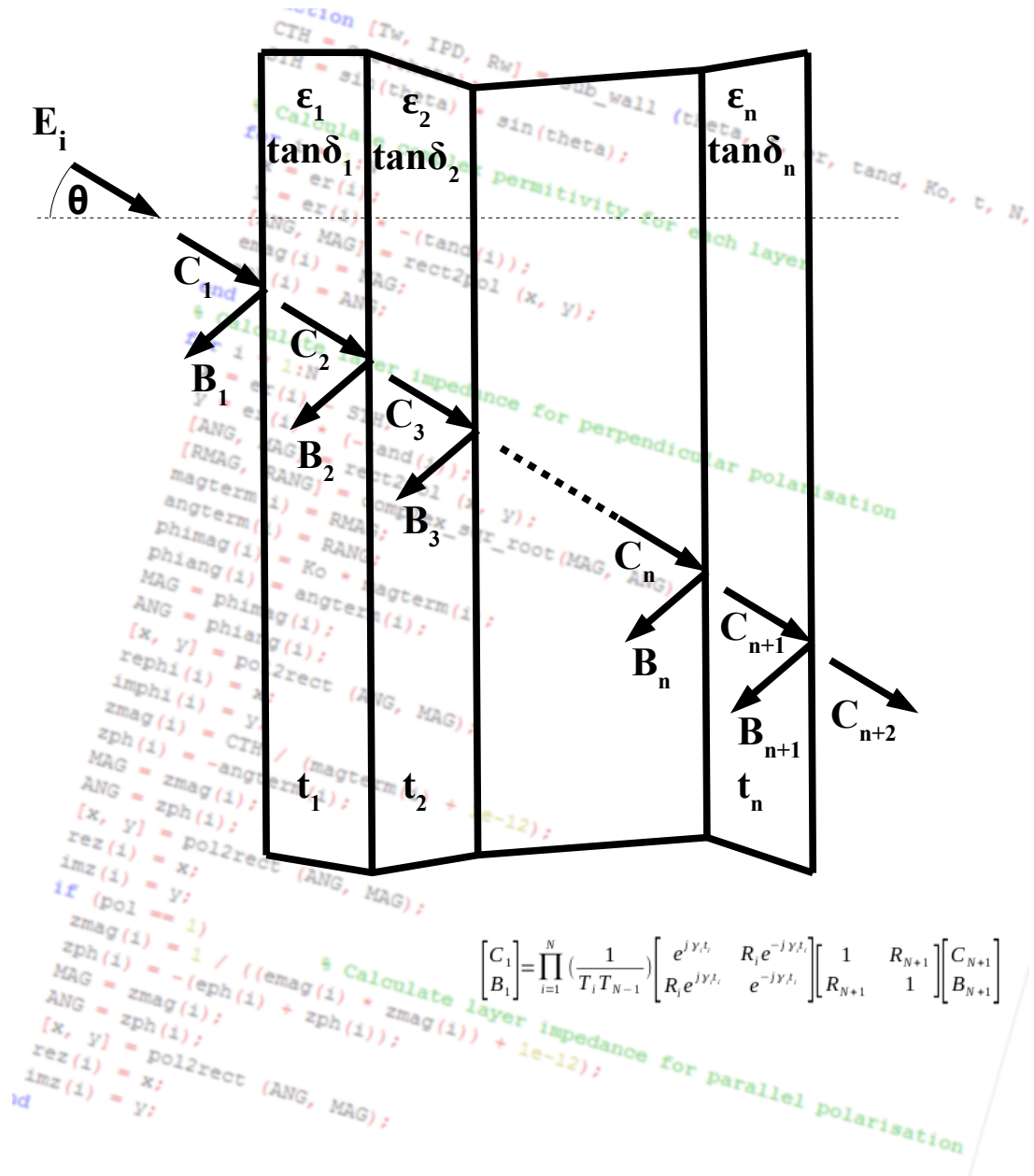


# A Software Tool for the Analysis of Multilayer Radomes

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May 2021

Version 1.2



## Multilayer Radome Analysis Software Instructions

This document describes the usage of the software written as a script for GNU Octave but should also work with Matlab which will predict the transmission, reflection and insertion phase delay performance when a perpendicular or parallel polarized wave is incident upon a single or multilayer radome such as an A or C-sandwich radome, or a dielectric stack-up of any number of layers. It is assumed that the dielectric layers are homogenous and isotropic in nature as shown in Figure 1.

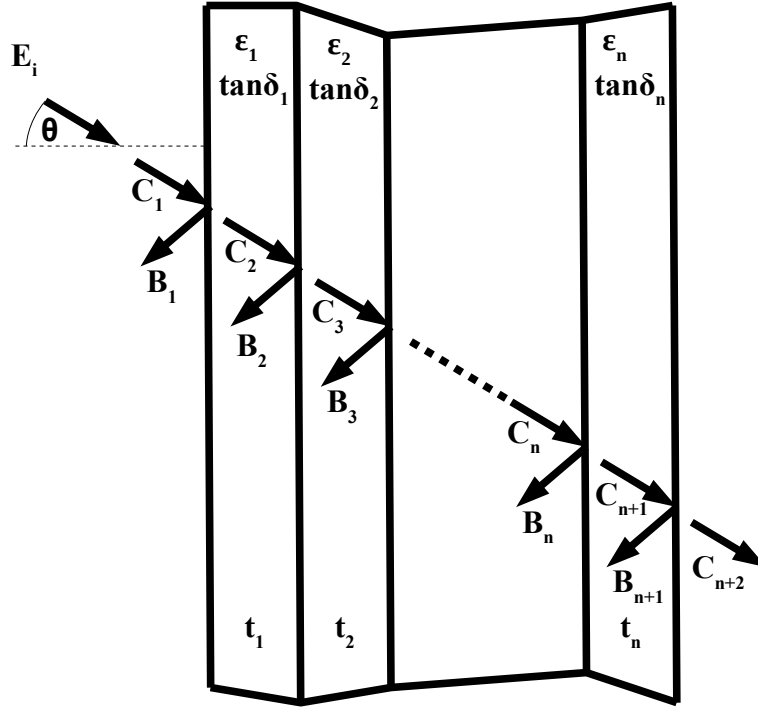


Figure.1

The analytical software is based on the boundary value solution of an N-layer dielectric wall using the Fresnel equations. This is described in the book “Analysis of Radome-Enclosed Antennas”, Dennis Kozakoff (Artech House, 1997), and will be repeated here for completeness. If the forward and reverse propagating waves are  $C_i$  and  $B_i$  respectively, the solution is:

