

Plan Merging Project

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Agenda

- Problem Setting
- ASP Components
- Solvers
 - Iterative Solving
 - Prioritized Planning
 - Conflict Based Search
- Benchmarking
- Conclusion



Problem Setting

- MAPF through plan merging.
- Non anonymous MAPF.
- Main focus on satisfiability, i.e. finding a set of valid, conflict free paths for all agents.
- Metrics of interest for valid solutions:
 - Sum of Costs (SoC) := The sum of all time steps required by each agent to reach its target.
 - Makespan := The maximum number of time steps required for all agents to reach their target
- Investigate tradeoff between runtime and solution quality with different approaches.



Conflict Detection

- Paths are represented by position atoms

`position(R, (X,Y), T)`

- Conflict types:

```
conflict(vertex,R,R', (X,Y), T) :-  
position(R, (X,Y), T), position(R', (X,Y), T), R!=R'.
```

```
conflict(edge,R,R', ((X,Y), (X',Y')), T-1) :-  
position(R, (X,Y), T-1), position(R, (X',Y'), T),  
position(R', (X',Y'), T-1), position(R', (X,Y), T), R!=R'.
```

```
conflict(vertex,R,R', (X,Y), T) :-  
position(R, (X,Y), T), goal(R', (X,Y)),  
goalReached(R', T'), R!=R', T >= T'.
```



Single Agent Pathfinding

Adapted Asprilo encoding based on Clingo's incremental mode.

```
{ move(r,D,t) : direction(D) } 1.  
position(r, (X+DX,Y+DY),t) :- move(r, (DX,DY),t),  
position(r, (X,Y),t-1).  
:- move(r, (DX,DY),t), position(r, (X,Y),t-1),  
not node((X+DX,Y+DY)).  
position(r,C,t) :- position(r,C,t-1), not move(r,_,t).
```

Check for each iteration if the goal has been reached.

```
#program check(t).  
#external query(t).  
goalReached(r,t) :- goal(r,C), position(r,C,t), not block(t).  
:- not goalReached(r,t), query(t).
```



Iterative Solving

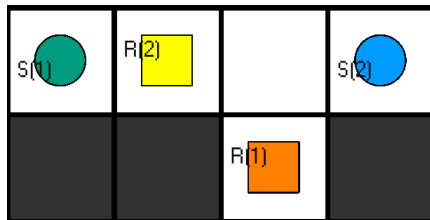
Idea:

- Solving one conflict at a time
- Separating conflict based on complexity
 - Conflict which can be solved by one agent waiting
 - Conflicts which can be solved by one agent evading the other



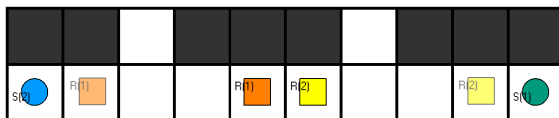
Vertex Conflict Handling

- Precondition: Conflict was found which can be solved with one agent waiting
- Agent which has to wait gets chosen based on priority:
 - Priority 1: The path of the agent is shorter than the one of the other agent
 - Priority 2: The agent has to move, for the other agent to continue



Edge Conflict Handling

- From the point of conflict both agents restep their own path to find a suitable point to evade the other agent
- Once all points are found the one nearest to the conflict time gets chosen
- The agent who dodges, evades onto the spot before the conflict would occur, waiting there before continuing as normal



Iterative Solving

Algorithm 1: Iterative solving

current.plans \leftarrow Node with optimal paths for all agents

while *True* **do**

 conflict \leftarrow Conflicts between paths p_1, \dots, p_n

if no conflicts in current.plans **then**

return current.plans

else

if *edge conflict in conflicts* **then**

 solveEdge()

continue

else

 solveVertex()

end

end

end



Prioritized Planning

- Idea: Plan agents paths sequentially according to a priority order.
- Agents have to avoid conflicts with agents of a higher priority.
- Prioritized Planning is not a complete solver.
- No guarantees on the quality of the solution.
- Runtime linear in the number of agents.

