

Extract a thermodynamically consistent subnetwork from a given model

1. Identify the largest subset of a model that admits a thermodynamically consistent flux
2. Specify a random subset of active/inactive reactions and present/absent metabolites
3. Compute the smallest thermodynamically consistent subnetwork containing a list of present metabolites and active reactions, and not containing a list of absent metabolites and inactive reactions

```
[solverOK,solverInstalled]=changeCobraSolver('ibm_cplex','all');
```

```
> changeCobraSolver: IBM ILOG CPLEX interface added to MATLAB path.  
> ibm_cplex (version 1210) is compatible and fully tested with MATLAB R2021a on your operating system.  
> changeCobraSolver: Solver for LP problems has been set to ibm_cplex.  
  
> changeCobraSolver: IBM ILOG CPLEX interface added to MATLAB path.  
> ibm_cplex (version 1210) is compatible and fully tested with MATLAB R2021a on your operating system.  
> changeCobraSolver: Solver for MILP problems has been set to ibm_cplex.  
  
> changeCobraSolver: IBM ILOG CPLEX interface added to MATLAB path.  
> ibm_cplex (version 1210) is compatible and fully tested with MATLAB R2021a on your operating system.  
> changeCobraSolver: Solver for QP problems has been set to ibm_cplex.  
  
> changeCobraSolver: IBM ILOG CPLEX interface added to MATLAB path.  
> ibm_cplex (version 1210) is compatible and fully tested with MATLAB R2021a on your operating system.  
> changeCobraSolver: Solver for MIQP problems has been set to ibm_cplex.  
> changeCobraSolver: Solver ibm_cplex not supported for problems of type EP. No solver set for this problem.  
> changeCobraSolver: Solver ibm_cplex not supported for problems of type NLP. No solver set for this problem.
```

```
%[solverOK,solverInstalled]=changeCobraSolver('gurobi','all');  
%[solverOK,solverInstalled]=changeCobraSolver('ibm_cplex','QP');
```

Load model

```
modelToLoad='circularToy';  
modelToLoad='ecoli_core';  
modelToLoad='modelRecon3MitoOpen';  
modelToLoad='Recon3DModel';  
%modelToLoad='iDopa';
```

Load a model

```
driver_thermoModelLoad
```

```
Model loaded: Recon3DModel  
lower bounds greater than zero  
Internal stoichiometric nullspace computed in 4.5238 seconds.
```

Stoichiometric consistency

```
if ~isfield(model,'SConsistentRxnBool') ||  
~isfield(model,'SConsistentMetBool')  
    massBalanceCheck=0;  
    %massBalanceCheck=1;
```

```

    printLevel=2;
    [SConsistentMetBool, SConsistentRxnBool,
    SInConsistentMetBool, SInConsistentRxnBool, unknownSConsistencyMetBool,
    unknownSConsistencyRxnBool, model,stoichConsistModel]...
        = findStoichConsistentSubset(model, massBalanceCheck, printLevel);
else
    %Extract stoich consistent submodel
    if any(~model.SConsistentMetBool)
        rxnRemoveMethod='inclusive';%maintains stoichiometric consistency
        [stoichConsistModel, rxnRemoveList] = removeMetabolites(model,
model.mets(~model.SConsistentMetBool),rxnRemoveMethod);
        SConsistentRxnBool2=~ismember(model.rxns,rxnRemoveList);
        if ~all(model.SConsistentRxnBool==SConsistentRxnBool2)
            error('inconsistent reaction removal')
        end
        try
            stoichConsistModel = removeUnusedGenes(stoichConsistModel);
        catch ME
            disp(ME.message)
        end
    else
        stoichConsistModel = model;
    end
end

[nMet,nRxn]=size(stoichConsistModel.S)

```

```

nMet = 5835
nRxn = 10600

```

Flux consistency

```

fluxConsistentParam.method='fastcc';%can handle additional constraints
fluxConsistentParam.printLevel=1;
[~,~,~,~,stoichConsistModel]=
findFluxConsistentSubset(stoichConsistModel,fluxConsistentParam);

```

Extract flux consistent submodel

```

if any(~stoichConsistModel.fluxConsistentRxnBool)
    rxnRemoveList =
stoichConsistModel.rxns(~stoichConsistModel.fluxConsistentRxnBool);
    stoichFluxConsistModel = removeRxns(stoichConsistModel,
rxnRemoveList,'metRemoveMethod','exclusive','ctrsRemoveMethod','inclusive');
    try
        stoichFluxConsistModel = removeUnusedGenes(stoichFluxConsistModel);
    catch ME
        disp(ME.message)
    end
else

```

```

    stoichFluxConsistModel = stoichConsistModel;
end
[nMet,nRxn]=size(stoichFluxConsistModel.S)

```

```

nMet = 5835
nRxn = 10600

```

Thermodynamic consistency

```

%save('debug_prior_to_findThermoConsistentFluxSubset.mat')
%return
param.printLevel = 1;
param.relaxBounds=0;
param.acceptRepairedFlux=1;
[thermoFluxConsistentMetBool,thermoFluxConsistentRxnBool,stoichFluxConsistMod
el,stoichFluxThermoConsistModel] =
findThermoConsistentFluxSubset(stoichFluxConsistModel,param);

```

```

--- findThermoFluxConsistentSubset START ----
    printLevel: 1
    relaxBounds: 0
    acceptRepairedFlux: 1
        epsilon: 1.0000e-06
        formulation: 'pqzw'
        iterationMethod: 'random'
            nMax: 20
        warmStartMethod: 'random'
        thetaMultiplier: 1.5000
            theta: 0.5000
        regularizeOuter: 0
    thermoConsistencyMethod: 'cycleFreeFlux'
        bigNum: 10000
        debug: 0

```

optCardThermo objective data:

```

0.1 = beta, the global weight on one-norm of internal reaction rate.
-5 = min(g0), the local weight on zero-norm of internal reaction rate.
-0 = max(g0), the local weight on zero-norm of internal reaction rate.
0 = min(h0), the local weight on zero-norm of metabolite production rate.
0 = max(h0), the local weight on zero-norm of metabolite production rate.

```

optimizeCardinality objective data:

0 min cardinality variables:

NaN mean(c(p))	NaN min(c(p))	NaN max(c(p))
1 lambda0	NaN min(k)	NaN max(k)
1 lambda1	NaN min(o(p))	NaN max(o(p))

5303 max cardinality variables:

-0 mean(c(q))	-0 min(c(q))	-0 max(c(q))
1 delta0	5 min(d)	5 max(d)
0 delta1	0 min(o(q))	0 max(o(q))

22879 cardinality free variables:

0.077 mean(c(r))	-0 min(c(r))	0.1 max(c(r))
0 alpha1	0 min(o(r))	0 max(o(r))

itn	theta	dx	del_obj	obj	linear	x 0	a(x)	x 1	y
1	0.50	7.6657e+05	-8.8e+06	-2.2e+04	1.6e+03	0	0	0	-236
2	0.75	184.22	-8.5e+02	-2.3e+04	1.1e+03	0	0	0	-238

3	1.12	98.541	-4.8e+02	-2.3e+04	7.3e+02	0	0	0	-239
4	1.69	61.895	-2.6e+02	-2.3e+04	4.9e+02	0	0	0	-239
5	2.53	40.001	-1.7e+02	-2.4e+04	3.3e+02	0	0	0	-239
6	3.80	26.092	-1.3e+02	-2.4e+04	2.2e+02	0	0	0	-239
7	5.70	18.183	-73	-2.4e+04	1.5e+02	0	0	0	-239
8	8.54	11.708	-68	-2.4e+04	97	0	0	0	-239
9	12.81	7.942	-34	-2.4e+04	65	0	0	0	-239
10	19.22	5.2426	-36	-2.4e+04	44	0	0	0	-239
11	28.83	3.5411	-48	-2.4e+04	29	0	0	0	-240
12	43.25	2.3919	-17	-2.4e+04	20	0	0	0	-240
13	64.87	1.6485	-13	-2.4e+04	14	0	0	0	-240
14	97.31	1.0952	-4.2	-2.4e+04	9.3	0	0	0	-240
15	145.96	0.76091	-2.9	-2.4e+04	6.5	0	0	0	-240
16	218.95	0.51853	-42	-2.4e+04	4.7	0	0	0	-240
17	328.42	0.53726	-14	-2.4e+04	3.5	0	0	0	-240

itn theta ||dx|| del_obj obj linear ||x||0 a(x) ||x||1 ||y||

Optimise cardinality reached the stopping criterion. Finished.

cycleFreeFlux: No solution found.

Debugging relaxation etc...

```

full: []
obj: []
rcost: []
dual: []
slack: []
solver: 'ibm_cplex'
algorithm: 'Automatic'
stat: 0
origStat: 3
origStatText: 'Model has been proved infeasible'
time: 0.0300
basis: []

```

itn	obj	obj_old	err(obj)	err(x)	card(v)	card(r)	card(p)	card(q)
0	14.072	66705	66691	165.16	3913	0	543	541
1	1391	14.072	1376.9	48.563	2734	0	692	717
2	944.42	1391	446.54	62.844	3799	0	652	666
3	1526.3	944.42	581.91	64.636	3026	0	712	702
4	828.59	1526.3	697.73	63.09	3157	0	574	605
5	992.49	828.59	163.9	55.391	3334	0	716	682
6	1074.4	992.49	81.866	59.058	3674	0	687	657
7	1300.5	1074.4	226.18	63.35	3238	0	700	708
8	1040.9	1300.5	259.63	62.911	3773	0	685	639
9	1327.8	1040.9	286.85	63.278	3013	0	703	667
10	814.59	1327.8	513.18	60.13	3064	0	614	603
11	1027.5	814.59	212.94	55.715	2717	0	628	614
12	677.72	1027.5	349.8	53.573	3435	0	602	618
13	1061.2	677.72	383.44	54.092	3505	0	734	693
14	1272.7	1061.2	211.54	62.794	3509	0	693	670
15	1197.8	1272.7	74.901	64.628	3152	0	669	689
16	971.72	1197.8	226.09	60.517	2983	0	585	622
17	903.71	971.72	68.006	56.208	2923	0	612	658
18	834.71	903.71	69	54.078	3806	0	671	642
19	1348.3	834.71	513.59	60.702	3075	0	720	659

itn obj obj_old err(obj) err(x) card(v) card(r) card(p) card(q)

Relaxed model is feasible.

Statistics:

599 lower bound relaxation(s)

576 upper bound relaxation(s)

0 steady state relaxation(s)

... done.

ans = 9.1346e-07

ans = 0

ans = 0

```

solution = struct with fields:
    stat: 1
    v: [19391x1 double]
    r: [23417x1 double]
    p: [19391x1 double]
    q: [19391x1 double]
solutionRelaxed1 = struct with fields:
    full: [19391x1 double]
    obj: 26.3611
    rcost: [19391x1 double]
    dual: [23417x1 double]
    slack: [23417x1 double]
    solver: 'ibm_cplex'
    algorithm: 'Automatic'
    stat: 1
    origStat: 1
    origStatText: 'Optimal solution found'
    time: 1.2415
    basis: []
solutionRelaxed2 = struct with fields:
    full: [19391x1 double]
    obj: 0
    rcost: [19391x1 double]
    dual: [23417x1 double]
    slack: [23417x1 double]
    solver: 'ibm_cplex'
    algorithm: 'Automatic'
    stat: 1
    origStat: 1
    origStatText: 'Optimal solution found'
    time: 0.6092
    basis: []
solutionRelaxed3 = struct with fields:
    full: [19391x1 double]
    obj: 0
    rcost: [19391x1 double]
    dual: [23417x1 double]
    slack: [23417x1 double]
    solver: 'ibm_cplex'
    algorithm: 'Automatic'
    stat: 1
    origStat: 1
    origStatText: 'Optimal solution found'
    time: 0.3797
    basis: []
cycleFreeFlux: No solution found, try using a different solver.

cycleFreeFlux: No solution found.
Debugging relaxation etc...
    full: []
    obj: []
    rcost: []
    dual: []
    slack: []
    solver: 'ibm_cplex'
    algorithm: 'Automatic'
    stat: 0
    origStat: 3
    origStatText: 'Model has been proved infeasible'
    time: 0.0305
    basis: []

itn      obj      obj_old    err(obj)    err(x)    card(v)    card(r)    card(p)    card(q)
0        14.072    66355      66341      164.43    3913       0          543        541

```

1	1391	14.072	1376.9	48.563	2734	0	692	717
2	944.42	1391	446.54	62.844	3799	0	652	666
3	1526.3	944.42	581.91	64.636	3026	0	712	702
4	828.59	1526.3	697.73	63.09	3157	0	574	605
5	992.49	828.59	163.9	55.391	3334	0	716	682
6	1074.4	992.49	81.866	59.058	3674	0	687	657
7	1300.5	1074.4	226.18	63.35	3238	0	700	708
8	1040.9	1300.5	259.63	62.911	3773	0	685	639
9	1327.8	1040.9	286.85	63.278	3013	0	703	667
10	814.59	1327.8	513.18	60.13	3064	0	614	603
11	1027.5	814.59	212.94	55.715	2717	0	628	614
12	677.72	1027.5	349.8	53.573	3435	0	602	618
13	1061.2	677.72	383.44	54.092	3505	0	734	693
14	1272.7	1061.2	211.54	62.794	3509	0	693	670
15	1197.8	1272.7	74.901	64.628	3152	0	669	689
16	971.72	1197.8	226.09	60.517	2983	0	585	622
17	903.71	971.72	68.006	56.208	2923	0	612	658
18	834.71	903.71	69	54.078	3806	0	671	642
19	1348.3	834.71	513.59	60.702	3075	0	720	659
itn	obj	obj_old	err(obj)	err(x)	card(v)	card(r)	card(p)	card(q)

Relaxed model is feasible.
Statistics:
599 lower bound relaxation(s)
576 upper bound relaxation(s)
0 steady state relaxation(s)
... done.
ans = 9.1346e-07
ans = 0
ans = 0
solution = struct with fields:
 stat: 1
 v: [19391x1 double]
 r: [23417x1 double]
 p: [19391x1 double]
 q: [19391x1 double]
solutionRelaxed1 = struct with fields:
 full: [19391x1 double]
 obj: 26.3611
 rcost: [19391x1 double]
 dual: [23417x1 double]
 slack: [23417x1 double]
 solver: 'ibm_cplex'
 algorithm: 'Automatic'
 stat: 1
 origStat: 1
 origStatText: 'Optimal solution found'
 time: 1.3163
 basis: []
solutionRelaxed2 = struct with fields:
 full: [19391x1 double]
 obj: 0
 rcost: [19391x1 double]
 dual: [23417x1 double]
 slack: [23417x1 double]
 solver: 'ibm_cplex'
 algorithm: 'Automatic'
 stat: 1
 origStat: 1
 origStatText: 'Optimal solution found'
 time: 0.5761
 basis: []
solutionRelaxed3 = struct with fields:
 full: [19391x1 double]
 obj: 0

```

rcost: [19391x1 double]
dual: [23417x1 double]
slack: [23417x1 double]
solver: 'ibm_cplex'
algorithm: 'Automatic'
stat: 1
origStat: 1
origStatText: 'Optimal solution found'
time: 0.3650
basis: []

```

Warning: cycleFreeFlux did not solve, trying v2QNTy

76.81% thermodynamically feasible internal fluxes (checked by v2QNTy method).

iter	card(y)	nz	%feas	int.nz.	tot %feas	int.nz.	tot
1	5303	7882		0.68		0.50	
2	2376	3075		1.00		0.69	
3	1427	1708		1.00		0.77	
4	1022	1296		1.00		0.83	
5	769	794		1.00		0.86	
6	606	587		1.00		0.88	
7	506	432		1.00		0.90	
8	449	377		1.00		0.91	
9	389	324		1.00		0.92	
10	348	301		1.00		0.93	
11	298	332		1.00		0.94	
12	254	384		1.00		0.95	
13	216	209		1.00		0.96	
14	191	200		1.00		0.97	
15	153	201		1.00		0.97	
16	151	162		1.00		0.97	
17	106	139		1.00		0.98	
18	102	161		1.00		0.98	
19	78	127		1.00		0.98	
20	91	128		1.00		0.98	
iter	card(y)	nz	%feas	int.nz.	tot %feas	int.nz.	tot

findThermoConsistentFluxSubset terminating early: n = nMax = 20
--- findThermoFluxConsistentSubset END ---