$$\begin{bmatrix} C_1 \\ B_1 \end{bmatrix} = \prod_{i=1}^N \left( \frac{1}{T_i T_{N-1}} \right) \begin{bmatrix} e^{j\gamma_i t_i} & R_i e^{-j\gamma_i t_i} \\ R_i e^{j\gamma_i t_i} & e^{-j\gamma_i t_i} \end{bmatrix} \begin{bmatrix} 1 & R_{N+1} \\ R_{N+1} & 1 \end{bmatrix} \begin{bmatrix} C_{N+1} \\ B_{N+1} \end{bmatrix} \quad (1)$$

where,

$t_i$  = Layer thickness of the  $i^{\text{th}}$  layer.

$R_i, T_i$  = Fresnel reflection and transmission coefficients of the  $i^{\text{th}}$  layer, respectively.

$\gamma_i$  = Propagation constant in the  $i^{\text{th}}$  layer.

Angle of incidence  $\theta$  is relative to the normal of the radome surface.

$$y_i = k_0 \sqrt{\varepsilon_{ri} - \sin^2(\theta)} \quad (2)$$

The permittivity of the  $i^{\text{th}}$  layer is given by  $\varepsilon_i$  and  $k_0$  is the wave number in a vacuum. Permittivity is given by:

$$\varepsilon_{ri} = \varepsilon'_{ri} (1 - j \tan(\delta_i)) \quad (3)$$

The Fresnel transmission and reflection coefficients are calculated from the following:

$$R_i = \frac{Z_i - Z_{i-1}}{Z_i + Z_{i-1}}; T_i = 1 - R_i \quad (4)$$

The wave impedance calculated depends on the polarization of the incident wave. For perpendicular polarization we have:

$$Z_i = \frac{\cos(\theta)}{\sqrt{\varepsilon_{ri} - \sin^2(\theta)}} \quad (5)$$

For parallel polarization we have:

$$Z_i = \frac{\sqrt{\varepsilon_{ri} - \sin^2(\theta)}}{\varepsilon_{ri} \cos(\theta)} \quad (6)$$

When the matrix (1) is multiplied out, the following is obtained:

$$\begin{bmatrix} C_1 \\ B_1 \end{bmatrix} = \begin{bmatrix} A_{11} & A_{12} \\ A_{21} & A_{22} \end{bmatrix} \begin{bmatrix} C_{N+2} \\ B_{N+2} \end{bmatrix} \quad (7)$$

The voltage reflection coefficient from the radome's front surface is:

$$R_w = \frac{B_1}{C_1} | (B_{N+2} = 0) = \frac{A_{21}}{A_{11}} \quad (8)$$

The voltage transmission coefficient is:

$$T_w = \frac{C_{N+2}}{C_1} | (B_{N+2} = 0) = \frac{1}{A_{11}} \quad (9)$$

The reflection and transmission coefficients are both complex numbers, therefore it can be expressed as a magnitude and insertion phase delay (IPD), this is an angle. The radome transmission efficiency is:

$$|T_w|^2 \quad (10)$$

These equations are shown for completeness so that the program can be more easily followed for those who do not have access to “Analysis of Radome-Enclosed Antennas”. Buy the book if it’s available, I thoroughly recommend it!

The program is written in GNU Octave which should be compatible with Matlab. The master file calls a number of functions which are saved in separate files and must be present in the same folder/directory as the main function or any other function that calls them. An exhaustive description of the code will not be given but the complete listing of all functions is given at the end of the document and important sections are commented.

It is necessary to specify the problem with only changing these lines:

```
% Enter user variables here...
N = 5; % Enter number of layers
fl = 17; % Enter lower frequency in GHz
fh = 32; % Enter upper frequency in GHz
no_of_freq_points = 301; % Enter No. of frequency points
no_inc_ang = 3; % No. of incidence angles
ang_inc_step = 15; % Increment angle of incidence
% Enter the dielectric constant/permittivity for each layer
er1 = 4.0; er2 = 1.1; er3 = 4.0; er4 = 1.1; er5 = 4.0;
% Enter the loss tangent/tand for each layer
tand1 = 0.003; tand2 = 0.001; tand3 = 0.003; tand4 = 0.001; tand5 = 0.003;
% Enter the layer thickness in mm for each layer
t1 = 0.24; t2 = 2.1; t3 = 0.48; t4 = 2.1; t5 = 0.24;

er = [er1, er2, er3, er4, er5] % Enter dielectric constants
tand = [tand1, tand2, tand3, tand4, tand5] % Enter tand values (loss tangent)
t = [t1, t2, t3, t4, t5] % Enter layer thickness in mm
% End of user variables
```

Values are entered as a vector (one dimensional array) in the order of dielectric layers. Add or remove layers as necessary. The above code is for a five layer stack-up.

If you require more or less plots for differing angles of incidence, set the “no\_inc\_ang”, increments can be set with “ang\_inc\_step”.

Note that this version of the program is written in a traditional program flow with for loops defined where necessary. It would be far more efficient to perform calculations using native complex number notation and matrix operations instead of converting numbers from Cartesian to polar form and vice versa and to use matrix operations. This may be done at a future date.

When the program is run, six plots will be generated. These are the reflection, transmission and insertion phase delay for both perpendicular and parallel polarization of the incident E-field. The code can be modified by the user to generate only what plots are necessary.

