Report on the CNN Code
PD-Internship
Lerner Paul
28/06/2018

Inspired by the works of Oh et al. and Bai et al. (cf. Report #3 and #4 respectively), I tried to use 1d CNN instead of a RNN.
Our work is then similar to Pereira et al. as we interpret the sensors signals as an image but instead of resizing it to a 2d, square image we keep it 1d. Moreover we keep the measures as an "image channel" dimension instead of having x columns for x measures as them (cf. report #2). Also, as them, we perform deep, end-to-end learning (we're the only two to do so on PD diagnosis via HaW, to the best of my knowledge, cf. report #2). Update : now catherine has done it, should we cite her even if her paper hasn't been published ?

Contents

1 Model architecture

Hypothesis :

1. As a 2d conv takes the spatial aspect of the data into account, a 1d conv takes the sequential aspect of the data into account
2. We don't need to predict a sequence so we don't need to pad the CNN layers or use causal convolutions as Bai et al. (cf. Report #4)
3. dilated convolutions allow the model to have a "large scope" before taking a decision (see Bai et al.).
4. a deep network will a priori extract advanced/complex features and we have don't have enough data for that.
5. we should aim for a feature map between 5 and 200 neurons, it's the number of features used by Mucha et al. and Drotar et al., respectively (cf. report #2)
6. stride is only good to reduce the dimensionality of the data/features
7. using a strided convolution or a strided pooling seems to be equivalent, therefore, intuitively, I prefer to use strided pooling and keep the stride of conv layer(s) at 1.

Questions :

1. how large should the kernel(s) be ?
2. should we first have a high dimensional data (i.e. with numerous filters) that we then pool or start with a small number of filters ?
3. how dilated should the conv(s) be ? Do the network needs to have a large scope ? I will first experiment without dilation.

In order to have the same sequence length on all samples I padded the samples to 16071 timesteps (max. length). We could also keep the data untrimmed and unpadded then pool with a kernel of the same size as the sequence length dimension in order to have only one neuron per filter. That's what I do in the CNN-baseline, see below :

1.1 Vanilla CNNs

1.1.1 CNN100-baseline

- only 1 conv layer with 100 kernels of size 1 (thus stride and dilation of 1) and ReLU activation and weight_norm regularization
- one pooling layer with a filter of 16071 (max length of the spiral) thus reducing the sequence to 1.
- dropout with probability 0.2

- one FC layer (fed the feature map of size 100) with a sigmoid activation

Later I might refer to this model as CNN***-baseline with *** being the number of kernels.

It's curious that we achieve decent results on all tasks with the CNN50-baseline (see 2 Results on multiple tasks) although we're not taking into account the sequential aspect of the data as we use a kernel size of 1.

1.1.2 Random Search

After padding all the spirals to 16071 (max. length), I performed a quick random search (~100 experiments) to find hyperparameters for a **2 layer CNN** in the following sets :

- learning_rate : {0.001, 0.0001}
- dropout : {0, 0.1, 0.2, 0.3, 0.4, 0.5}
- hidden_size : {4, 8, 16, 32}
- dilation : {1, 2, 4, 8, 16}
- conv_kernel : {1, 2, 4, 8, 16}
- pool_kernel : {8, 16, 32, 64, 128, 256, 512, 1024, 2048, 4096}

I achieved ~ 70% accuracy on the spiral task with 4 quite different models :
Table. Model hyperparameters displayed as [layer1, layer2].

learning rate	hidden_size	conv_kernel	pool_kernel	dilation	dropout
0.001	[4, 16]	[16, 2]	[512, 15]	[4, 16]	0
0.0001	[4, 32]	[2, 8]	[128, 118]	[8, 1]	0.1
0.001	[4, 32]	[16, 16]	[64, 128]	[2, 2]	0.3
0.001	[16, 32]	[8, 8]	[32, 474]	[1, 4]	0

It's quite hard to interpret this results, we can conclude that there's a lot of interactions between the different hyperparameters. Also the architecture is quite robust, most of the other "randomly" parametrized achieved more than 60% accuracy. Also we can see that none of these models has a convolutional kernel of size 1 as CNN***-baseline, although it achieves better results. This does not support hypothesis #4, we might extract deep features from the data. However these models achieve poor performance on other tasks like I and lektorka.
Thus I performed another random search for a **1 layer CNN** on the spiral task. The results reveal that the pool_kernel should be quite large, see figure below. We cannot make similar observations for the other hyper parameters as there is a lot of interaction between them (e.g. between convolutional kernel size and dilation). From this random search came out one model that turned out to outperform the baseline on most tasks, see 2 Results on multiple tasks). I called it **CNN-One** as it has only one layer.

Fig. 10 CV accuracy vs pooling kernel size over 170 experiments on the spiral task

1.2 Hierarchical Models

In order to augment the dataset, I tried splitting the tasks into subsequences : either stroke or "token" (e.g. "le", "les", see below). These models all have the same default : they're not applicable to the spiral task, although we might use only the first hierarchical block for it (see below).

