

Relational Algebra and MapReduce

Towards High-level Programming Languages

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Eurecom

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<http://lintool.github.io/MapReduceAlgorithms/>
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Relational Algebra and MapReduce

Introduction

- **Disclaimer**

- ▶ This is not a full course on Relational Algebra
- ▶ Neither this is a course on SQL

- **Introduction to Relational Algebra, RDBMS and SQL**

- ▶ Follow the video lectures of the Stanford class on RDBMS
<https://www.coursera.org/course/db>
- Note that you have to sign up for an account

- **Overview of this part**

- ▶ Brief introduction to simplified relational algebra
- ▶ Useful to understand Pig, Hive and HBase

Relational Algebra Operators

- **There are a number of operations on data that fit well the relational algebra model**
 - ▶ In traditional RDBMS, queries involve retrieval of **small amounts of data**
 - ▶ In this course, and in particular in this class, we should keep in mind the particular workload underlying MapReduce
 - Full scans of large amounts of data
 - Queries are not selective¹, they process all data
- **A review of some terminology**
 - ▶ A **relation** is a table
 - ▶ **Attributes** are the column headers of the table
 - ▶ The set of attributes of a relation is called a **schema**
Example: $R(A_1, A_2, \dots, A_n)$ indicates a relation called R whose attributes are A_1, A_2, \dots, A_n

¹This is true in general. However, most ETL jobs involve selection and projection to do data preparation.

Operators

● Let's start with an example

- ▶ Below, we have part of a relation called *Links* describing the structure of the Web
 - ▶ There are two *attributes*: *From* and *To*
 - ▶ A row, or *tuple*, of the relation is a pair of URLs, indicating the existence of a link between them
- The number of tuples in a real dataset is in the order of billions (10^9)

From	To
url1	url2
url1	url3
url2	url3
url2	url4
...	...

Operators

- **Relations (however big) can be stored in a distributed filesystem**
 - ▶ If they don't fit in a single machine, they're broken into pieces (think HDFS)
- **Next, we review and describe a set of relational algebra operators**
 - ▶ Intuitive explanation of what they do
 - ▶ “Pseudo-code” of their implementation in/by MapReduce

Operators

- **Selection:** $\sigma_C(R)$

- ▶ Apply condition C to each tuple of relation R
- ▶ Produce in output a relation containing only tuples that satisfy C

- **Projection:** $\pi_S(R)$

- ▶ Given a *subset* S of relation R attributes
- ▶ Produce in output a relation containing only tuples for the attributes in S

- **Union, Intersection and Difference**

- ▶ Well known operators on sets
- ▶ Apply to the set of tuples in two relations that have the **same schema**
- ▶ Variations on the theme: work on *bags*

Operators

• Natural join $R \bowtie S$

- ▶ Given two relations, *compare each pair of tuples*, one from each relation
- ▶ If the tuples agree on all the attributes common to both schema \rightarrow produce an output tuple that has components on each attribute
- ▶ Otherwise produce nothing
- ▶ *Join condition* can be on a subset of attributes

• Let's work with an example

- ▶ Recall the *Links* relation from previous slides
- ▶ Query (or data processing job): find the paths of length two in the Web

Join Example

- **Informally, to satisfy the query we must:**

- ▶ find the triples of URLs in the form (u, v, w) such that there is a link from u to v and a link from v to w

- **Using the join operator**

- ▶ Imagine we have two relations (with different schema), and let's try to apply the natural join operator
- ▶ There are two copies of *Links*: $L_1(U_1, U_2)$ and $L_2(U_2, U_3)$
- ▶ Let's compute $L_1 \bowtie L_2$
 - ★ For each tuple t_1 of L_1 and each tuple t_2 of L_2 , see if their U_2 component are the same
 - ★ If yes, then produce a tuple in output, with the schema (U_1, U_2, U_3)

Join Example

- What we have seen is called (to be precise) a **self-join**

- ▶ **Question:** How would you implement a self join in your favorite programming language?
- ▶ **Question:** What is the time complexity of your algorithm?
- ▶ **Question:** What is the space complexity of your algorithm?