## Comparisons between Analytic Software and CST FEM Solver

To confirm that the analytical software is giving the correct result, two benchmarks are presented below with equivalent simulations using CST Microwave Studio and its FEM solver with unit cell boundaries. Although unit cell FEM simulations may take a couple of minutes, the analytical method takes just seconds to complete and generate plots with the option for several angle of incidences. The results below are for 0° incidence.

## A-Sandwich Radome (3-layer stackup)

### A-Sandwich Sample

Outer Layers: plain weave GFRP, thickness 0.24mm,  $\epsilon_r = 4.0$ .

Core Layer: Millifoam RHC71, thickness 2.5mm,  $\epsilon_r = 1.1$ .

Values of  $\tan\delta$  are estimated to be 0.003 for GFRP, and 0.001 for the Millifoam, and these values were used for the analytical and numerical simulations for a like for like comparison.

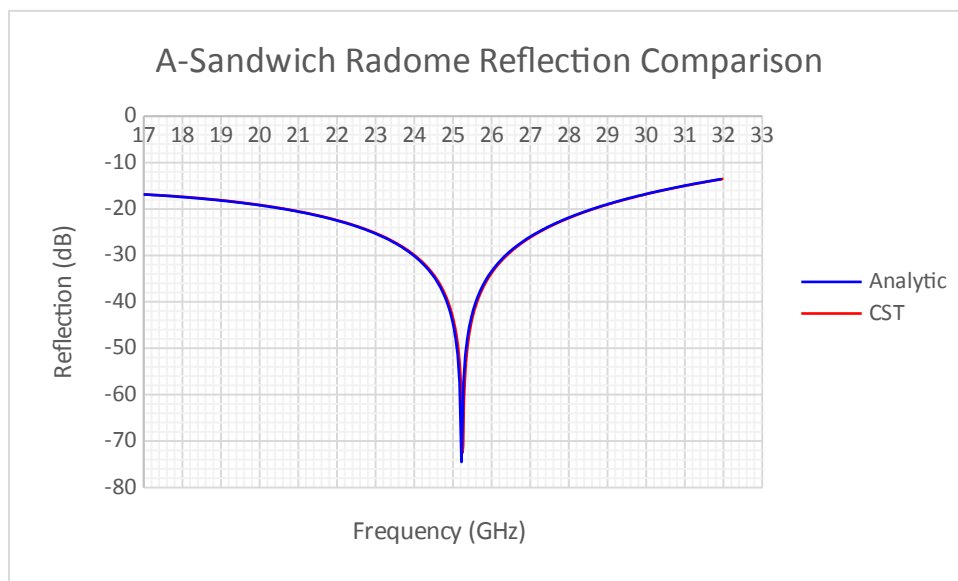


Figure. 2

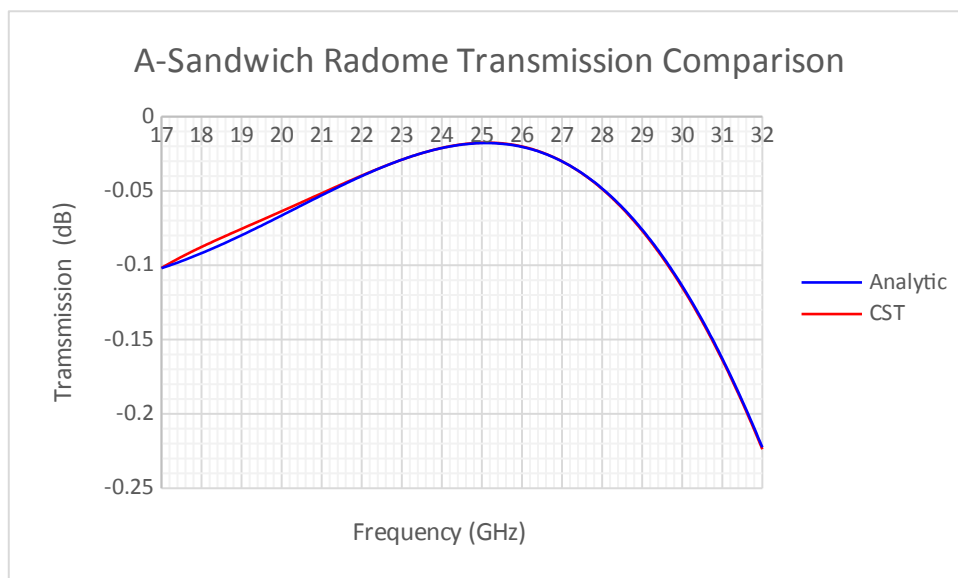


Figure. 3

## C-Sandwich Radome (5-layer stackup)

C-Sandwich Sample

Outer Layers: plain weave GFRP, thickness 0.24mm,  $\epsilon_r = 4.0$ .

Core Layers: Millifoam RHC71, thickness 2.1mm,  $\epsilon_r = 1.1$ .

Middle Layer: plain weave GFRP, thickness 0.48mm,  $\epsilon_r = 4.0$ .

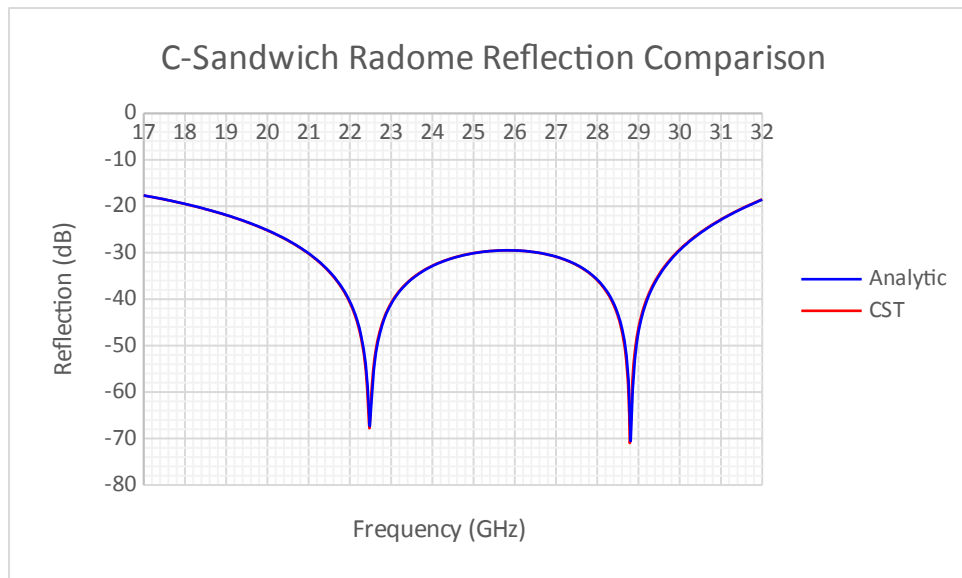
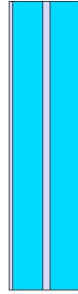