1.2.1 Hierarchical CNN

As with RNN, I tried to build a hierarchical CNN on the *l* task : I split the task into letters (i.e. *l*s). See figure below. Unlike the previous RNN experiment, here I individually standardized each letter. Moreover, I padded each letter to 1242 timesteps (max. length). Since the subjects n° 12, 21, 23, 44, 67 did 6 *l* instead of 5 I discarded their last *l*.
Some subjects had on-paper strokes between the ls so I concatenated those with the previous closest l in order to maintain 5 ls per subjects.
See 1.2.2 Hierarchical Stroke CNN for architecture figure.

With this Hierarchical CNN we're able to achieve 65% accuracy on 10-CV. This is the first time we're able to go above chance level with the *l* task.
The hyperparameters were found with a quick random search (~10 experiments) in the same sets as before except for the pool_kernel which was in $\{1, 2, 4, 8, 16, 32, 64, 128, 256, 512\}$.

The same experiment was conducted with the le task (split into 5 "le"). Results are very similar. Only difference between the models is that Hierarchical used a Pool1 of 128 instead of 32 in order to keep the output length to the same order of magnitude as with the l task.

The inconvenient with this model is that it's not applicable to all tasks. Moreover, it's hard to tell where to split the task into letters or in sub-task.
I compared this model with an equivalent CNN (e2h) which was fed the whole *l* task. The model is the same except that the input is whole *l* task padded to 4226 timesteps (max length) so there's no concatenation obviously. Moreover, in order to provide roughly the same number of parameters, The Pool1 has a stride of 24 instead of 32 so the output length would be 173, as close as possible to 180.

This equivalent model achieves 58% accuracy on 10 CV so it suggests that the letter split augments the dataset and allows the hierarchical model to generalize better than the simple model. See table below.
I conducted the same experiment on the spiral task, using a Pool1 of stride 64 instead of 32 so the output length would be as close as possible to 180. It provided similar results as with the l task. The Hierarchical and the e2h model have too much parameters for this amount of training data. Dropout of more than 0.1 has made the training unstable on several models.

I also tried to learn over the spiral task with the letter-level block of the Hierarchical model. Just using a Pool1 of stride 8000 instead of 32 so that the FC layer still had 32 features as an input.

Table. Experiment results w.r.t. architecture. Best results per task are print in bold.

Task	***Model***	***Training acc***	***Test acc***
spiral	**CNN50-baseline**	0.74 (± 0.04)	**0.67** (± 0.15)
l (whole task)	CNN50-baseline	0.65 (± 0.06)	0.60 (± 0.12)
l (5 letters)	**Hierarchical CNN**	0.98 (± 0.02)	**0.65** (± 0.10)
l (whole task)	e2h CNN	0.93 (± 0.04)	0.58 (± 0.09)
spiral	e2h CNN	0.99 (± 0.01)	0.57 (± 0.21)
spiral	Hierarchical letter-level block	0.88 (± 0.02)	0.60 (± 0.11)

1.2.2 Hierarchical Stroke CNN (HS CNN)

As you'll see in 5.1.2 on-paper and in-air strokes, I hypothesized that the hierarchical model (and by extension, all CNNs) used the same filters to monitor both on-paper and in-air strokes. However, we know that both are very different, so I assumed they disturbed the model. Thus I extended Hierarchical CNN to Hierarchical Stroke CNN (HS CNN) where there is two $Conv1$:

1. for the on-paper strokes
2. for the in-air strokes

In order to maintain the number of strokes to 9 (5 ls + 4 in-air strokes between) among all subjects I discarded the strokes that were previously concatenated (see 1.2.1 Hierarchical CNN).

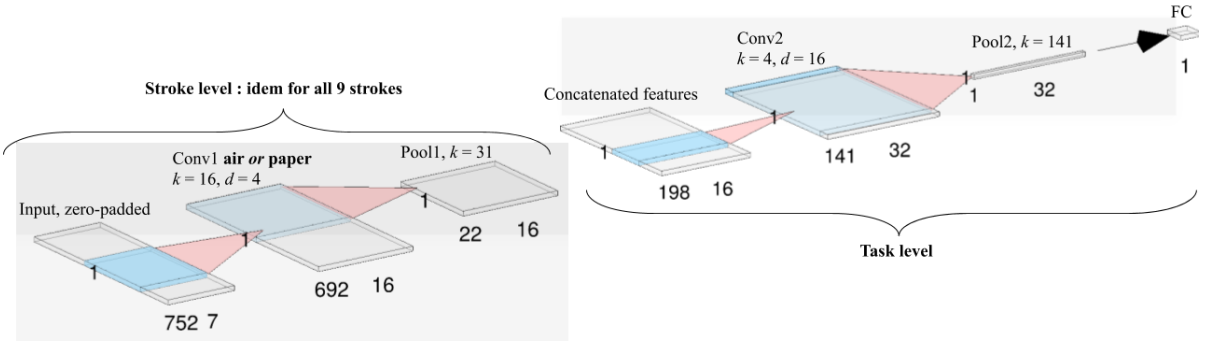


Fig. HS CNN. A dropout of 0.1 is applied after the pooling layers. Both Conv layers have ReLU activation and weight norm regularization. FC layer has Sigmoid activation. *k* stands for kernel size and *d* stands for dilation. Note that Conv1 is either Conv1_air or Conv1_paper and gets fed in-air and on-paper strokes, respectively.

