

Oh

Pauline

A thesis presented for the degree of
Bachelor of Science (Honours) (Physics)

School of Physics
Department of Science
The University of Sydney
Australia
February 19, 2026

Supervisor: Prof. Jane Professor

Co-Supervisor: Dr. Jack Supervisor

Co-Supervisor: Mr. June Supervisor

Tous les fichiers svg :

Dedication

For those who hate looking at a template with 500 lines of code and an extra 300 lines commented out.

Declaration

Acknowledgements

Contents

1 Introduction

1.1	Fermi gas preparation (+ Bose gas ?)	
1.1.1	TC	
1.1.2	Zeeman cooling	
1.1.3	Blue MOT	
1.1.3.1	The physics	
1.1.3.2	How to optimize the superposition with the repumper	
1.1.3.3	Comment on the hyperfine states (+boson 88)	
1.1.3.4	Optical setup (blue + repump)	
1.1.4	Repumper	
1.1.5	BB MOT	
1.1.5.1	First step	
1.1.5.2	Second step	
1.1.6	Stir	
1.1.7	Narrow MOT	
1.1.7.1	Optimization of the narrow MOT (intensity, frequency, effect on the size of the cloud)	
1.1.7.2	Optical setup	
1.1.8	ODT and evaporation	1
1.1.8.1	Charging the crossing	1
1.1.8.2	Optimization of the evaporation ramps : Dimple + reservoir, just reservoir, parameter to optimize (number of atoms, temperature)	1
1.1.8.3	Optical setup	1
1.1.9	Optical pumping	1
1.2	Spin measurement scheme	2

2 Ramsey interferometers on qudit 3

2.1	Preparation of arbitrary dimension Hilbert space	3
2.1.1	Raman process	3
2.1.1.1	$\delta m_F = \pm 1$	3
2.1.1.2	$\delta m_F = \pm 2$	3
2.1.2	Moglabs chain without cavity	3
2.1.3	Purification of the laser spectrum with a FP cavity	3
2.2	Interferometric sensing with multiple nuclear spin state	3
2.2.1	Driving long coherence time Rabi oscillations	3
2.2.1.1	Rabi oscillations	3

2.2.1.2	Interferometer of $su(2)$ symmetry	4
2.2.1.3	Discussion on inhomogeneities	4
2.2.2	Measuring two quantities at a time	4
2.2.2.1	Physical principle	4
2.2.2.2	Results	4
2.2.3	Measuring two non commuting observables	4
2.2.3.1	Principle	4
2.3	$SU(N)$ symmetry (ce qu'il faudrait pr la tester e.g densité gaz, alim- entation bobines -j, comment faire mieux que les chiffres actuels) . .	4
3	Engineering highly entangled system of photoassociated ^{87}Sr atoms	5
3.1	Introduction on photoassociation	5
3.1.1	Preamble on scattering theory	5
3.1.2	What is photoassociation	7
3.1.3	Molecular formalism/vocabulary (condon radius, optical length...) . .	8
3.1.4	External energy states	10
3.1.4.1	WKB approximation	11
3.1.4.2	11
3.1.5	Internal energy states	11
3.2	About photoassociation on other species	12
3.2.1	Mass scaling (^{88}Sr)	12
3.2.2	Ytterbium: hfs	13
3.3	Experimental setup	13
3.4	^{88}Sr Results	13
3.4.1	Technical issues of inhabitation of photoassociation	14
3.4.1.1	Laser width	14
3.5	^{87}Sr molecules	14
3.5.1	Physical sources of inhabitation of photoassociation	14
3.5.1.1	On $F = 9/2$: predissociation	14
3.5.1.2	Coupling to more energetic state from the IR	14
3.5.1.3	Node of wavefunction for some vibrational states	14
3.5.2	Energy landscape of ^{87}Sr - ^{87}Sr molecules	14
A	Algorithms	ii

List of Figures

1.1	Caption	
1.2	Caption	
1.3	Caption	
1.4	Caption	
1.5	Caption	
1.6	Caption	
1.7	Caption	
1.8	Caption	1
1.9	Caption	1
1.10	Caption	2
3.1	Caption	7
3.2	hund	9
3.3	u-g symmetry	10
3.4	Caption	11
3.5	Caption	12
3.6	Caption	13
3.7	Caption	14

List of Tables

Chapter 1

Introduction

1.1 Fermi gas preparation (+ Bose gas ?)

1.1.1 TC

Comment on increasing power in TC (thésard marc chesnais)

