## A Note for Rubbo (R&R ECTA)

Paul Weifeng Dai University of Chicago

November 14, 2021

## **Abstract**

This note is a short summary of Rubbo (R& R ECTA): Networks, Phillips Curves, and Monetary Policy.

- 1. Model: NK + multi-sector + IO network
- 2. Phillips curve:
  - (a) A unique measure, the divine coincidence index, has a slope independent of IO network and productivity fluctuations do not generate a residual.
    - i.  $\pi_t^{DC}$  weights sectors according to sales share and discounts those with more flexible prices.
    - ii. Intuition: Aggregate output gap is given by markup weighted by sale share. It requires discounting sector with more flexible price responses more given a shock and has less fluctuation of markup.
  - (b) All other Phillips curves are misspecified: flatter slopes and endogenous time varying residuals.
    - i. Slope:
      - A.  $\gamma + \varphi$  the elasticity of employment to real wage
      - B.  $\alpha$  impulse component of wage shock
      - C.  $(I \Omega \Delta)^{-1}$  propagation and rigidity adjustment
      - D.  $1-\overline{\delta}_{\beta}(\alpha)$  equilibrium feedback loop (an increase in real wage raises consumption price by  $\overline{\delta}_{\beta}(\alpha)$ , therefore nominal wages must increase more to sustain a given output)
    - ii. Intuition: flatter since sectors rely on intermediate input since wage changes are partially absorbed by sticky price through the production change and thus inflation response is muted.
    - iii. Divine coincidence: negative shock increase MC and prices (direct) and lower efficient real wage (indirect) do not counterbalance in multi-sector model.
  - (c) Examples
    - i. Roundabout economy: an overestimation if
      - A. Intermediate producers have stickier price than final good producers
      - B. Producers with more flexible prices use stickier intermediate input
      - C. Sectors with large labor share have large labor shares have stickier prices
    - ii. Vertical chain
    - iii. Horizontal economy
    - iv. Oil economy: sticky upstream labor sector + middle oil sector + downstream final good; Similar to downstream shock since oil shock are fully passed through final good producers, and increase consumer prices; the effect of final prices is proportional to wage rigidity

## 3. Welfare loss function:

- (a) Source of welfare loss: inefficient markups arising from pricing frictions, which distorts labor supply (factor suppression) and reduces labor productivity (misallocation)
  - i. Within sector misallocation: more severe in stickier sectors and when elasticity of substitution is large (large quantity response to relative price distortions)
  - ii. Cross-sector misallocation: dependent on how price distortions propagate through the input-output network and the amount of substitution that they induce across input and final goods
- 4. Optimal policy:
  - (a) Minimize welfare loss subject to Phillips curve
  - (b) Dynamic model:
    - i. Forward looking term (policy today affects misallocation tomorrow)
    - ii. Backward looking term (monetary policy can improve misallocation by influencing inflation expectations)
  - (c) No divine coincidence in multi-sector, CB trade-off: closing output gap versus efficient relative price across firms and sectors

- (d) Optimal: output gap stabilization by targeting divine coincidence index in the Taylor rule
- (e) Monetary policy cannot replicate efficient equilibrium  $\rightarrow$  greater welfare loss from misallocation
- (f) Choice of which inflation index to target is non-trivial.

## 5. Quantitative result:

- (a) One-sector and multi-sector models are quantitatively different
- (b) Two potential mechanism of declining slope over time:
  - i. An increase in intermediate input flows (IO): explanatory for the pre-1980 decline
  - ii. A shift in consumption towards stickier sectors: contribute to the flattening after 1980
- (c) Monetary non-neutrality due to IO linkage is confirmed by impulse response of consumer inflation.
- (d) This framework reconciles that wage Phillips curve is steeper than the price Phillips curve, and has not flattened over time since  $\delta_{wage}$  only captures the effect of changes in labor demand on wages, while  $\overline{\delta}_{\beta}(\alpha)$  incorporates the pass-through wage into consumer prices.
- (e) Endogenous cost-push shock is a significant driver of variation for consumption price inflation. Optimal monetary policy should allow for a small positive output gap even though this slightly raises inflation.
- (f) Consumption equivalence (in exchange of eliminating price frictions) 2.9% when CB implements optimal policy (this paper)> 0.05% (Lucas). Targeting consumer inflation yields 3.8% welfare loss.
- (g) Regression using divine coincidence index matches the empirical slope and has larger  $\mathbb{R}^2$  (Phillips curve is not affected by endogenous residuals).