

Universidade Federal da Paraíba
Departamento de Estatística
Probabilidade IV
Atividade 1 - teoria de conjuntos (1 ponto)
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1

$$B = \left\{ x ; x > \frac{9}{4} \text{ e } x < \frac{6}{5} \right\} \text{ e}$$

$$D = \{x ; x \text{ é divisível por } 0\}$$

2

$$\mathcal{P}(A) = \left\{ \begin{array}{l} \emptyset \\ \{a\}, \{b\}, \{c\}, \{d\}, \\ \{a, b\}, \{a, c\}, \{a, d\}, \{b, c\}, \{b, d\}, \{c, d\}, \\ \{a, b, c\}, \{a, b, d\}, \{a, c, d\}, \{b, c, d\} \\ \{a, b, c, d\} \end{array} \right\}$$

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- a) V
- b) F, $\{a\}$ não pertence a $\{a, b\}$, ele é subconjunto
- c) F, $\{0\}$ possui apenas um elemento e não é \emptyset
- d) F, \emptyset é um conjunto que não possui elementos
- e) F, apenas \emptyset é subconjunto de \emptyset
- f) V
- g) V
- h) V
- i) V
- j) F, $\{\{a, b, c, d\}\}$ possui apenas um elemento: $\{a, b, c, d\} \neq \{a, b\}$

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$$A \cap B = \{b, c, d\}$$

$$A \cap C = \{c\}$$

$$B \cap C = \{c, e\}$$

$$A \cap B \cap C = \{c\}$$

$$A \cup B = \{a, b, c, d, e\}$$

$$A \cup C = \{a, b, c, d, e, f\}$$

$$B \cup C = \{b, c, d, e, f\}$$

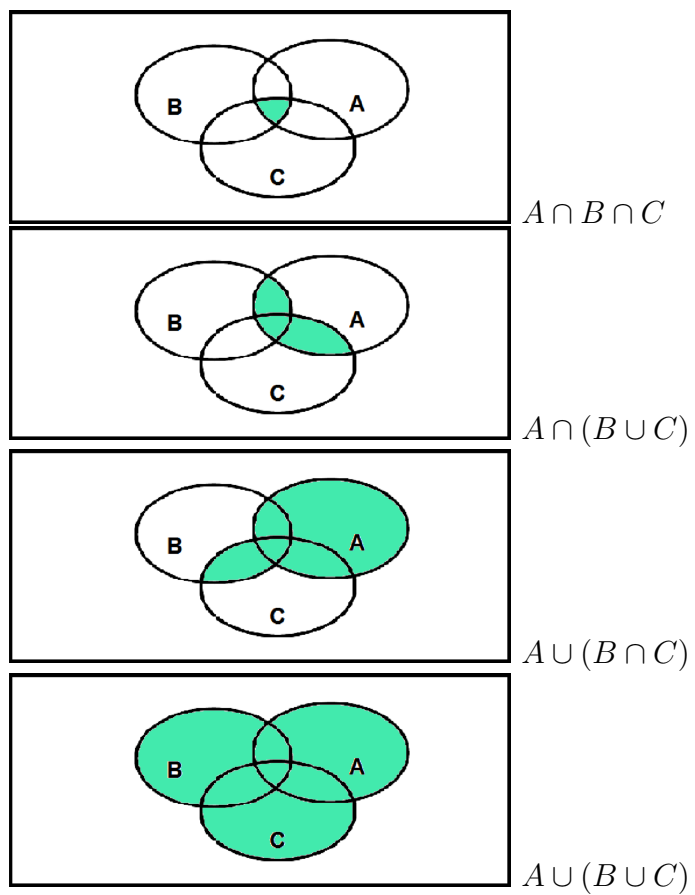
$$A \cup B \cup C = \{a, b, c, d, e, f\}$$