Figure. 4

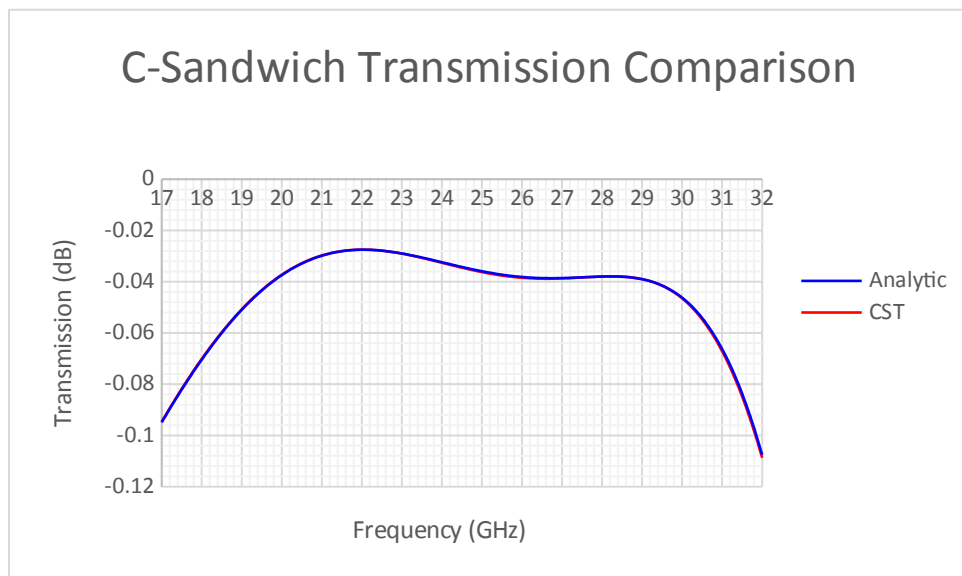


Figure. 5

## GNU Octave Code

```
% Program to calculate Transmission Loss, Insertion Phase Delay and Reflection
% for a multilayer radome.
% This program is a translation from 'Analysis of Radome-Enclosed Antennas'
% by Dennis J. Kozakoff, 1997, Artech House.
%
% Author: Dr Paul Klasmann
% Date: 05/11/2020      Version 1.1
%
% 1) Set N to equal the number of layers.
% 2) Set fl and fh to the lower and upper analysis frequency in GHz.
% 3) Set no_of_freq_points to a sensible value for the frequency range.
% 4) Setup the array values for the relative dielectric constant (er).
% 5) Setup the array values for the loss tangents (tand).
% 6) Setup the array values for the radome layer thicknesses (t) in mm.

close all
clear
clc
% Enter user variables here...
N = 5; % Enter number of layers
fl = 17; % Enter lower frequency in GHz
fh = 32; % Enter upper frequency in GHz
no_of_freq_points = 301; % Enter No. of frequency points
no_inc_ang = 3; % No. of incidence angles
ang_inc_step = 15; % Increment angle of incidence
% Enter the dielectric constant/permittivity for each layer
er1 = 4.0; er2 = 1.1; er3 = 4.0; er4 = 1.1; er5 = 4.0;
% Enter the loss tangent/tand for each layer
tand1 = 0.003; tand2 = 0.001; tand3 = 0.003; tand4 = 0.001; tand5 = 0.003;
% Enter the layer thickness in mm for each layer
t1 = 0.24; t2 = 2.1; t3 = 0.48; t4 = 2.1; t5 = 0.24;

er = [er1, er2, er3, er4, er5] % Enter dielectric constants
tand = [tand1, tand2, tand3, tand4, tand5] % Enter tand values (loss tangent)
t = [t1, t2, t3, t4, t5] % Enter layer thickness in mm
% End of user variables

finc = (fh-fl)/no_of_freq_points; % Frequency increment
eo = 8.854e-12; % Permittivity of free space (F/m)
RAD = pi/180; % For degree to radians conversion

% Begin Calculation
for pol = 0:1 % Pol=0 for Perpendicular Polarization
    array_index = 0; % Pol=1 for parallel polarization
    for f = fl:finc:fh
        array_index = array_index + 1;
        LAM = 300/f; % Lambda is wavelength in mm
        Ko = (2*pi/LAM); % Ko is wavenumber in mm^(-1)
        ANGLE = 0; % Initialize first incident angle to calculate
        for angle_index = 1:no_inc_ang;
            theta = ANGLE * RAD; % Theta is angle of incidence in radians
            % Call function sub_wall to perform main calculations
            [Tw, IPD, Rw] = sub_wall(theta, f, er, tand, Ko, t, N, pol);
            TwdB(array_index, angle_index) = 20 * log10(Tw);
            IPDdeg(array_index, angle_index) = -IPD / RAD;
            RwdB(array_index, angle_index) = 20 * log10(Rw);
            if(IPDdeg(array_index, angle_index) == -360)
                IPDdeg(array_index, angle_index) = 0;
            end
            ANGLE = ANGLE + ang_inc_step; % Increment angle of incidence
        end
    end
end
```

```

        end % END ANGLE LOOP
    end % END f LOOP

f = fl:finc:fh;
% Transmission Loss for perpendicular polarisation
if (pol == 0)
    % Plot TL for perpendicular polarisation
    figure
    for angle_index = 1:no_inc_ang;
        plot(f, TwdB(1:end,angle_index))
        hold on;
    end
    grid on
    set(gca,'linewidth',2, 'fontsize', 14, 'XTick', fl:1:fh)
    legendtext = ['0 degrees'; '15 degrees'; '30 degrees'; '45 degrees'; '60 degrees';
'75 degrees'];
    legend( legendtext, 'location', 'southeast' );
    title('Transmission Loss for Perpendicular Polarization','FontSize', 16);
    xlabel('Frequency (GHz)','FontSize', 14);
    ylabel('Transmission Loss (dB)','FontSize', 14);
    drawnow

    % Plot IPD for perpendicular polarisation
    figure
    for angle_index = 1:no_inc_ang;
        plot(f, IPDdeg(1:end,angle_index))
        hold on;
    end
    grid on
    set(gca,'linewidth',2, 'fontsize', 14, 'XTick', fl:1:fh)
    legendtext = ['0 degrees'; '15 degrees'; '30 degrees'; '45 degrees'; '60 degrees';
'75 degrees'];
    legend( legendtext, 'location', 'southeast' );
    title('Insertion Phase Delay for Perpendicular Polarization','FontSize', 16);
    xlabel('Frequency (GHz)','FontSize', 14);
    ylabel('Insertion Phase Delay (degrees)','FontSize', 14);
    drawnow

    % Plot Reflection for perpendicular polarisation
    figure
    for angle_index = 1:no_inc_ang;
        plot(f, RwdB(1:end,angle_index))
        hold on;
    end
    grid on
    set(gca,'linewidth',2, 'fontsize', 14, 'XTick', fl:1:fh)
    legendtext = ['0 degrees'; '15 degrees'; '30 degrees'; '45 degrees'; '60 degrees';
'75 degrees'];
    legend( legendtext, 'location', 'southeast' );
    title('Reflection for Perpendicular Polarization','FontSize', 16);
    xlabel('Frequency (GHz)','FontSize', 14);
    ylabel('Return Loss (dB)','FontSize', 14);
    drawnow

% Transmission Loss for Parallel Polarisation
elseif pol == 1
    % Plot TL for parallel polarisation
    figure
    for angle_index = 1:no_inc_ang;
        plot(f, TwdB(1:end,angle_index))
        hold on;
    end
    grid on