Size of the largest flux, stoich and thermo consistent submodel

```

[nMet,nRxn]=size(stoichFluxThermoConsistModel.S)
save(['~/work/sbgCloud/programModelling/projects/thermoModel/results/
thermoKernel/' modelToLoad
'_stoichFluxThermoConsistModel.mat'],'stoichFluxThermoConsistModel')

```

```

%modelToLoad='Recon3DModel';
load(['~/work/sbgCloud/programModelling/projects/thermoModel/results/
thermoKernel/' modelToLoad
'_stoichFluxThermoConsistModel.mat'],'stoichFluxThermoConsistModel')

```

Nullspace

Nullspace is necessary for backup check of thermodynamic consistency using thermoFlux2QNTy

```

[stoichFluxThermoConsistModel,rankK,nnzK,timeTaken] =
internalNullspace(stoichFluxThermoConsistModel);
rankK

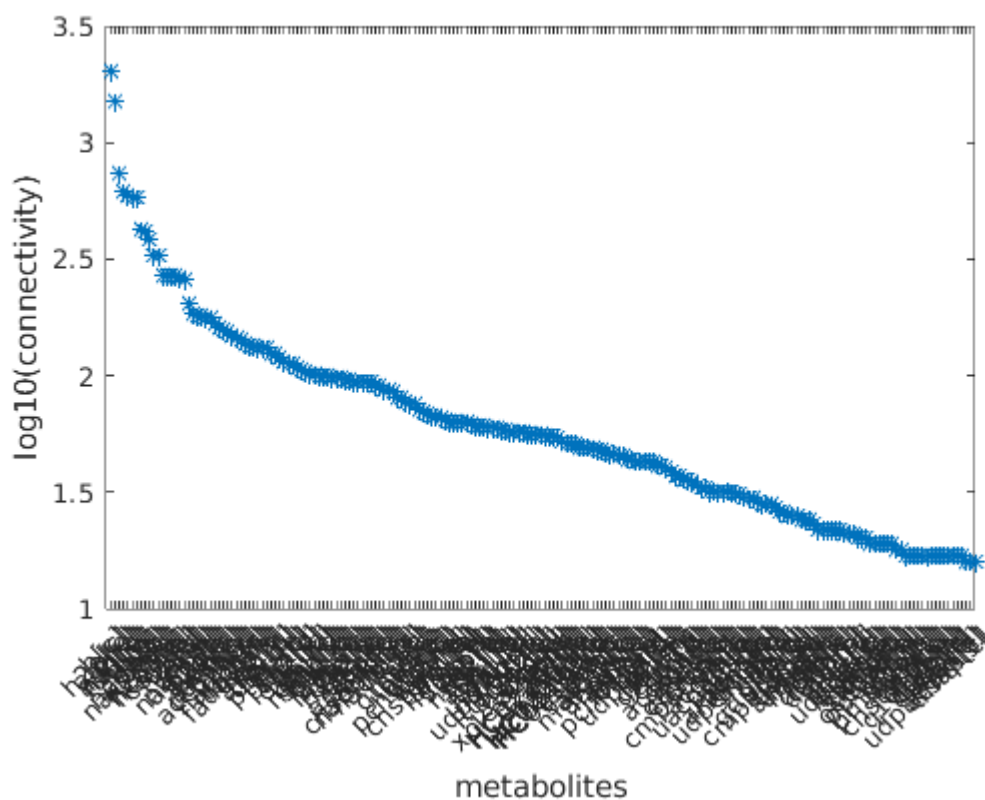
```

rankK = 5485

Data to define a thermodynamically consistent subnetwork

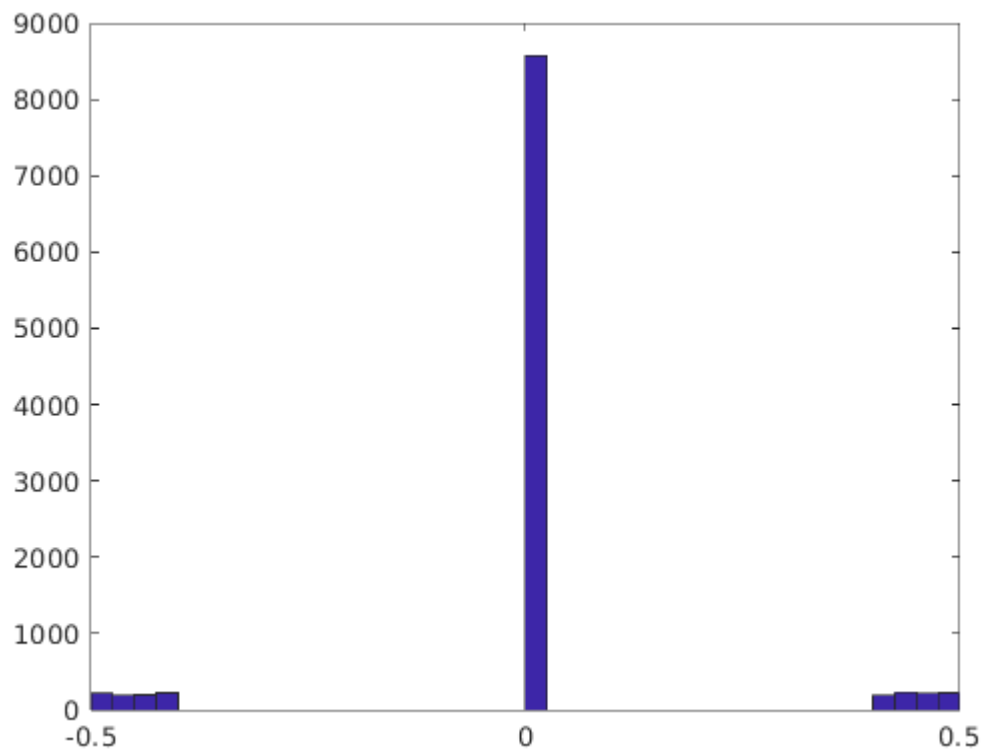
Setup random data to select a random subset

```
param.n=200;
[rankMetConnectivity,rankMetInd,rankConnectivity] =
rankMetabolicConnectivity(stoichFluxThermoConsistModel,param);
```

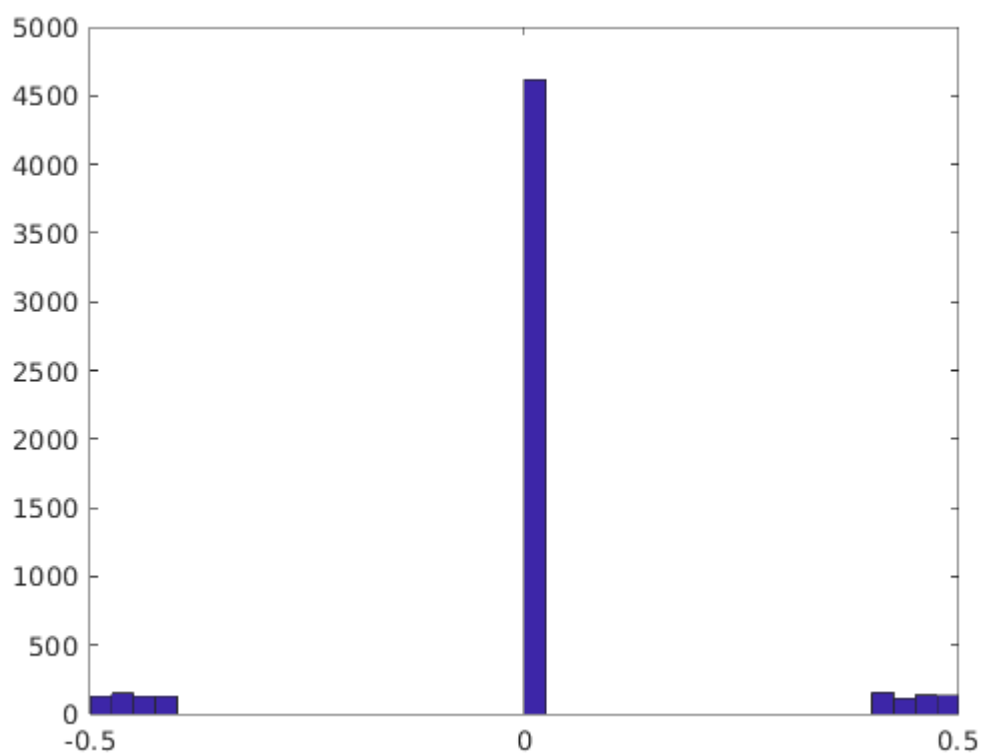


```
[nMet,nRxn]=size(stoichFluxThermoConsistModel.S);
rxnWeights=rand(nRxn,1)-0.5;
rxnWeights(~stoichFluxThermoConsistModel.SConsistentRxnBool)=0;

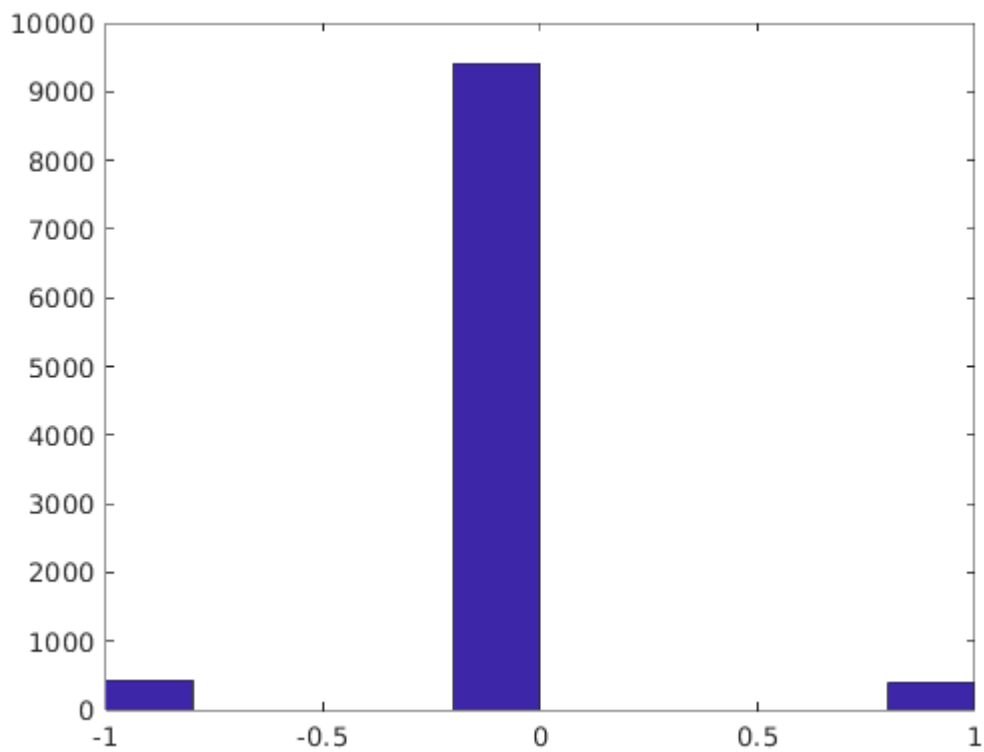
coreRxnBool=rxnWeights<-0.45;
removeRxnBool=rxnWeights>0.45;
if 0
    rxnWeights(rxnWeights>0.4)=1;
    rxnWeights(rxnWeights<-0.4)=-1;
end
rxnWeights(rxnWeights>=-0.4 & rxnWeights<=0.4)=0;
hist(rxnWeights,40)
```

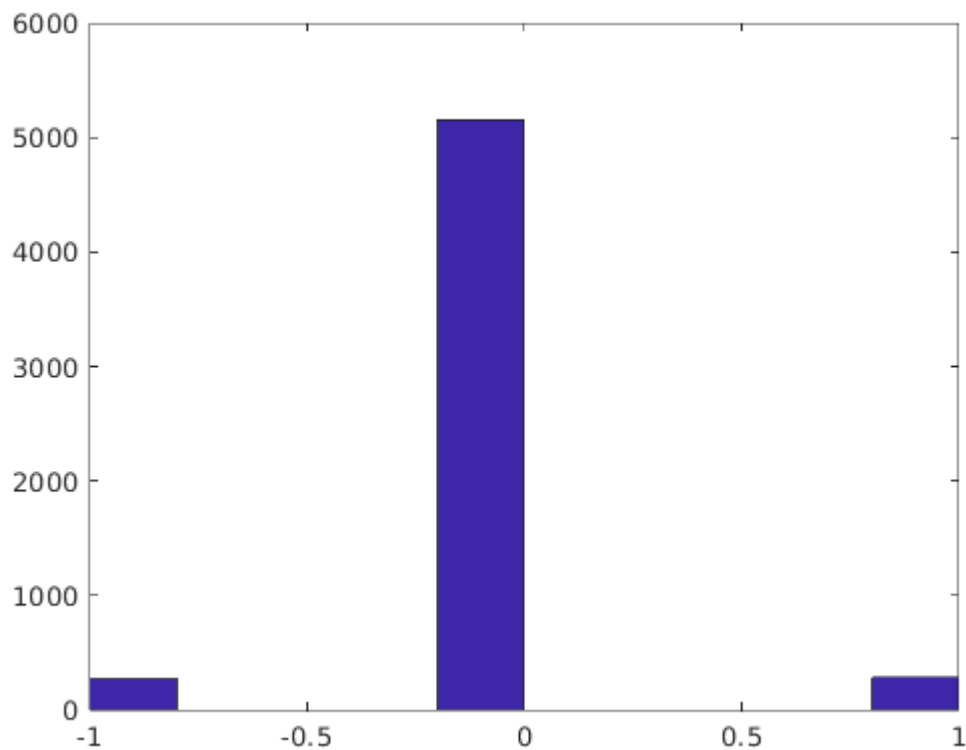
```
metWeights=rand(nMet,1)-0.5;
metWeights(rankMetInd(1:200))=0;
coreMetBool=metWeights<-0.45;
removeMetBool=metWeights>0.45;
if 0
    metWeights(metWeights>0.4)=1;
    metWeights(metWeights<-0.4)=-1;
end
metWeights(metWeights>=-0.4 & metWeights<=0.4)=0;
hist(metWeights,40)
```



```
nlt=length(coreRxnBool);  
activeInactiveRxn=zeros(nlt,1);  
activeInactiveRxn(coreRxnBool)=1;  
activeInactiveRxn(removeRxnBool)=-1;  
hist(activeInactiveRxn)
```



```
mlt=length(coreMetBool);  
presentAbsentMet=zeros(mlt,1);  
presentAbsentMet(coreMetBool)=1;  
presentAbsentMet(removeMetBool)=-1;  
if 0  
    activeInactiveRxn(:)=0;  
    presentAbsentMet(:)=0;  
end  
param.normalizeZeroNormWeights=0;  
  
hist(presentAbsentMet)
```



