

# Quiz 5

## Chemistry 3BB3; Winter 2006

1. Write the electronic Schrödinger equation for the hydrogen molecule cation,  $\text{H}_2^+$ , in SI units, showing the dependence on  $\hbar$ ,  $e$ ,  $m_e$ , etc..
  
- 2,3. What is the ground state electronic energy of the hydrogen molecule cation,  $\text{H}_2^+$ , in the united atom limit? What is the ground state wave function? (You can use atomic units in this problem.)
  
- 4,5. What is the ground state electronic energy of the hydrogen molecule cation,  $\text{H}_2^+$ , in the separated atom limit? What is the ground state wave function? (You can use atomic units in this problem.)

6-10. Complete the following table by filling in the appropriate properties for the molecular ground states.

Molecule	Bond Order	Multiplicity
$\text{H}_2$		
$\text{He}_2$		
$\text{Li}_2$		
$\text{Be}_2$		
$\text{B}_2$		
$\text{C}_2$		
$\text{N}_2$		
$\text{O}_2$		
$\text{F}_2$		
$\text{Ne}_2$		

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1. Write the electronic Schrödinger equation for the hydrogen molecule cation,  $\text{H}_2^+$ , in SI units, showing the dependence on  $\hbar$ ,  $e$ ,  $m_e$ , etc..

$$\left( -\frac{\hbar^2}{2m_e} \nabla^2 - \frac{e^2}{4\pi\epsilon_0 r_l} - \frac{e^2}{4\pi\epsilon_0 r_r} \right) \psi(r_l, r_r, \phi) = E \psi(r_l, r_r, \phi)$$

where  $r_l$  and  $r_r$  are the distances from the “left” and “right” nuclei, respectively

- 2,3. What is the ground state electronic energy of the hydrogen molecule cation,  $\text{H}_2^+$ , in the united atom limit? What is the ground state wave function? (You can use atomic units in this problem.)

$$E_{u.a.} = -\frac{2^2}{2} = -2 \text{ Hartree}$$

$$\psi_{u.a.} \propto e^{-2r}$$

- 4,5. What is the ground state electronic energy of the hydrogen molecule cation,  $\text{H}_2^+$ , in the separated atom limit? What is the ground state wave function? (You can use atomic units in this problem.)

$$E_{sep.a.} = -.5 \text{ Hartree}$$

$$\psi_{sep.a.} \propto (ce^{-\eta} \pm \sqrt{1-|c|^2} e^{-r_r})$$

where  $r_l$  and  $r_r$  are the distances from the “left” and “right” nuclei, respectively.

- 6-10. Complete the following table by filling in the appropriate properties for the molecular ground states.

Molecule	Bond Order	Multiplicity
$\text{H}_2$	1	1
$\text{He}_2$	0	1
$\text{Li}_2$	1	1
$\text{Be}_2$	0	1
$\text{B}_2$	1	3
$\text{C}_2$	2	1
$\text{N}_2$	3	1
$\text{O}_2$	2	3
$\text{F}_2$	1	1
$\text{Ne}_2$	0	1