

# Fiscal and Monetary Policy with Heterogeneous Agents

Replication of Auclert, Rognlie, and Straub (2024)

Replication Project

December 11, 2025

# Outline

1 Paper Summary

2 Model Equations

3 Extension and Replication

# 1. Research Context & Objectives

From TANK to HANK: The paper aims to extend the Two-Agent New Keynesian (TANK) framework into a canonical **Heterogeneous Agent New Keynesian (HANK)** model.

Three key puzzles to address:

- ① Excess Savings: Explaining the accumulation of savings following fiscal shocks.
- ② Forward Guidance: Addressing the larger variance in the effects of forward guidance.
- ③ Distributional Effects: Analyzing how aggregate shocks impact different segments of the population.

## 2. Specific Mechanisms Under Study

The authors focus on specific transmission channels that standard models overlook:

- Cyclicality of Income Risk:  
How income risk varies over the business cycle and impacts aggregate policy effects.
- Illiquid Accounts & MPCs:  
Modeling the correlation between wealth and Marginal Propensities to Consume (MPCs), specifically through "wealthy hand-to-mouth" households.
- Endogenous Portfolio Choice:  
The role of asset composition in the transmission mechanism.

### 3. Methodology: Sequence-Space & Shocks

Core Framework:

- New Keynesian Assumptions: Flexible prices and sticky wages.
- Agent Heterogeneity: Mass 1 of agents, ex-ante identical but ex-post different.
- Idiosyncratic Risk: Agents face shocks to labor productivity ( $e_{it}$ ) and time discount factor ( $\beta_{it}$ ).

Analytical Approach:

- Use of Sequence-Space methods for efficient decomposition.
- Focus on first-order "**MIT shocks**": Unexpected at date 0, perfect foresight thereafter.

## 4. Main Results

### Fiscal Policy Results

- **Fiscal:** Balanced budget is neutral; Deficit-financed is effective (if high-MPC agents benefit).
- **Monetary:** Exhibits "Monetary Equivalence" (same aggregate effects as standard NK).

### General Equilibrium Dynamics

- The role of Indirect Effects: In HANK models, indirect general equilibrium effects (income feedback) play a much more critical role than direct substitution effects.

# The Consumers' Program

Households maximize expected utility subject to budget and borrowing constraints.

## Maximization Problem:

$$\max_{\{c_{it}\}} \mathbb{E}_0 \left[ \sum_{t=0}^{\infty} \left( \prod_{s \leq t-1} \beta_{is} \right) \{\log(c_{it}) - v(n_{it})\} \right]$$

## Subject to:

$$\begin{aligned} c_{it} + a_{it} &\leq (1 + r_t^p)a_{it-1} + (1 - \tau_t)w_t e_{it} n_{it} \\ a_{it} &\geq 0 \end{aligned}$$

Note: Discount factors  $\beta_{is}$  are idiosyncratic and time-varying. Agents face a zero borrowing limit ( $a_{it} \geq 0$ ).

# Firms and Inflation

## Firms, Pricing & Dividends

- **Production:** Linear technology implies Marginal Cost = Wage ( $W_t$ ):

$$Y_t = N_t$$

- **Pricing:** Prices are a constant markup  $\mu$  over marginal cost:

$$P_t = \mu W_t \implies w_t = \frac{1}{\mu}$$

- **Dividends:** Real post-tax dividends are derived as:

$$d_t = (1 - \tau_t)(Y_t - w_t N_t) = (1 - \tau_t) \left(1 - \frac{1}{\mu}\right) Y_t$$

## Wage Phillips Curve

$$\pi_t^w = \kappa \left(v'(N_t) - \frac{1 - \tau_t}{\mu C_t}\right) + \beta \pi_{t+1}^w$$

Inflation is driven by the gap between the marginal cost of working and the marginal utility of consumption.

# Government and Market Clearing

## Government Policy

- Budget Constraint:

$$G_t + B_t = (1 + r_{t-1})B_{t-1} + \tau_t Y_t$$

- Monetary Policy (Taylor Rule):

$$1 + i_t = (1 + r_t)(1 + \pi_{t+1})$$

## Asset Pricing & Market Clearing

- No-Arbitrage Condition (Stock Pricing):

$$1 + r_t = \frac{p_{t+1} + d_{t+1}}{p_t}$$

- Asset Market Clearing:  $A_t = p_t + B_t$
- Goods Market Clearing:  $C_t + G_t = Y_t$
- Ex-post return:  $r_{t+1}^P = r_t$

# Calibration of the Baseline HA Model

The model is calibrated to match the US economy (wealth distribution and aggregates).

