

AI
LAB-10

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PRE-LAB:-

Given $P(A)$, $P(A \cup B)$, $P(B)$.

$$P(A|B) = \frac{P(A, B)}{P(B)}$$

IN LABS:-

(1) In a pack of cards we have 52 cards.

Out of which 13 are Diamonds
we have face cards = 3
(King, Queen, Jack)

Ace is not
a face card.

We have to draw a diamond
or a face card or both
at a time that is a face card

of diamond type.

To determine the probability of drawing a diamond $\#$ of drawing = 13

To determine the probability of drawing a face card $\#$ of face cards = 12

To determine the combination of both, such as queen of diamond or Jack of diamond or king of diamond

$\#$ queen of diamond = 1

king of diamond = 1

Jack of diamond = 1

We are requested to get, output as

25.0% , 23.1% , 1.9% .
for all 3 cases.

(2) In this experiment / question :

Egg \rightarrow car key

Egg \rightarrow empty

Egg \rightarrow empty

Jerry chooses & host the one of the other two,

Now we need to find the probability of Jerry winning in cases:-

(1) Staying with his choice

(2) Shifting his choice

The probability that the car key is in one of the golden eggs 1, 2 or 3 is

$$P(1) = 1/3, P(2) = 1/3, P(3) = 1/3.$$

Suppose Jerry chooses Egg-1 :-

Probability of host breaking

Egg-3 conditional on where the car

key is located is:-

$$P(III/1) = 1/2 \left(\text{Prob}(\text{host breaking Egg-3} \mid \text{given that car key is in Egg-1}) \right).$$

since Car key is in Egg-1 Host can break Egg-2 or 3.

$$P(III/2) = 1$$

$$P(III/3) = 0$$

Now what is the probability of the car key being in Egg-2 given that

Egg-3 was broken:-

We use Bayes law:-

$$P(2/III) = \frac{P(III/2) P(2)}{P(III/1) (P(1)) + P(III/2) P(2) + P(III/3) P(3)}$$

$$= \frac{(1/2)(1/3)}{(1/2)(1/3) + (1)(1/3) + 0(1/3)} = 2/3$$

Now,

Probability of car key in egg-1

$$\Rightarrow P(1/III) = \frac{P(III/1)P(1)}{P(III/1)P(1) + P(III/2)P(2) + P(III/3)P(3)}$$

$$= \frac{(1/2)(1/3)}{(1/2)(1/3) + (1)(1/3) + (0)(1/3)} = 1/3$$

\Rightarrow Switching the egg is better for Terry

Qp :- Monty Hall Problem with 3 Eggs
Proportion of wins without switching
: 0.3333

Proportion of wins with switching
: 0.6667

190030117 AI LAB 10 INLAB OUTPUTS:Q-1,2:

The image displays two screenshots of Google Colaboratory notebooks, showing Python code and its execution results.

Top Screenshot (LAB_10_IN_1):

```
[1] def event_probability(event_outcomes,sample_space):
    probability=(event_outcomes/sample_space)*100
    return round(probability,1)

[2] cards=52

[3] diamonds=13
    diamond_probability=event_probability(diamonds,cards)

[4] face_cards=12
    face_cards_probability=event_probability(face_cards,cards)

[5] queen_of_diamonds=1
    queen_of_diamond_probability=event_probability(queen_of_diamonds,cards)

print(str(diamond_probability)+'%')
print(str(face_cards_probability)+'%')
print(str(queen_of_diamond_probability)+'%')
```

Output:

```
25.0%
23.1%
1.9%
```

Bottom Screenshot (LAB_10_IN_2):

```
[33] import random

[41] def run_trail(switch_eggs,neggs=3):
    chosen_egg=random.randint(1,neggs)
    if switch_eggs:
        revealed_egg=3 if chosen_egg==2 else 2
        available_eggs=[dnum for dnum in range(1,neggs+1) if dnum not in (chosen_egg,revealed_egg)]
        chosen_egg=random.choice(available_eggs)
    return chosen_egg==1

[42] def run_trails(ntrails,switch_eggs,neggs=3):
    nwins=0
    for i in range(ntrails):
        if run_trail(switch_eggs,neggs):
            nwins+=1
    return nwins

neggs,ntrails=3,10000
nwins_without_switch = run_trails(ntrails,False,neggs)
nwins_with_switch= run_trails(ntrails,True,neggs)
print("Monty Hall Problem with {} doors".format(neggs))
print("Proportion of WINS without switching: {:.4f}".format(nwins_without_switch/ntrails))
print("Proportion of WINS with switching: {:.4f}".format(nwins_with_switch/ntrails))

Monty Hall Problem with 3 doors
Proportion of WINS without switching: 0.3339
Proportion of WINS with switching: 0.6698
```