Compute the smallest thermodynamically consistent subnetwork given a list of present/absent metabolites and active/inactive reactions

```
[tissueModel, thermoModelMetBool, thermoModelRxnBool] =
thermoKernel(stoichFluxThermoConsistModel, activeInactiveRxn, rxnWeights,
presentAbsentMet, metWeights,param);
```

```
--- thermoKernel START ---
thermoKernel parameters:
    printLevel: 1
    relaxBounds: 0
    acceptRepairedFlux: 1
        n: 200
    normalizeZeroNormWeights: 0
        formulation: 'pqzwr's'
        epsilon: 1.0000e-06
    removeOrphanGenes: 1
        nbMaxIteration: 30
        nMax: 20
        iterationMethod: 'greedyRandom'

    warmStartMethod: 'random'
        formulation: 'pqzwr's'
    thetaMultiplier: 1.5000
        theta: 0.5000
    regularizeOuter: 1
        epsilon: 1.0000e-06
        printLevel: 1
        relaxBounds: 0
    acceptRepairedFlux: 1
    thermoConsistencyMethod: 'cycleFreeFlux'
```

```
bigNum: 10000
debug: 0
```

optCardThermo objective data:

```
1 = beta, the global weight on one-norm of internal reaction rate.
-0.5 = min(g0), the local weight on zero-norm of internal reaction rate.
0.5 = max(g0), the local weight on zero-norm of internal reaction rate.
-0.5 = min(h0), the local weight on zero-norm of metabolite production rate.
0.5 = max(h0), the local weight on zero-norm of metabolite production rate.
```

optimizeCardinality objective data:

1393 min cardinality variables:

```
0 mean(c(p))          -0 min(c(p))          -0 max(c(p))
1 lambda0             0.4 min(k)             0.5 max(k)
0 lambda1             0 min(o(p))            0 max(o(p))
```

1912 max cardinality variables:

```
0 mean(c(q))          -0 min(c(q))          -0 max(c(q))
1 delta0             0.4 min(d)             0.5 max(d)
0 delta1             0 min(o(q))            0 max(o(q))
```

35242 cardinality free variables:

```
0.48 mean(c(r))       -0 min(c(r))          1 max(c(r))
0 alpha1             0 min(o(r))            0 max(o(r))
```

itn	theta	dx	del_obj	obj	linear	x 0	a(x)	x 1	y
1	0.50	9.6992e+05	-8.5e+07	7.9	11	1.64389	0.11	0	-14.90
2	0.75	4.5121	-1.7	6.2	12	2.0597	0.16	0	-15.84
3	1.12	2.8094	-1.8	4.4	12	1.65769	0.25	0	-17.51
4	1.69	3.0116	-2	2.4	12	1.23553	0.43	0	-18.81
5	2.53	3.0252	-2.3	0.041	13	1.23553	0.45	0	-19.68
6	3.80	2.7007	-3.3	-3.3	13	1.23553	0.47	0	-24.78
7	5.70	2.0612	-4.9	-8.2	14	1.23553	0.87	0	-25.69
8	8.54	1.9653	-2.8	-11	13	1.23553	0.9	0	-27.03
9	12.81	1.3137	-3.8	-15	12	1.23553	0.95	0	-30.49
10	19.22	1.2354	-4	-19	11	1.23553	1	0	-32.32
11	28.83	0.809	-2.2	-21	10	1.23553	1.1	0	-32.32
12	43.25	0.71837	-0.57	-21	9.6	1.23553	1.2	0	-32.32
13	64.87	0.46434	-0.55	-22	9.2	1.23553	1.2	0	-33.26
14	97.31	0.33824	-1.1	-23	8.9	1.23553	1.2	0	-33.26
15	145.96	0.21621	-0.14	-23	8.8	1.23553	1.2	0	-33.26
16	218.95	0.2235	-0.088	-23	8.7	1.23553	1.2	0	-33.26
17	328.42	0.10113	-0.058	-23	8.6	1.23553	1.2	0	-33.26
itn	theta	dx	del_obj	obj	linear	x 0	a(x)	x 1	y

Optimise cardinality reached the stopping criterion. Finished.

100.00% thermodynamically feasible internal fluxes (checked by cycleFreeFlux method).

```
warmStartMethod: 'random'
formulation: 'pqzwrS'
thetaMultiplier: 1.5000
theta: 0.5000
regularizeOuter: 1
epsilon: 1.0000e-06
printLevel: 1
relaxBounds: 0
acceptRepairedFlux: 1
thermoConsistencyMethod: 'cycleFreeFlux'
bigNum: 10000
debug: 0
```

optCardThermo objective data:

```
1 = beta, the global weight on one-norm of internal reaction rate.
-0.5 = min(g0), the local weight on zero-norm of internal reaction rate.
0.5 = max(g0), the local weight on zero-norm of internal reaction rate.
```

-0.5 = min(h0), the local weight on zero-norm of metabolite production rate.
0.5 = max(h0), the local weight on zero-norm of metabolite production rate.

optimizeCardinality objective data:

1393 min cardinality variables:

0 mean(c(p))	-0 min(c(p))	-0 max(c(p))
1 lambda0	0.4 min(k)	0.5 max(k)
0 lambda1	0 min(o(p))	0 max(o(p))

1912 max cardinality variables:

0 mean(c(q))	-0 min(c(q))	-0 max(c(q))
1 delta0	0.4 min(d)	0.5 max(d)
0 delta1	0 min(o(q))	0 max(o(q))

35242 cardinality free variables:

0.48 mean(c(r))	-0 min(c(r))	1 max(c(r))
0 alpha1	0 min(o(r))	0 max(o(r))

itn	theta	dx	del_obj	obj	linear	x 0	a(x)	x 1	y
1	0.50	9.6862e+05	-8.4e+07	8.1	11	3.74292	0.11	0	-13.29
2	0.75	2.3033	-1	7.1	10	2.06605	0.16	0	-12.36
3	1.12	2.5538	-1.1	6	10	2.06605	0.26	0	-13.24
4	1.69	2.8214	-1.1	4.8	11	1.23553	0.43	0	-14.56
5	2.53	3.0167	-2.9	2	12	1.23553	0.45	0	-17.11
6	3.80	2.0716	-2.1	-0.084	12	1.23553	0.47	0	-18.83
7	5.70	2.5196	-3.8	-3.9	13	0.832228	0.47	0	-20.67
8	8.54	1.9952	-3.6	-7.5	13	0.832228	0.5	0	-22.59
9	12.81	1.589	-3	-10	12	0.832228	0.55	0	-23.07
10	19.22	1.0613	-1.5	-12	10	0.832228	0.62	0	-23.07
11	28.83	0.69458	-0.65	-13	9.7	0.832228	0.73	0	-23.07
12	43.25	0.49103	-0.32	-13	9.3	0.832228	0.83	0	-23.07
13	64.87	0.24192	-0.24	-13	9	0.832228	0.83	0	-23.07
14	97.31	0.21816	-0.55	-14	8.9	0.832228	0.83	0	-23.47
15	145.96	0.17636	-0.075	-14	8.8	0.832228	0.83	0	-23.47
16	218.95	0.097141	-0.048	-14	8.7	0.832228	0.83	0	-23.47
17	328.42	0.16623	-0.031	-14	8.7	0.832228	0.83	0	-23.47
itn	theta	dx	del_obj	obj	linear	x 0	a(x)	x 1	y

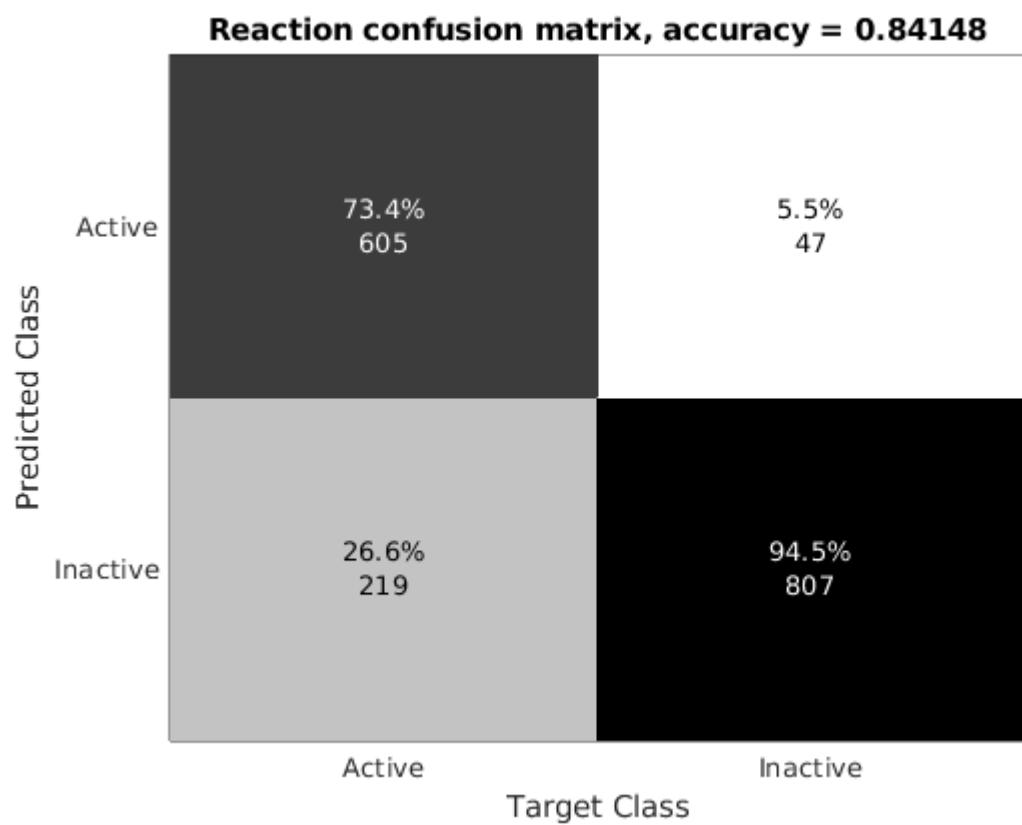
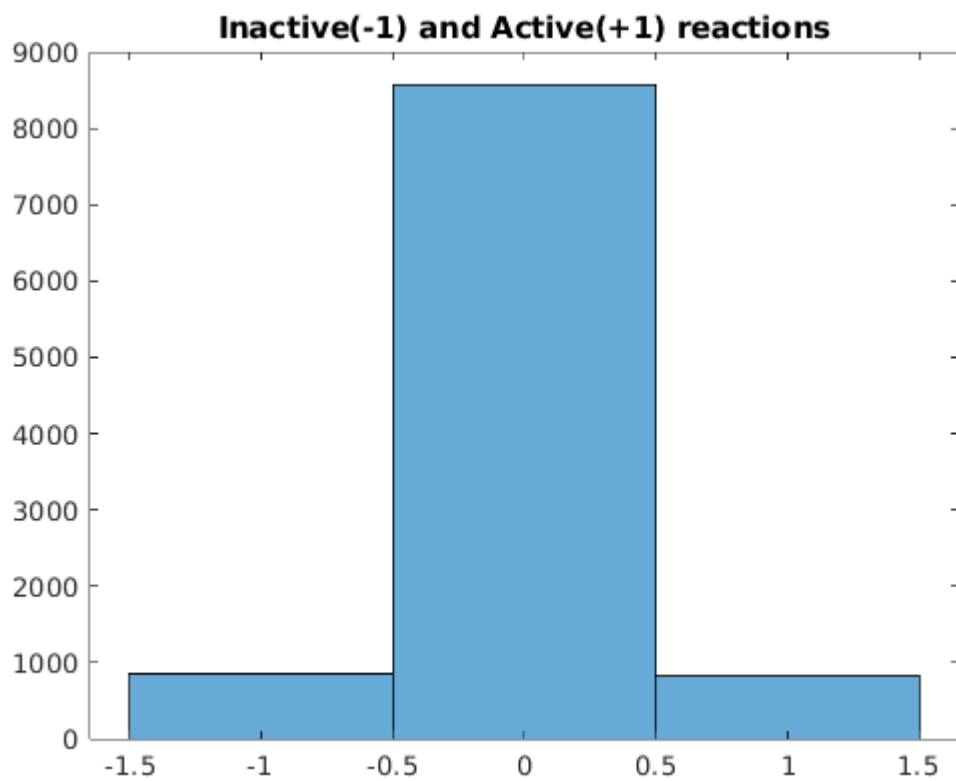
Optimise cardinality reached the stopping criterion. Finished.

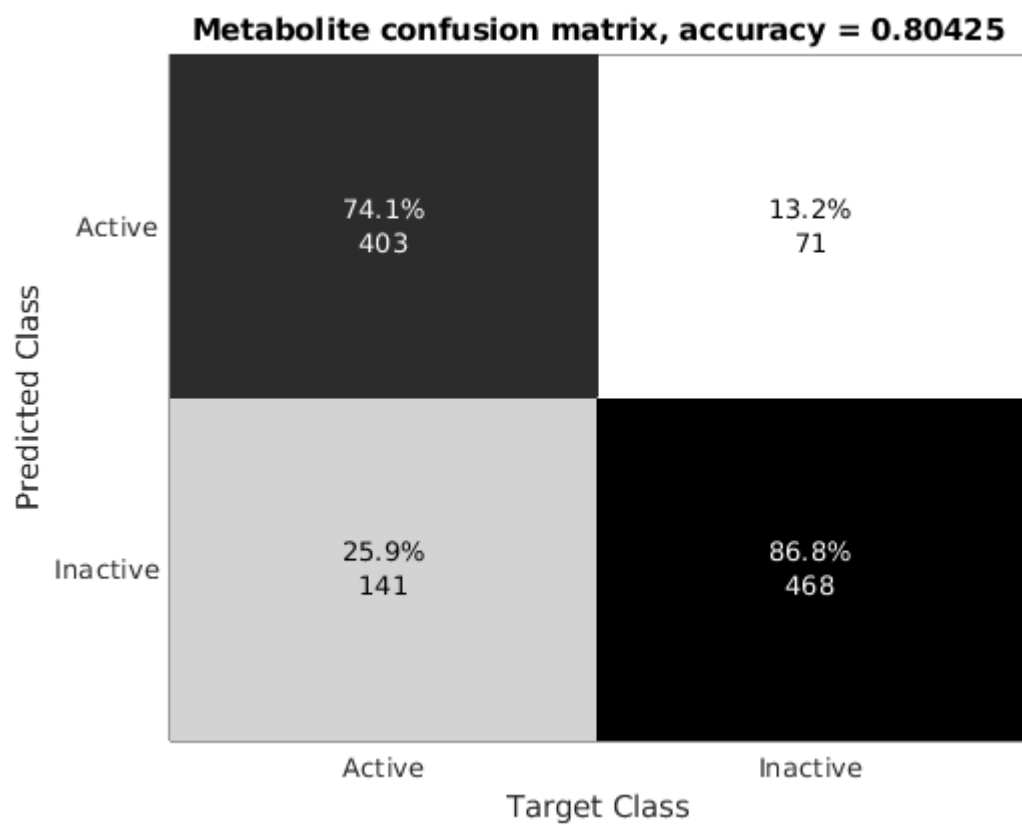
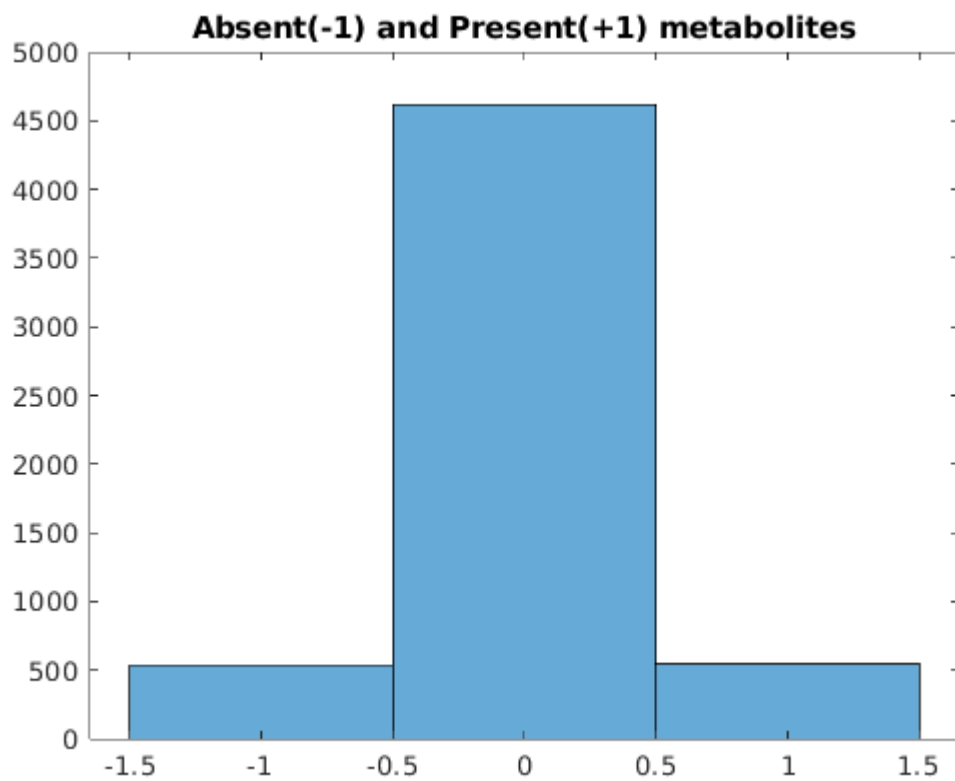
100.00% thermodynamically feasible internal fluxes (checked by cycleFreeFlux method).

