

$$\lambda = \frac{c}{f}, \text{ if } d < \frac{\lambda}{10} \Rightarrow \text{instant.}$$

$$I = \frac{\Delta Q}{\Delta t} \quad P = I \cdot V = I^2 R = \frac{V^2}{R}$$

$$I = \frac{V}{R} \quad R = \rho \cdot \frac{l}{A}$$

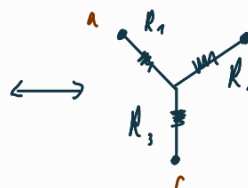
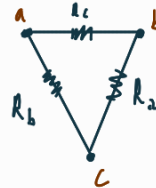
$$\frac{1}{R_{eq||}} = \sum \frac{1}{R_i} \quad R_{eq \text{ series}} = \sum R_i$$

$$\text{KCL: } \sum I_i = 0 \text{ in a node}$$

$$\text{KVL: } \sum V_i = 0 \text{ in a loop}$$

$$R \text{ in series, for } R_i: V_i = \frac{R_i}{\sum R_j} \cdot V$$

$$2 R \text{ in parallel: } I_1 = \frac{R_2}{R_1 + R_2} (I_1 + I_2)$$



$$P = R_1 R_2 + R_2 R_3 + R_1 R_3$$

$$S = R_a + R_b + R_c$$

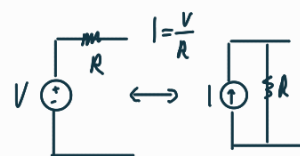
$$R_1 = \frac{R_b R_c}{S} \quad R_2 = \frac{R_a R_c}{S} \quad R_3 = \frac{R_a R_b}{S}$$

$$R_a = \frac{P}{R_1} \quad R_b = \frac{P}{R_2} \quad R_c = \frac{P}{R_3}$$

NVM: KCL equations in nodes

MCM: KVL equations in meshes

source transformation:



Thévenin 1) only independent sources

- short V - open C  
- calculate  $R_{Th} = R_{eq}$

Thévenin 2) otherwise:

- deactivate independent sources like in 1)  
- apply test C/V then calculate the other one;  $R_{Th} = \frac{V_T}{I_T}$

for max power:  $R_L = R_{Th}$

$$P = \frac{V_{Th}^2}{4 R_{Th}}$$

$V = L \frac{di}{dt}$	$I = C \frac{dv}{dt}$	average power: $p = \frac{1}{2} R \cdot I^2$	$L_{eq} = \sum L_i$ series	$\frac{1}{L_{eq  }} = \sum \frac{1}{L_i}$	$Z_L = j\omega L$
$\omega = \frac{1}{T} \cdot L$	$\omega = \frac{1}{T} \cdot C V^2$	$M = \sqrt{L_1 \cdot L_2}$ coupling coeff.	$\frac{1}{C_{eq  }} = \sum \frac{1}{C_i}$ series	$C_{eq} = \sum C_i$	$Z_C = \frac{1}{j\omega C}$
$p = i \cdot V = i \cdot L \cdot \frac{di}{dt}$	$p = V \cdot i = V \cdot C \cdot \frac{dv}{dt}$	$\omega = 2\pi f$			$\frac{1}{j} = -j$

$p e^{i\theta} = p (\cos \theta + i \sin \theta)$   $i(t) = i_0 \cos(\omega t + \theta) = i_0 \angle \theta$   $V(t) = V_0 \cos(\omega t + \theta) = V_0 \angle \theta$

RL:  $\tau = \frac{L}{R}$  natural resp.:  $i(t) = i_0 \cdot e^{-\frac{t}{\tau}}$  step resp.:  $i(t) = \frac{V_s}{R} + (i_0 - \frac{V_s}{R}) e^{-\frac{t}{\tau}}$   $v(t) = (V_s - IR) e^{-\frac{t}{\tau}}$

RC:  $\tau = RC$  natural resp.:  $v(t) = V_0 \cdot e^{-\frac{t}{\tau}}$  step resp.:  $i(t) = (i_s - \frac{V_0}{R}) e^{-\frac{t}{\tau}}$   $v(t) = V_s + (V_0 - V_s) e^{-\frac{t}{\tau}}$