Unsolvable instance for PP



Prioritized Planning Algorithm

Algorithm 2: Prioritized Planning

```
order  $\leftarrow \{a_1, \dots, a_n\}$ 
plans  $\leftarrow \emptyset$ 
for agent  $a_i \in$  order do
    // Plans conflict free path for  $a_i$ 
     $plan_i \leftarrow \text{plan\_path}(a_i, \text{plans})$ 
    if  $plan_i.cost < \infty$  then
        | plans  $\leftarrow$  plans  $\cup plan_i$ 
    else
        | return  $\emptyset$ 
    end
end
return plans
```



Avoiding conflicts

Avoiding vertex and edge conflicts with known plans.

```
:- position(r, (X,Y),t), position(R, (X,Y),t), r!=R.
```

```
:- position(r, (X,Y),t-1), move(r, (DX,DY),t),  
position(R, (X+DX,Y+DY),t-1), position(R, (X,Y),t), r!=R.
```

```
:- position(r, (X,Y),t), goal(R, (X,Y)), goalReached(R,T),  
r!=R, t > T.
```

```
block(1..T-1) :- position(R,C,T), goal(r,C), r!=R.
```



Schedule Optimization

- Initial order of agents impacts solvability and solution quality.
- **Problem:** Determine optimal order without actually testing every permutation.
- Heuristic approach: Order agents according to the number of conflicts in their initial plans.
- Idea: Agents with few conflicts should be prioritized, since they are less likely to block following agents.
- No formal guarantee on improving the solution →
Has to be evaluated empirically.



Backtracking

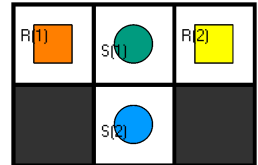
- Idea: Reorder agents if the current order is unsolvable.

Algorithm 3: Backtracking

```

order  $\leftarrow \{a_1, \dots, a_n\}$ 
orderings  $\leftarrow \{\text{order}\}$ 
while maxIter > 0 do
  if prioritized_planning(order) not satisfiable then
    orderings  $\leftarrow$  orderings  $\cup$  {All orders beginning with
       $a_1, \dots, a_i$ }
    Change agents  $a_i$  and  $a_{i-1}$ 
    order  $\leftarrow \{a_{i-1}, \dots, a_n\}$ 
    if order  $\in$  orderings then
      order  $\leftarrow$  Order with maximum distance to known
        orders.
    end
    orderings  $\leftarrow$  orderings  $\cup$  {order}
    maxIter  $\leftarrow$  maxIter - 1
  else
    return prioritized_planning(order)
  end
end

```



- Increases runtime complexity to $N!$ in the worst case.
- Marking unsolvable orders should improve performance on average.

Conflict Based Search

- Complete and optimal MAPF algorithm by Sharon et al.[1]
- Two level search.
 - High level search of conflict tree.
 - Low level path finding search.
- Our implementation: High level search in Python, low level search and conflict detection in ASP.



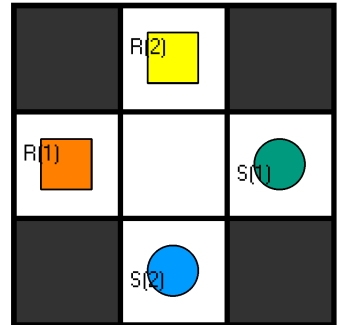
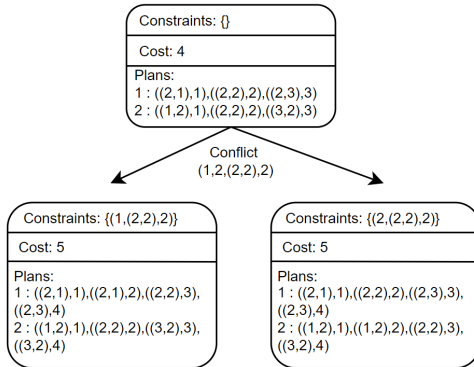
CBS Algorithm

Algorithm 4: Conflict Based Search (Base)

```
root  $\leftarrow$  Node with optimal paths for all agents
open  $\leftarrow$  {root}
while open not empty do
  current  $\leftarrow$  lowest cost node from open
  if no conflicts in current.plans then
    return current.plans
  else
    conflict  $\leftarrow$  conflict between agents  $a_1, a_2$  at  $(x, y, t)$ 
    for agent  $a_i$  in conflict do
      node  $\leftarrow$  current with additional constraint  $(a_i, x, y, t)$ 
      // computes path for  $a_i$ 
      node.low_level( $a_i$ )
      if node.cost  $< \infty$  then
        open  $\leftarrow$  open  $\cup$  {node}
      end
    end
  end
end
```



