

**Find the minimum value of  $f(x) = x^4 + 3x^2 + 10$**

**Manual calculation:**

**Iteration 1:**

Let  $x = 2$  and  $\eta = 0.011$

Gradient at  $x = 2$   $df(x)/dx \big|_{x=2} = 4(2)^3 + 6(2) = 32 + 12 = 44$

$\Delta x = -0.01 * 44 = -0.44$

Update  $x$  value as  $x = 2 - 0.44 = 1.56$

**Iteration 2:**

Gradient at  $x = 1.56$   $df(x)/dx \big|_{x=2} = 4(1.56)^3 + 6(1.56) = 24.54$

$\Delta x = -0.01 * 24.54 = -0.2454$

Update  $x$  value as  $x = 1.56 - 0.2454 = 1.31$

This process repeats until gradient is near to zero.