

AJ
LAB-10

190030117

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PRE-LAB:-

Given $P(A)$, $P(A \cup B)$, $P(B)$

$$P(A|B) = \frac{P(A, B)}{P(B)}$$

INLABS :-

(1) In a pack of cards we have 52 cards.

Out of which 13 are Diamonds
We have face cards = 3

(King, Queen,
Jack)

Ace is not
a face card.

We have to draw a diamond
or a face card or both
at a time that is a face card

of diamond type.

To determine the probability of drawing
a diamond # of drawing = 13

To determine the probability of
drawing a face card # of face cards = 12

To determine the combination of
both, such as queen of diamond or Jack
of diamond or king of diamond

queen of diamond = 1

king of diamond = 1

Jack of diamond = 1

We are requested to get, output as

25.0%, 23.1%, 1.9%.

for all 3 cases.

(Q) In this experiment / question ;

Egg \rightarrow car key

Egg \rightarrow empty

Egg \rightarrow empty

Jerry chooses & host the one of the other two,

Now we need to find the probability of Jerry winning in cases :-

(1) staying with his choice.

(2) shifting his choice

The probability that the car key is in one of the golden eggs 1, 2 or 3 is $P(1) = 1/3$, $P(2) = 1/3$, $P(3) = 1/3$.

Suppose Jerry chooses Egg-1 :-

Probability of host breaking Egg-3 conditional on where the car

key is located is:-

$P(1|1) = \frac{1}{2}$ (Prob (host breaking egg-3
given that car key is
in egg-1)).

Since Car key is in egg-1 Host
can break egg-2 or 3.

$$P(1|1) = 1$$

$$P(1|2) = 0$$

Now what is the probability of the
car key being in egg-2 given that

egg-3 was broken :-

We use Bayes law :-

$$P(2|1) = \frac{P(1|2) P(2)}{P(1|1) P(1) + P(1|2) P(2) + P(1|3) P(3)}$$

$$= \frac{\frac{1}{2} \times \frac{1}{3}}{\frac{1}{2} \times \frac{1}{3} + 0 \times \frac{1}{3} + 0 \times \frac{1}{3}} = \frac{1}{3}$$

Now,

Probability of carrying in egg-1

$$\Rightarrow P(1|111) = \frac{P(111|1)(P(1))}{P(111|1)(P(1)) + P(111|2)(P(2)) + P(111|3)(P(3))}$$

$$= \frac{(1/2)(1/3)}{(1/2)(1/3) + (1)(1/3) + (0)(1/3)} = 1/3$$

\Rightarrow switching the egg is better for Jerry

Q.P :- Property Hall Problem with 3 eggs
Proportion of wins without switching
: 0.3337

Proportion of wins with switching
: 0.6625.

190030117 AI LAB 10 INLAB OUTPUTS:Q-1,2:

LAB_10_IN_1

```
[1] def event_probability(event_outcomes,sample_space):
    probability=(event_outcomes/sample_space)*100
    return round(probability,1)

[2] cards=52

[3] diamonds=13
diamond_probability=event_probability(diamonds,cards)

[4] face_cards=12
face_cards_probability=event_probability(face_cards,cards)

[5] queen_of_diamonds=1
queen_of_diamond_probability=event_probability(queen_of_diamonds,cards)

print(str(diamond_probability)+"%")
print(str(face_cards_probability)+"%")
print(str(queen_of_diamond_probability)+"%")

25.0%
23.1%
1.9%
```

LAB_10_IN_2

```
[33] import random

[41] def run_trail(switch_eggs,neggs=3):
    chosen_egg=random.randint(1,neggs)
    if switch_eggs:
        revealed_egg=3 if chosen_egg==2 else 2
        available_eggs=[dnum for dnum in range(1,neggs+1) if dnum not in (chosen_egg,revealed_egg)]
        chosen_egg=random.choice(available_eggs)
    return chosen_egg==1

[42] def run_trails(ntrails,switch_eggs,neggs=3):
    nwins=0
    for i in range(ntrails):
        if run_trail(switch_eggs):
            nwins+=1
    return nwins

neggs,ntrails=3,10000
nwins_without_switch = run_trails(ntrails,False,neggs)
nwins_with_switch= run_trails(ntrails,True,neggs)
print("Monty Hall Problem with {} doors".format(neggs))
print("Proportion of WINS without switching: {:.4f}".format(nwins_without_switch/ntrails))
print("Proportion of WINS with switching:{:.4f}".format(nwins_with_switch/ntrails))

Monty Hall Problem with 3 doors
Proportion of WINS without switching: 0.3339
Proportion of WINS with switching: 0.6698
```