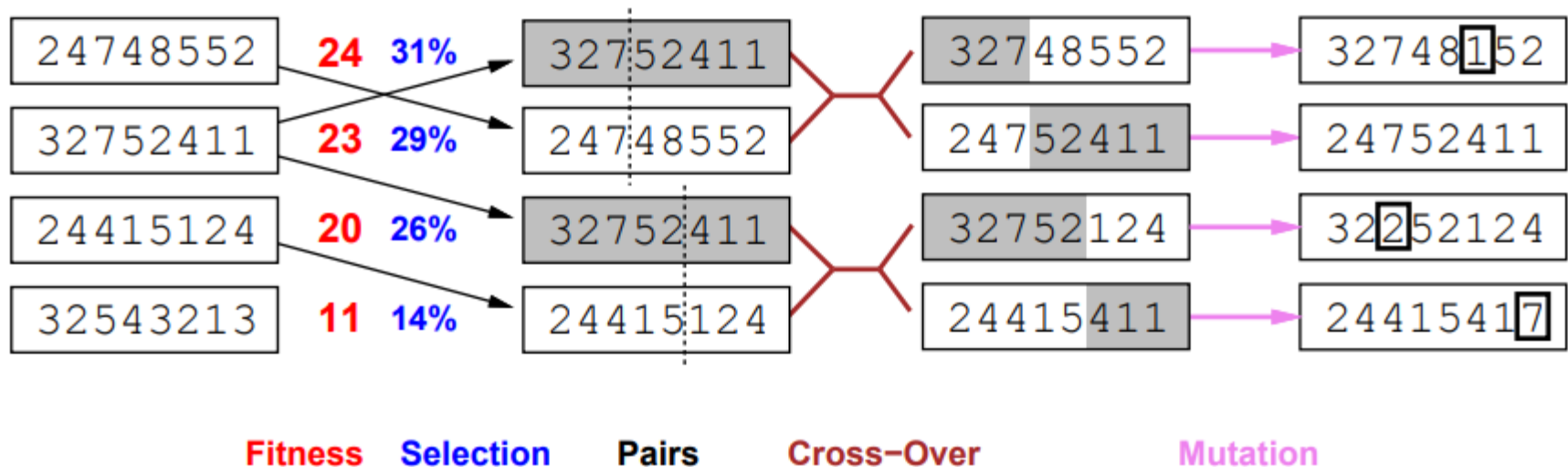


Genetic Algorithms

Chapter 4b (based on AIMA Slides)

Genetic Algorithms

= stochastic local beam search
+ generate successors from pairs of states



Genetic Algorithms

- ❖ In computer science and operations research, a **genetic algorithm (GA)** is a metaheuristic inspired by the process of natural selection that belongs to the larger class of evolutionary algorithms (EA). **Genetic algorithms** are commonly used to generate high-quality solutions to optimization and search problems by relying on bio-inspired operators such as mutation, crossover and selection.

Genetic Algorithms

- ❖ A **Genetic Algorithm** is a type of local search that mimics evolution by taking a population of strings, which encode possible solutions and combines them based on a fitness function to produce individuals that are more fit.

Selection

- ❖ **Selection** is the stage of a genetic algorithm in which individual genomes are chosen from a population for later breeding (using the crossover operator).

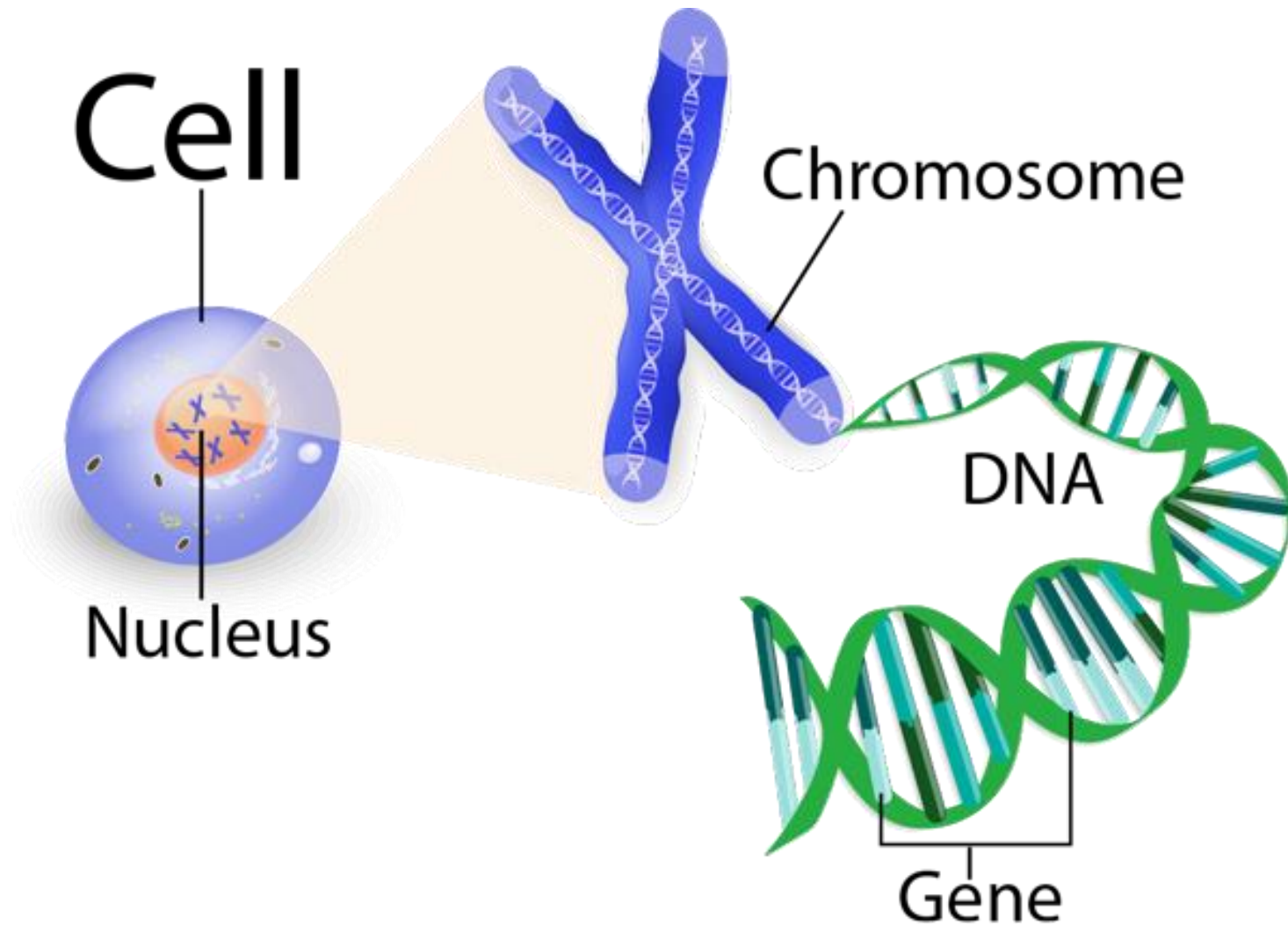
Crossover

- ❖ In GAs, **crossover** is a genetic operator used to vary the programming of a chromosome (or chromosomes) from one generation to the next. It is analogous to reproduction and biological crossover, upon which GA are based.
- ❖ **Crossover** is a process of taking more than one parent solutions and producing a child solution from them.