iter.	nz.flux.	%it.feas.int.flux.	%feas.inc.flux.	nz.prod.	%it.feas.nz.prod.	%feas.inc.prod.	fo
1	178	1.00	0.02	121	1.29	0.03	gre
2	208	1.00	0.04	155	1.19	0.10	gre
3	335	1.00	0.07	249	1.20	0.22	gre
4	424	1.00	0.11	301	1.28	0.35	gre
5	393	1.00	0.20	272	1.30	0.42	gre
6	505	1.00	0.29	354	1.29	0.51	gre
7	280	1.00	0.34	208	1.28	0.54	gre
8	378	1.00	0.41	281	1.30	0.58	gre
9	395	1.00	0.45	291	1.31	0.63	gre
10	272	1.00	0.50	211	1.28	0.65	gre
11	281	1.00	0.54	203	1.36	0.67	gre
12	315	1.00	0.59	228	1.36	0.68	gre
13	189	1.00	0.61	134	1.29	0.69	gre
14	358	1.00	0.65	258	1.40	0.70	gre
15	299	1.00	0.68	218	1.28	0.72	gre
16	166	1.00	0.69	116	1.30	0.72	gre
17	275	1.00	0.70	191	1.45	0.73	gre
18	249	1.00	0.71	175	1.45	0.73	gre
19	150	1.00	0.72	107	1.38	0.74	gre
20	235	1.00	0.73	176	1.36	0.74	gre

iter.	nz.flux.	%it.feas.int.flux.	%feas.inc.flux.	nz.prod.	%it.feas.nz.prod.	%feas.inc.prod.	fo
-------	----------	--------------------	-----------------	----------	-------------------	-----------------	----

thermoKernel terminating early: n = nMax = 20





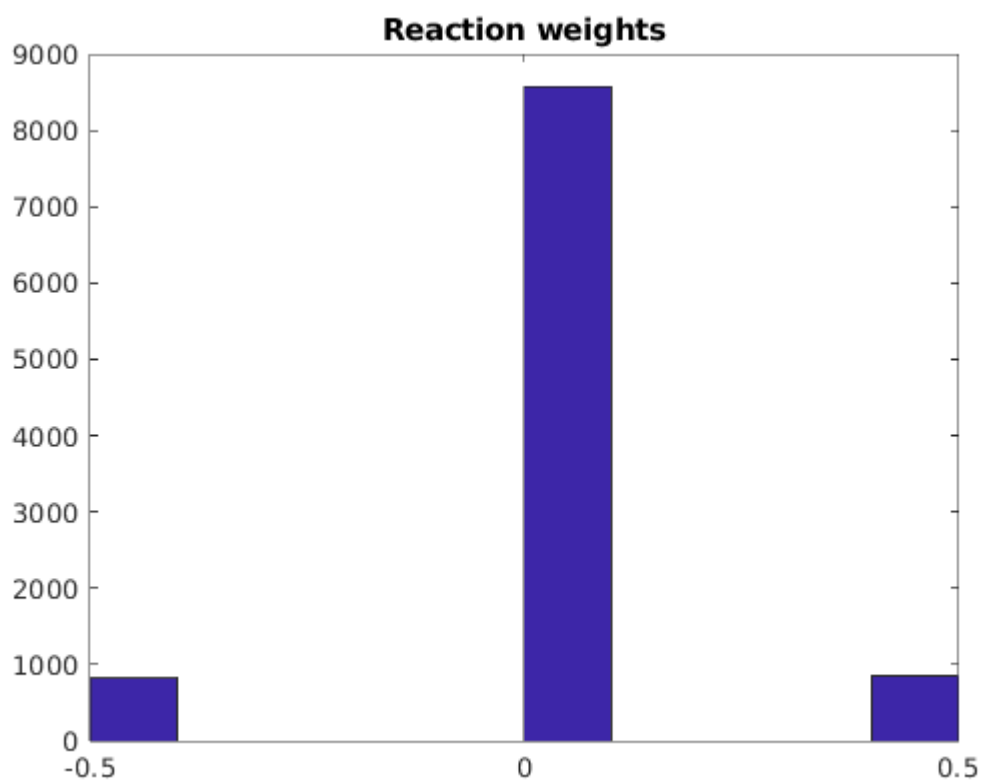
--- thermoKernel END ----

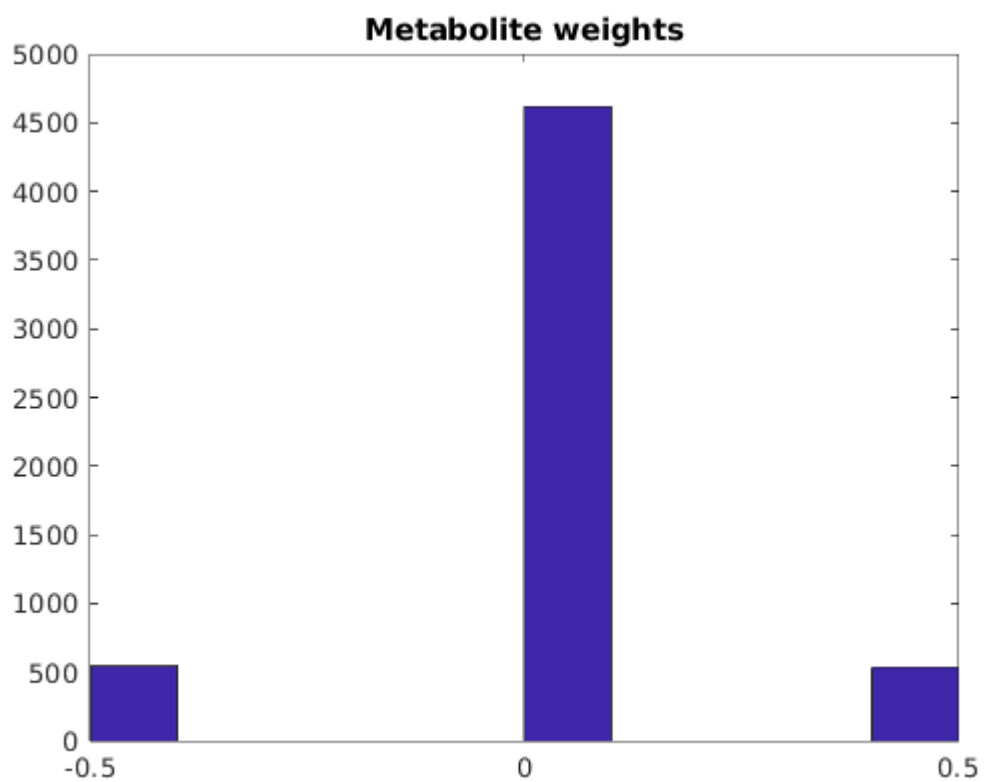
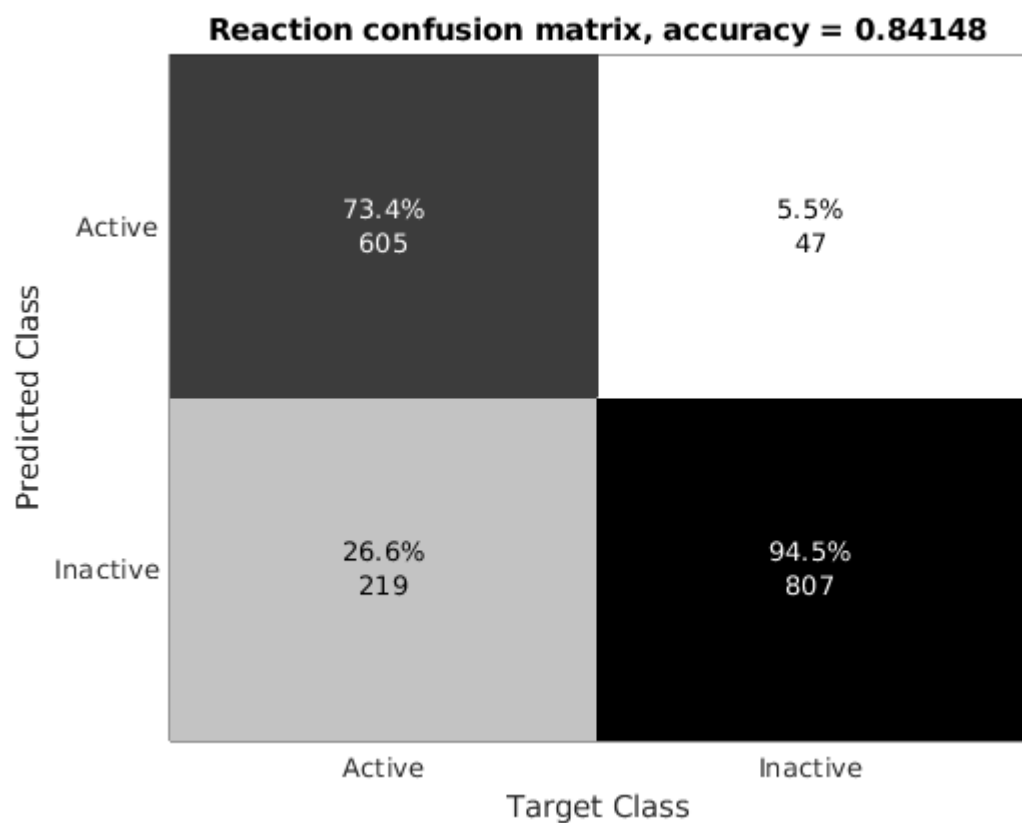
```
[nMet,nRxn]=size(tissueModel.S)
```


nMet = 2203
nRxn = 2986

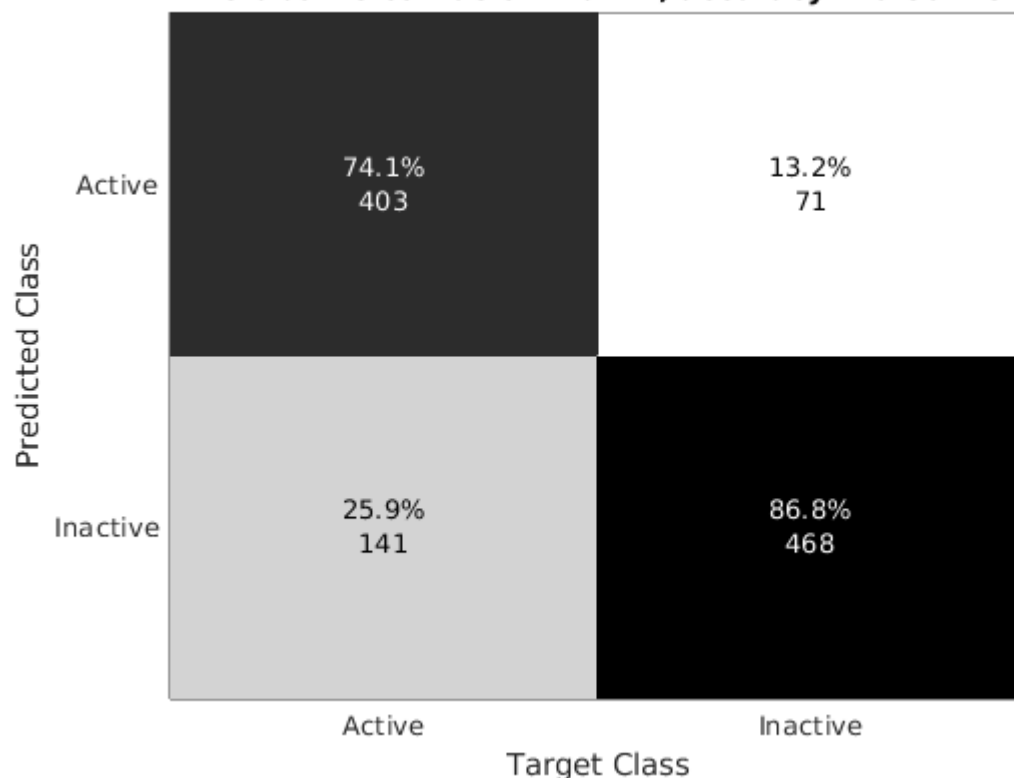
Compare the target versus predicted model

```
%plotThermoCoreStats(activeInactiveRxn, presentAbsentMet,  
thermoModelMetBool, thermoModelRxnBool);  
plotThermoKernelExtractStats(stoichFluxThermoConsistModel,  
activeInactiveRxn, rxnWeights, presentAbsentMet, metWeights,  
thermoModelMetBool, thermoModelRxnBool)
```





Metabolite confusion matrix, accuracy = 0.80425



Save weights

```
rxnWeightsTmp=rxnWeights;
metWeightsTmp=metWeights;
```

Submodel with just metabolites specified

```
metWeights=metWeightsTmp;
rxnWeights(:)=0;
[tissueModel, thermoModelMetBool, thermoModelRxnBool] =
thermoKernel(stoichFluxThermoConsistModel, activeInactiveRxn, rxnWeights,
presentAbsentMet, metWeights,param);
```

```
--- thermoKernel START ---
thermoKernel parameters:
    printLevel: 1
    relaxBounds: 0
    acceptRepairedFlux: 1
                    n: 200
    normalizeZeroNormWeights: 0
    formulation: 'pqzwr's'
    epsilon: 1.0000e-06
    removeOrphanGenes: 1
    nbMaxIteration: 30
    nMax: 20
    iterationMethod: 'greedyRandom'

    warmStartMethod: 'random'
    formulation: 'pqzwr's'
```

```

thetaMultiplier: 1.5000
    theta: 0.5000
regularizeOuter: 1
    epsilon: 1.0000e-06
    printLevel: 1
    relaxBounds: 0
acceptRepairedFlux: 1
thermoConsistencyMethod: 'cycleFreeFlux'
    bigNum: 10000
    debug: 0

optCardThermo objective data:
    1 = beta, the global weight on one-norm of internal reaction rate.
    0 = min(g0), the local weight on zero-norm of internal reaction rate.
    0 = max(g0), the local weight on zero-norm of internal reaction rate.
    -0.5 = min(h0), the local weight on zero-norm of metabolite production rate.
    0.5 = max(h0), the local weight on zero-norm of metabolite production rate.

optimizeCardinality objective data:

539 min cardinality variables:
    0 mean(c(p))          0 min(c(p))          0 max(c(p))
    1 lambda0             0.4 min(k)             0.5 max(k)
    0 lambda1             0 min(o(p))            0 max(o(p))

1088 max cardinality variables:
    0 mean(c(q))          0 min(c(q))          0 max(c(q))
    1 delta0             0.4 min(d)             0.5 max(d)
    0 delta1             0 min(o(q))            0 max(o(q))

36920 cardinality free variables:
    0.46 mean(c(r))       -0 min(c(r))          1 max(c(r))
    0 alpha1             0 min(o(r))            0 max(o(r))

itn   theta   ||dx||   del_obj   obj   linear   ||x||0   a(x)   ||x||1   ||y||
1     0.50   9.6648e+05 -8.4e+07   7.9     10     2.08529   0.087   0     -7.858
2     0.75   2.4394    -0.69     7.2     9.4     1.67053   0.13    0     -8.287
3     1.12   1.334     -0.47     6.7     9.3     1.23553   0.24    0     -8.287
4     1.69   3.7656    -1        5.7     12      1.23553   0.36    0     -8.287
5     2.53   3.2162    -1.7      4       11      1.23553   0.45    0     -8.737
6     3.80   2.1001    -1.8      2.1     11      1.23553   0.47    0    -10.00
7     5.70   1.3982    -1.2      0.95    10      1.23553   0.51    0    -10.00
8     8.54   0.78275   -1.5     -0.51   9.8     0.832228   0.5     0     -12.
9    12.81   0.52353   -1.8     -2.3    9.5     0.832228   0.55    0     -12.
10   19.22   0.37265   -0.29    -2.6    9.1     0.832228   0.62    0     -12.
11   28.83   0.33297   -0.11    -2.7    8.9     0.832228   0.73    0     -12.
12   43.25   0.19468   -0.5     -3.2    8.7     0.832228   0.83    0    -13.21
13   64.87   0.099656  -0.91    -4.1    8.7     0.832228   0.83    0    -15.03
14   97.31   0.11652   -1.5     -5.6    8.6     0.832228   0.83    0    -15.03
15  145.96   0.12539   -0.03    -5.6    8.6     0.832228   0.83    0    -15.03
16  218.95   0.067216  -0.018   -5.6    8.6     0.832228   0.83    0    -15.03
17  328.42   0.13964   -0.012   -5.6    8.6     0.832228   0.83    0    -15.03
itn   theta   ||dx||   del_obj   obj   linear   ||x||0   a(x)   ||x||1   ||y||
Optimise cardinality reached the stopping criterion. Finished.
100.00% thermodynamically feasible internal fluxes (checked by cycleFreeFlux method).
    warmStartMethod: 'random'
    formulation: 'pqzwrS'
    thetaMultiplier: 1.5000
    theta: 0.5000
regularizeOuter: 1
    epsilon: 1.0000e-06
    printLevel: 1
    relaxBounds: 0
acceptRepairedFlux: 1