CBS Example



Constraints

Constraining agent positions and movements.

```
:- constraint(r,C,t), position(r,C,t).
```

```
:- constraint(r,C,M,t-1), position(r,C,t-1), move(r,M,t).
```

```
block(1..T-1) :- constraint(r,C,T), goal(r,C).
```



Cost Functions for CBS

- CBS can optimize different cost functions.
- Cost function determines the value used to sort nodes in the open queue.
 - Sum of costs.
 - Makespan
 - Greedy $:=$ Cost function + number of conflicts in the node.
- Greedy search can produce sub-optimal solutions, but should improve performance.



Conflict Bypassing

- Improvement to CBS suggested by Boyarsky et al. [2]
- Bypass conflicts instead of branching if possible.

Algorithm 5: Bypass

```
conflict  $\leftarrow$  conflict between agents  $a_1, a_2$  at time  $t$ 
for agent  $a_i$  in conflict do
  node  $\leftarrow$  current with additional constraint for  $a_i$  at time  $t$ 
  node.low_level( $a_i$ )
  if node.cost  $\leq$  current.cost and node.ccount < current.ccount
    then
      open  $\leftarrow$  open  $\cup$  {node}
      break
  end
end
```

- Reduces number of branches in conflict tree.



Meta Agent CBS

- Idea: Merge heavily conflicting agents into meta agents.
- Trade off between high level and low level search.
- Requires tracking of conflicts through conflict matrix and MAPF solver for low level search.

Algorithm 6: Meta Agent CBS

```
conflict  $\leftarrow$  conflict between agents  $a_1, a_2$  at time  $t$ 
conflict_matrix( $a_1, a_2$ )  $\leftarrow$  conflict_matrix( $a_1, a_2$ ) + 1
if conflict_matrix( $a_1, a_2$ ) > merge_threshold then
    merge( $a_1, a_2$ )
    // computes path for meta agent  $a_{(1,2)}$ 
    node.low_level( $a_{(1,2)}$ )
    if node.cost <  $\infty$  then
        open  $\leftarrow$  open  $\cup$  {node}
    end
end
```



Meta Agent CBS II

Adapted single agent pathfinding ASP encoding as a low level MAPF solver. Main difference:

```
cost(N,t) :-
```

```
N = #sum{1, R, T : position(R,C,T), not goal (R,C)}.
```

```
#minimize{ N : cost(N,t)}.
```

Problem: We struggled to find an efficient minimization statement. Current implementation only provides close to optimal solutions in terms of makespan.



Improved CBS

- Further improvements to CBS suggested by Boyarsky et al. [3]



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- 1. Merge Reset: Whenever two (meta) agents are merged to a meta agent, restart the search from scratch with the new meta agent already merged.



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- 2. Prioritizing conflicts



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- 2. Prioritizing conflicts
 - Cardinal conflict := Both constraints lead to an increase in cost.



Improved CBS

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- 1. Merge Reset: Whenever two (meta) agents are merged to a meta agent, restart the search from scratch with the new meta agent already merged.
- 2. Prioritizing conflicts
 - Cardinal conflict := Both constraints lead to an increase in cost.
 - Semi cardinal conflict := One constraint leads to an increase in cost.



Improved CBS

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- 2. Prioritizing conflicts
 - Cardinal conflict := Both constraints lead to an increase in cost.
 - Semi cardinal conflict := One constraint leads to an increase in cost.
 - Non cardinal conflict := Both constraints do not increase cost.



Improved CBS

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- 1. Merge Reset: Whenever two (meta) agents are merged to a meta agent, restart the search from scratch with the new meta agent already merged.
- 2. Prioritizing conflicts
 - Cardinal conflict := Both constraints lead to an increase in cost.
 - Semi cardinal conflict := One constraint leads to an increase in cost.
 - Non cardinal conflict := Both constraints do not increase cost.
- Evaluate conflicts in a node and branch in order:
cardinal > semi cardinal > non cardinal.