Mutation

- ❖ **Mutation** is a genetic operator used to maintain genetic diversity from one generation of a population of genetic algorithm chromosomes to the next. It is analogous to biological mutation. **Mutation** alters one or more gene values in a chromosome from its initial state.

GAs & Biology



GA's & Biology

Population

1	1	2	3	4	5
----------	---	---	---	---	---

2	2	1	3	4	5
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3	1	2	5	4	3
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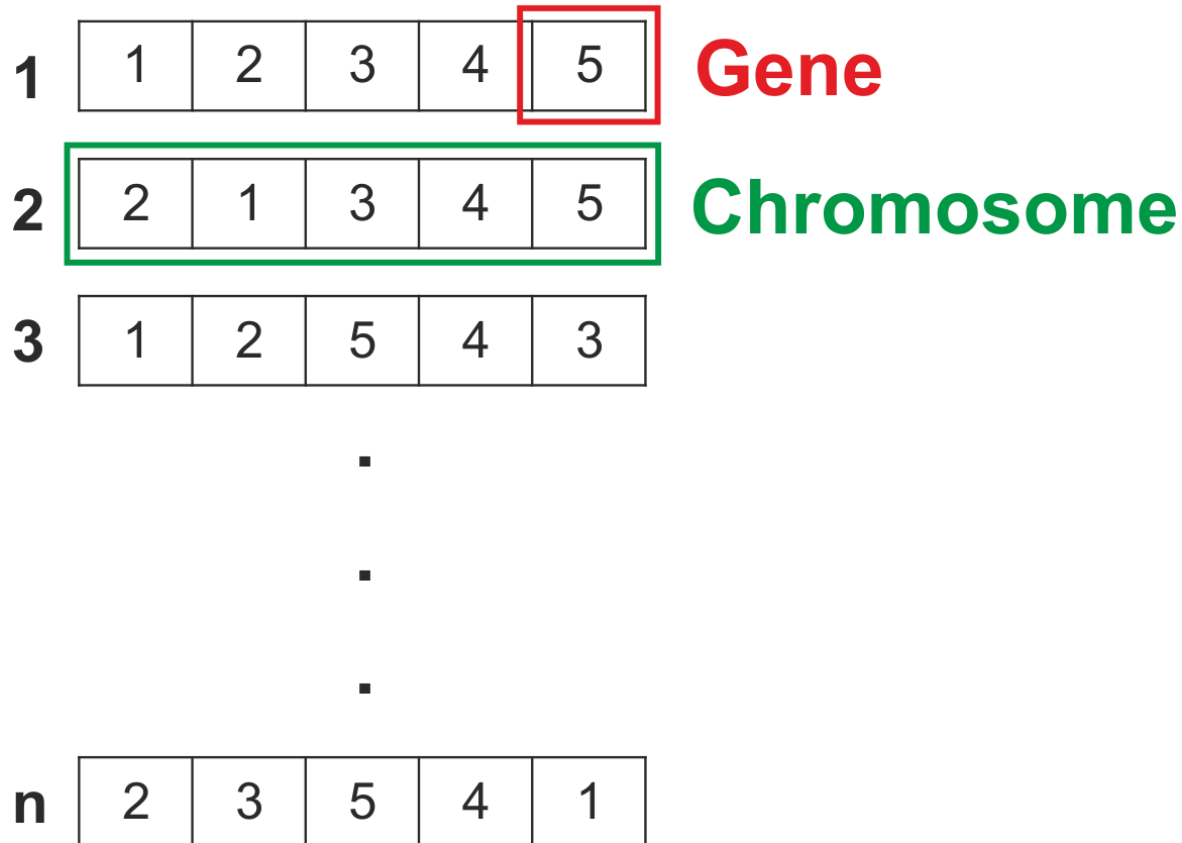
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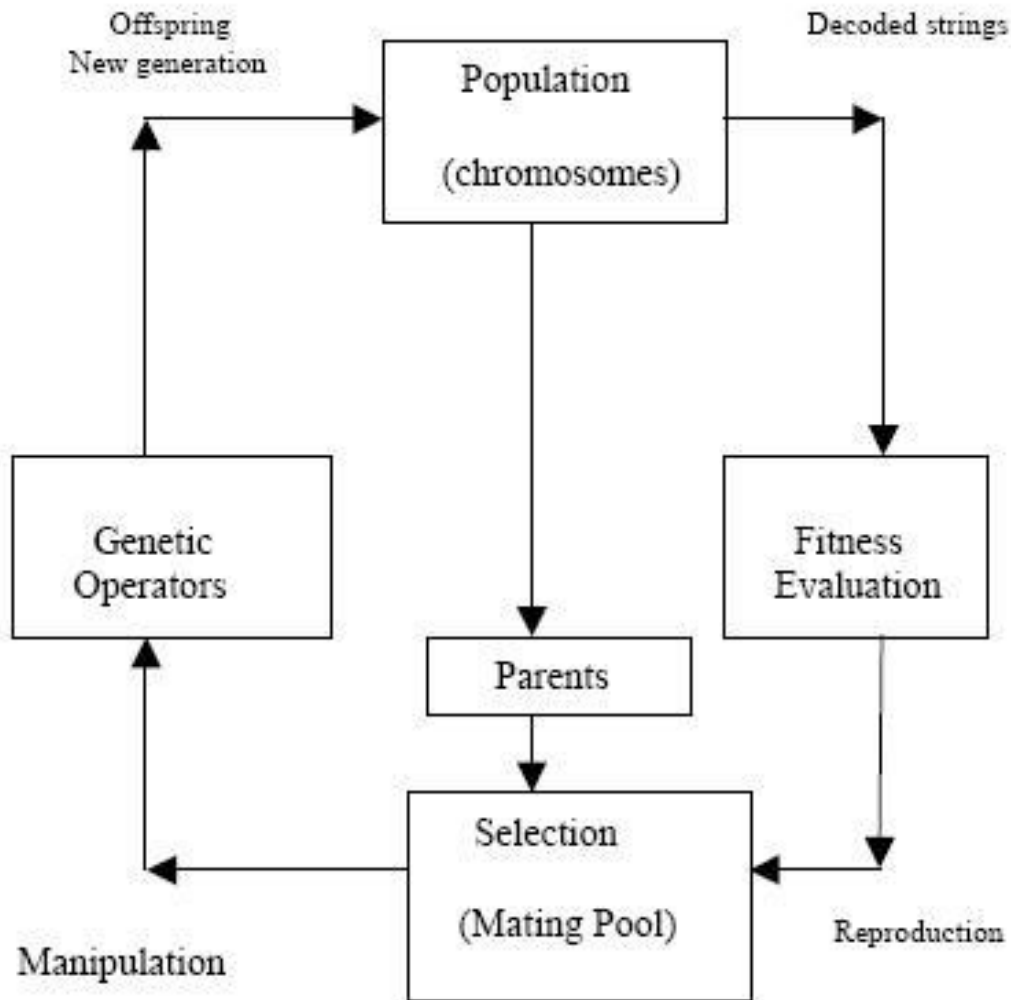
n	2	3	5	4	1
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GA's & Biology