1.1.2 Zeeman cooling

1.1.3 Blue MOT

1.1.3.1 The physics

1.1.3.2 How to optimize the superposition with the repumper

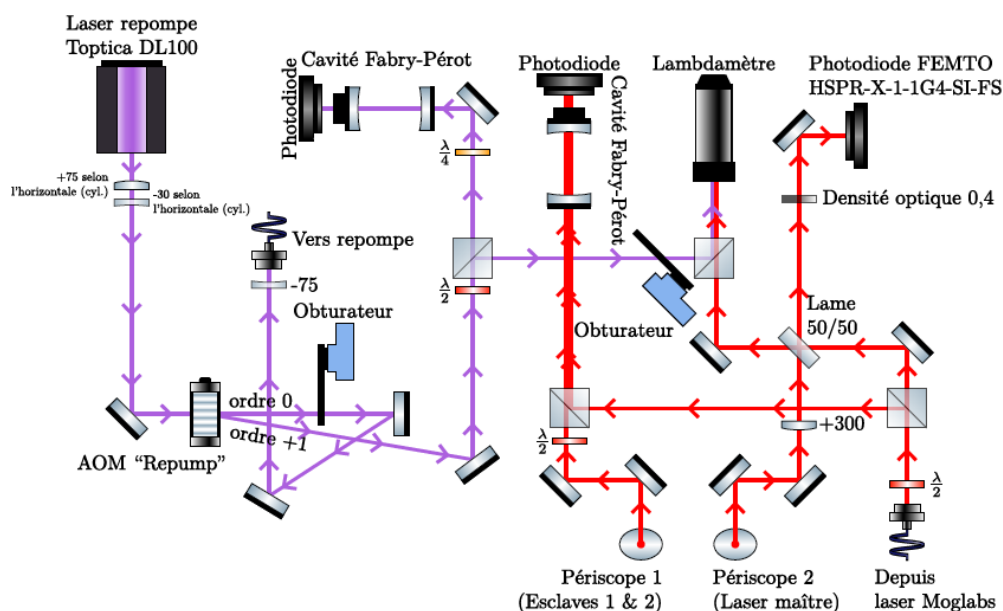


Figure 1.1: Caption

1.1.3.3 Comment on the hyperfine states (+boson 88)

1.1.3.4 Optical setup (blue + repump)

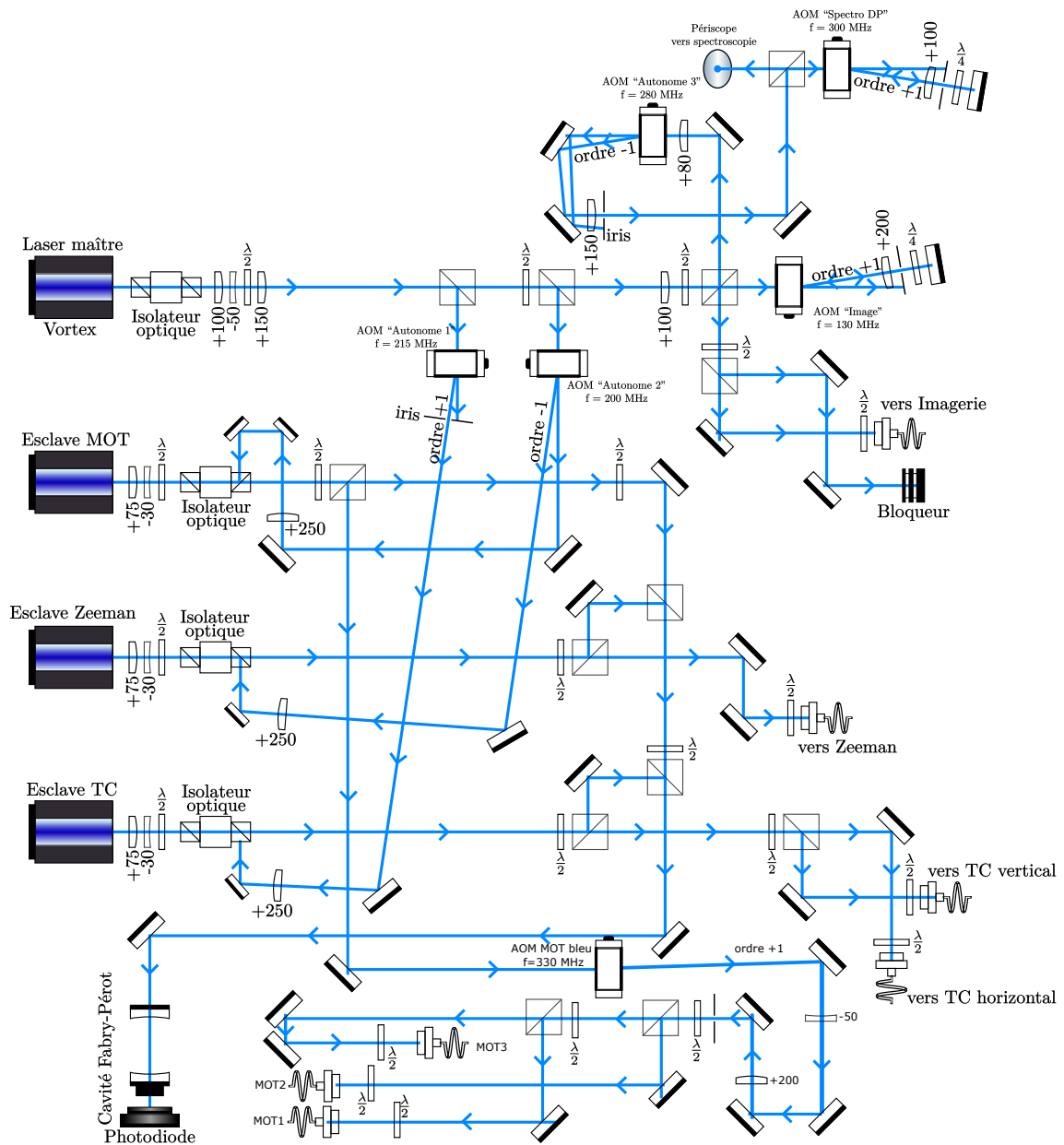


Figure 1.2: Caption

1.1.4 Repumper

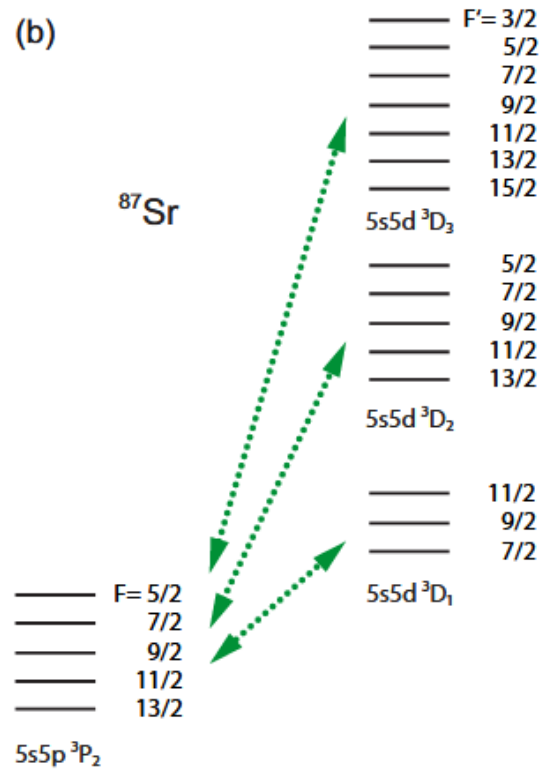


Figure 1.3: Caption