Variable	Value	Variable	Value
$r$ Real interest rate (annual)	2%	$\mu$ Markups	1.11
$A$ Assets to GDP (annual)	500%	$(\beta^L, \beta^H)$ Discount factors	(0.91, 1.00)
$B$ Bonds to GDP (annual)	100%	$\omega$ Share of patient	49%
$M_{00}$ Income-weighted MPC	0.2	$q$ Prob of new $\beta$ draw	1%
$G$ Gov. spending to GDP	20%	$T$ Taxes to GDP	22%

Table: Parameters matching the steady state targets

# The Transmission Mechanism: iMPCs & Fiscal Policy

## Aggregate Consumption Function

How does a tax cut ( $dT$ ) translate into consumption ( $dC$ )?

$$dC = \underbrace{(M^r - pmq') dr}_{\mathcal{M}^r} + \underbrace{\left( \frac{1}{\mu} M + \left(1 - \frac{1}{\mu}\right) mq' \right) (dY - dT)}_{\mathcal{M}}$$

## Decomposing the Mechanism:

- $dT$ : The fiscal shock. A tax cut increases disposable income directly.
- $\mathcal{M}$  (**The Multiplier Matrix**):
  - Weighted average of MPCs out of labor income ( $M$ ) and capital gains ( $m$ ).
- **General Equilibrium:**

Tax Cut ( $\downarrow dT$ )  $\xrightarrow{\mathcal{M}}$  Spending ( $\uparrow dC$ )  $\rightarrow$  Output ( $\uparrow dY$ )

*Note: High MPCs ( $M$ ) amplify the impact of tax cuts on aggregate demand.*

# Replication: Fiscal Policy Shocks

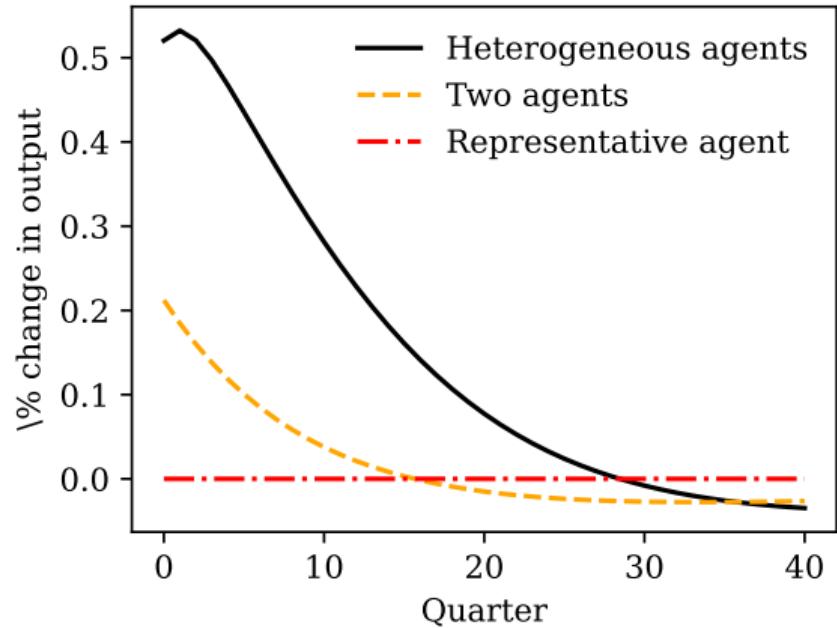


Figure: Deficit-Financed Policy (By Model)

