## Programare declarativă<sup>1</sup>

Module si Clase de Tipuri

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17 noiembrie 2017

<sup>&</sup>lt;sup>1</sup>bazat pe cursul Informatics 1: Functional Programming de la University of Edinburgh

## Module (simple)

### Module

#### Fișierul Geometry.hs

```
module Geometry
( sphereVolume, sphereArea
, cuboidVolume, cuboidArea
) where
sphereVolume :: Float -> Float
sphereVolume radius = (4.0 / 3.0) * pi * (radius ^ 3)
sphereArea :: Float -> Float
sphereArea radius = 4 * pi * (radius ^ 2)
cuboidVolume :: Float -> Float -> Float -> Float
cuboidVolume a b c = rectangleArea a b * c
cuboidArea :: Float -> Float -> Float -> Float
cuboidArea a b c = rectangleArea a b * 2 +
    rectangleArea a c * 2 + rectangleArea c b * 2
rectangleArea :: Float -> Float -> Float
rectangleArea a b = a * b
```

#### Module Structurate

## Fișierul Geometry/Sphere.hs

```
module Geometry.Sphere ( volume, area ) where volume :: Float \rightarrow Float volume radius = (4.0 \ / \ 3.0) \ * pi * (radius ^ 3) area :: Float \rightarrow Float area radius = 4 \ * pi * (radius ^ 2)
```

#### Fisierul Geometry/Cuboid.hs

```
module Geometry.Cuboid ( volume, area ) where
volume :: Float -> Float -> Float -> Float
volume a b c = rectangleArea a b * c
area :: Float -> Float -> Float
area a b c = rectangleArea a b * 2 +
    rectangleArea a c * 2 + rectangleArea c b * 2
rectangleArea :: Float -> Float
rectangleArea a b = a * b
```

```
Fisierul Geometry/Cube.hs
module Geometry.Cube (volume, area) where
import qualified Geometry.Cuboid as Cuboid
volume :: Float -> Float
volume side = Cuboid.volume side side
area :: Float -> Float
area side = Cuboid.area side side
```

#### Fisierul Main.hs

```
import qualified Geometry.Sphere as Sphere (volume)
import Geometry.Cuboid (volume)
import Geometry.Cube hiding (volume)
```

## **Abstractizare**

## Multimi implementate folosind liste

Fișierul SetListImpl.hs

(1)

```
module SetListImpl
(Set, empty, insert, set, element, equal, check) where
import Test. QuickCheck
type Set a = [a]
empty :: Set a
empty = []
insert :: a -> Set a -> Set a
insert x xs = x:xs
set :: [a] -> Set a
set xs = xs
```

## Multimi implementate folosind liste

Fișierul SetListImpl.hs

(2)

```
element :: Eq a => a -> Set a -> Bool
x 'element' xs = x 'elem' xs

equal :: Eq a => Set a -> Set a -> Bool
xs 'equal' ys = xs 'subset' ys && ys 'subset' xs
    where
    xs 'subset' ys = and [ x 'elem' ys | x <- xs ]</pre>
```

## Multimi implementate folosind liste

Proprietăți și teste

### Fişierul SetListImpl.hs

(3)

```
prop_element :: [Int] -> Bool
prop_element ys =
   and [ x 'element' s == odd x | x <- ys ]
   where
    s = set [ x | x <- ys, odd x ]
check =
    quickCheck prop_element</pre>
```

#### **GHCI**

```
SetListImpl> check
+++ OK, passed 100 tests.
```

Fișierul SetListImplTest.hs

```
module SetListImplTest where
import SetListImpl
test :: Int -> Bool
test n =
    s 'equal' t
    where
    s = set [1,2..n]
    t = set [n,n-1..1]

breakAbstraction :: Set a -> a
```