This greatly improved the results over the l task (see table below). Similar results have been obtained with le and les task. This supports my hypothesis that the model doesn't use the button_status measure to its full advantage.
However it's quite difficult to apply this model to other tasks because they contain a lot of "intra-word" stroke which are not the same among all subjects so it's hard to tell which stroke should be discarded (see below).

In order to resolve this problem we could :

1. use all strokes and pad the strokes' list with a matrix of zeros.
2. use a RNN instead of a CNN for the task-level block of HS CNN.

Table. Experiment results w.r.t. architecture. Best results are print in bold.

Task	***Model***	***Training acc***	***Test acc***
l (5 letters)	Hierarchical CNN	0.98 (± 0.02)	0.65 (± 0.10)
l (9 strokes)	**HS CNN**	0.98 (± 0.02)	**0.77** (± 0.16)
l (zero-padded to 15 strokes)	HS CNN	0.96 (± 0.03)	0.75 (± 0.11)
majority voting on zero-padded l, le and les tasks	HS CNN	1.00 (± 0.00)	**0.78** (± 0.13)

I tried the first point and it provided similar results on the l, le and les tasks (see table above). However, it doesn't work very well with the lektorka and tram task. This may be because the # of strokes is highly variable on these tasks, unlike in the l, le and les tasks. E.g. on the le task, most strokes will be either on-paper "le" or in-air movement between 2 "le"s. However, on, e.g. lektorka, depending on the subject, the strokes might be "lektorka", "lekt", or "l".

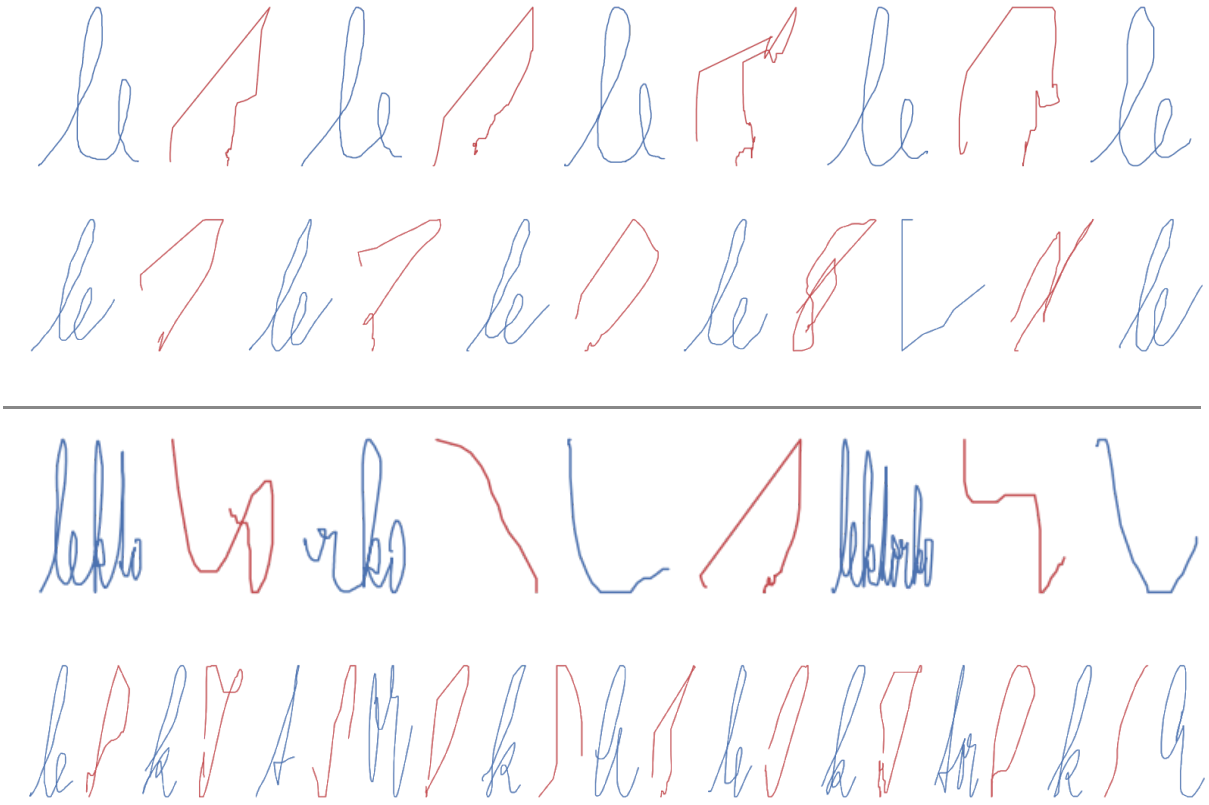


Fig. On-paper (blue) and in-air (red) strokes for subjects 70 (control, above) and 3 (PD, below) on tasks le (above) and lektorka (below). Note that the data has been standardized and that each stroke is displayed at its own scale.