```



```

    set(gca,'linewidth',2, 'fontsize', 14, 'XTick', fl:1:fh)
    legendtext = ['0 degrees'; '15 degrees'; '30 degrees'; '45 degrees'; '60 degrees';
'75 degrees'];
    legend( legendtext, 'location', 'southeast' );
    title('Transmission Loss for Parallel Polarization','FontSize', 16);
    xlabel('Frequency (GHz)','FontSize', 14);
    ylabel('Transmission Loss (dB)','FontSize', 14);
    drawnow

% Plot IPD for parallel polarisation
figure
for angle_index = 1:no_inc_ang;
plot(f, IPDdeg(1:end,angle_index))
hold on;
end
grid on
set(gca,'linewidth',2, 'fontsize', 14, 'XTick', fl:1:fh)
legendtext = ['0 degrees'; '15 degrees'; '30 degrees'; '45 degrees'; '60 degrees';
'75 degrees'];
legend( legendtext, 'location', 'southeast' );
title('Insertion Phase Delay for Parallel Polarization','FontSize', 16);
xlabel('Frequency (GHz)','FontSize', 14);
ylabel('Insertion Phase Delay (degrees)','FontSize', 14);
drawnow

% Plot Reflection for parallel polarisation
figure
for angle_index = 1:no_inc_ang;
plot(f, RwdB(1:end,angle_index))
hold on;
end
grid on
set(gca,'linewidth',2, 'fontsize', 14, 'XTick', fl:1:fh)
legendtext = ['0 degrees'; '15 degrees'; '30 degrees'; '45 degrees'; '60 degrees';
'75 degrees'];
legend( legendtext, 'location', 'southeast' );
title('Reflection for Parallel Polarization','FontSize', 16);
xlabel('Frequency (GHz)','FontSize', 14);
ylabel('Return Loss (dB)','FontSize', 14);
drawnow

end
end          % END pol LOOP

```

## Function sub\_wall

```
function [Tw, IPD, Rw] = sub_wall (theta, f, er, tand, Ko, t, N, pol)
    CTH = cos(theta);
    STH = sin(theta) * sin(theta);

    % Calculate complex permitivity for each layer
    for i = 1:N
        x = er(i);
        y = er(i) * -(tand(i));
        [ANG, MAG] = rect2pol (x, y);
        emag(i) = MAG;
        eph(i) = ANG;
    end
    % Calculate layer impedance for perpendicular polarisation
    for i = 1:N
        x = er(i) - STH;
        y = er(i) * (-tand(i));
        [ANG, MAG] = rect2pol (x, y);
        [RMAG, RANG] = complex_sqr_root(MAG, ANG);
        magterm(i) = RMAG;
        angterm(i) = RANG;
        phimag(i) = Ko * magterm(i);
        phiang(i) = angterm(i);
        MAG = phimag(i);
        ANG = phiang(i);
        [x, y] = pol2rect (ANG, MAG);
        rephi(i) = x;
        imphi(i) = y;
        zmag(i) = CTH / (magterm(i) + 1e-12);
        zph(i) = -angterm(i);
        MAG = zmag(i);
        ANG = zph(i);
        [x, y] = pol2rect (ANG, MAG);
        rez(i) = x;
        imz(i) = y;
        if (pol == 1) % Calculate layer impedance for parallel polarisation
            zmag(i) = 1 / ((emag(i) * zmag(i)) + 1e-12);
            zph(i) = -(eph(i) + zph(i));
            MAG = zmag(i);
            ANG = zph(i);
            [x, y] = pol2rect (ANG, MAG);
            rez(i) = x;
            imz(i) = y;
        end
    end
    % End of layer impedance calculation
    zmag(N+1) = 1;
    zph(N+1) = 0;
    rez(N+1) = 1;
    imz(N+1) = 0;
    % Do next loop i = 1 serperately from the loop to include z for space before radome
    % because indexing starts at 1 and not 0. Then proceed with loop starting i=2
    i = 1;
    x = rez(i) - 1;
    y = imz(i) - 0;
    [ANG, MAG] = rect2pol (x, y);
    NUMMAG = MAG;
    NUMANG = ANG;
    x = rez(i) + 1;
    y = imz(i) + 0;
    [ANG, MAG] = rect2pol (x, y);
```

```

DENMAG = MAG;
DENANG = ANG;
RMAG(i) = NUMMAG / DENMAG;
Rph(i) = NUMANG - DENANG;
MAG = RMAG(i);
ANG = Rph(i);
[x, y] = pol2rect (ANG, MAG);
reR(i) = x;
imR(i) = y;
reT(i) = 1 + reR(i);
imT(i) = imR(i);
x = reT(i);
y = imT(i);
[ANG, MAG] = rect2pol (x, y);
Tmag(i) = MAG;
Tph(i) = ANG;

