

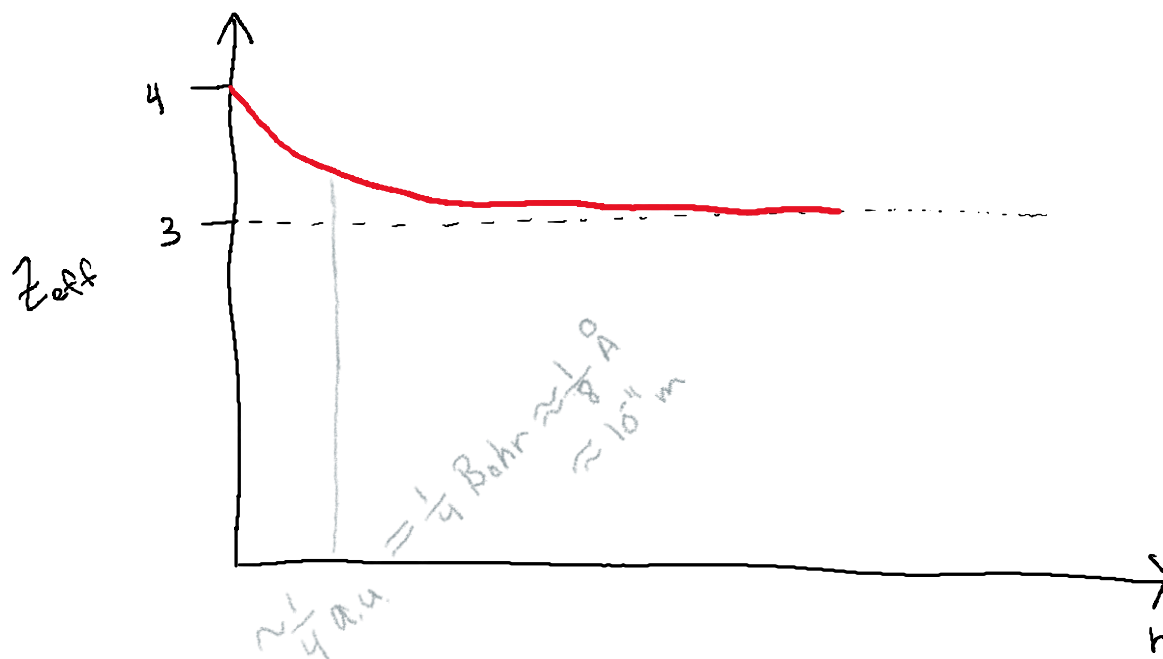
Quiz 13

CHEM 3PA3; Fall 2018

This quiz has 10 problems worth 10 points each. There are 10 bonus points....

- 1. Sketch the effective nuclear charge felt by an electron r units from the nucleus for the Beryllium dication, Be^{2+} . Clearly specify the appropriate limits as $r \rightarrow 0$ and $r \rightarrow +\infty$.**

This is a 2-electron atom. Near the nucleus, an electron feels the entire nuclear charge (+4). Far from the nucleus, the electron “sees” the nucleus (+4 charge) and the other electron (which is closer to the nucleus almost certainly (-1 charge) for a total charge of +3. The other electron can be assumed to be in $1s$ -like orbital (the electron that is far away makes the electron that is close to the nucleus feel like it is in a 1-electron atom) so the effective nuclear charge decays relatively quickly, on a length scale similar to the radius of the s -type orbital (which is about $\frac{1}{4}$ the size it was in a hydrogen atom). So a rough sketch would be:



- 2,3. Write the electronic Schrödinger equation and the nuclear Schrödinger equation for a N -electron P -atom molecule. You may use atomic units.**

Electronic Schrödinger Equation:

$$\left(\sum_{i=1}^N -\frac{1}{2} \nabla_i^2 + \frac{1}{2} \sum_{A=1}^P \sum_{B=1, B \neq A}^P \frac{Z_A Z_B}{|\mathbf{R}_A - \mathbf{R}_B|} + \frac{1}{2} \sum_{i=1}^N \sum_{j=1, j \neq i}^N \frac{1}{|\mathbf{r}_i - \mathbf{r}_j|} + \sum_{A=1}^P \sum_{i=1}^N \frac{-Z_A}{|\mathbf{r}_i - \mathbf{R}_A|} \right) \psi_{\text{el}}(\mathbf{r}_1 \dots \mathbf{r}_N | \mathbf{R}_1 \dots \mathbf{R}_P) = E(\mathbf{R}_1 \dots \mathbf{R}_P) \psi_{\text{el}}(\mathbf{r}_1 \dots \mathbf{r}_N | \mathbf{R}_1 \dots \mathbf{R}_P)$$

Nuclear Schrödinger Equation:

$$\left(\sum_{A=1}^P -\frac{1}{2} \nabla_A^2 + E(\mathbf{R}_1, \mathbf{R}_2, \dots, \mathbf{R}_P) \right) \chi_{\text{nuc}}(\mathbf{R}_1, \mathbf{R}_2, \dots, \mathbf{R}_P) = E_{\text{total}} \chi_{\text{nuc}}(\mathbf{R}_1, \mathbf{R}_2, \dots, \mathbf{R}_P)$$

4. What are the term symbols for the [Ar]4s²3d¹4p¹ excited state (Titanium)?

The 3d electron has $L = 2$ and $S = \frac{1}{2}$ and the 4p electron has $L = 1$ and $S = \frac{1}{2}$. The possible choices of orbital angular momentum then range from $L = |L_1 - L_2|, \dots, L_1 + L_2 = 1, 2, 3$ and the choices of spin-angular momentum range from $S = |S_1 - S_2|, \dots, S_1 + S_2 = 0, 1$.