I describe the second point in the next section.

1.2.3 Hierarchical Convolutional-Recurrent (H CRNN)

As splitting the strokes into air and paper improved the results over the H CNN, I assume that it would also for this model and didn't try to use full strokes.
As I explained in the last section, the HS CNN is hard to apply on most tasks which have a great varying number of strokes. So I replaced the task-level block of HS CNN with a RNN (On the lektorka task it provided similar results with a GRU and a LSTM). Thus there's no need to pad the strokes nor the list of strokes. The RNN is simply fed the concatenated features of length y (depending on the strokes' length) of the x strokes.
Surprisingly, the model achieves good results on the l task, unlike fully LSTM or GRU models we used previously. This may be because dependencies between timesteps are too long for a RNN. I again performed a random search on the l task and found a quite similar model (see figure below), as using the same hyperparameters as HS CNN led to overfitting (a LSTM with input of size 16 and hidden state of size 32 has 4352 parameters).

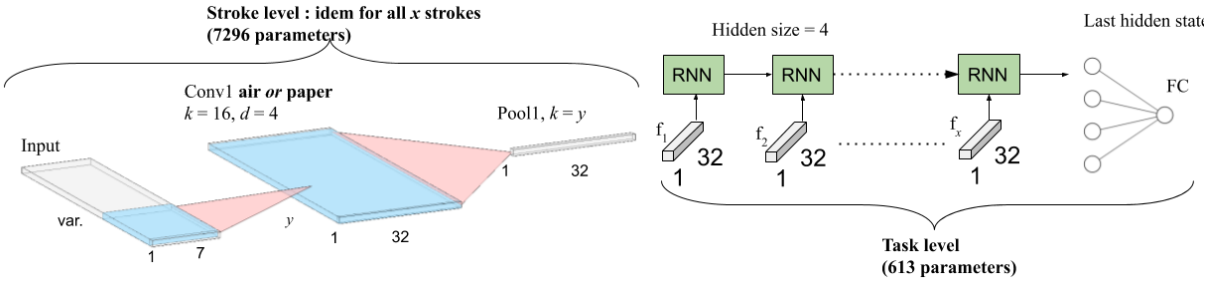


Fig. H CRNN. The kernel / stride of the Pooling layer is different between the tasks. It is set so that the result has a length of 1.

I said that there's no need to pad the strokes but that's an abuse of language because previously all strokes had to have the same length. However, we still have to pad the very short strokes to 61 timesteps as the first convolutional layer has a kernel size of 16 and a dilation of 4.

$$min = 1 + dilation \times (kernel - 1)$$

This approach is similar to Catherine's and also Chiu & Nichols who extracts character-level features from character embeddings using a CNN before feeding the feature vectors to a LSTM in order to perform Named Entity Recognition (NER). It's also similar to Granell et al. who slide a CNN which extracts features over a document before feeding those features to a LSTM for offline handwriting recognition.
This kind of model may be useful when the input data is very long, I think that the CNN layer acts as kind of dimensionality reduction, but I'm only conjecturing from our previous experiments.

See results in the 2 Results on multiple tasks. Moreover, using a CNN equivalent to the first block I achieved 64% accuracy on the spiral task;

1.3 Conclusions

- All of these models produce a relatively short feature map between 4 and 64 neurons which is fed to the FC layer (see also the plot in 1.1.2 Random Search). This partly supports hypothesis #5, partly because the models, even after
- The 1 layer CNNs are quite robust to the change of hyperparameters and adapts easily to all tasks.
- Except with the HS CNN and the H CRNN on tasks l, le and les, we don't significantly outperform the CNN50-baseline which doesn't take into account the sequential aspect of the data.

2 Results on multiple tasks

See 1 Model architecture for results w.r.t. model architecture.

Note that our models were not trained with the same number of epochs on all tasks, thus our results are a bit overoptimistic (between 1-5% accuracy). I don't know if we should display the results with models trained with the same n° of epochs on all tasks.