1.1.5 BB MOT

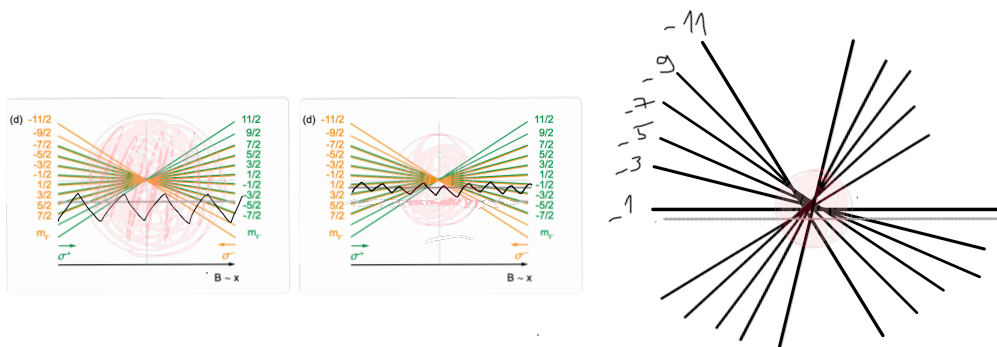


Figure 1.4: Caption

1.1.5.1 First step

1.1.5.2 Second step

1.1.6 Stir

Need a stir because :



Figure 1.5: Caption



Figure 1.6: Caption

1.1.7 Narrow MOT

cf p.43 S.Stellmer thesis

1.1.7.1 Optimization of the narrow MOT (intensity, frequency, effect on the size of the cloud)

Include images of the cloud for different I and detuning ?