```

```

thermoConsistencyMethod: 'cycleFreeFlux'
    bigNum: 10000
    debug: 0

optCardThermo objective data:
    1 = beta, the global weight on one-norm of internal reaction rate.
    0 = min(g0), the local weight on zero-norm of internal reaction rate.
    0 = max(g0), the local weight on zero-norm of internal reaction rate.
    -0.5 = min(h0), the local weight on zero-norm of metabolite production rate.
    0.5 = max(h0), the local weight on zero-norm of metabolite production rate.

optimizeCardinality objective data:

539 min cardinality variables:
    0 mean(c(p))          0 min(c(p))          0 max(c(p))
    1 lambda0             0.4 min(k)             0.5 max(k)
    0 lambda1             0 min(o(p))             0 max(o(p))

1088 max cardinality variables:
    0 mean(c(q))          0 min(c(q))          0 max(c(q))
    1 delta0             0.4 min(d)             0.5 max(d)
    0 delta1             0 min(o(q))             0 max(o(q))

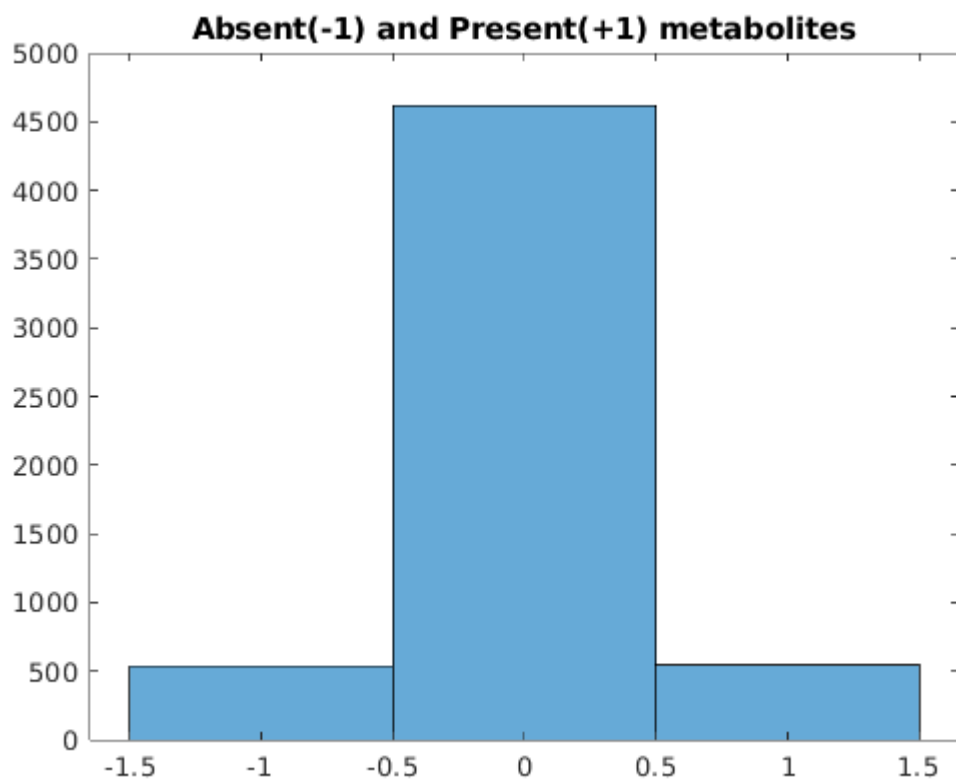
36920 cardinality free variables:
    0.46 mean(c(r))      -0 min(c(r))          1 max(c(r))
    0 alpha1            0 min(o(r))          0 max(o(r))

itn      theta      ||dx||      del_obj      obj      linear      ||x||0      a(x)      ||x||1      ||y||
  1      0.50      9.7116e+05      -8.5e+07      7.9          10      2.08529      0.079      0      -7.121
  2      0.75      2.4188      -0.68      7.2          9.5      1.23553      0.11      0      -7.551
  3      1.12      2.6941      -0.72      6.5          10      1.23553      0.24      0      -8.353
  4      1.69      4.9777      -0.99      5.5          11      1.23553      0.36      0      -8.353
  5      2.53      4.4276      -1.7      3.8          11      1.23553      0.45      0      -8.802
  6      3.80      2.3513      -2.2      1.6          11      1.23553      0.47      0      -10.52
  7      5.70      1.6188      -1.2      0.4          10      1.23553      0.51      0      -10.52
  8      8.54      0.63996      -0.59      -0.19      9.6      1.23553      0.56      0      -10.52
  9      12.81      0.55001      -0.9      -1.1      9.4      0.832228      0.55      0      -12.35
 10      19.22      0.4508      -1.5      -2.6      9.1      0.832228      0.62      0      -12.35
 11      28.83      0.42169      -0.11      -2.7      8.9      0.832228      0.73      0      -12.35
 12      43.25      0.24485      -0.032      -2.8      8.7      0.832228      0.83      0      -12.35
 13      64.87      0.19244      -0.075      -2.9      8.7      0.832228      0.83      0      -12.35
 14      97.31      0.10717      -0.042      -2.9      8.6      0.832228      0.83      0      -12.35
 15      145.96      0.083129      -0.023      -2.9      8.6      0.832228      0.83      0      -12.35
 16      218.95      0.070749      -0.015      -2.9      8.6      0.832228      0.83      0      -12.35
 17      328.42      0.14835      -0.0098      -2.9      8.6      0.832228      0.83      0      -12.35
itn      theta      ||dx||      del_obj      obj      linear      ||x||0      a(x)      ||x||1      ||y||
Optimise cardinality reached the stopping criterion. Finished.
100.00% thermodynamically feasible internal fluxes (checked by cycleFreeFlux method).
iter.  nz.flux.%it.feas.int.flux.  %feas.inc.flux.  nz.prod.%it.feas.nz.prod.  %feas.inc.prod.  fc
  1      137      1.00      NaN      95      1.21      0.03      gre
  2      186      1.00      NaN      139      1.17      0.08      gre
  3      297      1.00      NaN      226      1.19      0.20      gre
  4      467      1.00      NaN      349      1.30      0.37      gre
  5      203      1.00      NaN      149      1.23      0.43      gre
  6      282      1.00      NaN      213      1.24      0.51      gre
  7      285      1.00      NaN      201      1.32      0.56      gre
  8      213      1.00      NaN      156      1.30      0.60      gre
  9      168      1.00      NaN      124      1.27      0.62      gre
 10      132      1.00      NaN      97      1.20      0.63      gre
 11      248      1.00      NaN      184      1.33      0.66      gre
 12      111      1.00      NaN      78      1.22      0.66      gre
 13      200      1.00      NaN      148      1.36      0.68      gre
 14      112      1.00      NaN      77      1.25      0.68      gre
 15      984      1.00      NaN      709      1.26      0.70

```

16	1076	1.00	NaN	789	1.24	0.74
17	1024	1.00	NaN	744	1.27	0.74
18	1000	1.00	NaN	726	1.26	0.75
19	974	1.00	NaN	732	1.22	0.75
20	965	1.00	NaN	718	1.24	0.76

iter. nz.flux.%it.feas.int.flux. %feas.inc.flux. nz.prod. %it.feas.nz.prod. %feas.inc.prod. fo
 thermoKernel terminating early: n = nMax = 20



Metabolite confusion matrix, accuracy = 0.82548



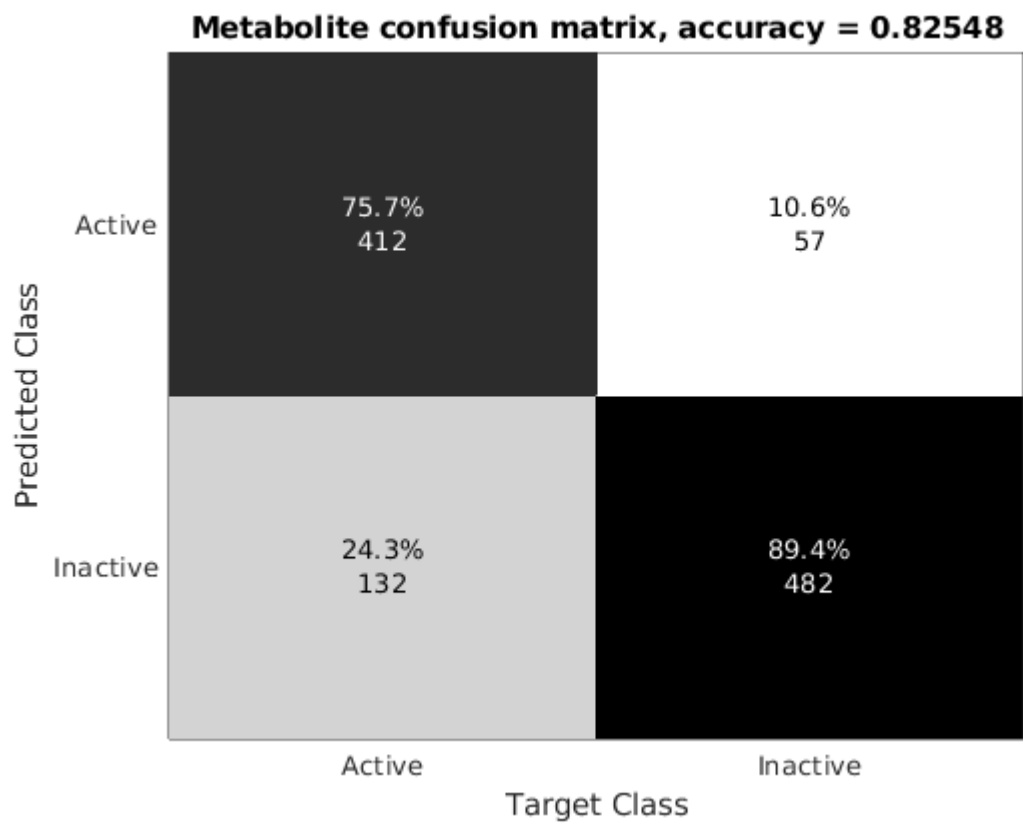
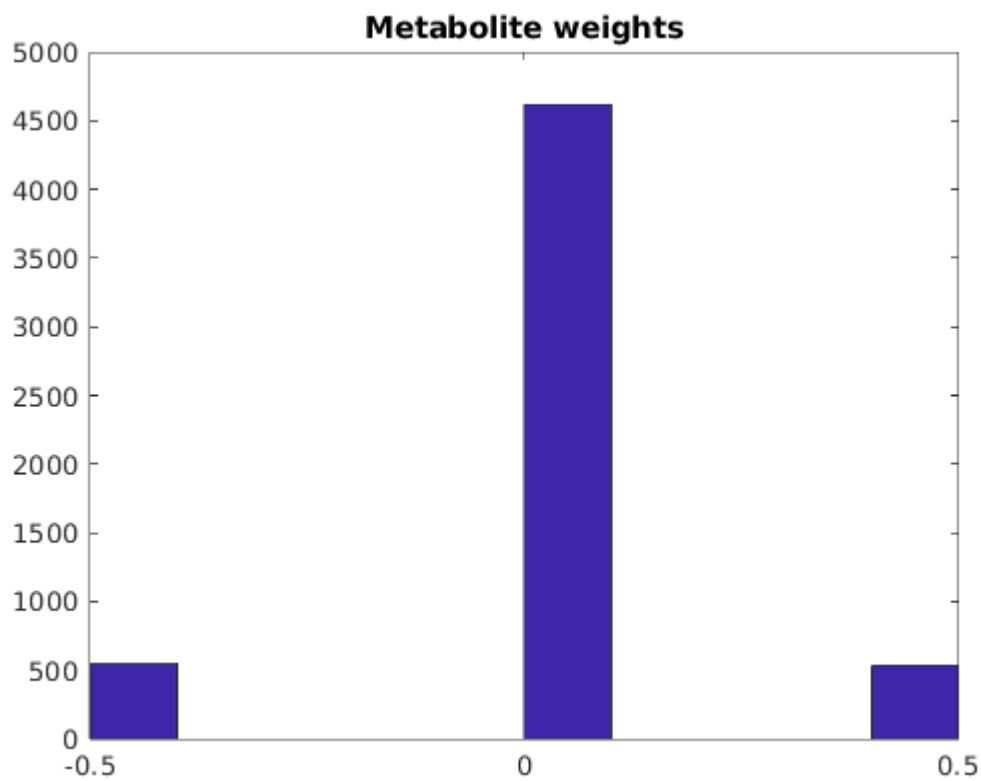
--- thermoKernel END ----

```
[nMet,nRxn]=size(tissueModel.S)
```

```
nMet = 1870
nRxn = 2635
```

Compare the target versus predicted model

```
plotThermoKernelExtractStats(stoichFluxThermoConsistModel,
activeInactiveRxn, rxnWeights, presentAbsentMet, metWeights,
thermoModelMetBool, thermoModelRxnBool)
```



Submodel with just reactions specified

```
rxnWeights=rxnWeightsTmp;
```



```
metWeights(:)=0;
[tissueModel, thermoModelMetBool, thermoModelRxnBool] =
thermoKernel(stoichFluxThermoConsistModel, activeInactiveRxn, rxnWeights,
presentAbsentMet, metWeights,param);
```

--- thermoKernel START ----

thermoKernel parameters:

```
    printLevel: 1
    relaxBounds: 0
    acceptRepairedFlux: 1
        n: 200
normalizeZeroNormWeights: 0
    formulation: 'pqzwrs'
    epsilon: 1.0000e-06
    removeOrphanGenes: 1
    nbMaxIteration: 30
        nMax: 20
    iterationMethod: 'greedyRandom'

    warmStartMethod: 'random'
        formulation: 'pqzwrs'
    thetaMultiplier: 1.5000
        theta: 0.5000
    regularizeOuter: 1
        epsilon: 1.0000e-06
        printLevel: 1
        relaxBounds: 0
    acceptRepairedFlux: 1
    thermoConsistencyMethod: 'cycleFreeFlux'
        bigNum: 10000
        debug: 0
```

optCardThermo objective data:

```
1 = beta, the global weight on one-norm of internal reaction rate.
-0.5 = min(g0), the local weight on zero-norm of internal reaction rate.
0.5 = max(g0), the local weight on zero-norm of internal reaction rate.
0 = min(h0), the local weight on zero-norm of metabolite production rate.
0 = max(h0), the local weight on zero-norm of metabolite production rate.
```

optimizeCardinality objective data:

854 min cardinality variables:

```
-0 mean(c(p))          -0 min(c(p))          -0 max(c(p))
1 lambda0              0.4 min(k)              0.5 max(k)
0 lambda1              0 min(o(p))              0 max(o(p))
```

824 max cardinality variables:

```
-0 mean(c(q))          -0 min(c(q))          -0 max(c(q))
1 delta0              0.4 min(d)              0.5 max(d)
0 delta1              0 min(o(q))              0 max(o(q))
```

36869 cardinality free variables:

```
0.46 mean(c(r))          -0 min(c(r))          1 max(c(r))
0 alpha1              0 min(o(r))              0 max(o(r))
```

itn	theta	dx	del_obj	obj	linear	x 0	a(x)	x 1	y
1	0.50	9.6945e+05	-8.5e+07	8.4	8.4	0.408362	0.02	0	-3.084
2	0.75	0.082294	-0.032	8.4	8.4	0.408362	0.028	0	-3.506
3	1.12	0.25722	-0.046	8.3	8.5	0.408362	0.03	0	-3.506
4	1.69	0.41187	-0.093	8.2	8.5	0.422161	0.0076	0	-3.506
5	2.53	5.4552e-14	-0.15	8.1	8.5	0.422161	0.011	0	-3.506
itn	theta	dx	del_obj	obj	linear	x 0	a(x)	x 1	y

Optimise cardinality reached the stopping criterion. Finished.

