Assignment - Module 4

18th January 2024

Instructions:

• Please go through the provided material fully while attempting the questions, and mention the intermediate steps clearly.

• Total Marks: 20 (4 marks for each sub part)

• Due date: 25th January 2024

Q 1. The shown 2-R manipulator in Figure 1 consists of mass-less rods of length L1 and L2 and masses m1 and m2.

- (a) Find the Kinetic and Potential Energies of m1, m2 and the entire manipulator.
- (b) Define the Lagrangian function for the manipulator
- (c) Using the Lagrangian function derive the Euler-Lagrange Dynamics for the manipulator.
- (d) Clearly show the Mass matrix(M), the combined Coriolis and Centripetal terms matrix(C), the gravity term matrix(G) for the standard Euler-Lagrange model for the manipulator.

$$M(\theta)\ddot{\theta} + C(\theta, \dot{\theta}) + g(\theta) = \tau \tag{1.1}$$

where $\theta = [{\theta_1}^T {\theta_2}^T]^T$

(e) Assuming 1.1 as the compact formulation for the Euler-Lagrange model you have derived, derive the control input $\tau_{desired}$.

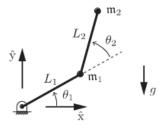


Figure 1: 2R Manipulator