1.1.7.2 Optical setup

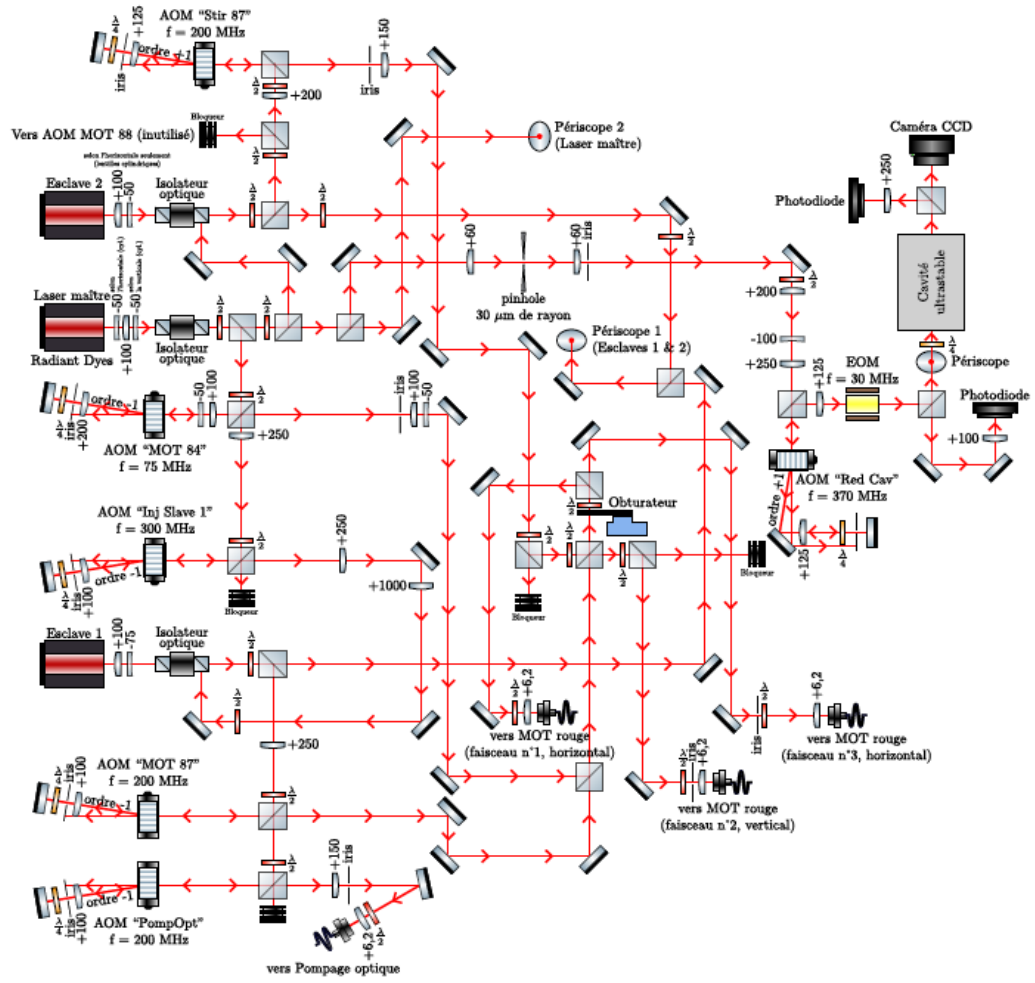


FIGURE 14 – Préparation des différents lasers rouges

Figure 1.7: Caption

1.1.8 ODT and evaporation

1.1.8.1 Charging the crossing



Figure 1.8: Caption

1.1.8.2 Optimization of the evaporation ramps : Dimple + reservoir, just reservoir, parameter to optimize (number of atoms, temperature)

Comment on the LS it does to each state

1.1.8.3 Optical setup

1.1.9 Optical pumping



Figure 1.9: Caption

1.2 Spin measurement scheme



Figure 1.10: Caption

Chapter 2

Ramsey interferometers on qudit

2.1 Preparation of arbitrary dimension Hilbert space

2.1.1 Raman process

2.1.1.1 $\delta m_F = \pm 1$

2.1.1.2 $\delta m_F = \pm 2$

2.1.2 Moglabs chain without cavity

2.1.3 Purification of the laser spectrum with a FP cavity

blablablagtg

2.2 Interferometric sensing with multiple nuclear spin state

2.2.1 Driving long coherence time Rabi oscillations

2.2.1.1 Rabi oscillations

Comment on what the FP could add as a longer coherence time of the qubit

2.2.1.2 Interferometer of $\text{su}(2)$ symmetry

2.2.1.3 Discussion on inhomogeneities

2.2.2 Measuring two quantities at a time

2.2.2.1 Physical principle

2.2.2.2 Results

2.2.3 Measuring two non commuting observables

2.2.3.1 Principle

2.3 $\text{SU}(N)$ symmetry (ce qu'il faudrait pr la tester
e.g densité gaz, alimentation bobines -; com-
ment faire mieux que les chiffres actuels)

Chapter 3

Engineering highly entangled system of photoassociated ^{87}Sr atoms

Engineering Dicke states

3.1 Introduction on photoassociation

3.1.1 Preamble on scattering theory

In a Born-Oppenheimer approximation the hamiltonian of a two-atom system is

$$\hat{V}_{BO} = -\frac{\hbar^2}{2\mu} \frac{d^2 u}{dr^2} + \left(\frac{\hbar^2 l(l+1)}{2\mu r^2} + V(r) \right) u(r) = E u(r) \quad (3.1)$$

$$V(r) = \frac{-C_n}{r^n}.$$

As in [1] we are going to change the basis of the solution with in different regions of the inter-atomic distance r . At long distance the kinetic energy of the atoms - first part of the hamiltonian - is dominant. For intermediate distances the force that counts is the van der Waals because the electronic shell start to overlap. At shorter distance it is the coulomb and van der Waals forces that are dominant.

The solution of the far distance potential is a superposition of incoming wave and a scattered one that acquire a phase δ_l

$$\psi(r) = \sin(kr - l\frac{\pi}{2}) + \tan(\delta_l) \cos(kr - l\frac{\pi}{2}) \quad (3.2)$$

at this position $r = a$ where the potential appears as a scattering boundary. This distance is called the scattering length. At low energies

Continuity of the wavefunction in every region should be respected. It gives

$$\tan(\delta_l) \propto k^{2l+1} \quad (3.3)$$

For s-waves, this express as

$$a = - \lim_{k \rightarrow 0} \tan(\delta_0)/k \quad (3.4)$$

A scattering cross section is usually defined from this physical quantity as the area of a disk with a radius equal to the scattering length, which gives the formula

$$\sigma = 4\pi a^2 \quad (3.5)$$

In ultracold gases, only s-wave atoms can collide because they do not have enough kinetic energy to pass the potential barrier of higher angular momentum states. It imposes that for fermions -by parity of the total wavefunction being antisymmetric- only atoms with even angular momentum can collide meaning their spin is in a singlet state as in the case of ^{87}Sr . For bosons it is the contrary : from an even orbital wavefunction, the spin wavefunction should be antisymmetric to collide.