100.00% thermodynamically feasible internal fluxes (checked by cycleFreeFlux method).

```
warmStartMethod: 'random'
formulation: 'pqzwrS'
thetaMultiplier: 1.5000
theta: 0.5000
regularizeOuter: 1
epsilon: 1.0000e-06
printLevel: 1
relaxBounds: 0
acceptRepairedFlux: 1
thermoConsistencyMethod: 'cycleFreeFlux'
bigNum: 10000
debug: 0
```

optCardThermo objective data:

```
1 = beta, the global weight on one-norm of internal reaction rate.
-0.5 = min(g0), the local weight on zero-norm of internal reaction rate.
0.5 = max(g0), the local weight on zero-norm of internal reaction rate.
0 = min(h0), the local weight on zero-norm of metabolite production rate.
0 = max(h0), the local weight on zero-norm of metabolite production rate.
```

optimizeCardinality objective data:

854 min cardinality variables:

```
-0 mean(c(p))          -0 min(c(p))          -0 max(c(p))
1 lambda0              0.4 min(k)              0.5 max(k)
0 lambda1              0 min(o(p))              0 max(o(p))
```

824 max cardinality variables:

```
-0 mean(c(q))          -0 min(c(q))          -0 max(c(q))
1 delta0              0.4 min(d)              0.5 max(d)
0 delta1              0 min(o(q))              0 max(o(q))
```

36869 cardinality free variables:

```
0.46 mean(c(r))        -0 min(c(r))          1 max(c(r))
0 alpha1              0 min(o(r))          0 max(o(r))
```

itn	theta	dx	del_obj	obj	linear	x 0	a(x)	x 1	y 1
1	0.50	9.6798e+05	-8.5e+07	8.4	8.4	0.830523	0.02	0	-3.506
2	0.75	0.11192	-0.032	8.4	8.4	0.408362	0.028	0	-3.506
3	1.12	0.25722	-0.046	8.3	8.5	0.408362	0.03	0	-3.506
4	1.69	0.41187	-0.093	8.2	8.5	0.422161	0.0076	0	-3.506
5	2.53	5.4552e-14	-0.15	8.1	8.5	0.422161	0.011	0	-3.506
itn	theta	dx	del_obj	obj	linear	x 0	a(x)	x 1	y 1

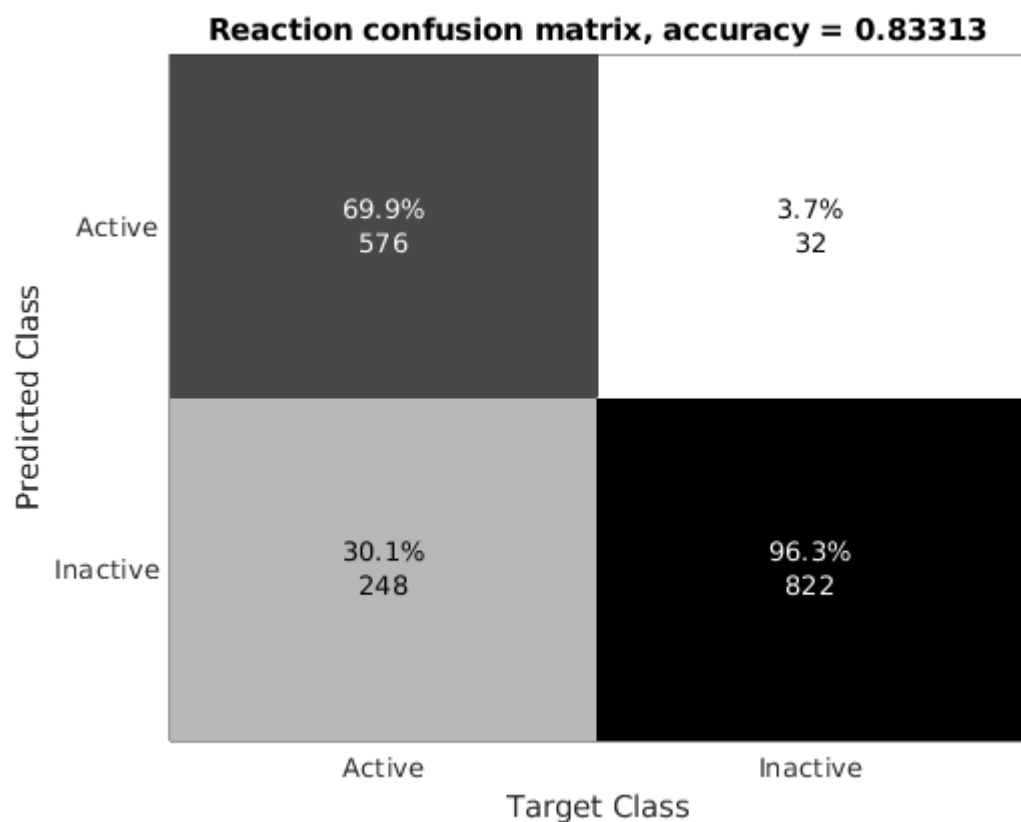
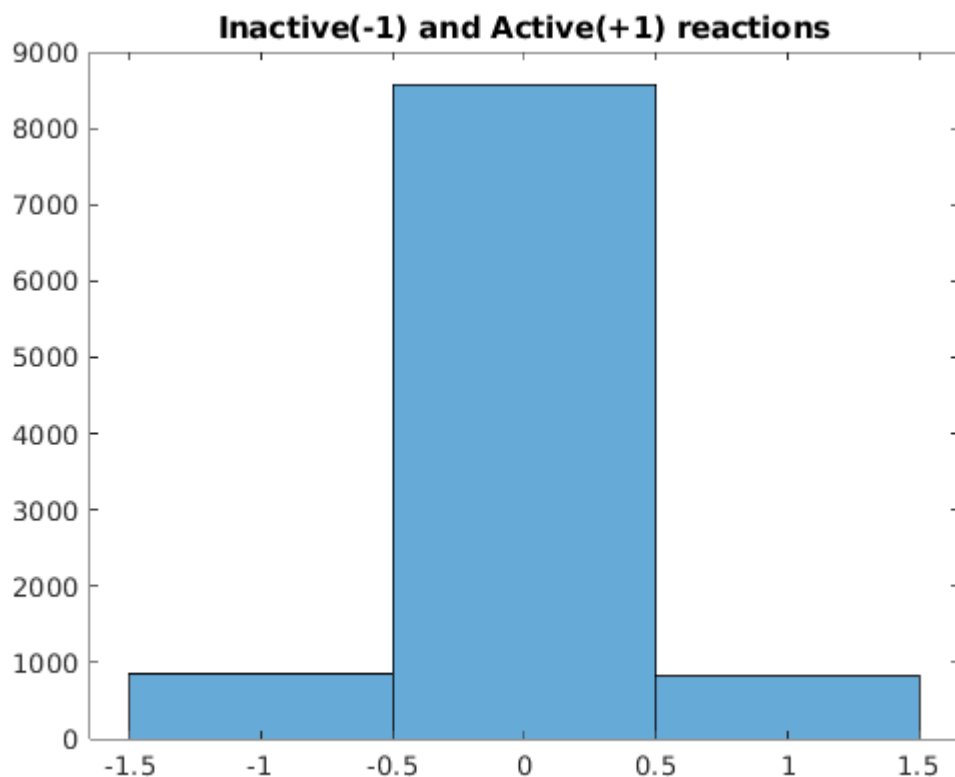
Optimise cardinality reached the stopping criterion. Finished.

100.00% thermodynamically feasible internal fluxes (checked by cycleFreeFlux method).

iter.	nz.flux.	%it.feas.int.flux.	%feas.inc.flux.	nz.prod.	%it.feas.nz.prod.	%feas.inc.prod.	fo
1	100	1.00	0.01	72	1.15	NaN	gre
2	99	1.00	0.01	70	1.21	NaN	gre
3	113	1.00	0.02	79	1.15	NaN	gre
4	113	1.00	0.03	83	1.12	NaN	gre
5	181	1.00	0.07	134	1.14	NaN	gre
6	240	1.00	0.14	183	1.14	NaN	gre
7	192	1.00	0.20	128	1.38	NaN	gre
8	184	1.00	0.24	130	1.31	NaN	gre
9	276	1.00	0.30	192	1.38	NaN	gre
10	267	1.00	0.35	193	1.28	NaN	gre
11	309	1.00	0.42	227	1.29	NaN	gre
12	293	1.00	0.49	209	1.44	NaN	gre
13	295	1.00	0.54	205	1.39	NaN	gre
14	214	1.00	0.57	173	1.25	NaN	gre
15	340	1.00	0.62	249	1.37	NaN	gre
16	284	1.00	0.66	203	1.37	NaN	gre
17	177	1.00	0.67	122	1.42	NaN	gre

18	116	1.00	0.67	87	1.20	NaN	gre
19	147	1.00	0.68	101	1.40	NaN	gre
20	199	1.00	0.70	139	1.42	NaN	gre

iter. nz.flux.%it.feas.int.flux. %feas.inc.flux. nz.prod. %it.feas.nz.prod. %feas.inc.prod. fc
 thermoKernel terminating early: n = nMax = 20



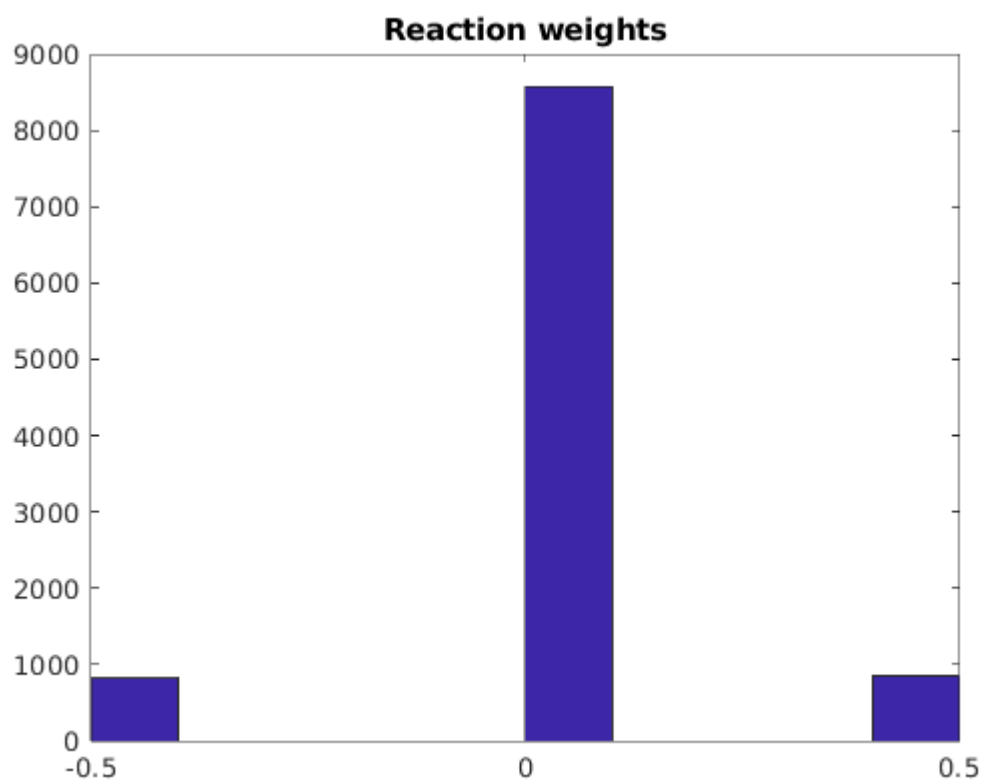
```
--- thermoKernel END ----
```

```
[nMet,nRxn]=size(tissueModel.S)
```

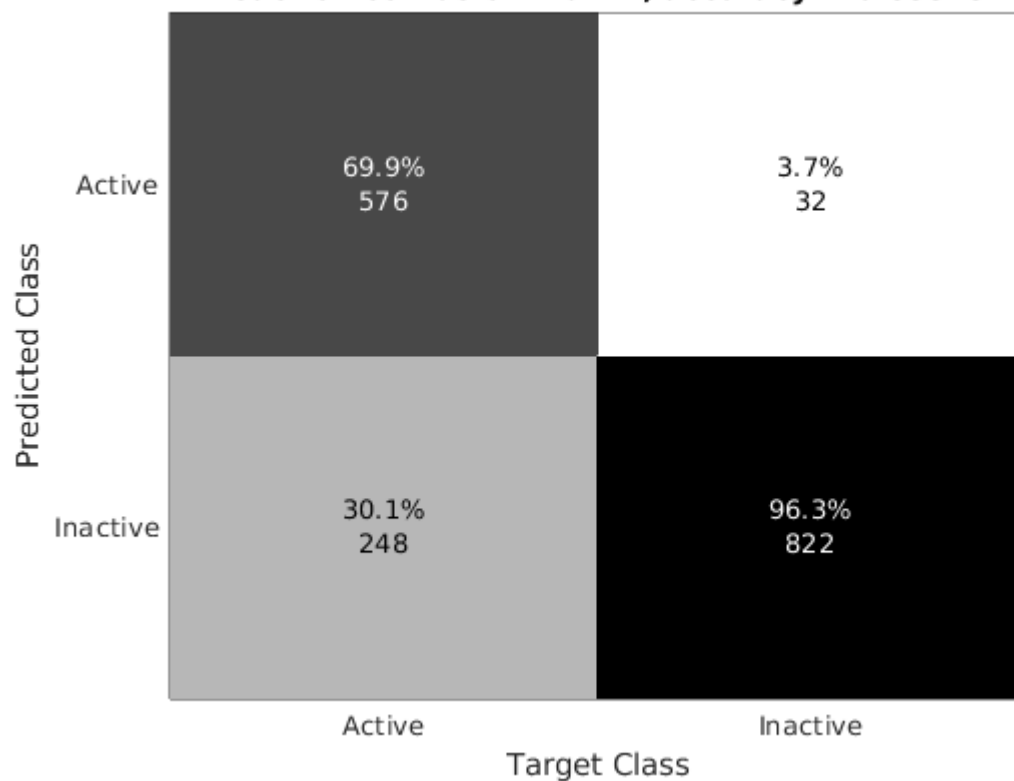
```
nMet = 1441  
nRxn = 1924
```

Compare the target versus predicted model

```
plotThermoKernelExtractStats(stoichFluxThermoConsistModel,  
activeInactiveRxn, rxnWeights, presentAbsentMet, metWeights,  
thermoModelMetBool, thermoModelRxnBool)
```