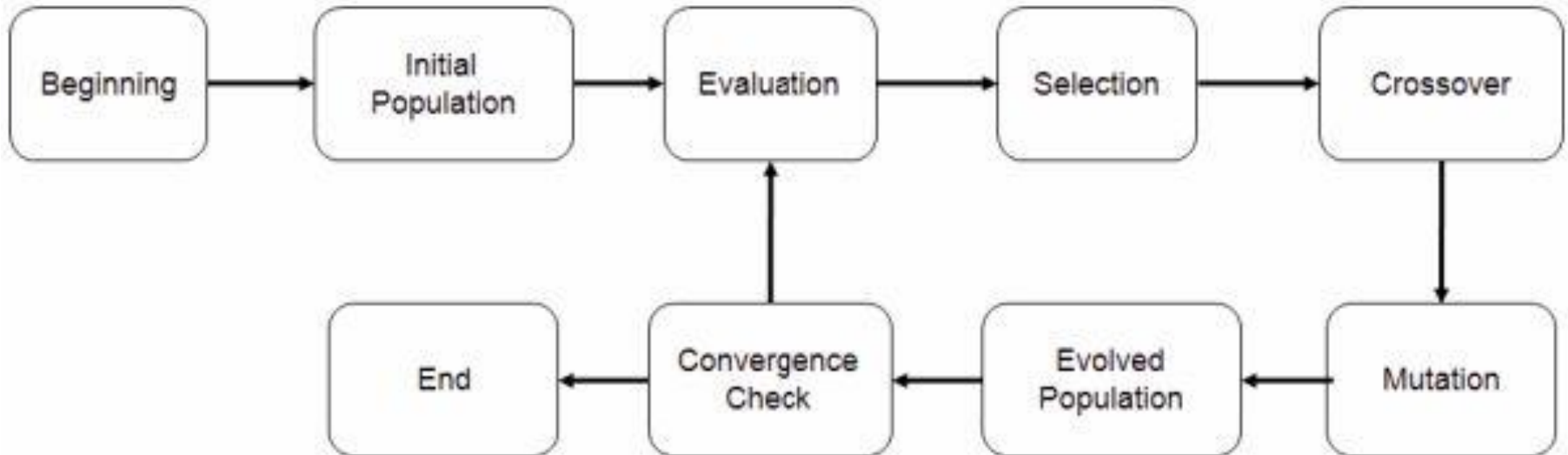
Population



GAs: The „Reproduction“ Cycle



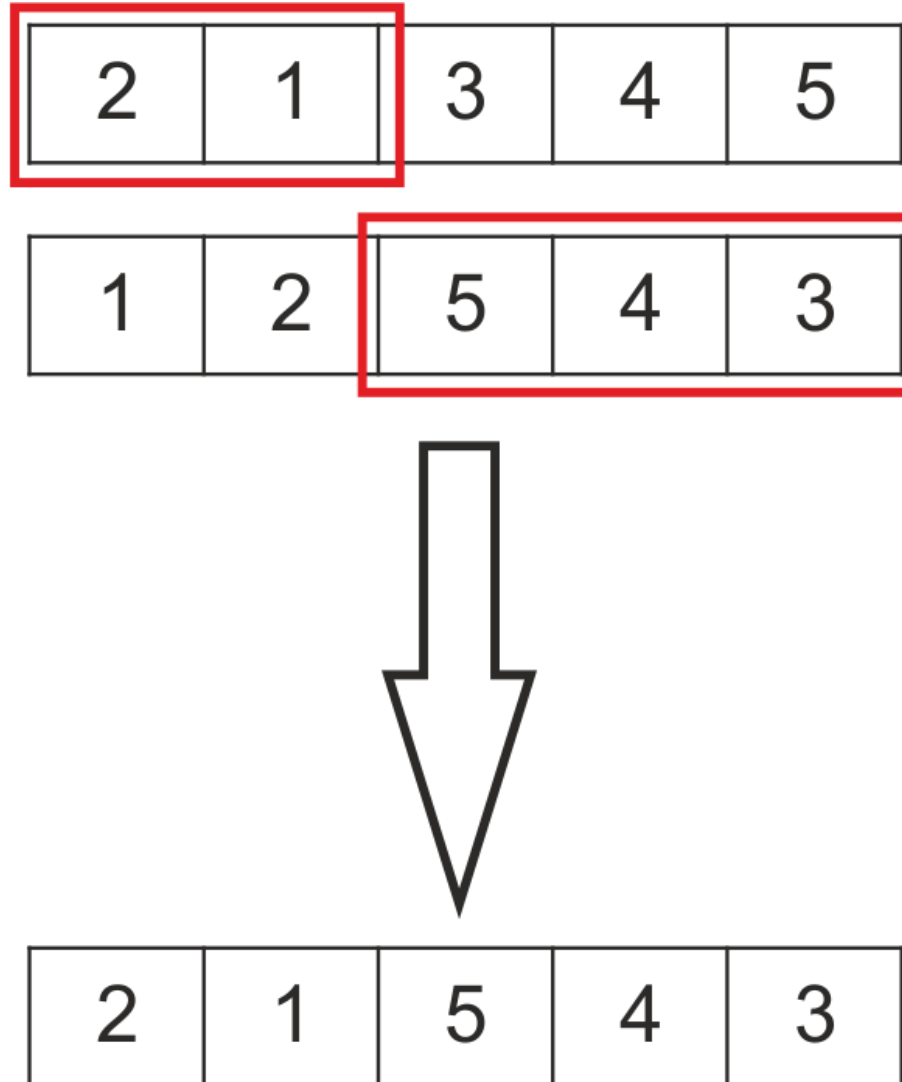
GAs: The „Reproduction“ Cycle



GA: Main Steps

- ❖ Initialization
 - ❖ Population
- ❖ **Selection**
 - ❖ Fitness Function
- ❖ **Crossover**
- ❖ **Mutation**

Crossover



One-Point Crossover

1

2

3

4

5

5

4

3

2

1

One-Point Crossover

1	2	3	4	5
---	---	---	---	---

5	4	3	2	1
---	---	---	---	---

Let's $i=3$

One-Point Crossover

1	2	3	4	5
---	---	---	---	---

5	4	3	2	1
---	---	---	---	---

Let's $i=3$

1	2	3		
---	---	---	--	--

5	4	3		
---	---	---	--	--

One-Point Crossover

1	2	3	4	5
---	---	---	---	---

5	4	3	2	1
---	---	---	---	---

Let's $i=3$

1	2	3	—	
---	---	---	---	--

5	4	3		
---	---	---	--	--

One-Point Crossover

1	2	3	4	5
---	---	---	---	---

5	4	3	2	1
---	---	---	---	---

Let's $i=3$

1	2	3	5	
---	---	---	---	--

5	4	3		
---	---	---	--	--

One-Point Crossover

1	2	3	4	5
---	---	---	---	---

5	4	3	2	1
---	---	---	---	---

Let's $i=3$

1	2	3	5	—
---	---	---	---	---

5	4	3		
---	---	---	--	--

One-Point Crossover

1	2	3	4	5
---	---	---	---	---

5	4	3	2	1
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Let's $i=3$

1	2	3	5	4
---	---	---	---	---

5	4	3		
---	---	---	--	--

One-Point Crossover

1	2	3	4	5
---	---	---	---	---

5	4	3	2	1
---	---	---	---	---

Let's $i=3$

1	2	3	5	4
---	---	---	---	---

5	4	3		
---	---	---	--	--

One-Point Crossover

1	2	3	4	5
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5	4	3	2	1
----------	----------	----------	----------	----------