3.1.2 What is photoassociation

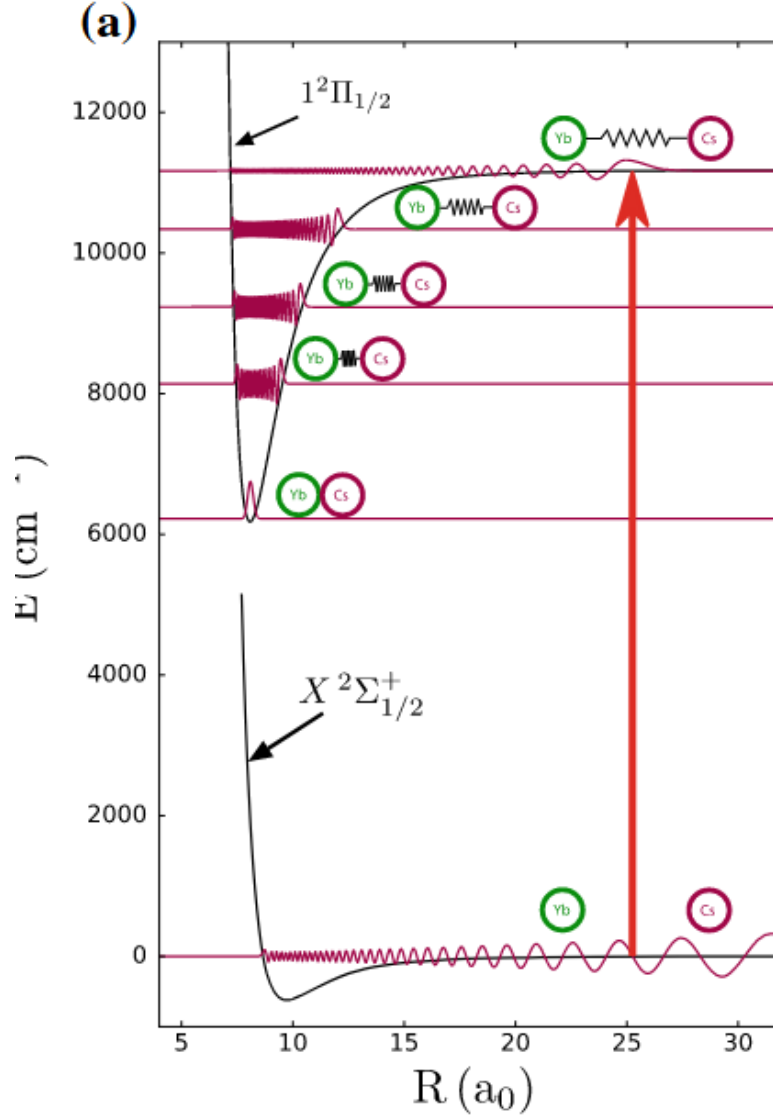


Figure 3.1: Caption

Photoassociating two atoms consists in bounding two colliding atoms with light that occurs mostly with two-body and three body losses.

As visible in 3.1 from a free state of a two-atoms system we couple them via a laser with a molecular vibrational state. In the case of spectroscopy we usually start with the least bounded state to have the atomic state reference. From that we sweep the atom frequency to address the molecular states red detuned from the atomic line. The quantity that will testify there is two-body losses is the atom number remaining in the trap after a photoassociation pulse. The molecule leaves the trap by acquiring kinetic energy from the binding energy. The experimental proof of photoassociation is given by

$$\frac{dN}{dt} = -\beta N^2 - \Gamma N \quad (3.6)$$

β the fitted parameter of two-body losses ($\beta = \frac{K_2 V_e}{2}$, K_2 in comparison with [2]) the two-body loss rate, V_e the effective volume of the cloud $(2\pi)^{3/2} \sigma_x \sigma_y \sigma_z$ for a density Gaussian distribution and Γ the one-body losses rate. This latter is limited by the vacuum quality and the lifetime of the atoms in the trap.

PA is mostly used in Feshbach resonance field because determining the exact position of the vibrational states enables by changing the magnetic field to tune the scattering length of the atoms and thus the interactions in the system.

3.1.3 Molecular formalism/vocabulary (condon radius, optical length...)

Optical length characterizes the strength of the photoassociation rate

$$K_2 = \frac{4\pi\hbar}{\mu} n l_{opt} \quad (3.7)$$

μ the reduced mass of the two atoms. This rate represents the ratio of the atoms that are lost by 2-body losses.

It contains the probability to transition from an initial vibrational i state to a final vibrational f state : **the Franck Condon factor** ([3])

$$F_{FC} = \left| \int_0^\infty \psi_i(r) \psi_f(r) dr \right|^2 \quad (3.8)$$

r the inter-nuclear distance. It depends directly with the overlap of the wavefunctions of the initial and final states. **The Condon radius** is the distance between the atoms for which this factor is maximum which also means that in a classical approach the atoms spend the most time at this position.

The good quantum numbers

We write the total angular momentum of the molecule $T = R + F = R + I + J$, F being the total spin of the two atoms $f_1 + f_2$, $J = j_1 + j_2$ is the angular momentum of the molecule that describes the spin-orbit coupling, and R the rotational angular momentum of the molecule.