10-CV accuracy compared to Drotar et al. and Moetesum et al.

task	***CNN50-baseline***	***CNN-One***	***H CRNN***	***Drotar***	***Moetesum***
spiral	0.67 (± 0.15)	0.68 (± 0.16)	NA	0.63	**0.76** ± 0.08
l	0.60 (± 0.12)	0.60 (± 0.14)	**0.72** (± 0.09)	**0.72**	0.62 ± 0.08
le	0.62 (± 0.17)	0.62 (± 0.17)	0.64 (± 0.13)	**0.71**	0.57 ± 0.09
les	0.60 (± 0.12)	0.65 (± 0.14)	**0.72** (± 0.10)	0.66	0.60 ± 0.08
lektorka	0.60 (± 0.20)	**0.68** (± 0.13)	0.63 (± 0.16)	0.65	0.60 ± 0.07
porovnat	0.62 (± 0.15)	0.60 (± 0.13)	0.55 (± 0.22)	**0.73**	0.51 ± 0.09
nepopadnout	0.58 (± 0.16)	0.54 (± 0.12)	0.61 (± 0.08)	**0.68**	**0.68** ± 0.0
tram	0.63 (± 0.09)	0.52 (± 0.14)	0.57 (± 0.16)	**0.76**	0.51 ± 0.08
all tasks[1]	0.60 (± 0.13)	0.63 (± 0.15)	0.68 (± 0.12)	0.81	**0.83** ± 0.09

CNN-One slightly outperforms CNN-50 baseline on most tasks and after majority voting which suggests that it's better to take into account.
Although it's not applicable to the spiral task, H CRNN provides the best classification accuracy among our models after majority voting (if we don't take into account HS CNN, see 1.2.2 Hierarchical Stroke CNN).
We achieve competitive results with Drotar et al. on the l, le and les tasks with the H CRNN (and we outperform them with the HS CNN, see 1.2.2 Hierarchical Stroke CNN).
We achieve competitive results with Moetesum et al. with all our models, except on the spiral task. Moreover, majority voting results are disappointing. I also try to fuse the probability outputs of the models instead of majority voting but it provided similar results.

[1] But spiral on the H CRNN

3 Data

3.1 Augmentation

As I did with the RNN, I tried to augment the data by adding noise and by translating it along either the x or y axis. I chose these augmentation techniques because they didn't decrease the model performance with the RNN, unlike other techniques. However, with the CNN50-baseline, it decreased performance.

3.2 Downsampling

In order to first reduce the dimensionality of the data, I downsampled it 10 times. I used SciPy's decimate function which applies an anti-aliasing filter : order 8 Chebyshev type I filter. This had bad effect on the CNN-baseline. It can probably be explained because the filter must somehow smooth the data which may loose important information for PD diagnosis (e.g. tremor).

4 Model training

Training with a learning rate of 10^{-3} or 10^{-4} seems to work with most models.

4.1 Batch training

With CNNs, we need the input data to be equally long (cf. 1 Model architecture). This allows for a batch training, thus I trained the model on batches of the size of the training and test set respectively, regardless of the number of subjects in it. It divided the training time by 5 on the CNN50-baseline. However, as I've read [add ref], the model is less efficient as the loss is averaged thus less relevant. See figures below.

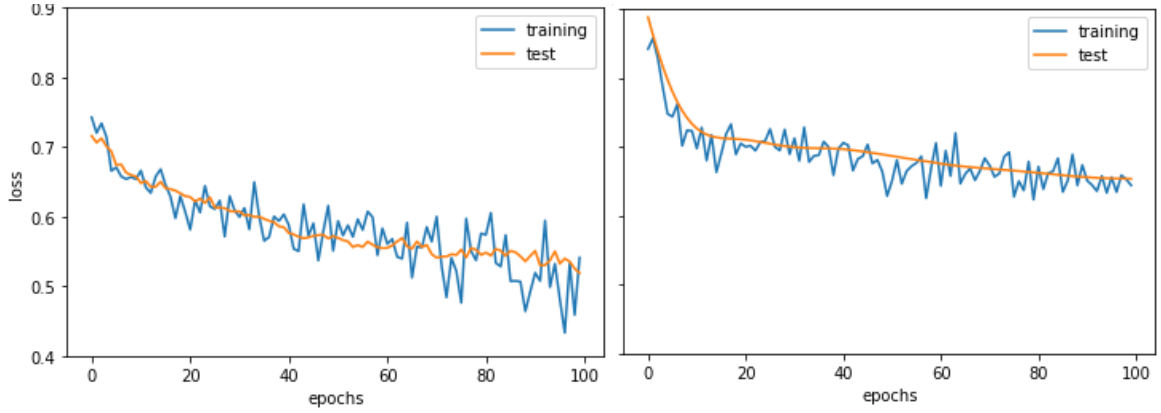
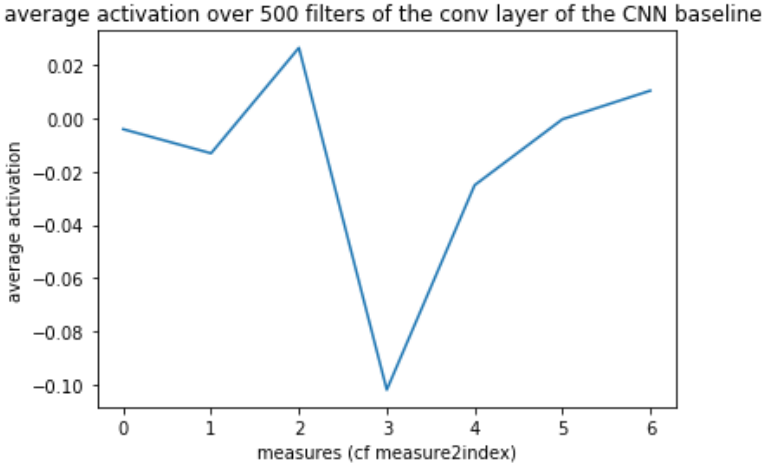