Improved CBS

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- 1. Merge Reset: Whenever two (meta) agents are merged to a meta agent, restart the search from scratch with the new meta agent already merged.
- 2. Prioritizing conflicts
 - Cardinal conflict := Both constraints lead to an increase in cost.
 - Semi cardinal conflict := One constraint leads to an increase in cost.
 - Non cardinal conflict := Both constraints do not increase cost.
- Evaluate conflicts in a node and branch in order:
cardinal > semi cardinal > non cardinal.
- Prioritizing cardinal conflicts should reduce size of the conflict tree. **Problem:** Evaluating conflicts is costly in our implementation.



Bechmarking - CBS

Table with maxed out execution time

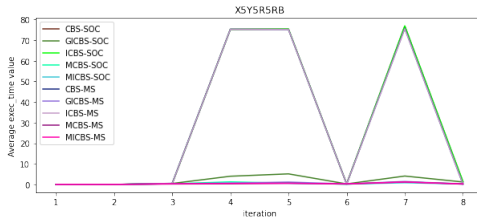
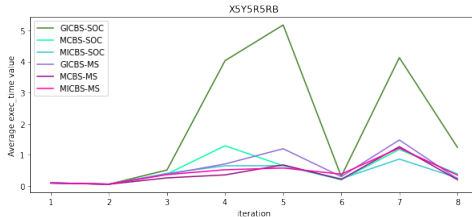


Table with slower CBS-versions removed



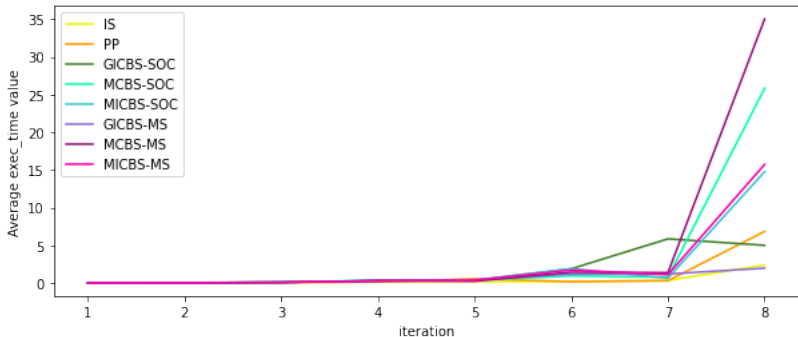
- We benchmarked our solvers based on instances with ever increasing difficulty.
- Base instance was the size of 5 x 5 and had 5 agent, with an extra random wall getting placed per iteration.
- One iteration contains 4 different instances from which we took the average.



Benchmarks - Compared

10 by 10 instance, with 3 vertical and horizontal lines, with one door between each section.

X10Y10Grid3R

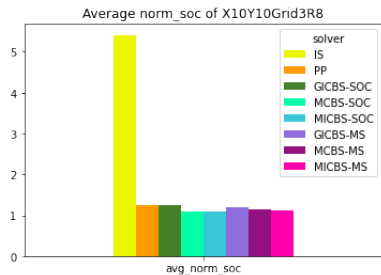
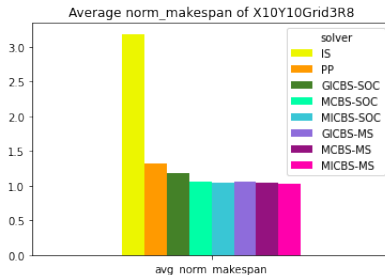


Iteration = number of Agents.



Benchmarks - Makespan / SOC

■ Makespan and Sum of Cost in relation to the unsolved instance



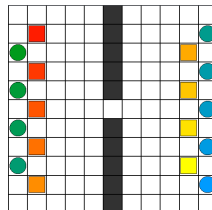
Benchmarks - Sauerbrei Raatschen

Plan-Sauerbrei-Raatschen-2



Solver	Ms	SoC	NoM	ET
IS	26	176	50	0.470
PP	8	49	46	0.122
PP-OPT	12	45	44	0.178
CBS-SOC	12	45	44	11.591
GICBS-SOC	12	45	44	3.603
ICBS-SOC	12	45	44	11.843
MCBS-SOC	8	47	42	2.683
MICBS-SOC	8	53	44	2.070
CBS-MS	9	52	46	31.564
GICBS-MS	11	51	44	13.544
ICBS-MS	8	50	44	27.841
MCBS-MS	8	48	44	2.017
MICBS-MS	8	53	44	2.016