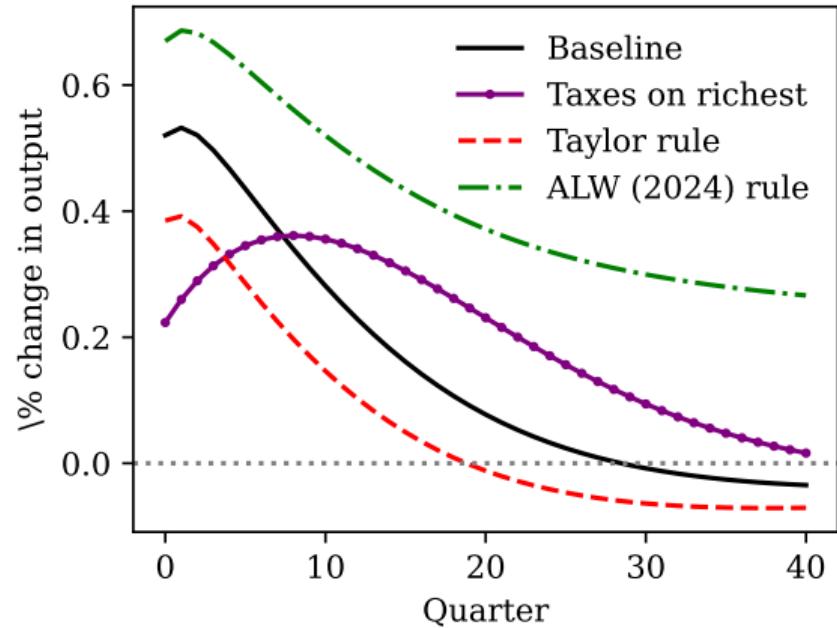


Figure: Deficit-Financed Policy (Alternative Rules)