Nenhum par de conjuntos são disjuntos pois nenhuma interseção resultou em vazio

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- | | | |
|------|------|------|
| a) V | f) V | k) V |
| b) F | g) V | l) V |
| c) F | h) F | m) V |
| d) V | i) F | n) V |
| e) V | j) V | o) V |

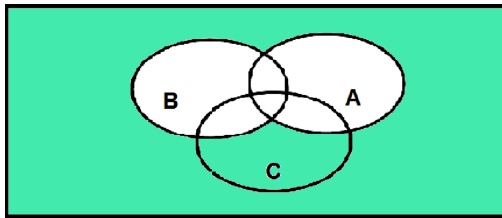
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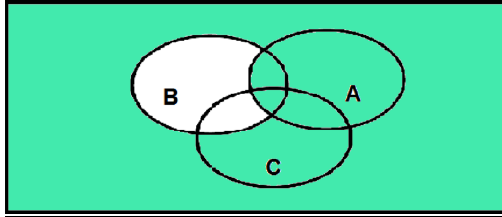
7

$$\begin{aligned}
 A - B &= \{a, b\} \\
 B - A &= \{e, f, g\} \\
 C - B &= \{b\} \\
 (A \cup C) - B &= \{a, b\} \\
 A - (B \cap C) &= \{a, b, c\} \\
 (A \cup B) - (A \cap C) &= \{a, c, e, f, g\}
 \end{aligned}$$

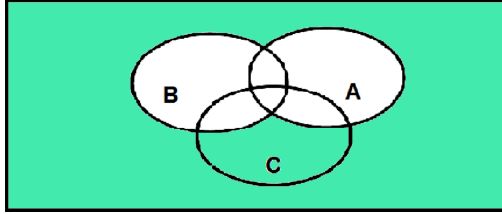
8



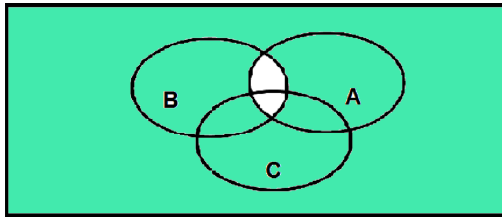
$$A^c - B$$



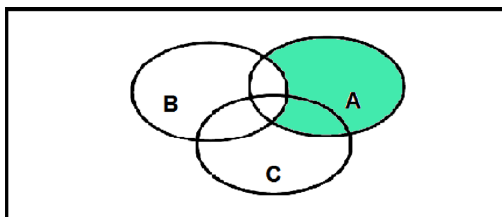
$$B^c \cup A$$



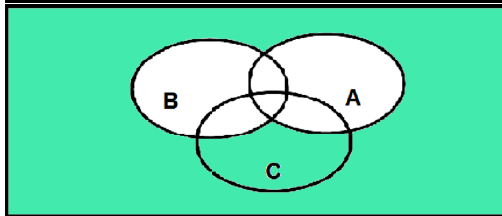
$$(A \cup B)^c$$



$$(A \cap B)^c$$



$$B^c \cap A$$



$$A^c - (A \cup B)$$

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$$\text{a) } (A - C) \cup (B - C) = (A \cap C^c) \cup (B \cap C^c) = (A \cup B) \cap C^c = (A \cup B) - C$$

$$\text{b) } (A - C) \cap (B - C) = (A \cap C^c) \cap (B \cap C^c) = (A \cap B) \cap C^c = (A \cap B) - C$$

■

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$$A \cap (B - A) = A \cap (B \cap A^c) = (A \cap A^c) \cap B = \emptyset \cap B = \emptyset$$

são disjuntos

$$A \cup (B - A) = A \cup (B \cap A^c) = (A \cup B) \cap (A \cup A^c) = (A \cup B) \cap U = A \cup B$$

■

$$A \cup B = [0, 5]$$

$$A \cap B = (3, 5)$$

$$B \cup C = (2, 5]$$

$$C \cup (A \cap B) = (2, 5)$$