

Haskell Programming Assignment

This assignment asks you to implement three functions in Haskell

1. Implement the **Merge Sort** algorithm as a Haskell function. The function should take a list of values in the Haskell class **Ord** and return a sorted list. The type signature will be

```
mergeSort :: (Ord a) => [a] -> [a]
```

Recall that merge sort works as follows:

- a. Split the list into two approximately equal sublists
- b. Sort each sublist using merge sort
- c. Merge the two sorted sublists.

I am providing some Java code for this algorithm. Your task is to convert this code into Haskell. Note that I made **merge** a private method, since it is only used in `mergeSort`. For the same reason, you should implement **merge** in Haskell using either the **where** or the **let** construct. (Of course, your implementation will be recursive instead of iterative. As a hint, you will need three base cases: merging two empty lists, merging an empty list with a non-empty list, and merging a non-empty list with an empty list.)

2. In class, we used denotational semantics to evaluate a decimal number using a function M_{dec} . We could define a similar function to evaluate *hexadecimal* numbers as follows:

```
M_hexDigit ('0') = 0, ..., M_hexDigit ('9') = 9,  
M_hexDigit ('A') = M_hexDigit ('a') = 10, ..., M_hexDigit ('B') = M_hexDigit ('b') = 11, ...,  
M_hexDigit ('F') = M_hexDigit ('f') = 15  
M_hex ("d") = M_hexDigit ('d') (Base case - one-digit string)  
M_hex ("dndn-1...d1d0") = M_hex ("dndn-1...d1") * 16 + M_hexDigit ('d0') 
```

Note that I am allowing both upper- and lower-case letters for the hexadecimal digits for 10,11,...,15.

Implement a Haskell function `mHexDigit` to return the numerical value of a single hexadecimal digit. You will need to use guards and the **ord** function from the Haskell module **Data.Char**. The Haskell type should be **mHexDigit::Char -> Int**

Now, implement a Haskell function **mHex::String -> Int** to evaluate a hexadecimal number given as a string.

Finally, since `mHexDigit` is only used by `mHex`, implement a Haskell function **mHex'::String -> Int** in which `mHexDigit` is defined using the **where** or **let** construct.

3. Implement a Haskell function **varmap::String -> [(String,Int)] -> Int**, based on the denotational-semantics function `VARMAP`, that takes an identifier and a list of identifier-value pairs and returns the value associated with the identifier in the list. To accommodate Haskell's static typing, you may assume the values are non-negative integers and use -1 in place of **undef**. You may also return -1 as an error code if the identifier is not in the list.

I am providing some sample runs using the GHCiWin of my implementations of these functions so that you can see how they should work in action (and test your implementation).

I am also providing some Haskell functions (together with a sample run) that illustrate the functions **ord**, **chr**, **fst**, and **snd** that you may find useful.