# Extension: Evolution of Inequalities

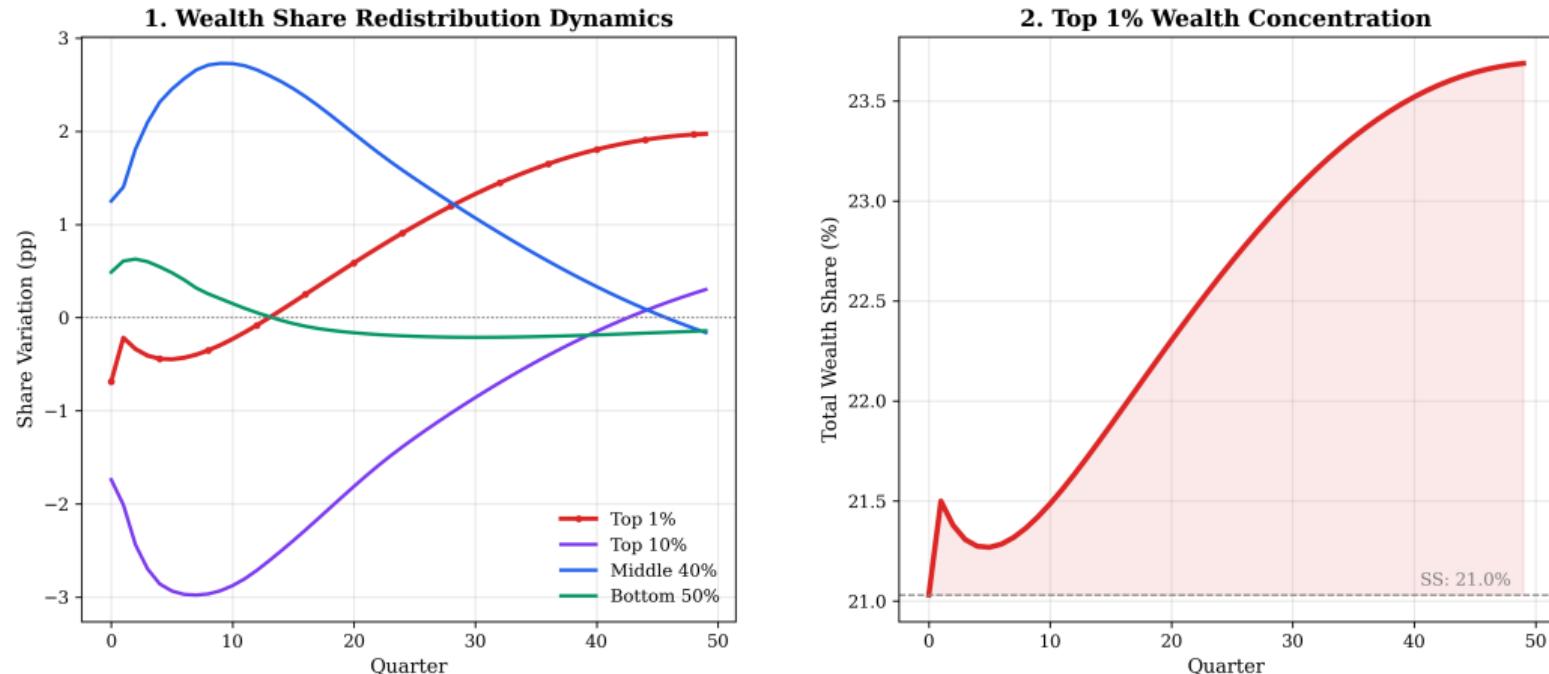


Figure: Inequality IRFs – Deficit-Financed Tax Cuts

# Extension: Evolution of Inequalities

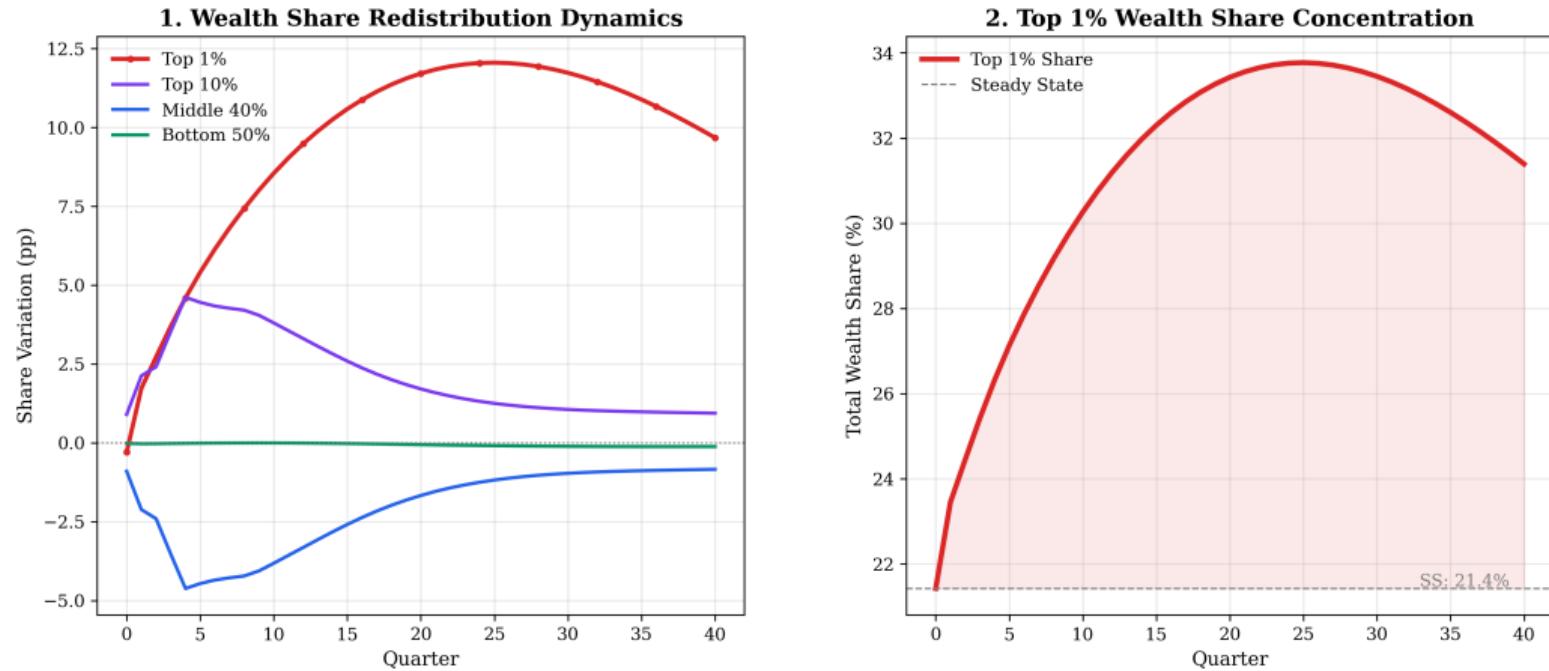


Figure: Inequality IRFs – Deficit-Financed Tax Cuts (Taxes on the Richest)