```

**% Continue from i=2**

```

for i = 2:(N+1)
    x = rez(i) - rez(i-1);
    y = imz(i) - imz(i-1);
    [ANG, MAG] = rect2pol (x, y);
    NUMMAG = MAG;
    NUMANG = ANG;
    x = rez(i) + rez(i-1);
    y = imz(i) + imz(i-1);
    [ANG, MAG] = rect2pol (x, y);
    DENMAG = MAG;
    DENANG = ANG;
    RMAG(i) = NUMMAG / DENMAG;
    Rph(i) = NUMANG - DENANG;
    MAG = RMAG(i);
    ANG = Rph(i);
    [x, y] = pol2rect (ANG, MAG);
    reR(i) = x;
    imR(i) = y;
    reT(i) = 1 + reR(i);
    imT(i) = imR(i);
    x = reT(i);
    y = imT(i);
    [ANG, MAG] = rect2pol (x, y);
    Tmag(i) = MAG;
    Tph(i) = ANG;
end

```

**% Matrix multiplications begin here**

```

Amag(1) = exp(-imphi(1) * t(1));
Amag(4) = 1 / Amag(1);
Amag(2) = RMAG(1) * Amag(4);
Amag(3) = RMAG(1) * Amag(1);
Aph(1) = rephi(1) * t(1);
Aph(2) = Rph(1) - Aph(1);
Aph(3) = Rph(1) + Aph(1);
Aph(4) = -Aph(1);

for K = 2:N
    Bmag(1) = exp(-imphi(K) * t(K));
    Bmag(4) = 1 / Bmag(1);
    Bmag(2) = RMAG(K) * Bmag(4);
    Bmag(3) = RMAG(K) * Bmag(1);
    Bph(1) = rephi(K) * t(K);
    Bph(2) = Rph(K) - Bph(1);
    Bph(3) = Rph(K) + Bph(1);

```

```

    Bph(4) = -Bph(1);
    [Amag, Aph] = cmult(Amag, Aph, Bmag, Bph);
end

Bmag(1) = 1;
Bmag(4) = 1;
Bmag(2) = RMAG(N + 1);
Bmag(3) = Bmag(2);
Bph(1) = 0;
Bph(2) = Rph(N + 1);
Bph(3) = Bph(2);
Bph(4) = 0;
[Amag, Aph] = cmult(Amag, Aph, Bmag, Bph);
tranmag = 1;
tranph = 0;

for j = 1:N + 1
    tranmag = tranmag * Tmag(j);
    tranph = tranph + Tph(j);
end

tranmag = 1 / (tranmag + 1e-12);

while (tranph > (2 * pi))
    tranph = tranph - (2 * pi);
endwhile

tranph = -tranph;
Tw = 1 / (tranmag * Amag(1));
Ttotph = -(tranph + Aph(1));
Rw = Amag(3) / Amag(1);
SUM = 0;
for j = 1:N
    SUM = SUM + t(j);
end

% Get IPD into correct quadrant
do
    if(Aph(1) < (CTH * Ko * SUM))
        Aph(1) = Aph(1) + (2 * pi);
    end
until (Aph(1) >= (CTH * Ko * SUM))

IPD = Aph(1) - (CTH * Ko * SUM);
endfunction

```

## Function cmult

```
function [Amag, Aph] = cmult(Amag, Aph, Bmag, Bph)
    for i = 1:2:3
        for j = 1:2
            R1 = Amag(i) * Bmag(j);
            R2 = Amag(i + 1) * Bmag(j + 2);
            E1 = Aph(i) + Bph(j);
            E2 = Aph(i + 1) + Bph(j + 2);
            R3 = (R1 * cos(E1)) + (R2 * cos(E2));
            E3 = (R1 * sin(E1)) + (R2 * sin(E2));
            Cmag(j + i - 1) = sqrt((R3*R3) + (E3*E3));
            if((R3 > 0) && (E3 > 0))
                PA = 0;
            elseif(R3 < 0)
                PA = pi;
            elseif((R3 > 0) && (E3 < 0))
                PA = 2 * pi;
            end
            Cph(j + i - 1) = atan(E3 / (R3 + 1e-12)) + PA;
        end
    end

    for i = 1:4
        Amag(i) = Cmag(i);
        Aph(i) = Cph(i);
    end
endfunction
```

## Function complex\_sqr\_root

```
function [RMAG, RANG] = complex_sqr_root(MAG, ANG)
    RMAG = sqrt(MAG);
    RANG = ANG / 2;
endfunction
```

## Function pol2rect

```
function [x, y] = pol2rect (ANG, MAG)

    x = MAG * cos(ANG);
    y = MAG * sin(ANG);

endfunction
```

