

- Number of visits in a recurrent state

- Staying forever in a transient state:

Gambler's win vs. a bank

$$U_i = \sum_{j \in T} p_{ij} U_j \quad i \in T$$

- Absorption in a recurrent class C :

Gambler's win vs. a bank

$$V_i = \sum_{j \in C} p_{ij} + \sum_{j \in T} p_{ij} V_j \quad i \in T$$

- Mean absorption time in C :

Coupon collector

$$W_i = 1 + \sum_{j \in T} p_{ij} W_j \quad i \in T$$

Gambler's win (finite state space)

- Transience criterion :

$$\exists \text{ bounded non-constant: } \sum_{k \in E} p_{jk} y_k = y_j$$

- Recurrence criterion :

$$\exists (y_i)_i : \sum_{k \in E} p_{jk} y_k \leq y_j, \quad y \rightarrow \infty$$

Queue model

- Suff. cond. for $\exists! \pi$:

$$\exists (x_j)_j, (y_j)_j : \sum_{k \in E} p_{jk} y_k \leq y_j - x_j, \quad x_j, y_j \rightarrow \infty$$

Queue model

- Moment generator function

Gambler's win