

5) a) $\langle \vec{x}, \vec{y} \rangle = 4 \cdot 1 + 2 \cdot 2 + 1 \cdot 3 = 11$

$$\cos \theta = \frac{\langle \vec{x}, \vec{y} \rangle}{|\vec{x}| \cdot |\vec{y}|} = \frac{11}{\sqrt{4^2 + 2^2 + 1^2} \cdot \sqrt{1^2 + 2^2 + 3^2}} = \frac{11}{7 \cdot \sqrt{6}}$$

$$\vec{x} \cdot \vec{y} = ((2 \cdot 3 - 1 \cdot 2), (-1 \cdot 1 - 4 \cdot 3), (4 \cdot 2 - 2 \cdot 1)) = (4, -13, 6)$$

b) $\langle \vec{x}, \vec{y} \rangle = -1 \cdot 0 + 0 \cdot 1 + 0 \cdot 0 = 0$

$$\cos \theta = \frac{\langle \vec{x}, \vec{y} \rangle}{|\vec{x}| \cdot |\vec{y}|} = \frac{0}{\sqrt{(-1)^2 + 0^2 + 0^2} \cdot \sqrt{0^2 + 1^2 + 0^2}} = 0$$

$$\vec{x} \cdot \vec{y} = ((0 \cdot 0 - 0 \cdot 1), (0 \cdot 0 - (-1) \cdot 0), ((-1) \cdot 1 - 0 \cdot 0)) = (0, 0, -1)$$

c) $\langle \vec{x}, \vec{y} \rangle = 1 \cdot 2 + 2 \cdot 2 + 0 \cdot 0 = 10$

$$\cos \theta = \frac{\langle \vec{x}, \vec{y} \rangle}{|\vec{x}| \cdot |\vec{y}|} = \frac{10}{\sqrt{1^2 + 2^2 + 0^2} \cdot \sqrt{2^2 + 2^2 + 0^2}} = 1$$

$$\vec{x} \cdot \vec{y} = ((2 \cdot 0 - 0 \cdot 2), (0 \cdot 2 - 1 \cdot 0), (1 \cdot 2 - 2 \cdot 2)) = (0, 0, 0)$$

• O item c) as retas são paralelas

• O item b) as retas são perpendiculares