

H8

c.ii) use secant method
within 10^{-3}

$$e^x = 3x + 4 \quad \text{on } [0, 4]$$

• initial guesses for x_0 and x_1 : $x_0 = 0$
 $x_1 = 4$

secant method:
$$x_{n+1} = \frac{x_n - x_{n-1}}{f(x_n) - f(x_{n-1})} \cdot f(x_n)$$

$$f(x) = e^x - 3x - 4$$

iteration 1:

$$x_0 = 0 \quad x_1 = 4$$

$$f(x_0) = e^0 - 3 \cdot 0 - 4 = -3.000 \quad (3dp)$$

$$f(x_1) = e^4 - 3 \cdot 4 - 4 = e^4 - 16 \approx 38.598 \quad (3dp)$$

$$x_2 = 4 - \frac{4 - 0}{(e^4 - 16) - (-3)} \cdot (e^4 - 16) \approx \underline{0.288} \quad (3sf)$$

$$f(x_2) = e^{0.288} - 3 \cdot (0.288) - 4 \approx \underline{-3.530} \quad (3dp)$$

iteration 2

$$x_0 = 4 \quad x_1 = 0.288$$

$$f(x_0) = -3$$

$$f(x_1) = -3.530$$

$$x = 0.288 - \frac{0.288 - 4}{-3.530 - (-3)} \cdot (-3.530) = \frac{6628}{1000} \approx 25.011$$

$$f(x_2) = e^{25.011} - 3 \cdot 25.011 - 4 =$$

iteration 3