Fig. CNN50-baseline, left : training on a single subject batch, right : training on a multiple subjects' batch.

5 Visualization & Interpretation

5.1 Convolutional Layer

5.1.1 Measures



With the CNN500-baseline, after training on the last fold for 100 epochs (achieving 83% accuracy on the last epoch) we can see that, in average, the neurons corresponding to the button_status measures are less activated than other. This is probably because most of button status are at 1 (i.e. on-paper) for the spiral task we trained on, thus there's no need for 500 filters to monitor it. Moreover, this measure is redundant with pressure. This could also be explained by the binary nature of the variable, it contains less information then other measures. The shape of the plot is similar with the hCNN on the l task which suggests that my first hypothesis is wrong.

As the classification accuracy suggests, 500 seems to be a too big number of filters, several of them seems to be monitoring the same thing :

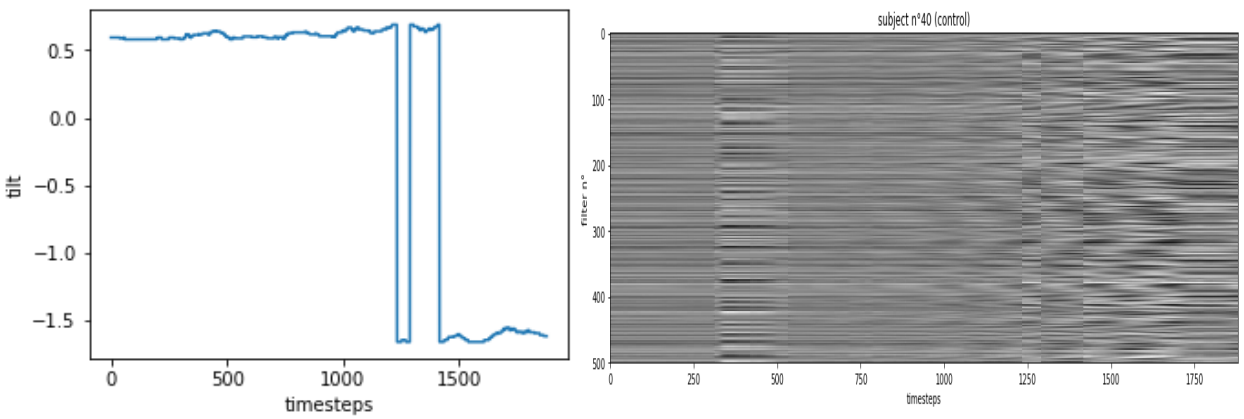


Fig. Subject n°40 (Control) Left : Tilt vs time, right : after a forward pass in the convolution layer (white means high activation, black low).

As you can see in the figure above, a lot of neurons seems to be highly activated when there's a drop in the tilt, see below for a zoom.

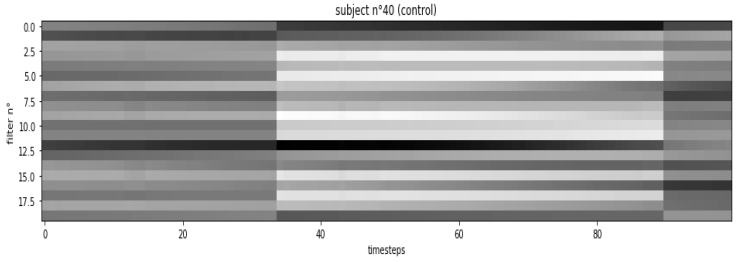


Fig. Zoom of the above figure : feature activation on filters 400 to 420 and timesteps 1200 to 1300.

As you can see, several filters activate at the exact same time : when there's a drop in the tilt measure (this has also been observed with subject n°8 (PD)). See below for details of filters 403 and 405.