Let's $i=3$

1	2	3	5	4
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5	4	3	-	
----------	----------	----------	----------	--

One-Point Crossover

1	2	3	4	5
----------	----------	----------	----------	----------

5	4	3	2	1
----------	----------	----------	----------	----------

Let's $i=3$

1	2	3	5	4
----------	----------	----------	----------	----------

5	4	3	1	
----------	----------	----------	----------	--

One-Point Crossover

1	2	3	4	5
---	---	---	---	---

5	4	3	2	1
---	---	---	---	---

Let's $i=3$

1	2	3	5	4
---	---	---	---	---

5	4	3	1	—
---	---	---	---	---

One-Point Crossover

1	2	3	4	5
---	---	---	---	---

5	4	3	2	1
---	---	---	---	---

Let's $i=3$

1	2	3	5	4
---	---	---	---	---

5	4	3	1	2
---	---	---	---	---

One-Point Crossover

1	2	3	4	5
---	---	---	---	---

5	4	3	2	1
---	---	---	---	---

Let's $i=3$

1	2	3	5	4
---	---	---	---	---

5	4	3	1	2
---	---	---	---	---

One-Point Crossover

1 2 3 4 5
5 4 3 2 1
 $i=3$ // random
D1: 1 2 3 5 4
D2: **5** 4 3 1 2

Two-Point Crossover

1	2	3	4	5	6	7
----------	----------	----------	----------	----------	----------	----------

7	6	2	4	3	5	1
----------	----------	----------	----------	----------	----------	----------

Two-Point Crossover

1	2	3	4	5	6	7
---	---	---	---	---	---	---

7	6	2	4	3	5	1
---	---	---	---	---	---	---

Let's $i=3, j=5$

Two-Point Crossover

1	2	3	4	5	6	7
---	---	---	---	---	---	---

7	6	2	4	3	5	1
---	---	---	---	---	---	---

Let's $i=3, j=5$

		3	4	5		
--	--	---	---	---	--	--

		2	4	3		
--	--	---	---	---	--	--

Two-Point Crossover

1	2	3	4	5	6	7
---	---	---	---	---	---	---

7	6	2	4	3	5	1
---	---	---	---	---	---	---

Let's $i=3, j=5$

		3	4	5	—	
--	--	---	---	---	---	--

		2	4	3		
--	--	---	---	---	--	--

Two-Point Crossover

1	2	3	4	5	6	7
---	---	---	---	---	---	---

7	6	2	4	3	5	1
---	---	---	---	---	---	---

Let's $i=3, j=5$

		3	4	5	—	
--	--	---	---	---	---	--

		2	4	3		
--	--	---	---	---	--	--

Two-Point Crossover

1	2	3	4	5	6	7
---	---	---	---	---	---	---

7	6	2	4	3	5	1
---	---	---	---	---	---	---

Let's $i=3, j=5$

		3	4	5	1	
--	--	---	---	---	---	--

		2	4	3		
--	--	---	---	---	--	--

Two-Point Crossover

1	2	3	4	5	6	7
---	---	---	---	---	---	---

7	6	2	4	3	5	1
---	---	---	---	---	---	---

Let's $i=3, j=5$

		3	4	5	1	—
--	--	---	---	---	---	---

		2	4	3		
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Two-Point Crossover

1	2	3	4	5	6	7
---	---	---	---	---	---	---

7	6	2	4	3	5	1
---	---	---	---	---	---	---

Let's $i=3, j=5$

		3	4	5	1	7
--	--	---	---	---	---	---

		2	4	3		
--	--	---	---	---	--	--

Two-Point Crossover

1	2	3	4	5	6	7
---	---	---	---	---	---	---

7	6	2	4	3	5	1
---	---	---	---	---	---	---

Let's $i=3, j=5$

—		3	4	5	1	7
---	--	---	---	---	---	---

		2	4	3		
--	--	---	---	---	--	--

Two-Point Crossover

1	2	3	4	5	6	7
---	---	---	---	---	---	---

7	6	2	4	3	5	1
---	---	---	---	---	---	---

Let's $i=3, j=5$

6		3	4	5	1	7
---	--	---	---	---	---	---

		2	4	3		
--	--	---	---	---	--	--

Two-Point Crossover

1	2	3	4	5	6	7
---	---	---	---	---	---	---

7	6	2	4	3	5	1
---	---	---	---	---	---	---

Let's $i=3, j=5$

6	—	3	4	5	1	7
---	---	---	---	---	---	---

		2	4	3		
--	--	---	---	---	--	--

Two-Point Crossover

1	2	3	4	5	6	7
---	---	---	---	---	---	---

7	6	2	4	3	5	1
---	---	---	---	---	---	---

Let's $i=3, j=5$

6	2	3	4	5	1	7
---	---	---	---	---	---	---

		2	4	3		
--	--	---	---	---	--	--

Two-Point Crossover

1	2	3	4	5	6	7
---	---	---	---	---	---	---

7	6	2	4	3	5	1
---	---	---	---	---	---	---

Let's $i=3, j=5$

6	2	3	4	5	1	7
---	---	---	---	---	---	---

		2	4	3		
--	--	---	---	---	--	--

Two-Point Crossover

1 2 3 4 5 (6) 7

7 6 2 4 3 (5) 1

Требование от индекса 6 и индекса
коде не сче сложным

D1: 6 2 3 4 5 1 7

D2: 1 5 2 4 3 6 7

Partially-mapped Crossover

1	2	3	4	5	6	7
----------	----------	----------	----------	----------	----------	----------

6	3	4	1	2	7	5
----------	----------	----------	----------	----------	----------	----------

Partially-mapped Crossover

1	2	3	4	5	6	7
---	---	---	---	---	---	---

6	3	4	1	2	7	5
---	---	---	---	---	---	---

Let's $i=3, j=5$

Partially-mapped Crossover

1	2	3	4	5	6	7
---	---	---	---	---	---	---

6	3	4	1	2	7	5
---	---	---	---	---	---	---

Let's $i=3, j=5$

		3	4	5		
--	--	---	---	---	--	--

		4	1	2		
--	--	---	---	---	--	--

Partially-mapped Crossover

1	2	3	4	5	6	7
6	3	4	1	2	7	5

Let's $i=3, j=5$

		3	4	5		
		4	1	2		

Partially-mapped Crossover

1	2	3	<u>4</u>	5	6	7
6	3	<u>4</u>	1	2	7	5

Let's $i=3, j=5$

		3	4	5		
		4	1	2		

Partially-mapped Crossover

1	2	3	4	5	6	7
---	---	---	---	---	---	---

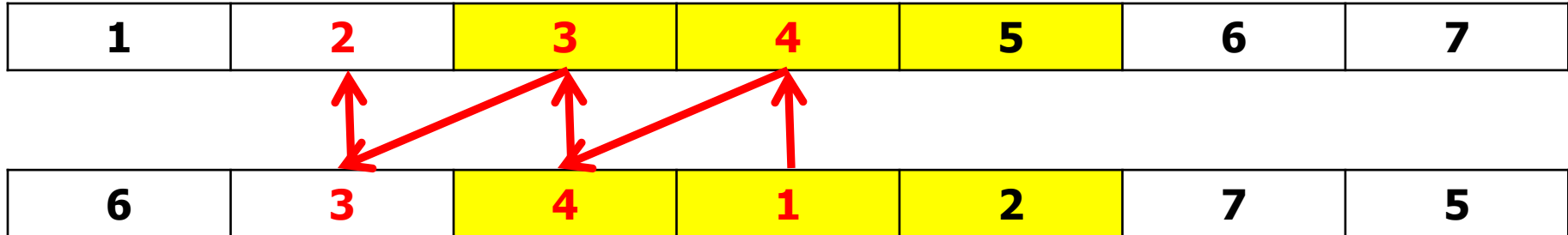
6	3	4	1	2	7	5
---	---	---	---	---	---	---