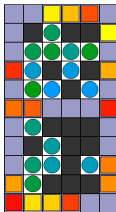
Plan-Sauerbrei-Raatschen-1



Solver	Ms	SoC	NoM	ET
IS	31	279	133	2.088
PP	23	153	129	1.347
PP-OPT	28	171	135	2.355
MICBS-SOC	21	153	147	788.276

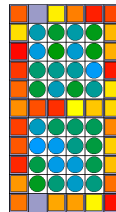
Benchmarks - Steven Pan

x6_y11_r16_fo1_cmw1_cx4_cy4_rom2
_instance_002



Solver	Ms	SoC	NoM	ET
PP	20	201	160	38.000
PP-OPT	23	229	175	44.000
GICBS-MS	14	175	140	141.726

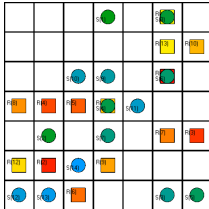
x6_y11_r32_fo2_cmw1_cx4_cy4_rom2
_instance_004



Solver	Ms	SoC	NoM	ET
PP	22	353	285	12.500
PP-OPT	24	339	291	1.480

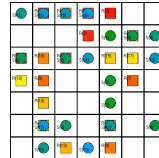
Benchmarks - Moek Andreev

ex14



Solver	Ms	SoC	NoM	ET
PP	10	73	71	0.471
PP-OPT	10	69	69	0.728
CBS-SOC	9	65	63	2.848
GICBS-SOC	9	69	65	4.190
ICBS-SOC	9	65	63	2.222
MCBS-SOC	9	65	63	2.658
MICBS-SOC	9	65	63	113.399
CBS-MS	9	71	67	2.578
GICBS-MS	9	72	63	2.561
ICBS-MS	9	72	63	3.743

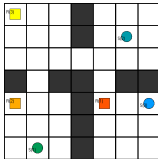
ex8



Solver	Ms	SoC	NoM	ET
PP	10	98	96	0.483
PP-OPT	10	108	100	0.903
CBS-SOC	10	94	94	5.806
GICBS-SOC	10	99	96	4.684
ICBS-SOC	10	94	92	3.762
MCBS-SOC	10	95	94	7.440
CBS-MS	10	101	100	4.535
GICBS-MS	10	100	96	3.805
ICBS-MS	10	100	96	5.467

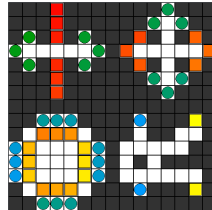
Benchmarks - Jan Behrens

small_room



Solver	Ms	SoC	NoM	ET
IS	14	40	29	0.155
PP	11	30	29	0.100
PP-OPT	11	30	29	0.188
CBS-SOC	11	30	29	0.762
GICBS-SOC	11	30	29	0.376
ICBS-SOC	11	30	29	0.764
MCBS-SOC	11	30	29	0.492
MICBS-SOC	12	33	31	0.639
CBS-MS	11	30	29	0.784
GICBS-MS	11	30	29	0.357
ICBS-MS	11	30	29	0.768
MCBS-MS	11	30	29	0.410
MICBS-MS	12	33	31	0.634

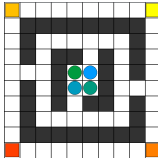
mix



Solver	Ms	SoC	NoM	ET
PP	11	195	162	0.597
PP-OPT	11	195	162	0.886
MICBS-SOC	11	185	164	53.831
MICBS-MS	11	185	164	27.951