5. What is the predicted order of the states according to Hund's rules.

So the states are $^3F, ^3D, ^3P, ^1F, ^1D, ^1P$ in Hunds rule order. If we add on the J values, we have $^3F_2, ^3F_3, ^3F_4, ^3D_1, ^3D_2, ^3D_3, ^3P_0, ^3P_1, ^3P_2, ^1F_3, ^1D_2, ^1P_1$.

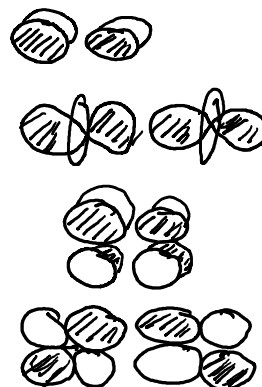
6. What is the predicted order of states according to the Kutzelnigg-Morgan and Russell-Meggers rules?

According to the Kutzelnigg-Morgan and Russell-Meggers rules, the $L = 2$ states have odd parity and the $L = 1$ and $L = 3$ states have even parity. Moreover, $L_{\text{opt}} = \frac{2+1}{\sqrt{2}} = 2.12$. So the predicted order of states is $^1D, ^3D, ^3F, ^3P, ^1F, ^1P$.

7-10. For each of the following orbitals, assign a symmetry label $\{\sigma, \pi, \delta, \dots\}, \{u, g\}, \{+, -\}$.

Assume that the orbitals are the atomic orbitals of the left and right atom in the separated-atom limit, and that the molecule is a homonuclear diatomic molecule. Assume that the bond axis is the z axis. Circle whether the orbital is bonding or antibonding.

Orbital	Symmetry-Label	Bonding/Antibonding (circle one)
$\psi_{2p_y}^{(l)}(\mathbf{r}) + \psi_{2p_y}^{(r)}(\mathbf{r})$	$1\pi_u^-$	bonding antibonding
$\psi_{3d_0}^{(l)}(\mathbf{r}) + \psi_{3d_0}^{(r)}(\mathbf{r})$	$6\sigma_g^+$	bonding antibonding
$\psi_{3d_{xy}}^{(l)}(\mathbf{r}) + \psi_{3d_{xy}}^{(r)}(\mathbf{r})$	$1\delta_g^-$	bonding antibonding
$\psi_{3d_{xz}}^{(l)}(\mathbf{r}) - \psi_{3d_{xz}}^{(r)}(\mathbf{r})$	$5\pi_u^+$	bonding antibonding

**Bonus (10 points): What is the lowest-energy term symbol for the [Ar]4s²3d⁷ configuration (Cobalt)?**

This is the same, essentially, as the Scandium example in quiz #8. The ground-state term is 4F . A representative Slater determinant (with maximum $M_L = 3$ and $M_S = \frac{3}{2}$) is $|\dots 3d_{+2}^{\uparrow} 3d_{+2}^{\downarrow} 3d_{+1}^{\uparrow} 3d_{+1}^{\downarrow} 3d_0^{\uparrow} 3d_{-1}^{\uparrow} 3d_{-2}^{\uparrow}\rangle$. It is a more than half-filled shell so the J -decorated ground-state term is $^4F_{9/2}$.

Name _____

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- 2,3. Write the electronic Schrödinger equation and the nuclear Schrödinger equation for a N-electron P-atom molecule. You may use atomic units.**

Electronic Schrödinger Equation:

Nuclear Schrödinger Equation:

Name_____

Student #_____

4. What are the term symbols for the $[\text{Ar}]4s^23d^14p^1$ excited state (Titanium)?

5. What is the predicted order of the states according to Hund's rules?

6. What is the predicted order of states according to the Kutzelnigg-Morgan and Russell-Meggers rules?

7-10. For each of the following orbitals, assign a symmetry label $\{\sigma, \pi, \delta, \dots\}, \{u, g\}, \{+, -\}$. Assume that the orbitals are the atomic orbitals of the left and right atom in the separated-atom limit, and that the molecule is a homonuclear diatomic molecule. Assume that the bond axis is the z axis. Circle whether the orbital is bonding or antibonding.

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$\psi_{3d_{xy}}^{(l)}(\mathbf{r}) + \psi_{3d_{xy}}^{(r)}(\mathbf{r})$		bonding antibonding
$\psi_{3d_{xz}}^{(l)}(\mathbf{r}) - \psi_{3d_{xz}}^{(r)}(\mathbf{r})$		bonding antibonding

Bonus (10 pts): What is the lowest-energy term symbol for the $[\text{Ar}]4s^23d^7$ configuration (Cobalt)?