Let's $i=3, j=5$

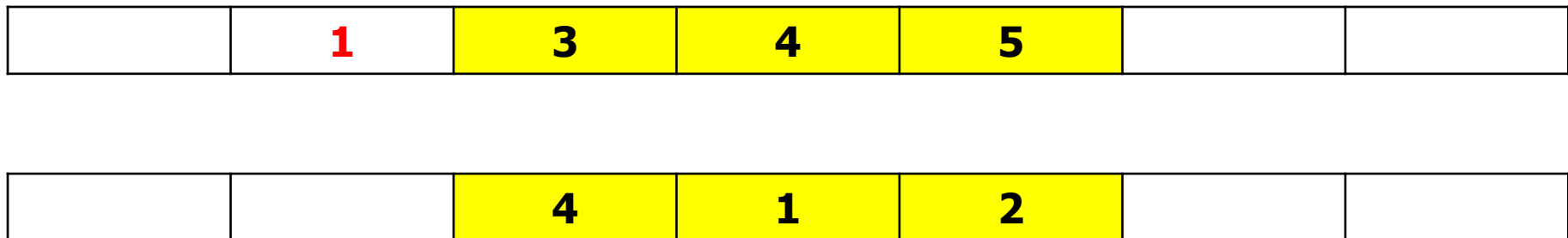
		3	4	5		
--	--	---	---	---	--	--

		4	1	2		
--	--	---	---	---	--	--

Partially-mapped Crossover



Let's $i=3, j=5$



Partially-mapped Crossover

1	2	3	4	5	6	7
---	---	---	---	---	---	---

6	3	4	1	2	7	5
---	---	---	---	---	---	---

Let's $i=3, j=5$

	1	3	4	5		
--	---	---	---	---	--	--

		4	1	2		
--	--	---	---	---	--	--

Partially-mapped Crossover

1	2	3	4	5	6	7
---	---	---	---	---	---	---

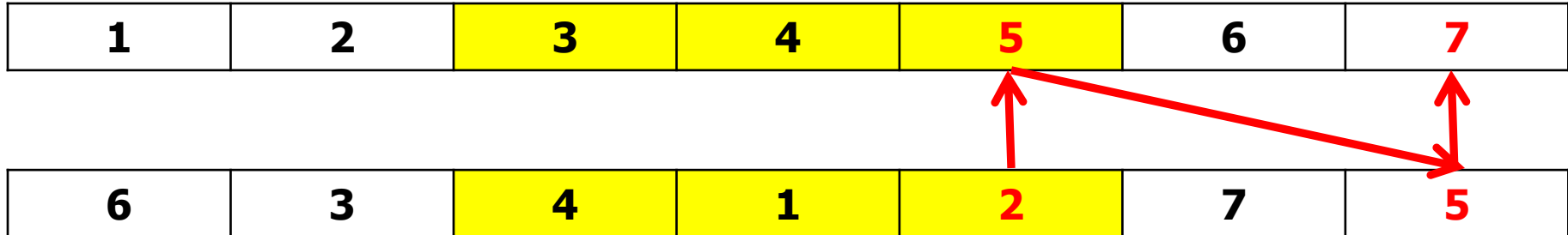
6	3	4	1	2	7	5
---	---	---	---	---	---	---

Let's $i=3, j=5$

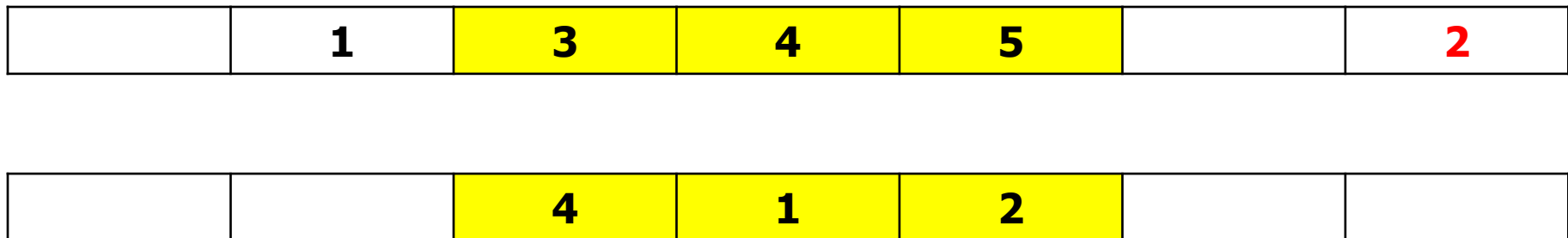
	1	3	4	5		
--	---	---	---	---	--	--

		4	1	2		
--	--	---	---	---	--	--

Partially-mapped Crossover



Let's $i=3, j=5$



Partially-mapped Crossover

1	2	3	4	5	6	7
---	---	---	---	---	---	---

6	3	4	1	2	7	5
---	---	---	---	---	---	---

Let's $i=3, j=5$

	1	3	4	5		2
--	---	---	---	---	--	---

		4	1	2		
--	--	---	---	---	--	--

Partially-mapped Crossover

1	2	3	4	5	6	7
---	---	---	---	---	---	---

6	3	4	1	2	7	5
---	---	---	---	---	---	---

Let's $i=3, j=5$

—	1	3	4	5	—	2
---	---	---	---	---	---	---

		4	1	2		
--	--	---	---	---	--	--

Partially-mapped Crossover

1	2	3	4	5	6	7
---	---	---	---	---	---	---

6	3	4	1	2	7	5
---	---	---	---	---	---	---

Let's $i=3, j=5$

6	1	3	4	5	7	2
---	---	---	---	---	---	---

		4	1	2		
--	--	---	---	---	--	--

Partially-mapped Crossover

1	2	3	4	5	6	7
---	---	---	---	---	---	---

6	3	4	1	2	7	5
---	---	---	---	---	---	---

Let's $i=3, j=5$

6	1	3	4	5	7	2
---	---	---	---	---	---	---

		4	1	2		
--	--	---	---	---	--	--

Partially-mapped Crossover

$1\ 2\ \underline{3\ 4\ 5}\ 6\ 7$
 $6\ 3\ \underline{4\ 1\ 2}\ 7\ 5$

A) compare \hookrightarrow D1 - D2
 D1: $--\ 3\ 4\ 5\ --$
 D2: $--\ 4\ 1\ 2\ --$

B) compare segments \hookrightarrow , so D1 \rightarrow 1 and 2
 $\textcircled{1} \rightarrow 4 \rightarrow 4 \rightarrow \underline{3} \rightarrow 3 \rightarrow \textcircled{2}$
 \Rightarrow D1: $--\ 1\ \underline{3\ 4\ 5}\ \text{--}$