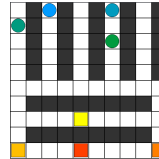
Benchmarks - Glätzer Akil

mini_maze



Solver	Ms	SoC	NoM	ET
IS	23	90	64	0.443
PP	15	58	56	0.234
PP-OPT	15	58	56	0.391
CBS-SOC	15	58	56	0.376
GICBS-SOC	15	58	56	0.361
ICBS-SOC	15	58	56	0.398
MCBS-SOC	15	58	56	0.364
MICBS-SOC	15	58	56	0.372
CBS-MS	15	58	56	0.408
GICBS-MS	15	58	56	0.401
ICBS-MS	15	58	56	0.358
MCBS-MS	15	58	56	0.453
MICBS-MS	15	58	56	0.494

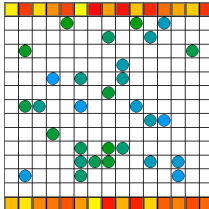
warehouse



PP	17	60	60	0.255
PP-OPT	17	60	60	0.443
CBS-SOC	17	60	60	0.366
GICBS-SOC	17	60	60	0.377
ICBS-SOC	17	60	60	0.383
MCBS-SOC	17	60	60	0.370
MICBS-SOC	17	60	60	0.353
CBS-MS	17	60	60	0.384
GICBS-MS	17	60	60	0.380
ICBS-MS	17	60	60	0.364
MCBS-MS	17	60	60	0.370
MICBS-MS	17	60	60	0.363

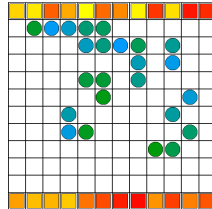
Benchmarks - Cordova Khatova

30_merged_plans



Solver	Ms	SoC	NoM	ET
PP	19	316	307	2.382
PP-OPT	19	321	307	4.635
CBS-SOC	19	303	303	9.287
GICBS-SOC	19	304	303	12.997
ICBS-SOC	19	303	303	10.856
MCBS-SOC	19	303	303	11.494
MICBS-SOC	19	303	303	61.630
CBS-MS	19	303	303	15.251
GICBS-MS	19	337	307	17.904
ICBS-MS	19	337	307	22.749
MCBS-MS	19	303	303	14.711

24_merged_plans

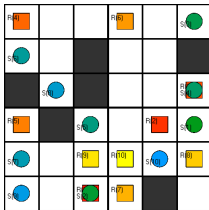


Solver	Ms	SoC	NoM	ET
PP	15	263	239	1.374
PP-OPT	15	261	237	2.384
CBS-SOC	16	236	235	216.957
GICBS-SOC	15	249	233	37.274
ICBS-SOC	16	236	233	265.565
CBS-MS	15	260	237	30.610
GICBS-MS	15	258	233	22.595
ICBS-MS	15	259	239	57.423

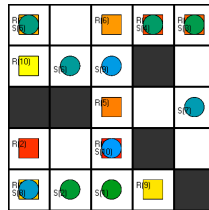


Benchmarks - Nemes Murphy

6_by_6_agents_10_obstacles_6_1



5_by_5_agents_10_obstacles_5_2



Solver	Ms	SoC	NoM	ET
PP	10	58	56	0.149
PP-OPT	10	53	52	0.282
CBS-SOC	10	50	48	2.363
GICBS-SOC	10	52	50	0.821
ICBS-SOC	10	50	48	2.372
MCBS-SOC	10	51	50	0.732
MICBS-SOC	10	51	48	2.387
CBS-MS	10	65	56	20.891
GICBS-MS	10	52	50	1.199
ICBS-MS	10	52	50	1.879
MCBS-MS	10	54	50	13.019

Solver	Ms	SoC	NoM	ET
PP	9	52	41	4.048
MCBS-SOC	9	52	47	13.441
MICBS-SOC	9	46	43	32.535
MCBS-MS	9	52	47	10.904
MICBS-MS	9	46	43	28.284

Conclusion

- **Iterative Solving:** Poor range of solvable instances and solution quality, decent runtime.
- **Prioritized Planning:** Acceptable runtime and solution quality, backtracking can be further improved.
- **CBS:** Impractical runtime for larger instances, ICBS, MACBS and GCBS are not well optimized → lots of room for improvement.
- To many solvers. Focus on 1-2 solvers would have left more time for optimization.



Sources I

- [1] Guni Sharon **and others**. “Conflict-based search for optimal multi-agent pathfinding”. in *Artificial Intelligence*: 219 (2015), **pages** 40–66.
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