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Sobre

This is a *sample* book written in **Markdown**. You can use anything that Pandoc's Markdown supports; for example, a math equation $a^2 + b^2 = c^2$.

Uso

Each **bookdown** chapter is an .Rmd file, and each .Rmd file can contain one (and only one) chapter. A chapter *must* start with a first-level heading: # A good chapter, and can contain one (and only one) first-level heading.

Use second-level and higher headings within chapters like: ## A short section or ### An even shorter section.

The index.Rmd file is required, and is also your first book chapter. It will be the homepage when you render the book.

Render book

You can render the HTML version of this example book without changing anything:

- 1. Find the **Build** pane in the RStudio IDE, and
- 2. Click on **Build Book**, then select your output format, or select "All formats" if you'd like to use multiple formats from the same book source files.

Or build the book from the R console:

bookdown::render_book()

To render this example to PDF as a bookdown::pdf_book, you'll need to install XeLaTeX. You are recommended to install TinyTeX (which includes XeLaTeX): https://yihui.org/tinytex/.

Preview book

As you work, you may start a local server to live preview this HTML book. This preview will update as you edit the book when you save individual .Rmd files. You can start the server in a work session by using the RStudio add-in "Preview book", or from the R console:

6 SUMÁRIO

bookdown::serve_book()

Parte I Conhecendo o Octave e o Python

Introdução ao Octave

1.1 Comandos Básicos em Octave

Esta é uma forma de montar uma matriz 3×3 em **Octave**

```
M = [1 \ 2 \ 3; 4 \ 5 \ 6; 7 \ 8 \ 9]
```

```
## M =
##
## 1 2 3
## 4 5 6
## 7 8 9
```

All chapter sections start with a second-level (##) or higher heading followed by your section title, like the sections above and below here. You can have as many as you want within a chapter.

An unnumbered section

Chapters and sections are numbered by default. To un-number a heading, add a {.unnumbered} or the shorter {-} at the end of the heading, like in this section.

Introdução ao Python

2.1 Comandos Básicos em Python

Esta é uma forma de montar uma matriz 3×3 em Python

Parte II

Resolução de Sistemas e Aproximação de Funções

Sistemas de Equações

3.1	Equações	Não-L	ineares

- 3.1.1 Método de Newton
- 3.1.2 Método das Secantes
- 3.1.3 Método de Regula Falsi
- 3.1.4 Sistemas de Equações não lineares
- 3.1.5 Equações Polinomiais
- 3.2 Solução de Equações Lineares: Métodos Exatos
- 3.2.1 Decomposição LU
- 3.2.2 Eliminação de Gauss
- 3.2.3 Decomposição de Cholesky

Se uma matriz **A** for **simétrica** e **positiva definida**, então A pode ser decomposta da forma:

$$A = GG^T$$

• Matriz Simétrica

Uma matriz simétrica é aquela no qual suas componentes $a_{i,j}$ tem valores iguais as componentes $a_{j,i}$, isto é:

$$a_{i,j} = a_{j,i}$$

• Matriz Positiva Definida

Uma matriz é dita positiva definida se ocorre um dos seguintes fatos:

- 1. Os autovalores de A são todos positivos
- 2. Os menores principais são positivos
- 3. $v^T A v > 0, \forall v \neq 0$

Abaixo um o teorema 1 define o método para execução de Cholesky

Teorema 1 Se uma matriz A for simétrica e positiva definida, então existe uma única matriz triangular G, com elementos diagonais positivos tal que $A = GG^T$.

Isto é, para um caso 3×3 é possível representar

$$\begin{pmatrix} a_{11} & a_{12} & a_{13} \\ a_{21} & a_{22} & a_{23} \\ a_{31} & a_{32} & a_{33} \end{pmatrix} = \begin{pmatrix} g_{11} & 0 & 0 \\ g_{21} & g_{22} & 0 \\ g_{31} & g_{32} & g_{33} \end{pmatrix} \begin{pmatrix} g_{11} & g_{21} & g_{31} \\ 0 & g_{22} & g_{32} \\ 0 & 0 & g_{33} \end{pmatrix}$$

Para encontrar os coeficientes da matriz G, é então feito os seguintes processos

$$g_{11} = \sqrt{a_{11}}$$
 (i)

$$g_{i1} = \frac{a_{i1}}{q_{11}} \tag{ii}$$

$$g_{ii} = \left(a_{ii} - \sum_{k=1}^{i-1} g_{ik}^2\right)^{1/2} \tag{iii}$$

$$g_{ij} = \frac{\left(a_{ij} - \sum_{k=1}^{j-1} g_{ik} g_{jk}\right)}{g_{jj}}$$
 (iv)

Os passos (iii) e (iv) devem ser intercalados, vista a depedência dos fatores de uma equação na outra, desta forma é indicado o cálculo do valor da diagonal principal e os valores abaixo deste.

Por exemplo, após calcular a componente g_{22} calcular as demais componentes da coluna 2 (pelo passo iv), e somente ao término deste, ir para a componente g_{33} .

