

# 1 Resources

Book: Timmerman . “Invitation to QG’s and Duality.” Section on  $SU_q(2)$ .  
Papers. Functional analysis.

- Woronowicz. “Twisted  $SU(2)$  group.”
- Woronowicz. “Compact matrix pseudogroups.”
- Woronowicz. “Compact Quantum Groups.”

Peter-Weyl theory.

- Koornwinder. “Orthogonal polynomials in connection to QGs”
- Masuda, Mimachi, Makagami, et al. “Representations of QGs and a q-analog of orthogonal polynomials.”

# 2 Compact (Matrix) Quantum Groups

Vague idea:  $G \subset M_N(\mathbb{C})$ , a compact group. Things you’d like: representations, harmonic analysis.

$$L^2(G) = \bigoplus_{\pi \in \text{Irr}(G)} L^2_{\pi}(G)$$

where

$$L^2_{\pi}(G) = \text{span}\{\pi_{ij}\}_{i,j \leq \dim(\pi)}$$

So, try to reformulate “without points.” I.e. think in terms of algebras instead of matrices, etc. From Gelfand:  $G \leftrightarrow C(G)$ . Can recover topology. To encode group structure, take duals of multiplication maps.