$\textcircled{2} \rightarrow 5 \rightarrow 5 \rightarrow \textcircled{7}$
 \Rightarrow D1: $--\ 1\ \underline{3\ 4\ 5}\ --\ 2$

C) replace the remaining elements from P1 and P2
 D1: $\textcircled{6}\ 1\ \underline{3\ 4\ 5}\ \textcircled{7}\ 2$

Cycle Crossover

8	4	7	3	6	2	5	1	9	0
----------	----------	----------	----------	----------	----------	----------	----------	----------	----------

0	1	2	3	4	5	6	7	8	9
----------	----------	----------	----------	----------	----------	----------	----------	----------	----------

Cycle Crossover

8	4	7	3	6	2	5	1	9	0
---	---	---	---	---	---	---	---	---	---

0	1	2	3	4	5	6	7	8	9
---	---	---	---	---	---	---	---	---	---

--	--	--	--	--	--	--	--	--	--

--	--	--	--	--	--	--	--	--	--

Cycle Crossover

8	4	7	3	6	2	5	1	9	0
----------	----------	----------	----------	----------	----------	----------	----------	----------	----------

0	1	2	3	4	5	6	7	8	9
----------	----------	----------	----------	----------	----------	----------	----------	----------	----------

--	--	--	--	--	--	--	--	--	--

--	--	--	--	--	--	--	--	--	--

Cycle Crossover

8	4	7	3	6	2	5	1	9	0
----------	----------	----------	----------	----------	----------	----------	----------	----------	----------

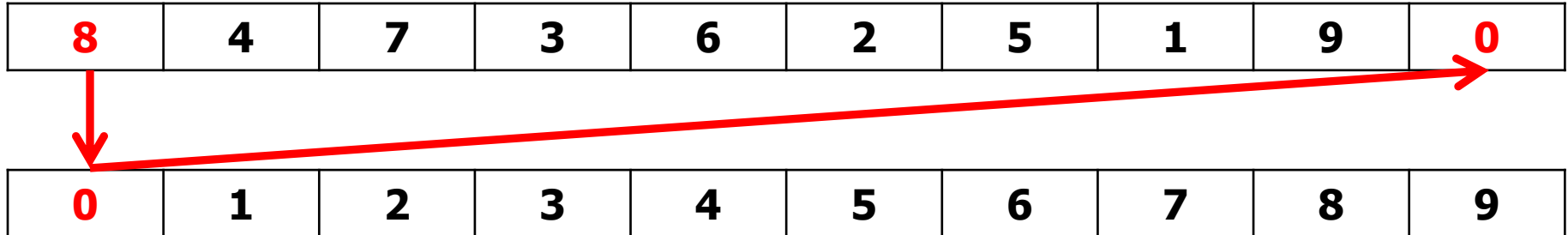


0	1	2	3	4	5	6	7	8	9
----------	----------	----------	----------	----------	----------	----------	----------	----------	----------

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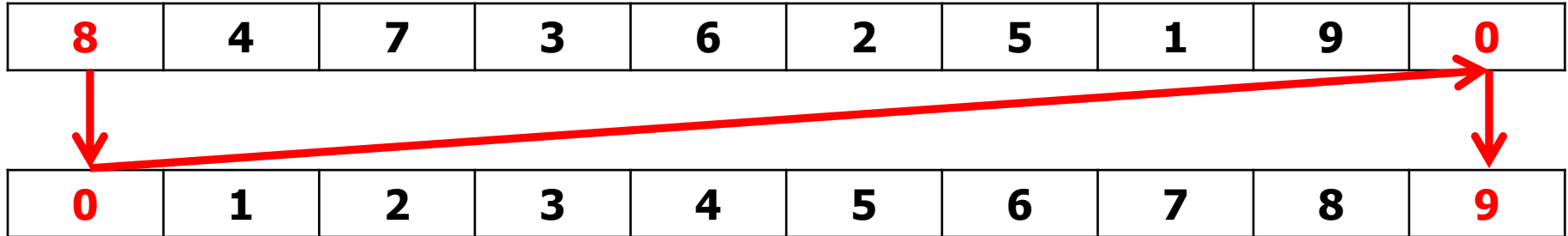
Cycle Crossover



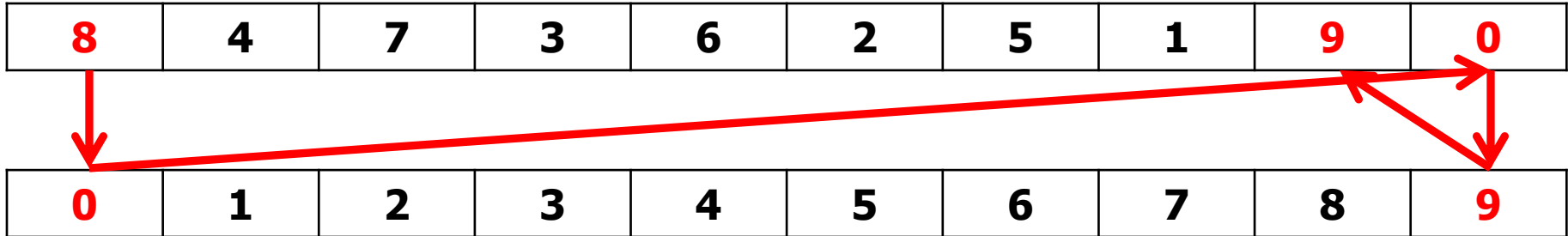
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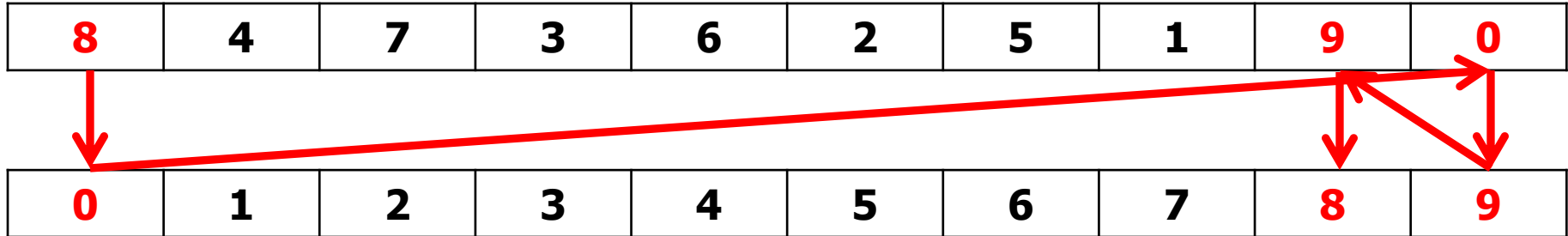
Cycle Crossover