RLC:  $s^2 + 2\zeta s + \omega_0^2 = 0$   $C \& L \text{ in } || \Rightarrow \zeta = \frac{1}{2RC}$   $\zeta > \omega_0$  over damped  
 $\omega_0 = \frac{1}{\sqrt{LC}}$   $s_{1,2} = -\zeta \pm \sqrt{\zeta^2 - \omega_0^2}$   $C \& L \text{ in series} \Rightarrow \zeta = \frac{R}{2L}$   $\zeta < \omega_0$  under damped  
 $\zeta = \omega_0$  critically damped

natural resp: parallel:  $x(t) = v(t)$  | series:  $x(t) = i_L(t) = i_c(t)$

over:  $x(t) = A_1 e^{s_1 t} + A_2 e^{s_2 t}$   $x(0) = A_1 + A_2$   $x'(0) = A_1 s_1 + A_2 s_2$

under:  $x(t) = (B_1 \cos(\omega_d t) + B_2 \sin(\omega_d t)) e^{-\zeta t}$   $\omega_d = \sqrt{\omega_0^2 - \zeta^2}$   $x(0) = B_1$   $x'(0) = -\zeta B_1 + \omega_d B_2$

crit:  $x(t) = (D_1 t + D_2) e^{-\zeta t}$   $x(0) = D_2$   $x'(0) = D_1 - \zeta D_2$

step resp: parallel:  $x(t) = v_c(t)$  | series:  $x(t) = v_L(t)$   $x_f = x(\infty)$

over:  $x(t) = x_f + A_1 e^{s_1 t} + A_2 e^{s_2 t}$   $x(0) = x_f + A_1 + A_2$   $x'(0) = A_1 s_1 + A_2 s_2$

under:  $x(t) = x_f + (B_1 \cos \omega_d t + B_2 \sin \omega_d t) e^{-\zeta t}$   $x(0) = x_f + B_1$   $x'(0) = -\zeta B_1 + \omega_d B_2$

crit:  $x(t) = x_f + (D_1 + D_2 t) e^{-\zeta t}$   $x(0) = x_f + D_2$   $x'(0) = D_1 - \zeta D_2$

Energy in RL:  $\frac{1}{2} L_1 i_1^2 + \frac{1}{2} L_2 i_2^2 + \dots + M i_1 i_2 + \dots$

Volume charge density:  $\rho$   
 Current:  $I$ ; E potential:  $V$   
 Volume current density:  $\vec{J}$   
 Electric field intensity:  $\vec{E}$   
 Electric flux density:  $\vec{D}$   
 Magnetic field intensity:  $\vec{H}$   
 Magnetic flux density:  $\vec{B}$   
 M potential:  $A$

ES: Gauss law:  $\oint \vec{E} \cdot d\vec{S} = \frac{Q_{\text{int}}}{\epsilon_0}$   
 no MF:  $\begin{cases} \nabla \times \vec{E} = 0 \\ \nabla \cdot \vec{E} = \frac{\rho}{\epsilon_0} \end{cases} \Rightarrow \oint \vec{E} \cdot d\vec{l} = 0, \oint \vec{E} \cdot d\vec{s} = \frac{Q}{\epsilon_0}$   
 Coulomb's law:  $\vec{F} = \frac{1}{4\pi\epsilon_0} \cdot \frac{q_1 q_2}{R^2}$   
 $\vec{E} = -\nabla V$ ; Joules:  $P = \int_V (\vec{E} \cdot \vec{J}) dV$   
 Ohm: micro  $\vec{J} = \sigma \vec{E}$ , macro:  $I = \frac{V}{R}$   
 equation of continuity:  $\nabla \cdot \vec{J} = -\frac{\partial \rho}{\partial t}$

MS: Ampere's law:  $\frac{1}{\mu_0} \oint \vec{B} \cdot d\vec{l} = I$   
 Gauss law:  $\oint \vec{B} \cdot d\vec{S} = 0$ , solenoid wtf:  $B = \mu_0 n I$   
 $\nabla \cdot \vec{B} = 0 \Rightarrow$  Poisson:  $\nabla^2 A = -\mu_0 \vec{J} \Rightarrow \nabla^2 V = -\frac{\rho}{\epsilon}$   
 $\nabla \times \vec{B} = \mu_0 \vec{J}$  | Biot-Savart:  $\vec{B} = \int_C d\vec{B}$   
 M dipole moment:  $\vec{m} = \vec{a}_m |S$ , self inductance  $L_{11} = \frac{\lambda_{11}}{I_1}$   
 M energy:  $W = \frac{1}{2} \sum_{k=1}^N I_k \Phi_k$ ;  $W_m = \frac{1}{2} \int_V (\vec{A} \cdot \vec{J}) dV$ ; M force:  $\vec{F}_m = I \oint d\vec{l} \times \vec{B}$

Maxwell: ES/MS independent  
 integral:  $\oint \vec{D} \cdot d\vec{s} = Q_{\text{encl.}}$   
 $\oint \vec{E} \cdot d\vec{l} = 0$   
 $\oint \vec{B} \cdot d\vec{s} = 0$   
 $\oint \vec{H} \cdot d\vec{l} = I_{\text{encl.}}$   
 diff:  $\nabla \cdot \vec{D} = \rho_v$   
 $\nabla \times \vec{E} = 0$   
 $\nabla \cdot \vec{B} = 0$   
 $\nabla \times \vec{H} = \vec{J}$