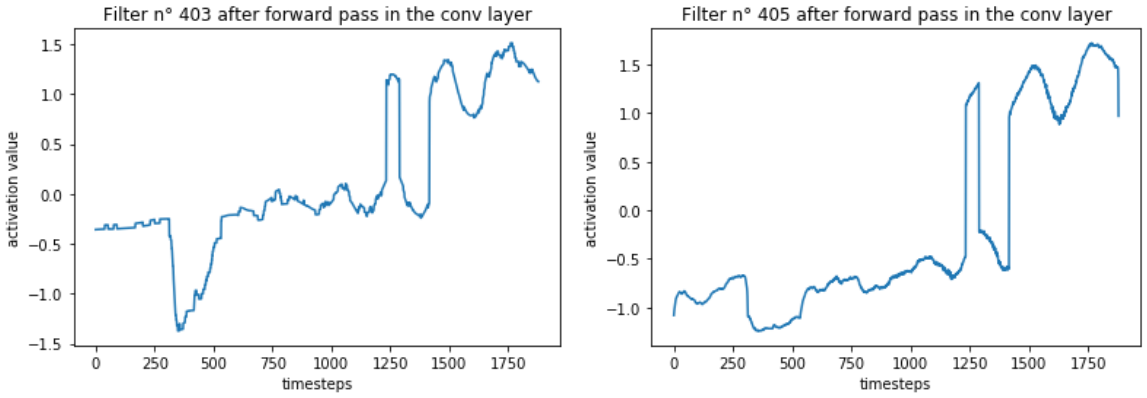


Fig. Activation of filters 403 and 405 (left and right, respectively).

Similar observations can be made when there's drop in other measure's, e.g. pressure or button_status (see average activation plot). Some filters seems to monitor different measure at the same time, see below.
With the Random-Search-CNNs with 2 layers (cf. 1.1.2 Random Search) which had only 4 filters in the first conv layer, none of these 4 filters seemed to monitor only one measure like above but several measures like below. This suggests that interaction between the measures is crucial.

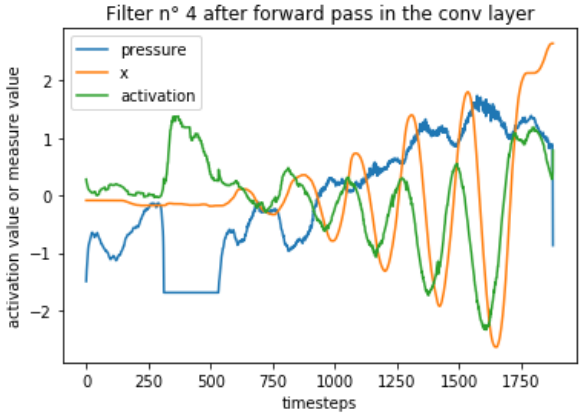


Fig. Filter 4 plotted along pressure and x-coordinate. We can see that the filter first activates when there's a drop in the pressure but then seems to follow the x coordinate.