Fișierul SetListImplTest.hs

```
module SetListImplTest where
import SetListImpl
test :: Int -> Bool
test n =
    s 'equal' t
    where
    s = set [1,2..n]
    t = set [n,n-1..1]

breakAbstraction :: Set a -> a
breakAbstraction = head
```

Fișierul SetListImplTest.hs

```
module SetListImplTest where
import SetListImpl
test :: Int -> Bool
test n =
   s 'equal' t
  where
    s = set [1,2..n]
    t = set [n, n-1..1]
breakAbstraction :: Set a -> a
breakAbstraction = head
```

Nu e functie

Fișierul SetListImplTest.hs

```
module SetListImplTest where
import SetListImpl
test :: Int -> Bool
test n =
   s 'equal' t
  where
    s = set [1,2..n]
    t = set [n, n-1..1]
breakAbstraction :: Set a -> a
breakAbstraction = head

    Nu e functie

head (set [1,2,3]) == 1 /= 3 == head (set [3,2,1])
```

# Încapsulare

```
module SetListAbs
(Set, empty, insert, set, element, equal, check) where
import Test. QuickCheck
data Set a = MkSet [a]
empty :: Set a
empty = MkSet []
insert :: a -> Set a -> Set a
insert x (MkSet xs) = MkSet (x:xs)
set :: [a] -> Set a
set xs = MkSet xs
```

## Încapsulare

#### Proprietăți și teste

```
Fișierul SetListAbs.hs
```

```
(3)
```

```
prop_element :: [Int] -> Bool
prop_element ys =
    and [ x 'element' s == odd x | x <- ys ]
    where
    s = set [ x | x <- ys, odd x ]

check =
    quickCheck prop_element</pre>
```

#### **GHCI**

```
SetListAbs > check
+++ OK, passed 100 tests.
```

Fișierul SetListAbsTest.hs

```
module SetListAbsTest where
import SetListAbs
test :: Int -> Bool
test n =
    s 'equal' t
    where
    s = set [1,2..n]
    t = set [n,n-1..1]
breakAbstraction :: Set a -> a
```

Fișierul SetListAbsTest.hs

```
module SetListAbsTest where
import SetListAbs
test :: Int -> Bool
test n =
   s 'equal' t
  where
    s = set [1, 2..n]
    t = set [n, n-1..1]
breakAbstraction :: Set a -> a
breakAbstraction = head -- eroare de tipuri
```

## Încapsulare = Ascundere de informație

### **module** ListAbs(Set,empty,**insert**,set,element,equal)

```
> ghci SetListAbs.hs
Ok, modules loaded: SetListAbs
*SetListAbs> let s0 = set [2,7,1,8,2,8]
*SetListAbs> let MkSet xs = s0 in xs
Not in scope: data constructor 'MkSet'
```

#### **module** SetListAbs(Set(MkSet),empty,**insert**,set,element,equal)

```
> ghci SetListAbs.hs
*SetListAbs> let s0 = set [2,7,1,8,2,8]
*SetListAbs> let MkSet xs = s0 in xs
[2,7,1,8,2,8]
*SetListAbs> head xs
```

## Clase de tipuri

## Test de apartenență

Folosind descrieri de liste

Folosind recursivitate

Folosind functii de nivel înalt

elem :: Eq 
$$a \Rightarrow a \rightarrow [a] \rightarrow Bool$$

#### Folosind descrieri de liste

elem 
$$x ys = or [x == y | y <- ys]$$

#### Folosind recursivitate

elem 
$$x [] = False$$
  
elem  $x (y:ys) = x == y || elem x ys$ 

#### Folosind functii de nivel înalt

elem x ys = foldr (||) False (map 
$$(x ==) ys$$
)

#### Dar nu pentru orice tip

```
*Main> elem 1 [2,3,4]
False
*Main> elem 'o' "word"
True
*Main> elem (1, 'o') [(0, 'w'),(1, 'o'),(2, 'r'),(3, 'd')]
True
*Main> elem "word" ["list", "of", "word"]
True
*Main> elem (\langle x - \rangle x) [(\langle x - \rangle - x), (\langle x - \rangle - (-x))]
No instance for (Eq (a \rightarrow a)) arising from a use of 'elem'
Possible fix: add an instance declaration for (Eq (a -> a))
```