## Function rect2pol

```
function [ANG, MAG] = rect2pol (x, y)

    MAG = sqrt((x^2) + (y^2));

    if ((x>0) && (y>0))
        corr = 0;
    elseif ((x<0) && (y<0))
        corr = pi;
    elseif ((x>0) && (y<0))
        corr = 0;
    elseif (x<0) && (y>0)
        corr = pi;
    elseif (x>0) && (y==0)
        corr = 0;
    end
```

```
    corr = 0;
elseif (x<0) && (y==0)
    corr = pi;
elseif (x==0) && (y!=0)
    corr = 0;
elseif (x==0) && (y==0)
    ANG = 0;
    return;
end

ANG = atan(y / (x + 1e-12)) + corr;

endfunction
```

## Bonus Material

### 1D FDTD Simulation of the C-Sandwich Radome

In addition to the analytical method described in this document the following is a Matlab/Octave code for a 1D FDTD (Finite Difference Time Domain) numerical calculation that produced the plot shown in the figure below. This gives further validation of the analytical method and provides an alternative way to simulate multilayer radomes. The FDTD code assumes a plane wave travelling in the z direction with a direction normal to the radome.

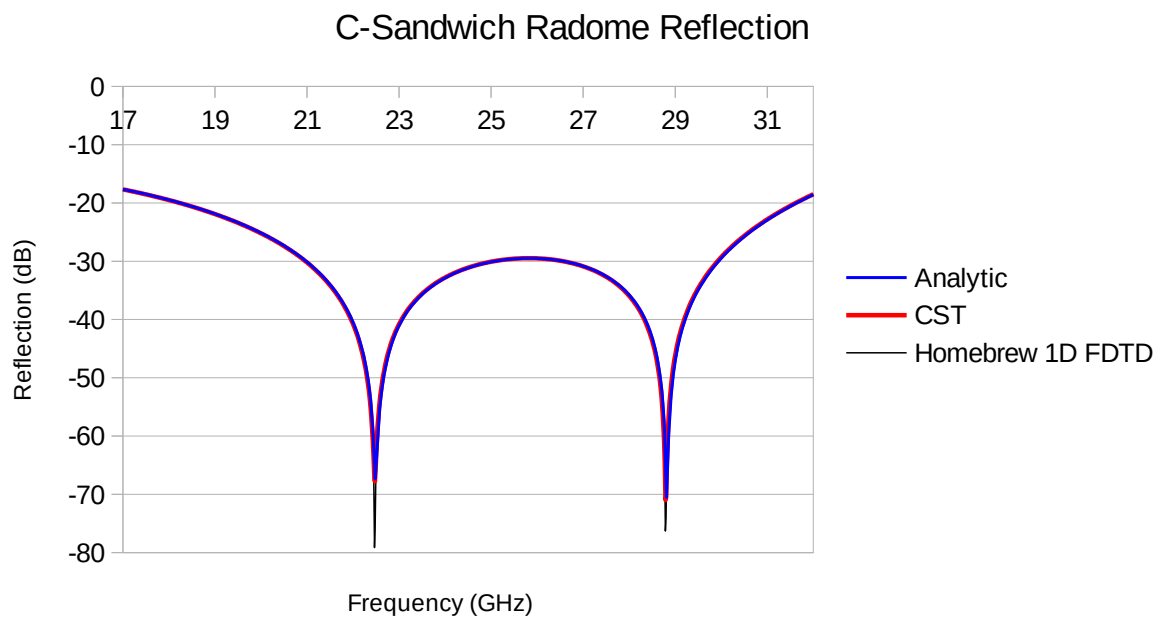


Figure. 6

The code listing for the FDTD simulation is shown on the following pages.

```

% Multilayer_Radome_1D_FDTD.m
% Calculate Reflectance and Transmittance of a multilayer radome

% INITIALIZE MATLAB
close all;
clc;
clear all;

% UNITS
meters = 1;
seconds = 1;

centimeters = 1e-2 * meters;
millimeters = 1e-3 * meters;
inches       = 2.54 * centimeters;
hertz        = 1/seconds;
kilohertz    = 1e3 * hertz;
megahertz    = 1e6 * hertz;
gigahertz    = 1e9 * hertz;

% CONSTANTS
c0 = 299792458 * meters/seconds;
e0 = 8.8541878176e-12 * 1/meters;
u0 = 1.2566370614e-6 * 1/meters;

%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
% STEP 1 -- DASHBOARD
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%

% SOURCE PARAMETERS
fmin = 17.0 * gigahertz;
fmax = 32.0 * gigahertz;
NFREQ = 500;
FREQ = linspace(fmin,fmax,NFREQ);

% DEVICE PARAMETERS FOR MULTILAYER RADOME
er1 = 1.1; % Millifoam
er2 = 4.0; % GFRP
er3 = 1.0; % Air
L1  = 2.1 * millimeters;
L2  = 0.24 * millimeters;
L3  = 0.48 * millimeters;

urmax = 1;

% GRID PARAMETERS
ermax = max([er1 er2 er3]); % Find greatest dielectric constant
nmax  = sqrt(ermax * urmax); % Greatest dk used to calculate refractive index

DDAT = [L2 L1 L3 L1 L2]; % Setup material length array
erDAT = [er2 er1 er2 er1 er2]; % Setup material dielectric constant array

NRES_LAM = 60; % Resolution in cells per wavelength
NRES_D    = 2; %
NSPC      = [100 100]; % Buffer of free space before and after device

%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
% STEP 2 -- CALCULATE GRID
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%

% CALCULATE INITIAL GRID RESOLUTION
Lmin  = min([L1 L2 L3]); % Find minimum physical length
lam_min = c0/fmax/nmax; % Calculate minimum lambda at fmax and in nmax

```



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dz1      = lam_min/NRES_LAM; % Minimum dz based on resolution min lam / resolution
dz2      = Lmin/NRES_D;      % Find min dz based on Lmin physical dimension
dz       = min([dz1 dz2]);   % Choose dz to be smallest of dz1 and dz2