3.2.3.1 Função de Cholesky (Python)

```
import numpy as np

#Funcao que verifica a simetria

def simetrica(U):
    for i in range(len(U)):
        for j in range(len(U[0])):
            if U[i][j] != U[j][i]:
                 return 0
    return 1

#Funcao que verifica se a matriz é positiva definida

def pos_def(U):
    auval,auvec = np.linalg.eig(U)
    cont = 0;
    for i in range(len(auval)):
        if auval[i]>0:
```

```
cont = cont+1
  if cont == len(U):
   return 1
 return 0
#Funcao que faz a soma para os termos G[i][i]
def SomaCho1(U,i):
  soma1 = 0
  for k in range(0,i):
    soma1 = soma1 + np.power(U[i][k],2)
 return soma1
#Funcao que faz a soma para os termos G[i][j]
def SomaCho2(U,i,j):
  soma2 = 0
 for k in range(0,j):
    soma2 = soma2 + U[i][k]*U[j][k]
 return soma2
#Funcao para o Calculo da Decomposicao de Cholesky
def MeuCholesly(A):
  G = np.zeros((len(A),len(A)))
  if simetrica(A) == pos_def(A):
    G[0][0] = np.sqrt(A[0][0])
    for i in range(1,len(A)):
      G[i][0] = A[i][0]/G[0][0]
    for j in range(1,len(A)):
      for i in range(j,len(A)):
        if i==j:
          G[i][j] = np.sqrt(A[i][i] - SomaCho1(G,i))
          #print(SomaCho1(G,i))
        else:
          G[i][j] = (A[i][j] - SomaCho2(G,i,j))/G[j][j]
          \#print(SomaCho2(G, i, j))
    G = np.round(G, 4)
   return G
  else:
    return print('Não é possível usar Decomposição de Cholesky')
```

Exemplo matriz 3×3

Exemplo matriz 4×4

```
## array([[ 3., 0., 0., 0.],
## [ 0., 3., 0., 0.],
## [-9., -3., 3., 0.],
## [ 6., -9., 0., 2.]])
```

3.2.3.2 Comando linalg.Cholesky

3.3 Solução de Equações Lineares: Métodos Iterativos

3.3.1 Método de Gauss Seidel

Footnotes and citations

4.1 Footnotes

Footnotes are put inside the square brackets after a caret ^[]. Like this one ¹.

4.2 Citations

Reference items in your bibliography file(s) using @key.

For example, we are using the **bookdown** package [Xie, 2021] (check out the last code chunk in index.Rmd to see how this citation key was added) in this sample book, which was built on top of R Markdown and **knitr** [Xie, 2015] (this citation was added manually in an external file book.bib). Note that the .bib files need to be listed in the index.Rmd with the YAML bibliography key.

The RStudio Visual Markdown Editor can also make it easier to insert citations: https://rstudio.github.io/visual-markdown-editing/#/citations

 $^{^{1}\}mathrm{This}$ is a footnote.

Blocks

5.1 Equações

Aqui está uma equação.

$$f(k) = \binom{n}{k} p^k (1-p)^{n-k}$$
 (5.1)

You may refer to using \Oref(eq:binom), like see Equation (5.1).

5.2 Theorems and proofs

Labeled theorems can be referenced in text using \@ref(thm:tri), for example, check out this smart theorem 2.

Teorema 2 For a right triangle, if c denotes the length of the hypotenuse and a and b denote the lengths of the **other** two sides, we have

$$a^2 + b^2 = c^2$$

Read more here https://bookdown.org/yihui/bookdown/markdown-extensions-by-bookdown.html.

5.3 Callout blocks

The R Markdown Cookbook provides more help on how to use custom blocks to design your own callouts: https://bookdown.org/yihui/rmarkdown-cookbook/custom-blocks.html

22 CAPÍTULO 5. BLOCKS

Sharing your book

6.1 Publishing

HTML books can be published online, see: https://bookdown.org/yihui/bookdown/publishing.html

6.2 404 pages

By default, users will be directed to a 404 page if they try to access a webpage that cannot be found. If you'd like to customize your 404 page instead of using the default, you may add either a _404.Rmd or _404.md file to your project root and use code and/or Markdown syntax.

6.3 Metadata for sharing

Bookdown HTML books will provide HTML metadata for social sharing on platforms like Twitter, Facebook, and LinkedIn, using information you provide in the index.Rmd YAML. To setup, set the url for your book and the path to your cover-image file. Your book's title and description are also used.

This gitbook uses the same social sharing data across all chapters in your book- all links shared will look the same.

Specify your book's source repository on GitHub using the edit key under the configuration options in the _output.yml file, which allows users to suggest an edit by linking to a chapter's source file.

Read more about the features of this output format here:

https://pkgs.rstudio.com/bookdown/reference/gitbook.html

Or use:

?bookdown::gitbook

Referências Bibliográficas

Yihui Xie. *Dynamic Documents with R and knitr*. Chapman and Hall/CRC, Boca Raton, Florida, 2nd edition, 2015. URL http://yihui.org/knitr/. ISBN 978-1498716963.

Yihui Xie. bookdown: Authoring Books and Technical Documents with R Markdown, 2021. URL https://CRAN.R-project.org/package=bookdown. R package version 0.24.