## Clasa de tipuri pentru egalitate

```
class Eq a where
 (==) :: a -> a -> Bool
instance Eq Int where
 (==) = eaInt
instance Eq Char where
                 = ord \times == ord \vee
 X == V
instance (Eq a, Eq b) => Eq (a,b) where
 (u,v) == (x,y) = (u == x) && (v == v)
instance Eq a => Eq [a] where
          = True
 [] == []
 [] == y:ys = False
           = False
 x:xs == []
 x:xs == y:ys = (x == y) && (xs == ys)
```

## Clasă de tipuri = dicționar de funcții

```
type EqDict a = EqD \{ eq :: a \rightarrow a \rightarrow Bool \}
elem :: EqDict a \rightarrow a \rightarrow [a] \rightarrow Bool
```

Folosind descrieri de liste

Folosind recursivitate

Folosind functii de nivel înalt

```
type EqDict a = EqD \{ eq :: a \rightarrow a \rightarrow Bool \}
elem :: EqDict a \rightarrow a \rightarrow [a] \rightarrow Bool
```

Folosind descrieri de liste

```
elem (EqD eq) x ys = or [x 'eq' y | y < -ys]
```

#### Folosind recursivitate

#### Folosind functii de nivel înalt

```
elem d \times ys = foldr (||) False (map (eq d x) ys)
```

```
dInt :: EqDict Int
dInt = EqD eqInt
dChar :: EqDict Char
dChar = EqD (\ x \ y \rightarrow ord \ x == ord \ y)
dPair :: (EqDict a, EqDict b) -> EqDict (a,b)
dPair (EqD eqa, EqD eqb) = EqD eq
  where (u,v) 'eq' (x,y) = (u 'eqa' x) && (v 'eqb' y)
dList :: EqDict a -> EqDict [a]
dList (EqD eqa) = EqD eq
 where
    [] 'eq' [] = True
    [] 'eq' (y:ys) = False
    (x:xs) 'eq [] = False
    (x:xs) 'eq' (y:ys) = (x 'eqa' y) && (xs 'eq' ys)
```

```
*Main> elem dlnt 1 [2,3,4]
False
*Main> elem dChar 'o' "word"
True
*Main> elem (dPair (dInt,dChar))
             [(1, 'o'), [(0, 'w'), (1, 'o'), (2, 'r'), (3, 'd')]
True
*Main> elem (dList dChar) "word" ["list", "of", "word"]
True
```

## Eq, Ord, Show

## Eq, Ord, Show

```
class Eq a where
  (==) :: a -> a -> Bool
  (/=) :: a -> a -> Bool
 -- minimum definition: (==)
 x /= v = not (x == v)
class (Eq a) => Ord a where
 (<) :: a \rightarrow a \rightarrow Bool
 (<=) :: a -> a -> Bool
 (>) :: a -> a -> Bool
 (>=) :: a -> a -> Bool
 -- minimum definition: (<=)</pre>
 x < y = x <= y && x /= y
 X > Y = Y < X
 X >= V = V <= X
```

class Show a where
show :: a -> String

## Bool

```
instance Eq Bool where
 False == False = True
 False == True = False
 True == False = False
 True == True = True
instance Ord Bool where
 False <= False = True
 False <= True = True
 True <= False = False
 True <= True = True
instance Show Bool where
 show False = "False"
 show True = "True"
```

### Perechi

```
instance (Eq a, Eq b) => Eq (a,b) where
  (x,y) == (x',y') = x == x' && y == y'

instance (Ord a, Ord b) => Ord (a,b) where
  (x,y) <= (x',y') = x < x' || (x == x' && y <= y')

instance (Show a, Show b) => Show (a,b) where
  show (x,y) = "(" ++ show x ++ "," ++ show y ++ ")"
```