- To continue the example

- ▶ Say you are not interested in the entire two-hop path but just the start and end nodes
- ▶ Then you do a projection and the notation would be: $\pi_{U_1, U_3}(L_1 \bowtie L_2)$

Operators

- **Grouping and Aggregation:** $\gamma_X(R)$

- ▶ Given a relation R , partition its tuples according to their values in one set of attributes G
 - ★ The set G is called the **grouping attributes**
- ▶ Then, for each group, aggregate the values in certain other attributes
 - ★ Aggregation functions: SUM, COUNT, AVG, MIN, MAX, ...

- **In the notation, X is a list of elements that can be:**

- ▶ A grouping attribute
- ▶ An expression $\theta(A)$, where θ is one of the (five) aggregation functions and A is an attribute **NOT** among the grouping attributes

Operators

- **Grouping and Aggregation:** $\gamma_X(R)$

- ▶ The result of this operation is a relation with one tuple for each group
- ▶ That tuple has a component for each of the grouping attributes, with the value common to tuples of that group
- ▶ That tuple has another component for each aggregation, with the aggregate value for that group

- **Let's work with an example**

- ▶ Imagine that a social-networking site has a relation `Friends(User, Friend)`
- ▶ The tuples are pairs (a, b) such that b is a friend of a
- ▶ Query: compute the number of friends each member has

Grouping and Aggregation Example

● How to satisfy the query

$\gamma_{User, COUNT(Friend)}(Friends)$

- ▶ This operation groups all the tuples by the value in their first component
- There is one group for each user
- ▶ Then, for each group, it counts the number of friends

● Some details

- ▶ The `COUNT` operation applied to an attribute does not consider the values of that attribute
- ▶ In fact, it counts the number of tuples in the group
- ▶ In SQL, there is a “count distinct” operator that counts the number of different values

Computing Selection

- **In practice, selections do not need a full-blown MapReduce implementation**

- ▶ They can be implemented in the **map phase alone**
- ▶ Actually, they could also be implemented in the reduce portion

- **A MapReduce implementation of $\sigma_C(R)$**

Map: ★ For each tuple t in R , check if t satisfies C
 ★ If so, emit a key/value pair (t, t)

Reduce: ★ Identity reducer
 ★ **Question:** single or multiple reducers?

- **NOTE: the output is not exactly a relation**

- ▶ **WHY?**

Computing Projections

- **Similar process to selection**

- ▶ But, projection may cause same tuple to appear several times

- **A MapReduce implementation of $\pi_S(R)$**

Map: ★ For each tuple t in R , construct a tuple t' by eliminating those components whose attributes are not in S

★ Emit a key/value pair (t', t')

Reduce: ★ For each key t' produced by any of the Map tasks, fetch $t', [t', \dots, t']$

★ Emit a key/value pair (t', t')

- **NOTE: the reduce operation is **duplicate elimination****

- ▶ This operation is associative and commutative, so it is possible to optimize MapReduce by using a `Combiner` in each mapper

Computing Unions

- **Suppose relations R and S have the same schema**

- ▶ Map tasks will be assigned chunks from either R or S
- ▶ Mappers don't do much, just pass by to reducers
- ▶ Reducers do duplicate elimination

- **A MapReduce implementation of union**

Map: ²

- ★ For each tuple t in R or S , emit a key/value pair (t, t)

Reduce:

- ★ For each key t there will be either one or two values
- ★ Emit (t, t) in either case

²Hadoop MapReduce supports reading multiple inputs.

Computing Intersections

- **Very similar to computing unions**

- ▶ Suppose relations R and S have the same schema
- ▶ The map function is the same (an identity mapper) as for union
- ▶ The reduce function must produce a tuple only if both relations have that tuple

- **A MapReduce implementation of intersection**

Map: ★ For each tuple t in R or S , emit a key/value pair (t, t)

Reduce: ★ If key t has value list $[t, t]$ then emit the key/value pair (t, t)
 ★ Otherwise, emit the key/value pair (t, NULL)

Computing difference

- **Assume we have two relations R and S with the same schema**

- ▶ The only way a tuple t can appear in the output is if it is in R but not in S
- ▶ The map function passes tuples from R and S to the reducer
- ▶ NOTE: it must inform the reducer whether the tuple came from R or S

- **A MapReduce implementation of difference**

Map: ★ For a tuple t in R emit a key/value pair $(t, 'R')$ and for a tuple t in S , emit a key/value pair $(t, 'S')$

