## A Note for Kocherlakota (1996)

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## **Abstract**

This note is a short summary of Kocherlakota (1996). This paper is on Section 6: Asset Pricing of ECON 330 Theory of Income I reading list at University of Chicago.

- 1. Equity premium puzzle: stocks are not sufficiently riskier than Treasury bills to explain the spread of return.
- 2. Risk free rate puzzle: alothough individuals like consumption to be very smooth, and although the risk free rate is very low, they still save enough the per capita consumption grows rapidly.
- 3. Puzzles are implied by three assumptions:
  - (a) Preferences: standard power utility, agent maximizing expected discounted life-long utility
  - (b) Complete asset market: individual can write insurance contracts against any possible contingency
  - (c) No cost for trading asset: taxes and brokerage fess are trivial.
- 4. What are the puzzles?
  - (a) Data
    - i. The average real rate return per year: stock 7%; bond 1%.
    - ii. High per capita consumption growth per year: about 1.8%.
    - iii. Covariance of per capital growth with stock return is only slightly bigger than that with bond return.
  - (b) The original statement of the puzzles
    - i. Key assumptions in Mehra and Prescott (1985)
      - A. Frictionless asset markets
      - B. Complete market
      - C. Representative agents maximizes  $\mathbb{E}_0\left[\sum_{s=0}^{\infty}\beta^s(c_{t+s})^{1-\alpha}/(1-\alpha)\right]$
    - ii. Results: Restrict  $\beta$  between 0 and 1,  $\alpha$  between 0 and 10, for any value gives the expected real return to the Treasury bill less than 4%, the equity premium is less than .35%.
  - (c) More robust restatement of the puzzles: while the covariance between stock and per capita consumption is positive, it is not sufficiently large enough to deter the representative with a RRA coefficient less than 8.5 from wanting to borrow and invest in stocks.
- 5. Preference modification

(a) Generalized expected utility

$$U_t = \left\{ c_t^{1-\rho} + \beta \left[ \mathbb{E}_t U_{t+1}^{1-\alpha} \right]^{\frac{1-\rho}{1-\rho}} \right\}^{\frac{1}{1-\rho}}$$
 (1)

where degree of risk aversion is governed by  $\alpha$  and the elasticity of intertemporal substitution is governed by  $1/\rho$ , which allows  $\alpha$  and  $1/\rho$  high simultaneously to match the data.

- (b) Habit formation
  - i. Intuition: a person consumers a lot this period will get used to that high level of consumption will will strongly desire consumption in next period
  - ii. Mathematically,  $u'(c_t)$  is an increasing function of  $c_{t-1}$ .

$$\mathbb{E}_t \left[ \sum_{s=0}^{\infty} \beta^s \frac{(c_{t+s} - \lambda c_{t+s-1})^{1-\alpha}}{1-\alpha} \right]$$
 (2)

- (c) Relative consumption: 'Keeping up with the Joneses'
  - i. Intuition: the individual's utility is a function not just of his own consumption but of societal levels of consumption
  - ii. Mathematically, <sup>1</sup>

$$\mathbb{E}_t \left[ \beta^s \frac{(c_{t+s}^{1-\alpha} C_{t+s-1}^{\lambda})}{1-\alpha} \right] \tag{3}$$

- 6. Incomplete market and trading cost
  - (a) Incomplete market: no state-contingent asset to insure all future state.
    - i. Infinite horizon economies calibrated to US data suggests the difference between incomplete markets interest rate and complete market rate is small.
  - (b) Trading cost: borrowing and short sales constraint
    - i. Borrowing and shore sales constraint do not quantitatively appear to have much impact on the size of equity premium.
  - (c) Transaction cost: information costs, brokerage fees, load fees, the bid-ask spread and taxes.
    - i. Aiyagari and Gertler (1991) and Heaton and Lucas (1995): the only way to explain the equity premium using transaction cost is to assert that there are significant differences in trading cost across stock and bond market
  - (d) Market segmentation: for whatever reason, only a subset of investors are actively involved in asset trade.
    - i. Cannot explain the equity premium

## References

AIYAGARI, S. R. AND M. GERTLER (1991): "Asset returns with transactions costs and uninsured individual risk," *Journal of Monetary Economics*, 27, 311–331.

HEATON, J. AND D. LUCAS (1995): "The importance of investor heterogeneity and financial market imperfections for the behavior of asset prices," in *Carnegie-Rochester Conference Series on Public Policy*, Elsevier, vol. 42, 1–32.

KOCHERLAKOTA, N. R. (1996): "The equity premium: It's still a puzzle," *Journal of Economic literature*, 34, 42–71.

<sup>&</sup>lt;sup>1</sup>I think there is a typo in the original paper of this equation. See equation (9) of Kocherlakota (1996)

Mehra, R. and E. C. Prescott (1985): "The equity premium: A puzzle," *Journal of monetary Economics*, 15, 145–161.