude that at  $x = 2$ , the function  $f(x)$  has

a) a local min.

b) a local max.

c) an inflection point.

d) an undefined derivative.

e) none of the above.

17. Calculate the equation of the tangent line to  $y = \frac{1}{x}$  at  $x = 2$

a)  $y = -\frac{1}{2}x + \frac{1}{2}$

b)  $y = -\frac{1}{2}x + 2$

c)  $y = -\frac{1}{4}x + \frac{1}{2}$

d)  $y = x + \frac{1}{2}$

e)  $y = -\frac{1}{4}x + 1$

18. Find the absolute maximum and minimum values for the function  $f(x) = \ln(x^2 + 1)$  on the interval  $[-1, 3]$

a) maximum value = 2.30, minimum value = 1.1

b) maximum value = 3.62, minimum value = 1.1

c) maximum value = 2.30, minimum value = 0

d) maximum value = 3.62, minimum value = 0

e) maximum value = 1.32, minimum value = 1

19. Find the derivative of the function  $f(x) = \tan(xe^x)$ .

a)  $(1+x)e^x \sec^2(xe^x)$

b)  $e^x \sec^2(xe^x)$

c)  $(1+x)e^x \tan(xe^x)$

d)  $e^x \cos^2(xe^x)$

e)  $\sec^2(xe^x)$

20. If  $f'(x) = \frac{1}{2\sqrt{x}}$  and  $f(9) = 5$

a)  $f(x) = \frac{3}{4}x^{-3/2} + \frac{11}{4}$

b)  $f(x) = \sqrt{x} + \frac{7}{2}$

c)  $f(x) = \frac{1}{2}\sqrt{x} + 3$

d)  $f(x) = \frac{1}{2}\sqrt{x} + \frac{7}{2}$

e)  $f(x) = \sqrt{x} + 2$

21. A particle moves along a wire with velocity  $v(t) = 4\cos(2t)$ . Find the net change in position between time  $t = 0$  and  $t = \pi$

a)  $1 + \pi$

b)  $2\pi$

c)  $4\pi$

d)  $0$

e)  $\frac{\pi}{2}$

22. Alex wants to make a box with a square base, closed on all sides. He has 600 square inches of cardboard. What is the maximum volume of the box in cubic inches?

a) 598.32

b) 643.60

c) 1000

d) 1284.81

e) 1500

23. Calculate the indefinite integral  $\int \frac{1}{x} + \sec(3x) \tan(3x) dx$

a)  $\ln|x| + 3\sec(3x) + C$

b)  $\frac{2}{x^2} + \frac{1}{3}\sec(3x) + C$

c)  $\ln|x| + \frac{1}{3}\sec(3x) + C$

d)  $-\frac{2}{x^2} + \frac{1}{3}\tan(3x) + C$

e)  $\ln|x| + \frac{1}{3}\cot(3x) + C$





29. What is the average value of the function  $f(x) = \sin(x)$  on  $[0, \pi]$

a)  $2$

b)  $-2\pi$

c)  $-\frac{\pi}{2}$

d)  $\pi$

e)  $\frac{2}{\pi}$

30. Find the inverse function to  $f(x) = \ln(x+2) - \ln(x-3) + 7$ .

a)  $\frac{-2e^{x-7} - 3}{-e^{x-7} - 1}$

b)  $\frac{-3e^{x-7} - 2}{-e^{x-7} - 1}$

c)  $\frac{-3e^{x-7} - 2}{-e^{x-7} + 1}$

d)  $\frac{-2e^{x-1} - 3}{-e^{x-1} + 7}$

e)  $\frac{-2e^{x-3} - 2}{-e^{x-3} - 7}$

END OF EXAM