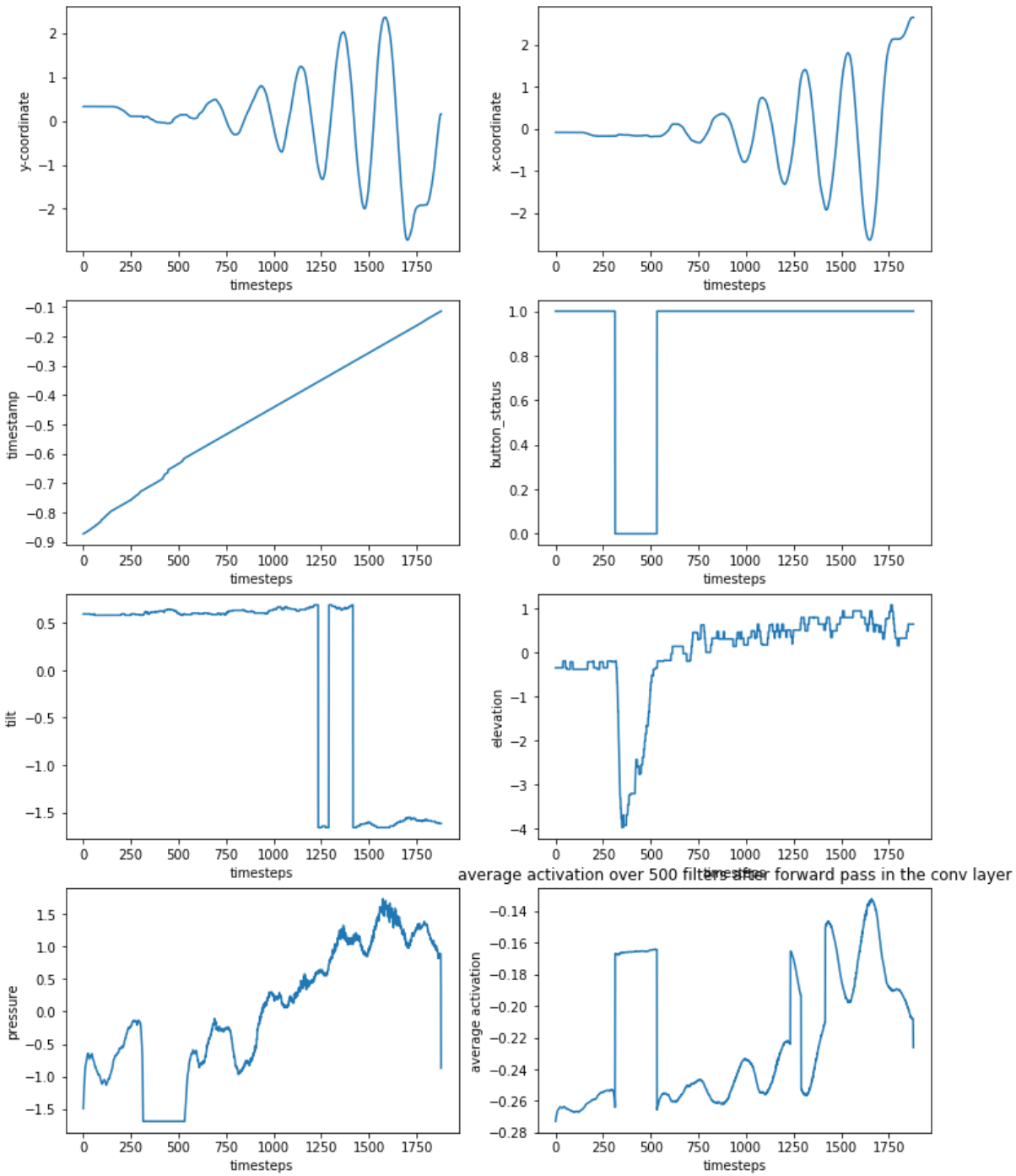
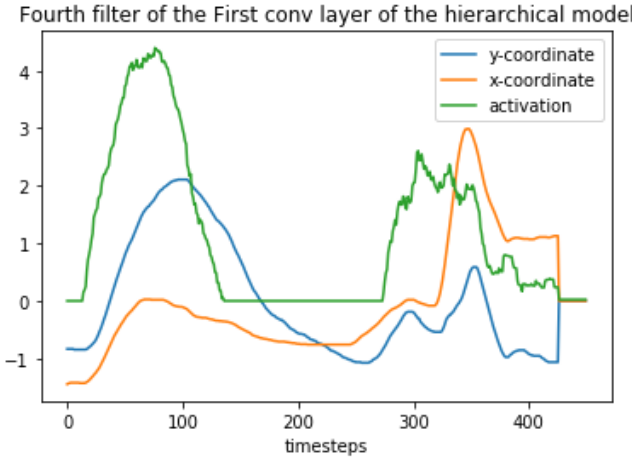


Fig. Subject's 40 (PD) measures vs time and average activation after forward pass in the conv layer (bottom right). We can see extremums in the average activation that match extremums in the measures (e.g peak around 1250 timesteps that we have observed above).

The first conv layer of the hCNN provides similar insights but the second layer is more difficult to interpret as it's more abstract.

5.1.2 on-paper and in-air strokes

With the hierarchical model on the l task, even on folds with good classification accuracy, the neurons seem to be monitoring the same thing regardless of in-air or on-paper strokes. See the plot below.



Plot. Fourth filter seems to monitor both x and y coordinate. The stroke is on-paper until timesteps ~300.

This suggests :

1. training separate models on in-air and on-papers stroke might be useful
2. on the contrary, we don't need to differentiate in-air and on-paper strokes and similar conjectures can be made from both (unlikely).

Deprecated Conclusion - Todo List of 06.06 (keep for reference)

These first experiments with CNNs provide encouraging results : we now outperform Moetesum et al. on the l task and Drotar et al. on the spiral task with 2 different models, respectively. Further experiments are required.

I think I should probably discuss and compare my results with Catherine. It should be interesting to compare her model (CNN2d that takes as input Gramian angular field or spectrogram) and mine. By the way I wonder if she knows the work of Afonso et al. and why motivated her use of Short Time Fourier Transform over Discrete wavelet transform.

I also wanted to extract some features from the data, e.g. speed. On June 18th we decided that it was better to focus only on deep learning for now.

Conclusion

We should discuss about it, try to synthesize my work since the beginning.
I'd like to explore transfer learning methods (coming from online HaW recognition ?). I'm motivated because Moetesum et al. didn't fine-tune their model and just used AlexNet (trained on ImageNet) convolutional layers (cf. report #2).

References

Chiu, J. P., & Nichols, E. (2016). Named entity recognition with bidirectional LSTM-CNNs. *Transactions of the Association for Computational Linguistics*, *4*, 357-370.

Granell, E., Chammas, E., Likforman-Sulem, L., Martínez-Hinarejos, C. D., Mokbel, C., & Cîrstea, B. I. (2018). Transcription of spanish historical handwritten documents with deep neural networks. *Journal of Imaging*, *4*(1), 15.

LeNail, (2019). NN-SVG: Publication-Ready Neural Network Architecture Schematics. Journal of Open Source Software, 4(33), 747, https://doi.org/10.21105/joss.00747