Reaction confusion matrix, accuracy = 0.83313



Submodel with just active metabolites specified

```
metWeightsRed=metWeightsTmp;
rxnWeightsRed=rxnWeightsTmp*0;
metWeightsRed(metWeightsRed>=0)=0;
```

```
[tissueModel, thermoModelMetBool, thermoModelRxnBool] =
thermoKernel(stoichFluxThermoConsistModel, activeInactiveRxn, rxnWeightsRed,
presentAbsentMet, metWeightsRed,param);
```

```
--- thermoKernel START ---
thermoKernel parameters:
    printLevel: 1
    relaxBounds: 0
    acceptRepairedFlux: 1
                    n: 200
    normalizeZeroNormWeights: 0
        formulation: 'pqzwr's'
        epsilon: 1.0000e-06
    removeOrphanGenes: 1
        nbMaxIteration: 30
        nMax: 20
    iterationMethod: 'greedyRandom'

    warmStartMethod: 'random'
        formulation: 'pqzwr's'
    thetaMultiplier: 1.5000
```

```

        theta: 0.5000
    regularizeOuter: 1
        epsilon: 1.0000e-06
        printLevel: 1
        relaxBounds: 0
    acceptRepairedFlux: 1
    thermoConsistencyMethod: 'cycleFreeFlux'
        bigNum: 10000
        debug: 0

optCardThermo objective data:
    1 = beta, the global weight on one-norm of internal reaction rate.
    0 = min(g0), the local weight on zero-norm of internal reaction rate.
    0 = max(g0), the local weight on zero-norm of internal reaction rate.
    -0.5 = min(h0), the local weight on zero-norm of metabolite production rate.
    0 = max(h0), the local weight on zero-norm of metabolite production rate.

optimizeCardinality objective data:

0 min cardinality variables:
    NaN mean(c(p))          NaN min(c(p))          NaN max(c(p))
    1 lambda0              NaN min(k)              NaN max(k)
    0 lambda1              NaN min(o(p))            NaN max(o(p))

1088 max cardinality variables:
    0 mean(c(q))            0 min(c(q))            0 max(c(q))
    1 delta0                0.4 min(d)              0.5 max(d)
    0 delta1                0 min(o(q))            0 max(o(q))

37459 cardinality free variables:
    0.45 mean(c(r))         -0 min(c(r))         1 max(c(r))
    0 alpha1                0 min(o(r))         0 max(o(r))

itn    theta    ||dx||    del_obj    obj    linear    ||x||0    a(x)    ||x||1    ||y||
  1    0.50    9.6587e+05    -8.5e+07    7.4      13         0         0         0    -14.77
  2    0.75     5.8717     -2.6      4.8      14         0         0         0    -14.32
  3    1.12     3.0027     -2.1      2.7      13         0         0         0    -15.21
  4    1.69     5.6907     -2.2     0.55     13         0         0         0    -17.00
  5    2.53     5.2054     -4.5     -3.9     14         0         0         0    -20.17
  6    3.80     2.462      -3.4     -7.3     13         0         0         0    -21.59
  7    5.70     1.606      -2.7    -10      12         0         0         0    -22.5
  8    8.54     1.0881     -1.7    -12      11         0         0         0    -22.5
  9   12.81     0.80985    -0.89    -13      10         0         0         0    -22.5
 10   19.22     0.49523    -0.58    -13      9.4        0         0         0    -22.5
 11   28.83     0.38668    -0.36    -13       9         0         0         0    -22.5
 12   43.25     0.28276    -0.38    -14      8.8        0         0         0    -23.47
 13   64.87     0.21412    -0.94    -15      8.7        0         0         0    -23.47
 14   97.31     0.16629    -0.083   -15      8.6        0         0         0    -23.47
 15  145.96     0.084169   -0.26   -15      8.5        0         0         0    -25.28
 16  218.95     0.12117    -1.6   -17      8.5        0         0         0    -25.28
 17  328.42     0.16767    -0.14   -17      8.5        0         0         0    -25.74
itn    theta    ||dx||    del_obj    obj    linear    ||x||0    a(x)    ||x||1    ||y||
Optimise cardinality reached the stopping criterion. Finished.
100.00% thermodynamically feasible internal fluxes (checked by cycleFreeFlux method).
    warmStartMethod: 'random'
    formulation: 'pqzwrS'
    thetaMultiplier: 1.5000
        theta: 0.5000
    regularizeOuter: 1
        epsilon: 1.0000e-06
        printLevel: 1
        relaxBounds: 0
    acceptRepairedFlux: 1
    thermoConsistencyMethod: 'cycleFreeFlux'

```

```
bigNum: 10000
debug: 0
```

optCardThermo objective data:

```
1 = beta, the global weight on one-norm of internal reaction rate.
0 = min(g0), the local weight on zero-norm of internal reaction rate.
0 = max(g0), the local weight on zero-norm of internal reaction rate.
-0.5 = min(h0), the local weight on zero-norm of metabolite production rate.
0 = max(h0), the local weight on zero-norm of metabolite production rate.
```

optimizeCardinality objective data:

0 min cardinality variables:

```
NaN mean(c(p))      NaN min(c(p))      NaN max(c(p))
1 lambda0           NaN min(k)       NaN max(k)
0 lambda1           NaN min(o(p))    NaN max(o(p))
```

1088 max cardinality variables:

```
0 mean(c(q))      0 min(c(q))      0 max(c(q))
1 delta0          0.4 min(d)    0.5 max(d)
0 delta1          0 min(o(q))    0 max(o(q))
```

37459 cardinality free variables:

```
0.45 mean(c(r))    -0 min(c(r))      1 max(c(r))
0 alpha1           0 min(o(r))    0 max(o(r))
```

itn	theta	dx	del_obj	obj	linear	x 0	a(x)	x 1	y
1	0.50	9.6895e+05	-8.5e+07	8.1	9	0	0	0	-6.131
2	0.75	1.691	-0.42	7.7	8.8	0	0	0	-6.561
3	1.12	2.8196	-0.42	7.3	10	0	0	0	-6.561
4	1.69	3.3125	-0.91	6.4	11	0	0	0	-6.561
5	2.53	3.3113	-2.3	4.1	11	0	0	0	-7.845
6	3.80	1.408	-1	3	11	0	0	0	-8.276
7	5.70	1.4232	-1.5	1.5	10	0	0	0	-8.728
8	8.54	0.75486	-0.82	0.71	9.6	0	0	0	-9.635
9	12.81	0.5787	-1.1	-0.43	9.2	0	0	0	-9.635
10	19.22	0.45877	-0.29	-0.72	8.9	0	0	0	-9.635
11	28.83	0.19759	-0.19	-0.91	8.7	0	0	0	-9.635
12	43.25	0.17445	-0.12	-1	8.6	0	0	0	-9.635
13	64.87	0.1615	-0.44	-1.5	8.5	0	0	0	-11.45
14	97.31	0.14097	-1.5	-2.9	8.5	0	0	0	-11.45
15	145.96	0.12588	-0.026	-3	8.5	0	0	0	-11.45
16	218.95	0.086138	-0.015	-3	8.5	0	0	0	-11.45
17	328.42	0.074785	-0.01	-3	8.5	0	0	0	-11.45
itn	theta	dx	del_obj	obj	linear	x 0	a(x)	x 1	y

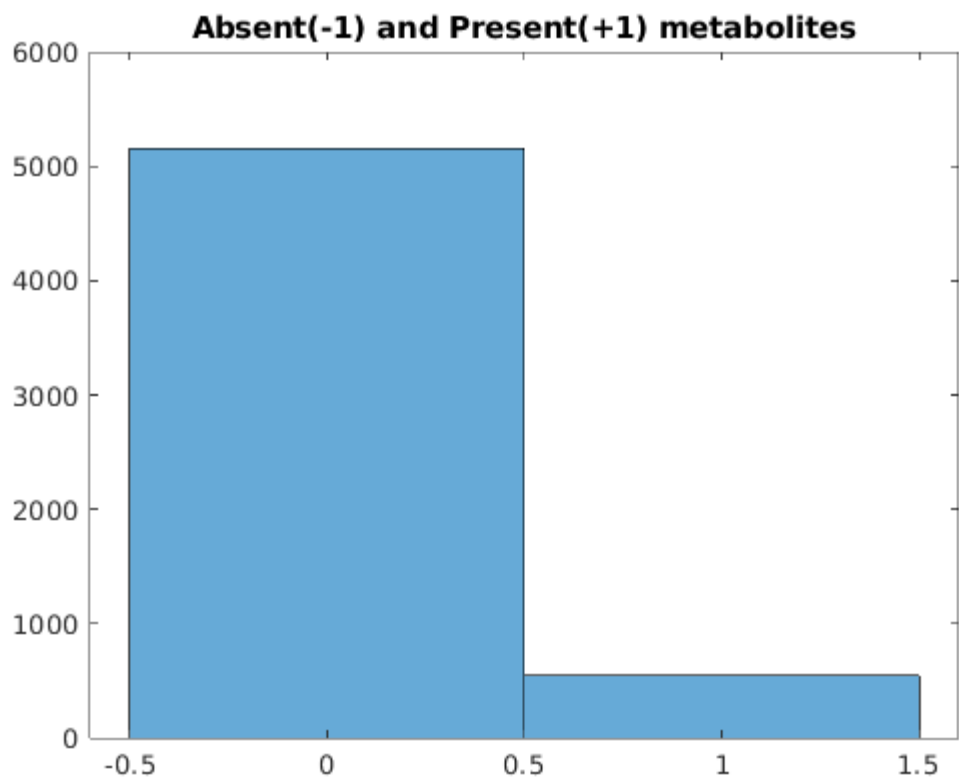
Optimise cardinality reached the stopping criterion. Finished.

100.00% thermodynamically feasible internal fluxes (checked by cycleFreeFlux method).

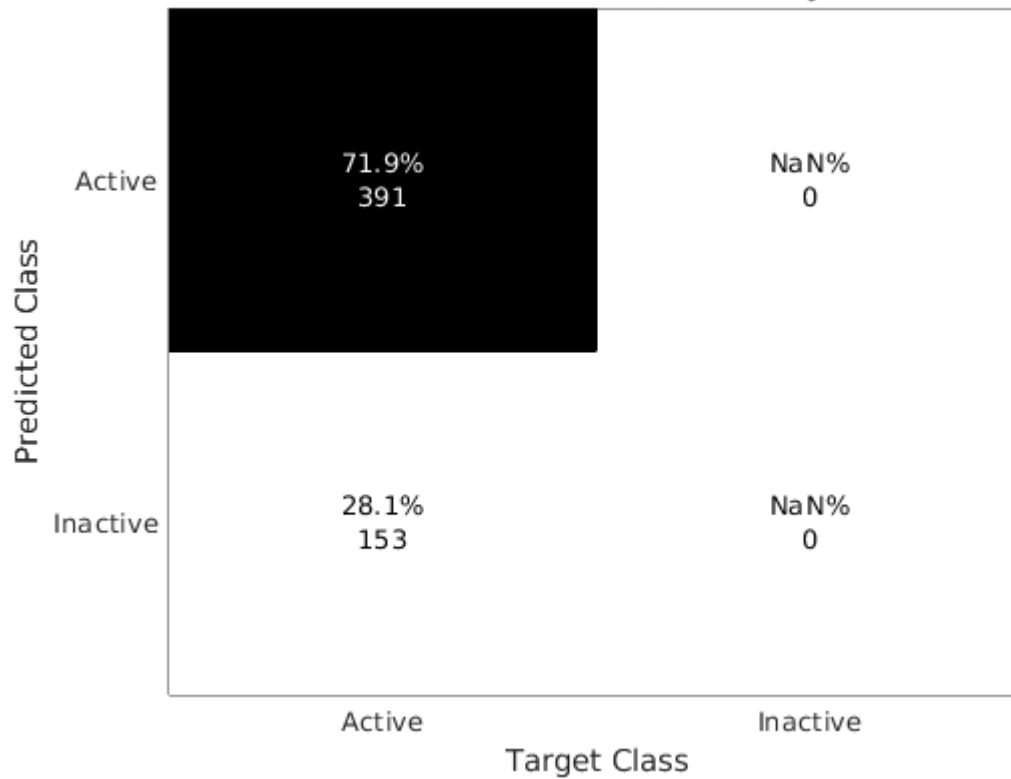
iter.	nz.flux.	%it.feas.int.flux.	%feas.inc.flux.	nz.prod.	%it.feas.nz.prod.	%feas.inc.prod.	fc
1	122	1.00	NaN	86	1.16	0.02	gre
2	230	1.00	NaN	172	1.16	0.10	gre
3	231	1.00	NaN	183	1.18	0.18	gre
4	352	1.00	NaN	263	1.22	0.31	gre
5	283	1.00	NaN	206	1.32	0.40	gre
6	274	1.00	NaN	199	1.37	0.47	gre
7	275	1.00	NaN	201	1.34	0.54	gre
8	175	1.00	NaN	139	1.19	0.56	gre
9	130	1.00	NaN	97	1.20	0.58	gre
10	307	1.00	NaN	235	1.34	0.62	gre
11	243	1.00	NaN	183	1.31	0.65	gre
12	120	1.00	NaN	84	1.29	0.65	gre
13	218	1.00	NaN	158	1.32	0.67	gre
14	113	1.00	NaN	80	1.24	0.67	gre
15	131	1.00	NaN	99	1.30	0.68	gre
16	129	1.00	NaN	92	1.30	0.69	gre

17	164	1.00	NaN	116	1.30	0.69	gre
18	166	1.00	NaN	123	1.26	0.70	gre
19	165	1.00	NaN	117	1.35	0.71	gre
20	141	1.00	NaN	95	1.36	0.72	gre

iter. nz.flux.%it.feas.int.flux. %feas.inc.flux. nz.prod. %it.feas.nz.prod. %feas.inc.prod. fo
 thermoKernel terminating early: n = nMax = 20