Cycle Crossover



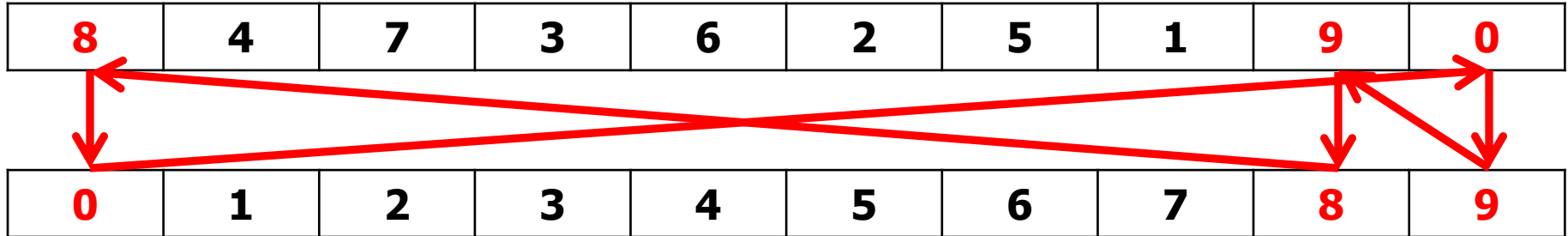
Cycle Crossover



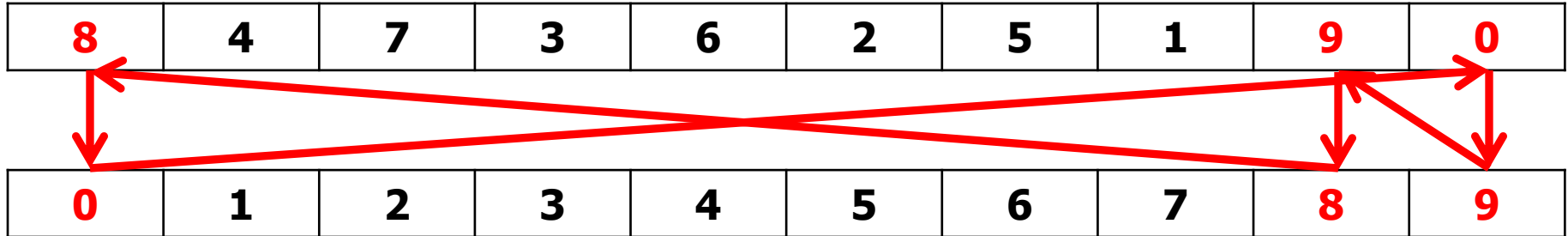
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Cycle Crossover



Cycle Crossover



8								9	0
---	--	--	--	--	--	--	--	---	---

0								8	9
---	--	--	--	--	--	--	--	---	---

Cycle Crossover

<u>8</u>	4	7	3	6	2	5	1	<u>9</u>	<u>0</u>
----------	---	---	---	---	---	---	---	----------	----------

<u>0</u>	1	2	3	4	5	6	7	<u>8</u>	<u>9</u>
----------	---	---	---	---	---	---	---	----------	----------

8								9	0
---	--	--	--	--	--	--	--	---	---

0								8	9
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Cycle Crossover

<u>8</u>	4	7	3	6	2	5	1	<u>9</u>	<u>0</u>
----------	---	---	---	---	---	---	---	----------	----------

<u>0</u>	1	2	3	4	5	6	7	<u>8</u>	<u>9</u>
----------	---	---	---	---	---	---	---	----------	----------

8								9	0
---	--	--	--	--	--	--	--	---	---

0								8	9
---	--	--	--	--	--	--	--	---	---

Cycle Crossover

<u>8</u>	4	7	3	6	2	5	1	<u>9</u>	<u>0</u>
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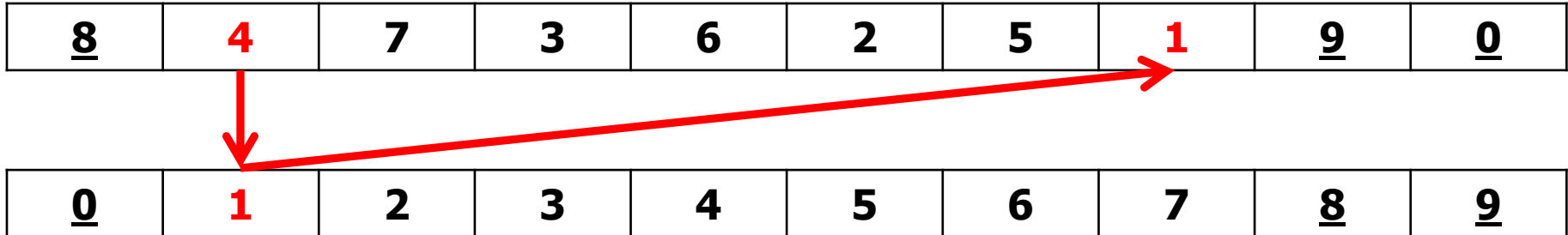


<u>0</u>	1	2	3	4	5	6	7	<u>8</u>	<u>9</u>
----------	---	---	---	---	---	---	---	----------	----------

8								9	0
---	--	--	--	--	--	--	--	---	---

0								8	9
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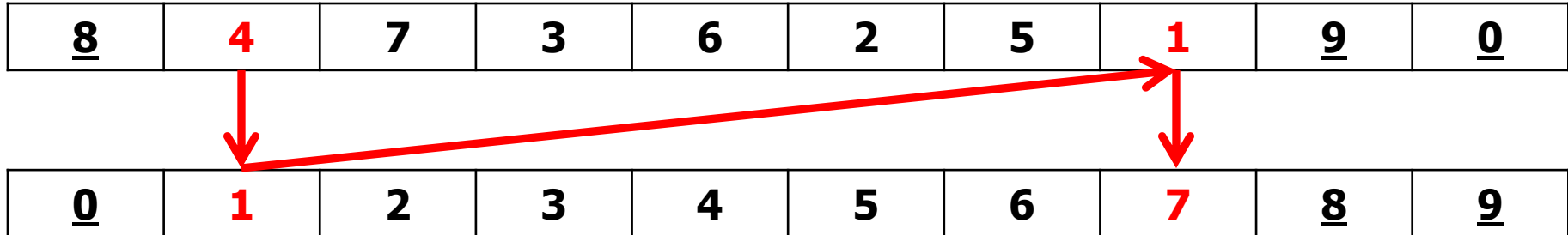
Cycle Crossover



