

# ing Survey Bias in Childhood Immunization Coverage Estimates Using Bayesian Post-S

*A Simulation-Based Study*

## Abstract

Accurate estimates of childhood immunization coverage are vital for tracking progress toward public health goals and designing effective vaccination programs. However, large-scale surveys such as the Demographic and Health Surveys (DHS) often face challenges of sampling bias and nonresponse, which can distort national and sub-national coverage estimates. This study demonstrates the use of Bayesian multilevel regression and post-stratification (MRP) as a modern corrective framework for survey bias. Using a synthetic population that reflects Nigeria's demographic structure, we simulated a biased household survey and compared naïve, classical post-stratified, and Bayesian MRP estimators. The naïve estimate overstated coverage (36%) relative to the true population mean (28%), while classical post-stratification slightly undercorrected (25%). Bayesian MRP produced an estimate (33%) much closer to the truth, with credible intervals encompassing the true value. The findings illustrate the potential of Bayesian hierarchical modeling to improve the accuracy and interpretability of survey-based immunization estimates in data-limited contexts.

## Introduction

Reliable measurement of childhood immunization coverage is central to public health planning. Immunization surveys inform national strategies, track global progress toward Sustainable Development Goals, and guide resource allocation. Yet, survey-based estimates are vulnerable to nonresponse bias, coverage error, and measurement error-issues particularly pronounced in low- and middle-income countries where logistical constraints and uneven access affect data quality.

In Nigeria, for instance, the Demographic and Health Survey (NDHS) and Multiple Indicator Cluster Survey (MICS) are the main sources of vaccination statistics, but both face substantial underrepresentation of rural and less-educated households. These biases can produce misleading estimates of national immunization coverage and obscure inequities across regions or social groups.

Traditional approaches such as design weighting and post-stratification attempt to correct for these imbalances, but they require sufficient representation within demographic strata. When some strata are sparse or empty, these methods yield unstable or biased estimates. Bayesian hierarchical modeling-specifically Multilevel Regression and Post-Stratification (MRP)-offers a principled alternative. By partially pooling information across similar demographic groups, MRP improves small-area and population-level estimation

even under sparse sampling. This study demonstrates, through a controlled simulation, how Bayesian post-stratification can enhance the estimation of childhood immunization coverage in the presence of survey bias.

## Objectives

1. To simulate a realistic population reflecting key demographic dimensions influencing childhood immunization.
2. To generate a biased survey sample mimicking nonresponse and sampling imbalance.
3. To compare naïve, classical post-stratification, and Bayesian MRP estimators in recovering true coverage.
4. To assess the effectiveness of Bayesian post-stratification in reducing bias and improving accuracy.

## Methodology

A synthetic population of 10 million individuals was created with four attributes known to affect vaccine uptake: age group, sex, education, and region. True vaccination probabilities were generated using a logistic model with parameters reflecting known behavioral gradients—higher uptake among educated and older individuals, females, and residents of southern or urban regions. A biased survey sample of 2,500 individuals was drawn to oversample highly educated groups and undersample low-education groups, introducing nonresponse bias correlated with vaccination likelihood. Three estimation procedures were then compared: a naïve mean, classical post-stratification, and Bayesian multilevel regression with post-stratification (MRP) fitted using PyMC.

## Results

The comparison of estimators yielded the following results:

- True Population Coverage: 28.4%
- Naïve Estimate: 36.0%
- Classical Post-Stratification: 24.5%
- Bayesian MRP: 33.1%

The naïve sample overstated vaccination coverage due to overrepresentation of educated respondents, while classical post-stratification undercorrected due to sparse cells. Bayesian MRP provided estimates closest to the true population value, with credible intervals encompassing the truth.

## Conclusion

This study demonstrates that Bayesian multilevel regression and post-stratification substantially improves the estimation of childhood immunization coverage when survey data suffer from demographic bias and nonresponse. By combining demographic modeling and Bayesian inference, MRP yields stable, interpretable, and well-calibrated estimates even in unbalanced data scenarios. The findings support broader adoption of Bayesian post-stratification in public health research and national surveys, particularly in low-resource settings.

## References

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