Reduce: ★ For each key t , do the following:
★ If it is associated to $'R'$, then emit (t, t)
★ If it is associated to $['R', 'S']$ or $['S', 'R']$, or $['S']$, emit the key/value pair (t, NULL)

Computing the natural Join

- **This topic is subject to continuous refinements**

- ▶ There are many JOIN operators and many different implementations
- ▶ We've seen some of them in the laboratory sessions

- **Let's look at two relations $R(A, B)$ and $S(B, C)$**

- ▶ We must find tuples that agree on their B components
- ▶ We shall use the B -value of tuples from either relation as the key
- ▶ The value will be the other component and the name of the relation
- ▶ That way the reducer knows from which relation each tuple is coming from

Computing the natural Join

• A MapReduce implementation of Natural Join

Map: ★ For each tuple (a, b) of R emit the key/value pair $(b, ('R', a))$

★ For each tuple (b, c) of S emit the key/value pair $(b, ('S', c))$

Reduce: ★ Each key b will be associated to a list of pairs that are either $('R', a)$ or $('S', c)$

★ Emit key/value pairs of the form

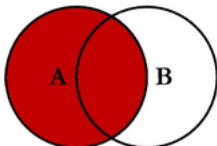
$(b, [(a_1, b, c_1), (a_2, b, c_2), \dots, (a_n, b, c_n)])$

• NOTES

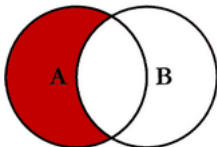
- ▶ **Question:** what if the MapReduce framework wouldn't implement the distributed (and sorted) group by?
- ▶ In general, for n tuples in relation R and m tuples in relation S all with a common B -value, then we end up with nm tuples in the result
- ▶ If all tuples of both relations have the same B -value, then we're computing the **Cartesian product**

Overview of SQL Joins

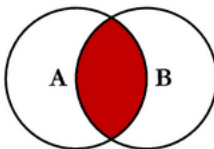
SQL JOINS



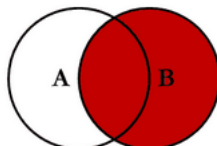
```
SELECT <select_list>
FROM TableA A
LEFT JOIN TableB B
ON A.Key = B.Key
```



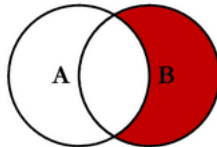
```
SELECT <select_list>
FROM TableA A
LEFT JOIN TableB B
ON A.Key = B.Key
WHERE B.Key IS NULL
```



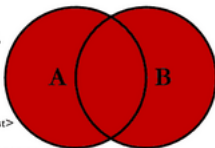
```
SELECT <select_list>
FROM TableA A
INNER JOIN TableB B
ON A.Key = B.Key
```



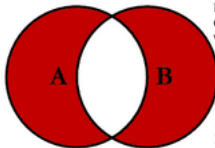
```
SELECT <select_list>
FROM TableA A
RIGHT JOIN TableB B
ON A.Key = B.Key
```



```
SELECT <select_list>
FROM TableA A
RIGHT JOIN TableB B
ON A.Key = B.Key
WHERE A.Key IS NULL
```



```
SELECT <select_list>
FROM TableA A
FULL OUTER JOIN TableB B
```



```
SELECT <select_list>
FROM TableA A
FULL OUTER JOIN TableB B
ON A.Key = B.Key
```

Grouping and Aggregation in MapReduce

- **Let $R(A, B, C)$ be a relation to which we apply $\gamma_{A, \theta(B)}(R)$**

- ▶ The map operation prepares the grouping
- ▶ The grouping is done by the framework
- ▶ The reducer computes the aggregation
- ▶ Simplifying assumptions: one grouping attribute and one aggregation function

- **MapReduce implementation of $\gamma_{A, \theta(B)}(R)$ ³**

Map: ★ For each tuple (a, b, c) emit the key/value pair (a, b)

Reduce: ★ Each key a represents a group

 ★ Apply θ to the list $[b_1, b_2, \dots, b_n]$

 ★ Emit the key/value pair (a, x) where $x = \theta([b_1, b_2, \dots, b_n])$

³Note here that we are also projecting.