We define the projection of the different angular momentum on the inter-nuclear axis as

$$\Omega = \Lambda + \Sigma \quad (3.9)$$

with Λ the projection of the orbital momentum of the molecule on the internuclear axis and Σ the projection of the momentum spin.

M_T is the projection of the total angular momentum T onto a defined quantization axis.

For the rotational quantum number there is a parity of the total wavefunction that needs to be fulfilled. In addition there are only s-wave collisions in cold gases then the part of the wavefunction should be odd the spin one antisymmetric

$$|\Psi\rangle = (|\phi_e\rangle_A |\phi_g\rangle_B + (-1)^R |\phi_e\rangle_B |\phi_g\rangle_A) \otimes |\chi\rangle \quad (3.10)$$

$|\phi_e\rangle$ and $|\phi_g\rangle$ are the electronic wavefunctions of the two atoms A and B in ground and excited state respectively, $|\chi\rangle$ is the spin wavefunction. It gives accessible values $R = 0, 2$ or $4 \dots$

The hamiltonian of the homonuclear molecule For $^1S_0 - ^3P_1$ molecular state there is a strong spin-orbit coupling that couples its related momentum to the internuclear axis (3.2), quantified by Ω and described as Hund's case (c)

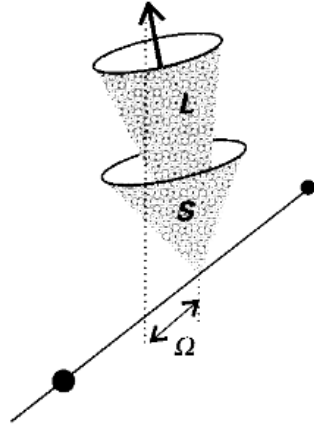


Fig. 11.4 A vector diagram for Hund's case (c), in which the spin-orbit coupling is very strong.

Figure 3.2: hund

The experiment presented in the following section is photoassociation in the $F = 11/2$ hyperfine state. We will focus in this state to simplify the discussion.

Say we have one atom in the 1S_0 state and one in the 3P_1 state: we can have a total spin of $J = 0, 1$ or 2 . It gives possible values of total atomic angular momentum F :

$$\text{For } J = 0, \quad F = \frac{9}{2} \quad (3.11)$$

$$\text{For } J = 1, \quad F = \frac{7}{2}, \frac{9}{2}, \frac{11}{2} \quad (3.12)$$

$$\text{For } J = 2, \quad F = \frac{5}{2}, \frac{7}{2}, \frac{9}{2}, \frac{11}{2}, \frac{13}{2} \quad (3.13)$$

We have one atom with $f_1 = 9/2$ from the 1S_0 state and one in the 3P_1 state with $f_2 = 11/2$. The possible values of total angular momentum of the molecule are

$$\text{For } R = 0, \quad T = 1, 2, 3 \dots 10 \quad (3.14)$$

$$\text{For } R = 2, \quad T = 1, 2 \dots 12 \quad (3.15)$$

$$\text{For } R = 4, \quad T = 1, 2 \dots 14 \quad (3.16)$$

As for atoms there are selection rules for transitions from a free state to a molecular state fixed by the angular momentum of the electrons. $\Delta J = 0, \pm 1$ gives $\Delta T = 0, \pm 1$ with $T = 0 \rightarrow T = 0$ forbidden.

Another element to describe the molecule is the symmetry of the orbital wavefunction. For an even wavefunction the exchange of the two atoms A and B does not change the sign of the wavefunction, as in left figures 3.3. We say the potential is **gerade**. The probability of finding electrons in between the two atoms is high compared to the **ungerade** potential where the odd wavefunction cancels the probability of finding electrons in between.

