

MA(n) :

$$v(t) = c_0 \eta(t) + c_1 \eta(t-1) + \dots + c_n \eta(t-n)$$

$$\gamma(\tau) = \begin{cases} (c_0^2 + c_1^2 + \dots + c_n^2) \lambda^2 & \tau=0 \\ (c_0 c_1 + c_1 c_2 + \dots + c_{n-1} c_n) \lambda^2 & |\tau|=1 \\ (c_0 c_2 + c_1 c_3 + \dots + c_{n-2} c_n) \lambda^2 & |\tau|=2 \\ \vdots & \vdots \\ c_0 c_n \lambda^2 & |\tau|=n \\ 0 & |\tau|>n \end{cases} \quad \Rightarrow \quad \begin{cases} k_0 \lambda^2 & \tau=0 \\ k_1 \lambda^2 & |\tau|=1 \\ k_2 \lambda^2 & |\tau|=2 \\ \vdots & \vdots \\ k_n \lambda^2 & |\tau|=n \\ 0 & |\tau|>n \end{cases}$$

covariance function

$$\begin{aligned} P(\omega) &= \gamma(0) + \sum_{\tau=1}^{+\infty} \gamma(\tau) 2 \cos(\omega \tau) \\ &= k_0 \lambda^2 + \sum_{\tau=1}^n \gamma(\tau) 2 \cos(\omega \tau) \\ &= \left(k_0 + 2 \left(\sum_{\tau=1}^n k_\tau \cos(\omega \tau) \right) \right) \lambda^2 \end{aligned}$$

spectrum

$$W(z) = \frac{c_0 z^n + c_1 z^{n-1} + \dots + c_n}{z^n}$$

transfer function

AR(n) :

$$v(t) = a_1 v(t-1) + \dots + a_n v(t-n) + \eta(t)$$

$$W(z) = \frac{z^n}{z^n - a_1 z^{n-1} - \dots - a_n}$$