## Liste

```
instance Eq a => Eq [a] where
  [] == [] = True
  [] == (y:ys) = False
 (x:xs) == [] = False
  (x:xs) == (y:ys) = x == y & xs == ys
instance Ord a => Ord [a] where
  [] <= ys = True
 (x:xs) \leftarrow [] = False
  (x:xs) \leftarrow (y:ys) = x < y \mid \mid (x == y && xs <= ys)
instance Show a => Show [a] where
 show [] = "[]"
 show (x:xs) = "[" ++ showSep x xs ++ "]"
   where
     showSep x [] = show x
     showSep x (y:ys) = show x ++ "," ++ showSep y ys
```

## Derivare automata pentru tipuri algebrice

```
data Bool = False | True
          deriving (Eq, Ord, Show)

data Pair a b = MkPair a b
          deriving (Eq, Ord, Show)

data List a = Nil | Cons a (List a)
          deriving (Eq, Ord, Show)
```

## Mulțimi ca instanță a lui Eq

```
instance Eq (Set a) where
s == t = s 'equal' t
```

#### Observatie

- Diferit față de implementarea implicită dată de deriving
- Deoarece egalitatea de mulțimi e mai mult decât egalitatea sintactică

## Numere

## Clase de tipuri pentru numere

```
class (Eq a, Show a) \Rightarrow Num a where
  (+),(-),(*) :: a -> a -> a
 negate :: a -> a
 fromInteger -> a
 -- minimum definition: (+),(-),(*),fromInteger
 negate x = fromInteger 0 - x
class (Num a) => Fractional a where
  (/)
       :: a -> a -> a
 recip :: a -> a
 fromRational :: Rational -> a
 — minimum definition: (/), fromRational
 recip x = 1/x
class (Num a, Ord a) => Real a where
 toRational :: a -> Rational
class (Real a, Enum a) => Integral a where
 div, mod :: a \rightarrow a \rightarrow a
 tolnteger :: a -> Integer
```

## Instanțe pentru tipul predefinit Float

### Să definim numerele naturale

Fișierul Natural.hs

(1)

```
module Natural (Nat) where
import Test. QuickCheck
data Nat = MkNat Integer
invariant :: Nat -> Bool
invariant (MkNat x) = x >= 0
instance Eq Nat where
  MkNat x == MkNat y = x == y
instance Ord Nat where
  MkNat x \le MkNat y = x \le y
instance Show Nat where
```

**show** (MkNat x) = show x

### Teste de consistentă

```
Fisierul Natural.hs
                                      (3)
  prop plus :: Integer -> Integer -> Property
  prop plus m n =
     (m >= 0) \&\& (n >= 0) ==> (m+n >= 0)
  prop times :: Integer -> Integer -> Property
  prop times m n =
     (m >= 0) \&\& (n >= 0) ==> (m*n >= 0)
  prop minus :: Integer -> Integer -> Property
  prop minus m n =
     (m >= 0) \&\& (n >= 0) \&\& (m >= n) ==> (m-n >= 0)
```

#### Fisierul NaturalTest.hs

module NaturalTest where **import** Natural

```
m, n :: Nat
m = fromInteger 2
n = fromInteger 3
```

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#### **Testare**

```
> ghci NaturalTest
Ok, modules loaded: NaturalTest, Natural.
* NaturalTest > m
2
*NaturalTest> n
3
* NaturalTest > m+n
5
*NaturalTest> n-m
* NaturalTest > m-n
*** Exception: -1 is negative
* NaturalTest > m*n
6
*NaturalTest> fromInteger (-5) :: Nat
*** Exception: -5 is negative
*NaturalTest> MkNat (-5)
Not in scope: data constructor 'MkNat'
```