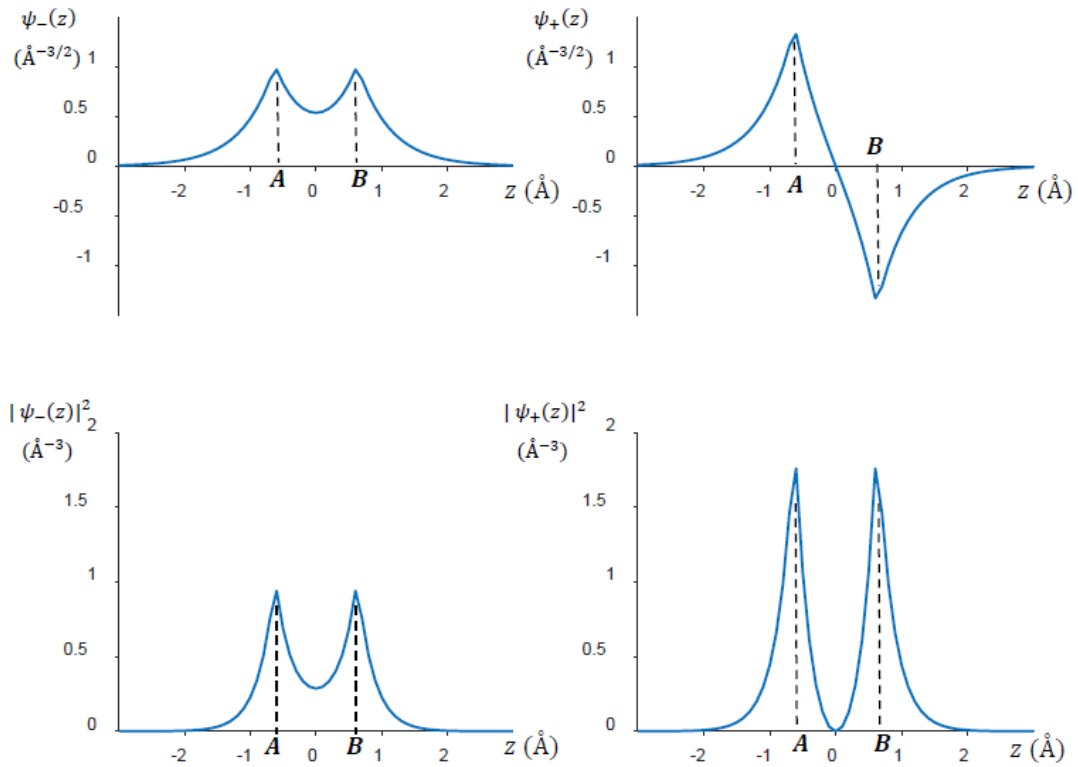


Figure 8.5 : Evolution le long de l'axe internucléaire Oz ($x=0, y=0$) des fonctions d'onde liante $|\psi_{-}\rangle$ et antiliante $|\psi_{+}\rangle$ et des densités de probabilité de présence de l'électron associées $|\psi_{-}|^2$ et $|\psi_{+}|^2$. La distance internucléaire est fixée à $R = 1,25 \text{ \AA}$ (minimum de E_{-}).

Figure 3.3: u-g symmetry

3.1.4 External energy states

To describe two-body losses of a photoassociation process, we can change the study basis depending on the distance between the two atoms by approximating dominant

couplings over others. (Hund's cases)

The hamiltonian of the two-atom system is given in [2] by

$$\hat{H} = \frac{\hat{p}_r^2}{2\mu} + \frac{\hbar^2}{2\mu r^2} R(R+1) + \hat{V}_{BO} + \hat{H}_{HF} \quad (3.17)$$

with

$$\hat{V}_{BO} = \frac{-C_6}{r^6} \left(1 - \frac{\sigma^6}{r^6} \right) - s \frac{C_3^\Omega}{r^3} \quad (3.18)$$

$$\hat{H}_{hf} = A(\mathbf{i}_1 \cdot \mathbf{j}_1) + B \frac{3(\mathbf{i}_1 \cdot \mathbf{j}_1)^2 + \frac{3}{2}(\mathbf{i}_1 \cdot \mathbf{j}_1) - i_1(i_1+1)j_1(j_1+1)}{2i_1(2i_1-1)2j_1(2j_1-1)} \quad (3.19)$$

$s = \pm 1$ for gerade and ungerade potentials respectively. The hyperfine term of the atom in 1S_0 is zero because its electronic angular momentum is zero. The BO potential do not count the $1/r^2$ potential because we are in the s-wave regime ($l=0$) so the electronic shell do not repulse the atoms at short distance.

3.1.4.1 WKB approximation

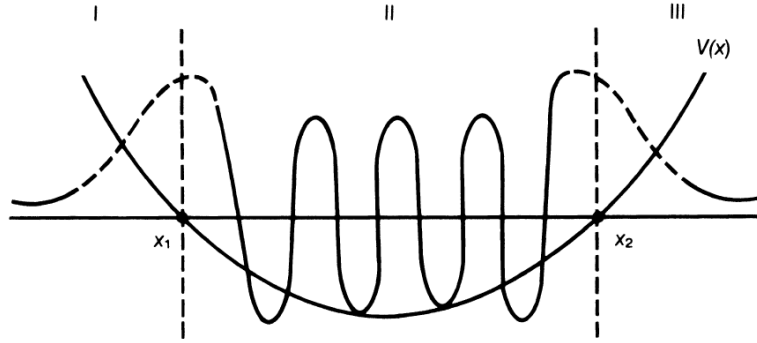


FIGURE 2.1. Schematic diagram for behavior of wave function $u_E(x)$ in potential well $V(x)$ with turning points x_1 and x_2 .