% SNAP GRID TO CRITICAL DIMENSIONS
nz = ceil(Lmin/dz)
dz = Lmin/nz

% CALCULATE NUMBER OF GRID CELLS
Nz = ceil(L2/dz) + ceil(L1/dz) + ceil(L3/dz) + ceil(L1/dz) + ceil(L2/dz) + sum(NSPC) +
3

% CALCULATE ARRAY OF E FIELD POSITION
za = [0:Nz-1]*dz;

%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
% STEP 3 -- MODEL DEVICE ON THE GRID
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%

% INITIALIZE MATERIALS
ERxx = er3*ones(1,Nz); % er3 is free-space permitivity
URyy = ones(1,Nz);     % ur = 1 since non magnetic material

% CALCULATE START AND STOP INDICIES OF SLAB & INCORPORATE SLAB INTO ERxx
nz0 = 2 + NSPC(1) + 1; % nz0 is start of radome
nz1 = nz0;              % set nz1 to start index of radome
for nd = 1 : length(DDAT)
    nz2 = nz0 + round(sum(DDAT(1:nd))/dz) - 1; % Loop for start/stop of each layer
in DDAT
    ERxx(nz1:nz2) = erDAT(nd); % Insert er for material
    nz1 = nz2 + 1;
end

plot(za/millimeters,ERxx) % Uncomment to plot er of structure layers

%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
% STEP 4 -- CALCULATE THE TIME STEP
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%

% DETERMINE REFRACTIVE INDEX AT BOUNDARIES
nbc = sqrt(URyy(1)*ERxx(1));

% CALCULATE TIME STEP FOR PABC
dt = nbc*dz/(2*c0);

%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
% STEP 5 -- CALCULATE THE SOURCE
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%

% POSITION OF SOURCE
k_src = 2; % 2nd cell into simulation domain, from the left.

% CALCULATE GAUSSIAN PULSE PARAMETERS
tau = 0.5/fmax;
t0 = 3*tau;

% CALCULATE TIME ARRAY
N = 2000;
t = [0:N-1]*dt;

% CALCULATE Ex SOURCE
Exsrc = exp(-((t - t0)/tau).^2);

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% CALCULATE Hy SOURCE
nsrc = sqrt(ERxx(k_src)*URyy(k_src));
s = 0.5*nsrc*dz/c0 - dt/2;
A = sqrt(ERxx(k_src)/URyy(k_src));
Hysrc = A*exp(-((t - t0 + s)/tau).^2);

%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
% STEP 6 -- CALCULATE UPDATE COEFFICIENTS
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%

% CALCULATE UPDATE COEFFICIENTS
mEx = -(c0*dt/dz)./ERxx;
mHy = -(c0*dt/dz)./URyy;

%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
% STEP 7 -- INITIALIZE FOURIER TRANSFORMS
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%

% CALCULATE KERNELS
K = exp((-1i*2*pi*dt)*FREQ);

% INITIALIZE FOURIER TRANSFORM ARRAYS
ExR = zeros(1,NFREQ);
ExT = zeros(1,NFREQ);
SRC = zeros(1,NFREQ);

%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
% STEP 8 -- INITIALIZE FIELDS TO ZERO
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%

% INITIALIZE FIELDS TO ZERO
Ex = zeros(1,Nz);
Hy = zeros(1,Nz);

% INITIALIZE BOUNDARY FIELD TERMS
E1 = 0;    E2 = 0;
H1 = 0;    H2 = 0;

%
% MAIN FDTD LOOP -- ITERATE OVER TIME
%
for n = 1 : N

    % Step a -- Update Ex Boundary Terms
    E2 = E1;
    E1 = Ex(Nz);

    % Step b -- Update Ex
    Ex(1) = Ex(1) + mEx(1)*(Hy(1) - H2); % Direchlet BC so Hy(0) = 0
    for k = 2 : Nz
        Ex(k) = Ex(k) + mEx(k)*(Hy(k) - Hy(k-1));
    end

    % Step c -- Incorporate TF/SF Correction Term
    Ex(k_src) = Ex(k_src) - mEx(k_src)*Hysrc(n);

    % Step d -- Update Hy Boundary Terms
    H2 = H1;
    H1 = Hy(1);

    % Step e -- Update Hy
    for k = 1 : Nz -1

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    Hy(k) = Hy(k) + mHy(k)*(Ex(k+1) - Ex(k));
end
Hy(Nz) = Hy(Nz) + mHy(Nz)*(E2 - Ex(Nz)); % WDirchlet BC so Ex(k+1) = 0

% Step f -- Incorporate TF/SF Correction Term
Hy(k_src-1) = Hy(k_src - 1) - mHy(k_src - 1)*Exsrc(n);

% Step g -- Update Fourier Transforms
for nf = 1 : NFREQ
    ExR(nf) = ExR(nf) + (K(nf)^n)*Ex(1);
    ExT(nf) = ExT(nf) + (K(nf)^n)*Ex(Nz);
    SRC(nf) = SRC(nf) + (K(nf)^n)*Exsrc(n);
end

% Step h -- Visualize Simulation
if ~mod(n,50)

    % Calculate Spectra
    REF = abs(ExR./SRC).^2;
    TRN = abs(ExT./SRC).^2;
    CON = REF + TRN;

    % Prepare Figure Window
    clf;
    % Show Fields
    subplot(212);
    plot(za/millimeters,Ex, '-b');
    hold on;
    plot(za/millimeters,Hy, '-r');
    hold off;
    xlim([za(1) za(Nz)]/millimeters/meters);
    ylim([-1.8 1.8]);
    xlabel('z-axis');
    title(['Step ' num2str(n) ' of ' num2str(N) ]);
    % Show Spectra
    subplot(211);
    plot(FREQ/gigahertz,10*log10(REF), '-r');
    hold on;
    plot(FREQ/gigahertz,10*log10(TRN), '-b');
    plot(FREQ/gigahertz,10*log10(CON), ':k');
    hold off;
    xlim([fmin fmax]/gigahertz);
    ylim([-80 1.3]); % Change limits to suit...
    xlabel('Frequency (GHz)');
    title('Spectra');
    drawnow;
end
end
end

```

END OF DOCUMENT