Metabolite confusion matrix, accuracy = 0.71875



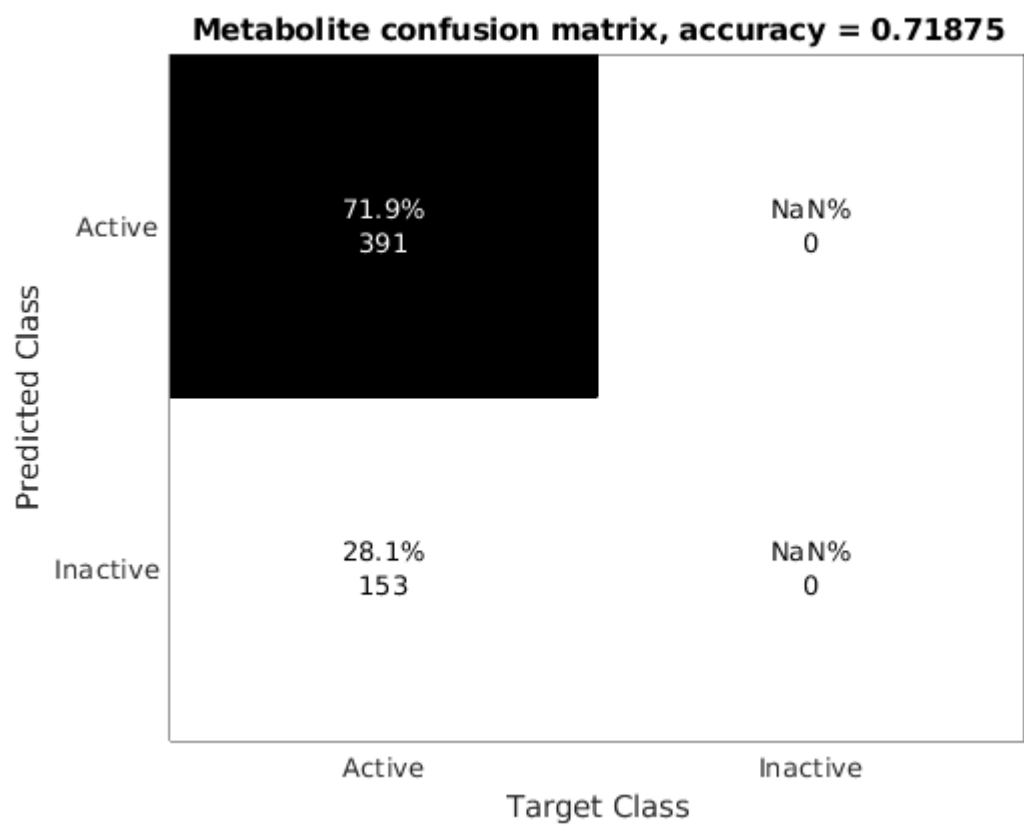
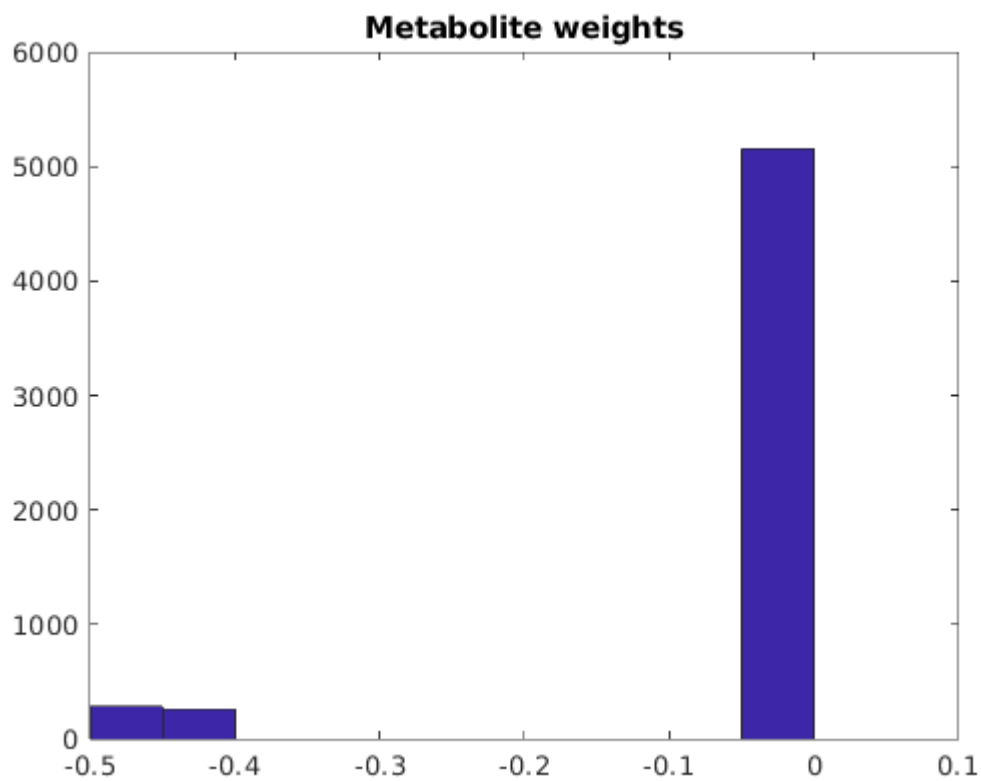
--- thermoKernel END ----

```
[nMet,nRxn]=size(tissueModel.S)
```

```
nMet = 1448
nRxn = 1753
```

Compare the target versus predicted model

```
plotThermoKernelExtractStats(stoichFluxThermoConsistModel,
activeInactiveRxn, rxnWeightsRed, presentAbsentMet, metWeightsRed,
thermoModelMetBool, thermoModelRxnBool)
```



Submodel with just active reactions specified

```
rxnWeightsRed=rxnWeightsTmp;
```

```

metWeightsRed=metWeightsTmp*0;
rxnWeightsRed(rxnWeightsRed>=0)=0;
[tissueModel, thermoModelMetBool, thermoModelRxnBool] =
thermoKernel(stoichFluxThermoConsistModel, activeInactiveRxn, rxnWeightsRed,
presentAbsentMet, metWeightsRed,param);

```

--- thermoKernel START ----

thermoKernel parameters:

```

    printLevel: 1
    relaxBounds: 0
    acceptRepairedFlux: 1
        n: 200
    normalizeZeroNormWeights: 0
        formulation: 'pqzwrS'
        epsilon: 1.0000e-06
    removeOrphanGenes: 1
        nbMaxIteration: 30
        nMax: 20
        iterationMethod: 'greedyRandom'

    warmStartMethod: 'random'
        formulation: 'pqzwrS'
    thetaMultiplier: 1.5000
        theta: 0.5000
    regularizeOuter: 1
        epsilon: 1.0000e-06
        printLevel: 1
        relaxBounds: 0
    acceptRepairedFlux: 1
    thermoConsistencyMethod: 'cycleFreeFlux'
        bigNum: 10000
        debug: 0

```

optCardThermo objective data:

```

1 = beta, the global weight on one-norm of internal reaction rate.
-0.5 = min(g0), the local weight on zero-norm of internal reaction rate.
0 = max(g0), the local weight on zero-norm of internal reaction rate.
-0 = min(h0), the local weight on zero-norm of metabolite production rate.
-0 = max(h0), the local weight on zero-norm of metabolite production rate.

```

optimizeCardinality objective data:

0 min cardinality variables:

NaN mean(c(p))	NaN min(c(p))	NaN max(c(p))
1 lambda0	NaN min(k)	NaN max(k)
0 lambda1	NaN min(o(p))	NaN max(o(p))

824 max cardinality variables:

-0 mean(c(q))	-0 min(c(q))	-0 max(c(q))
1 delta0	0.4 min(d)	0.5 max(d)
0 delta1	0 min(o(q))	0 max(o(q))

37723 cardinality free variables:

0.45 mean(c(r))	-0 min(c(r))	1 max(c(r))
0 alpha1	0 min(o(r))	0 max(o(r))

itn	theta	dx	del_obj	obj	linear	x 0	a(x)	x 1	y
1	0.50	9.6384e+05	-8.4e+07	8.4	8.5	0	0	0	-3.118
2	0.75	1.1692	-0.091	8.3	8.4	0	0	0	-3.548
3	1.12	0.15183	-0.062	8.3	8.4	0	0	0	-3.506
4	1.69	0.092443	-0.084	8.2	8.4	0	0	0	-3.506
5	2.53	0.44167	-0.14	8.1	8.5	0	0	0	-3.506
6	3.80	0.31473	-0.25	7.8	8.5	0	0	0	-3.956

itn	theta	dx	del_obj	obj	linear	x 0	a(x)	x 1	y
7	5.70	1.8987	-0.76	7	9.6	0	0	0	-4.903
8	8.54	1.0204	-1.2	5.8	9.4	0	0	0	-5.394
9	12.81	1.4536	-1.1	4.8	10	0	0	0	-5.832
10	19.22	0.67982	-0.85	3.9	9.8	0	0	0	-5.832
11	28.83	0.60377	-0.54	3.4	9.2	0	0	0	-5.832
12	43.25	0.45629	-0.35	3	8.9	0	0	0	-5.832
13	64.87	0.57354	-0.22	2.8	8.7	0	0	0	-5.832
14	97.31	0.4286	-0.13	2.7	8.5	0	0	0	-5.832
15	145.96	0.145	-0.036	2.7	8.5	0	0	0	-5.832
16	218.95	0.11648	-0.019	2.6	8.5	0	0	0	-5.832
17	328.42	0.083385	-0.012	2.6	8.5	0	0	0	-5.832

Optimise cardinality reached the stopping criterion. Finished.
100.00% thermodynamically feasible internal fluxes (checked by cycleFreeFlux method).

```

warmStartMethod: 'random'
formulation: 'pqzwrns'
thetaMultiplier: 1.5000
theta: 0.5000
regularizeOuter: 1
epsilon: 1.0000e-06
printLevel: 1
relaxBounds: 0
acceptRepairedFlux: 1
thermoConsistencyMethod: 'cycleFreeFlux'
bigNum: 10000
debug: 0

```

optCardThermo objective data:

- 1 = beta, the global weight on one-norm of internal reaction rate.
- 0.5 = min(g0), the local weight on zero-norm of internal reaction rate.
- 0 = max(g0), the local weight on zero-norm of internal reaction rate.
- 0 = min(h0), the local weight on zero-norm of metabolite production rate.
- 0 = max(h0), the local weight on zero-norm of metabolite production rate.

optimizeCardinality objective data:

0 min cardinality variables:

	NaN mean(c(p))	NaN min(c(p))	NaN max(c(p))
1 lambda0		NaN min(k)	NaN max(k)
0 lambda1		NaN min(o(p))	NaN max(o(p))

824 max cardinality variables:

	-0 mean(c(q))	-0 min(c(q))	-0 max(c(q))
1 delta0		0.4 min(d)	0.5 max(d)
0 delta1		0 min(o(q))	0 max(o(q))

37723 cardinality free variables:

	0.45 mean(c(r))	-0 min(c(r))	1 max(c(r))
0 alphas		0 min(o(r))	0 max(o(r))

itn	theta	dx	del_obj	obj	linear	x 0	a(x)	x 1	y
1	0.50	9.6834e+05	-8.4e+07	8.4	8.5	0	0	0	-3.540
2	0.75	1.251	-0.098	8.3	8.4	0	0	0	-3.970
3	1.12	0.091425	-0.056	8.3	8.4	0	0	0	-3.506
4	1.69	0.092443	-0.084	8.2	8.4	0	0	0	-3.506
5	2.53	0.44167	-0.14	8.1	8.5	0	0	0	-3.506
6	3.80	0.31473	-0.25	7.8	8.5	0	0	0	-3.956
7	5.70	1.8987	-0.76	7	9.6	0	0	0	-4.903
8	8.54	1.0204	-1.2	5.8	9.4	0	0	0	-5.394
9	12.81	1.4536	-1.1	4.8	10	0	0	0	-5.832
10	19.22	0.67982	-0.85	3.9	9.8	0	0	0	-5.832
11	28.83	0.60377	-0.54	3.4	9.2	0	0	0	-5.832
12	43.25	0.45629	-0.35	3	8.9	0	0	0	-5.832
13	64.87	0.57354	-0.22	2.8	8.7	0	0	0	-5.832

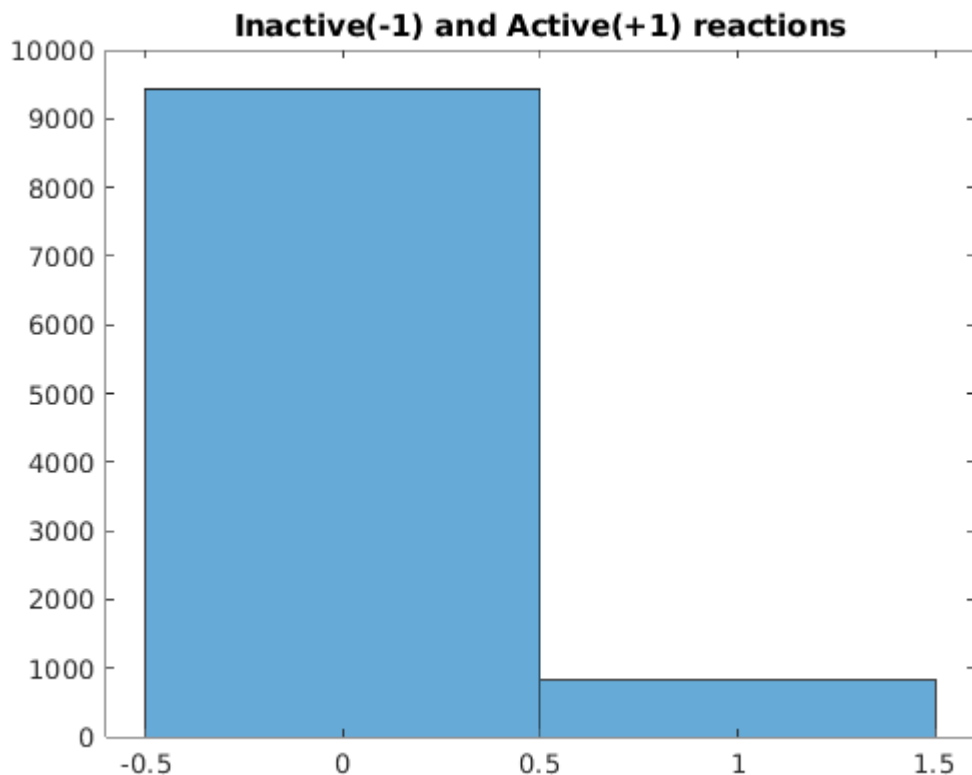
14	97.31	0.4286	-0.13	2.7	8.5	0	0	0	-5.832
15	145.96	0.145	-0.036	2.7	8.5	0	0	0	-5.832
16	218.95	0.11648	-0.019	2.6	8.5	0	0	0	-5.832
17	328.42	0.083385	-0.012	2.6	8.5	0	0	0	-5.832
itn	theta	dx	del_obj	obj	linear	x 0	a(x)	x 1	y

Optimise cardinality reached the stopping criterion. Finished.

100.00% thermodynamically feasible internal fluxes (checked by cycleFreeFlux method).

iter.	nz.flux.	%it.feas.	int.flux.	%feas.inc.flux.	nz.prod.	%it.feas.	nz.prod.	%feas.inc.prod.	fc
1	111	1.00	0.02	74	1.24	NaN	gre		
2	110	1.00	0.02	76	1.24	NaN	gre		
3	132	1.00	0.03	93	1.22	NaN	gre		
4	127	1.00	0.04	94	1.18	NaN	gre		
5	215	1.00	0.10	152	1.24	NaN	gre		
6	190	1.00	0.15	138	1.23	NaN	gre		
7	247	1.00	0.21	175	1.29	NaN	gre		
8	268	1.00	0.28	193	1.34	NaN	gre		
9	300	1.00	0.36	217	1.27	NaN	gre		
10	284	1.00	0.43	201	1.42	NaN	gre		
11	234	1.00	0.47	162	1.37	NaN	gre		
12	325	1.00	0.53	235	1.39	NaN	gre		
13	217	1.00	0.56	155	1.39	NaN	gre		
14	223	1.00	0.59	158	1.29	NaN	gre		
15	197	1.00	0.60	137	1.37	NaN	gre		
16	136	1.00	0.61	94	1.29	NaN	gre		
17	189	1.00	0.63	135	1.39	NaN	gre		
18	222	1.00	0.65	148	1.47	NaN	gre		
19	316	1.00	0.68	219	1.42	NaN	gre		
20	155	1.00	0.69	114	1.34	NaN	gre		

iter.	nz.flux.	%it.feas.	int.flux.	%feas.inc.flux.	nz.prod.	%it.feas.	nz.prod.	%feas.inc.prod.	fc
thermoKernel terminating early: n = nMax = 20									



Reaction confusion matrix, accuracy = 0.68811



--- thermoKernel END ----

```
[nMet,nRxn]=size(tissueModel.S)
```

```
nMet = 1449  
nRxn = 1915
```

Compare the target versus predicted model

```
plotThermoKernelExtractStats(stoichFluxThermoConsistModel,  
activeInactiveRxn, rxnWeightsRed, presentAbsentMet, metWeightsRed,  
thermoModelMetBool, thermoModelRxnBool)
```