Figure 3.4: Caption

3.1.4.2

3.1.5 Internal energy states

Leroy-Bernstein approx

3.2 About photoassociation on other species

3.2.1 Mass scaling (88Sr)

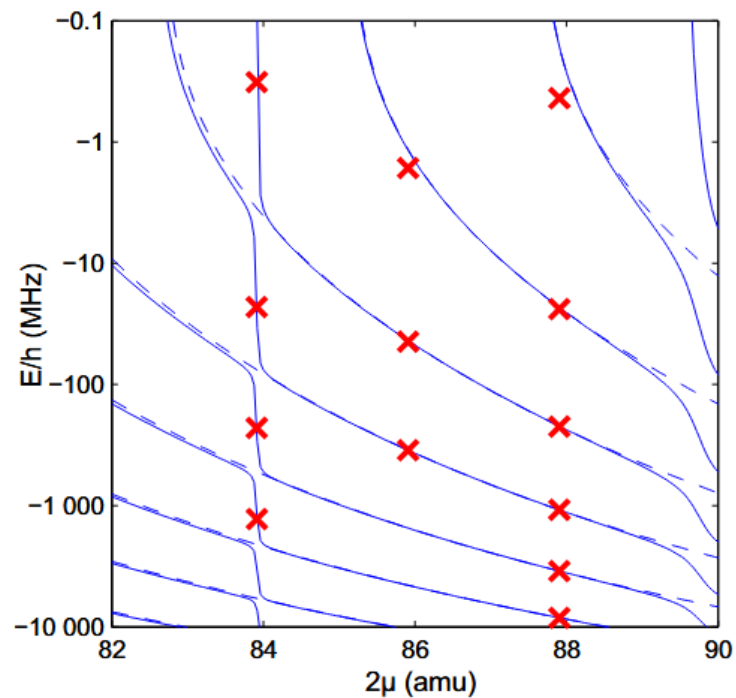


Figure 3.5: Caption

3.2.2 Ytterbium: hfs

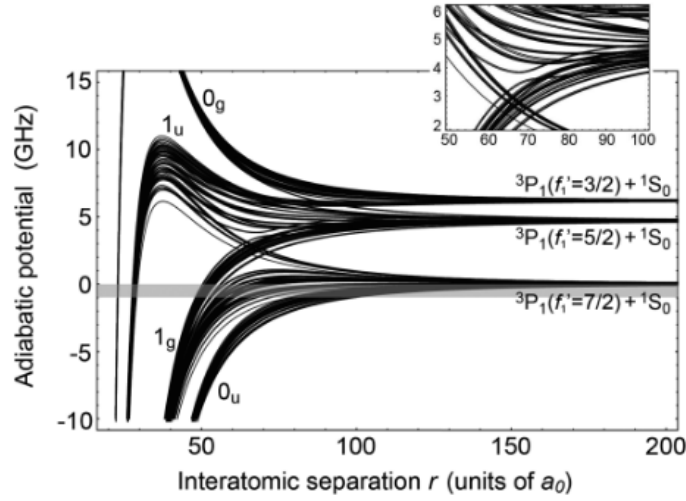


FIG. 2. Adiabatic molecular potentials for a $^{173}\text{Yb}_2$ dimer in the $^1S_0 + ^3P_1$ channel as functions of the interatomic separation r . The molecular potentials for 205 different (T, F, R) configurations are displayed, which are accessible via PA from the initial s -wave colliding atoms in the $^1S_0 + ^1S_0$ channel. At large r , the potentials converge to three asymptotic branches which correspond to excited atomic states with hyperfine numbers of $f'_1 = 3/2$, $5/2$, and $7/2$. Some of the potentials have a local minimum (inset), possibly hosting purely long-range bound states [14]. The energy offset is adjusted to the $f'_1 = 7/2$ asymptote. The shaded region indicates the spectral range of our measurements.

Figure 3.6: Caption

3.3 Experimental setup

3.4 ^{88}Sr Results

Lopt, power broadening, thermal broadening...

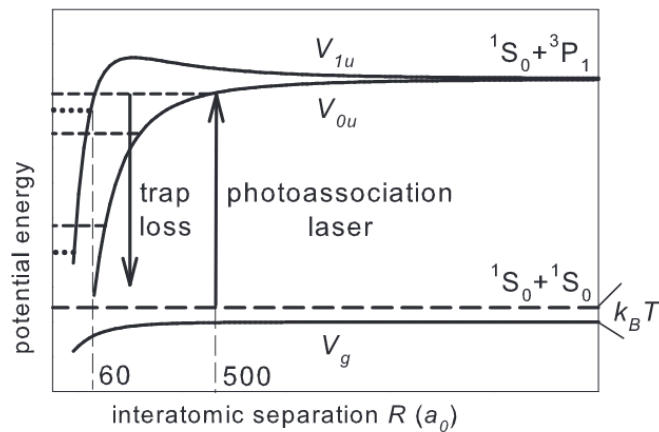


Figure 3.7: Caption

3.4.1 Technical issues of inhabilitation of photoassociation

3.4.1.1 Laser width

3.5 ⁸⁷Sr molecules

Lopt questions sur nb quantique / choix de pompage optique

3.5.1 Physical sources of inhabilitation of photoassociation

3.5.1.1 On $F = 9/2$: predissociation

3.5.1.2 Coupling to more energetic state from the IR

3.5.1.3 Node of wavefunction for some vibrational states

3.5.2 Energy landscape of ⁸⁷Sr-⁸⁷Sr molecules

Conclusion

Bibliography

- [1] J. Dalibard, “Les interactions entre atomes dans les gaz quantiques,”
- [2] J. H. Han, J. H. Kang, M. Lee, and Y.-i. Shin, “Photoassociation spectroscopy of ultracold ^{173}Yb atoms near the intercombination line,” *Physical Review A*, vol. 97, p. 013401, Jan. 2018. arXiv:1710.03072 [physics].
- [3] A. Guttridge, *Photoassociation of Ultracold CsYb Molecules and Determination of Interspecies Scattering Lengths*. Springer Theses, Cham: Springer International Publishing, 2019.

Appendix A

Algorithms