

THEORY

In order to determine the number of Monte - Carlo trials I use the variance of the mean value

$$\begin{aligned}
 Var[m_{r^{10}}] &= E[(m_{r^{10}} - E[r^{10}])^2] = E[(\sum r_i^{10} / n - E[r^{10}])^2] = \\
 &= E[(\sum (r_i^{10} - E[r^{10}]) / n)^2] = E[(\sum (\xi_i) / n)^2] = E[(\xi_1 + \xi_2 + \dots)(\xi_1 + \xi_2 + \dots)] / n^2 = \\
 &= \sum E[\xi_i^2] / n^2 + 2 \sum E[\xi_i \xi_{i+1}] / n^2 + 2 \sum E[\xi_i \xi_{i+2}] / n^2 + \dots
 \end{aligned}$$

The first term equals to the sum of population standard deviations divided by n^2

Other terms equal to zero with the assumption of statistical independence of ξ_i

In more detail:

$$E[\xi_i \xi_{i+k}] = E[(r_i^{10} - E[r^{10}])(r_{i+k}^{10} - E[r^{10}])] = E[r_i^{10} r_{i+k}^{10}] - (E[r^{10}])^2$$

$$E[\xi_i \xi_{i+k}] = 0 \quad \text{for} \quad E[r_i^{10} r_{i+k}^{10}] = E[r_i^{10}] E[r_{i+k}^{10}]$$

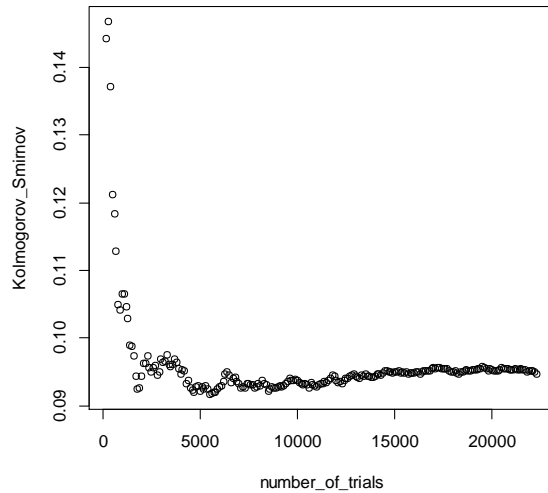
In general, other terms are not zero because overlapping returns imply statistical dependence of ξ_i .

$$E[r_i^{10} r_{i+10}^{10}] = E\left[\frac{P_{i+10} - P_i}{P_i} \frac{P_{i+20} - P_{i+10}}{P_{i+10}}\right] = \dots$$

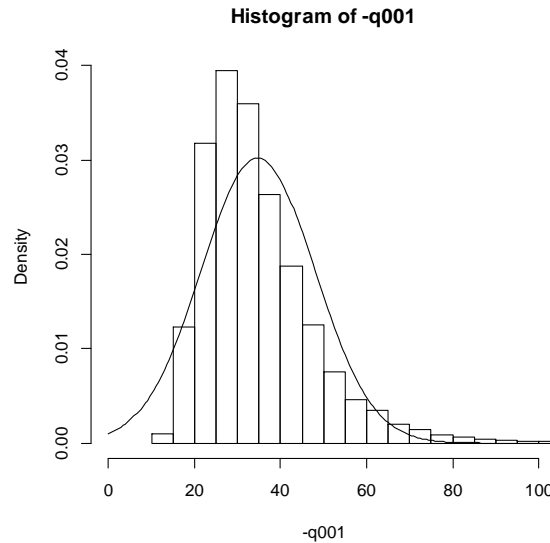
I did not proceed further. I define the stopping condition as:

$$\sqrt{Var[m_{r^{10}}]} / E[r^{10}] = \sigma_{population} / (\sqrt{n} E[r^{10}]) = 0.5\% / 100 = 0.005$$

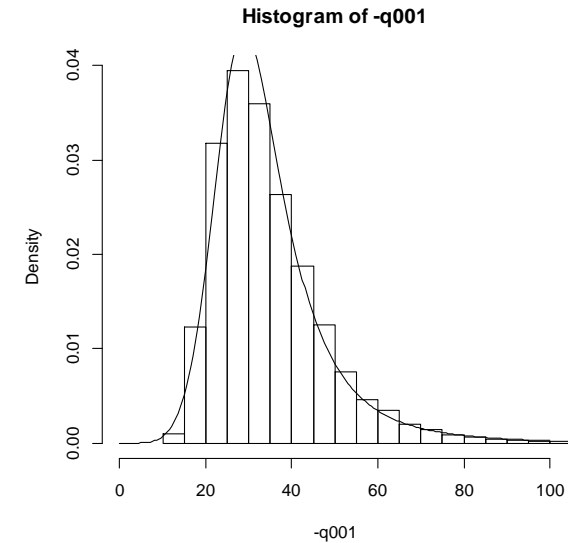
RESULTS



Kolmogorov Smirnov test for normal distribution of 0.01 quantile (q_{001}). The defined above stopping condition provides well the stationarity.



However, normal distribution is not the best choice.



Burr distribution looks much better.