Time varying (dynamic)  
 $\oint \vec{D} \cdot d\vec{s} = Q_{\text{encl.}}$   
 $\oint \vec{E} \cdot d\vec{l} = -\int_S \frac{\partial \vec{B}}{\partial t} \cdot d\vec{S}$   
 $\oint \vec{B} \cdot d\vec{s} = 0$   
 $\oint \vec{H} \cdot d\vec{l} = I_{\text{encl.}} + \int_S \frac{\partial \vec{D}}{\partial t} \cdot d\vec{S}$   
 $\nabla \cdot \vec{D} = \rho_v$   
 $\nabla \times \vec{E} = -\frac{\partial \vec{B}}{\partial t}$   
 $\nabla \cdot \vec{B} = 0$   
 $\nabla \times \vec{H} = \vec{J} + \frac{\partial \vec{D}}{\partial t}$  where:  $\nabla \cdot \vec{J} = -\frac{\partial \rho}{\partial t}$

gradient:  $\nabla V = \vec{a} \cdot \frac{dV}{dn}$   
 divergence:  $\nabla \cdot \vec{A} = \lim_{\Delta V \rightarrow 0} \frac{\oint_S \vec{A} \cdot d\vec{s}}{\Delta V} \Rightarrow \oint_S \vec{A} \cdot d\vec{s} = \int_V (\nabla \cdot \vec{A}) dV$  div. th.  
 curl:  $\nabla \times \vec{A} = \lim_{\Delta S \rightarrow 0} \frac{\oint_{\vec{a}_n} (\oint_C \vec{A} \cdot d\vec{l})}{\Delta S}$   
 Stoke's theorem:  $\nabla \times \vec{A} = \lim_{\Delta S \rightarrow 0} \frac{\oint_{\vec{a}_n} (\oint_C \vec{A} \cdot d\vec{l})}{\Delta S} \Rightarrow \oint_C \vec{A} \cdot d\vec{l} = \int_S (\nabla \times \vec{A}) \cdot d\vec{S}$   
 scalar Laplacian:  $\nabla^2 V = \nabla \cdot (\nabla V) = \frac{\partial^2 V}{\partial x^2} + \frac{\partial^2 V}{\partial y^2} + \frac{\partial^2 V}{\partial z^2}$   
 vector Laplacian:  $\nabla^2 \vec{A} = \nabla(\nabla \cdot \vec{A}) - \nabla \times \nabla \times \vec{A} = \vec{a}_x(\nabla^2 A_x) + \vec{a}_y(\nabla^2 A_y) + \vec{a}_z(\nabla^2 A_z)$   
 conservative V.F.:  $\nabla \times (\nabla V) = 0$  ES potential  
 solenoidal:  $\nabla \cdot (\nabla \times \vec{A}) = 0$  MS potential  
 Helmholtz:  $sg, sp$   
 Faraday's law:  $\oint \vec{E} \cdot d\vec{l} = -\int_S \frac{\partial \vec{B}}{\partial t} \cdot d\vec{S}$  or  $\nabla \times \vec{E} = -\frac{\partial \vec{B}}{\partial t}$   
 modified Ampere:  $\nabla \times \vec{H} = \vec{J} + \frac{\partial \vec{D}}{\partial t}$

Homogeneous Maxwell:  
 $\nabla \times \vec{E} = -\mu \frac{\partial \vec{H}}{\partial t}$   
 $\nabla \times \vec{H} = \epsilon \frac{\partial \vec{E}}{\partial t}$   
 $\nabla \cdot \vec{E} = 0$   
 $\nabla \cdot \vec{H} = 0$   
 $\frac{\partial}{\partial t} = j\omega$   
 $\nabla \times \vec{E} = -j\omega \mu \vec{H}$   
 $\nabla \times \vec{H} = j\omega \epsilon \vec{E}$   
 $\nabla \cdot \vec{E} = 0$   
 $\nabla \cdot \vec{H} = 0$   
 potentials (timevarying):  $\vec{E} = -\nabla V - \frac{\partial \vec{A}}{\partial t}$   
 $\nabla^2 \vec{A} - \mu \epsilon \frac{\partial^2 \vec{A}}{\partial t^2} = -\mu \vec{J}$   
 $\nabla^2 V - \mu \epsilon \frac{\partial^2 V}{\partial t^2} = -\frac{\rho}{\epsilon}$   
 $\vec{B} = \nabla \times \vec{A}$

$$\begin{aligned} \nabla^2 \vec{E} - \mu \epsilon \frac{\partial^2 \vec{E}}{\partial t^2} &= 0 \\ \nabla^2 \vec{H} - \mu \epsilon \frac{\partial^2 \vec{H}}{\partial t^2} &= 0 \end{aligned} \quad \text{E.M. wave propagation}$$