8								9	0
---	--	--	--	--	--	--	--	---	---

0								8	9
---	--	--	--	--	--	--	--	---	---

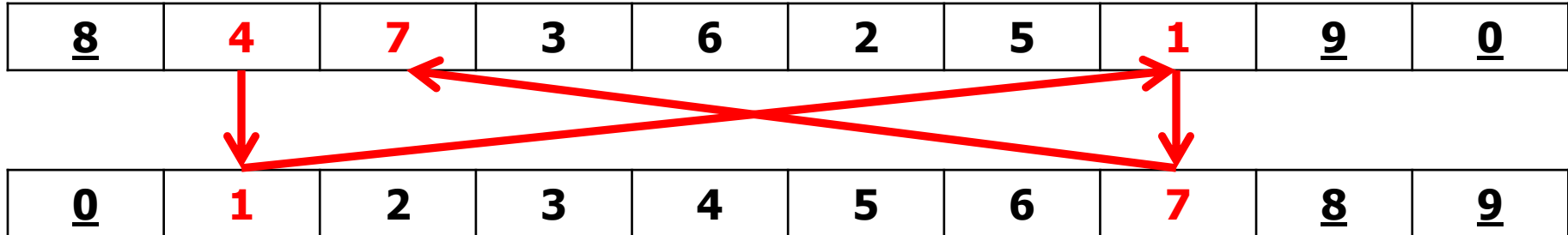
Cycle Crossover



8								9	0
---	--	--	--	--	--	--	--	---	---

0								8	9
---	--	--	--	--	--	--	--	---	---

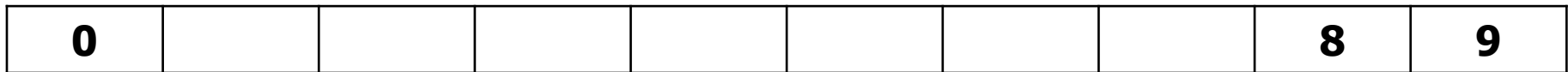
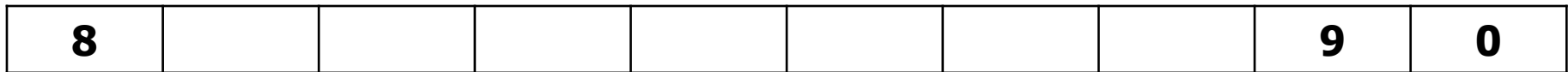
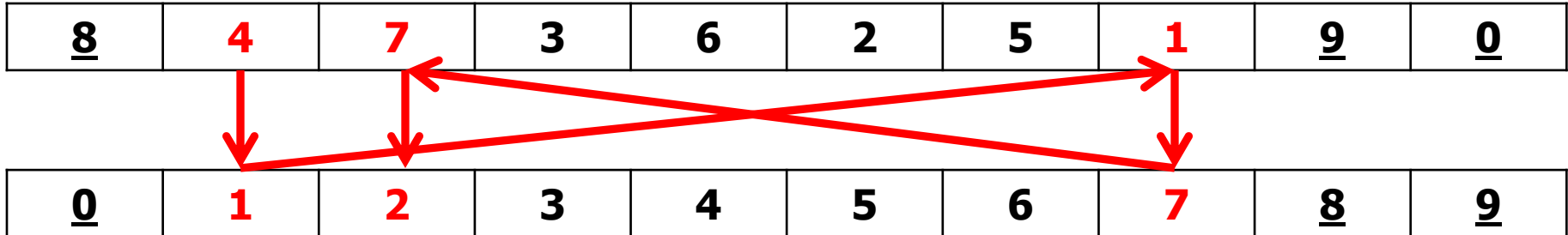
Cycle Crossover



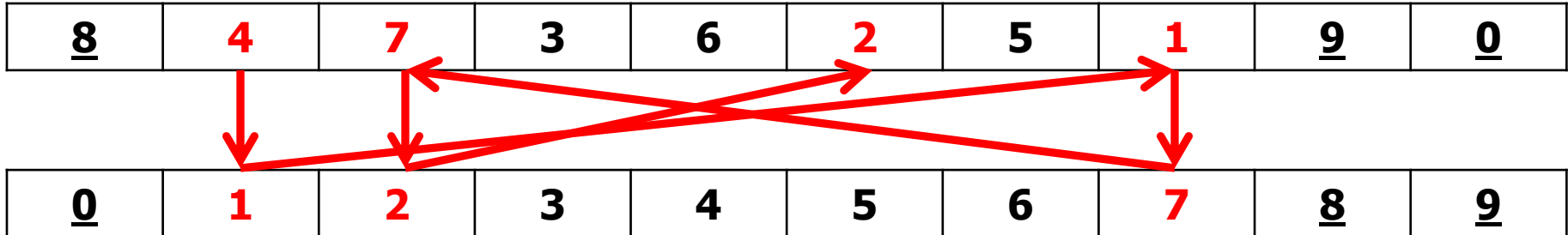
8								9	0
---	--	--	--	--	--	--	--	---	---

0								8	9
---	--	--	--	--	--	--	--	---	---

Cycle Crossover



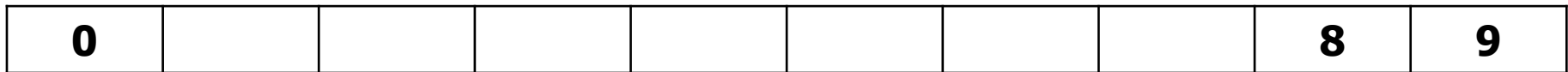
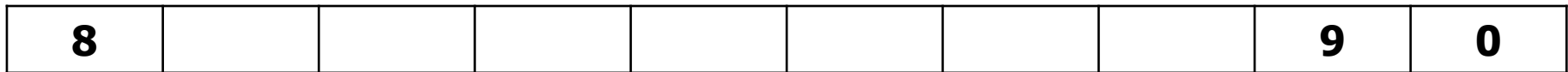
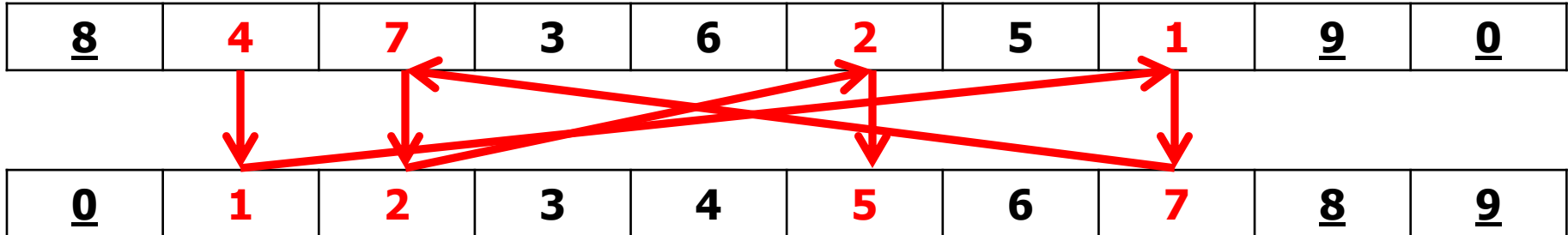
Cycle Crossover



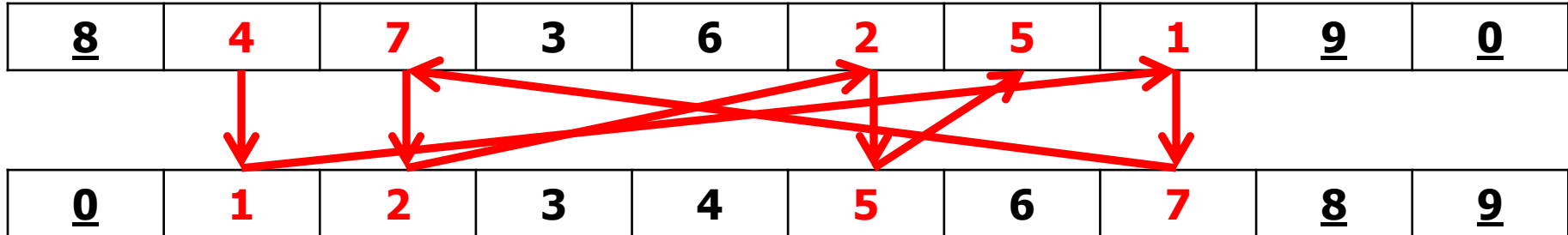
8								9	0
---	--	--	--	--	--	--	--	---	---

0								8	9
---	--	--	--	--	--	--	--	---	---

Cycle Crossover



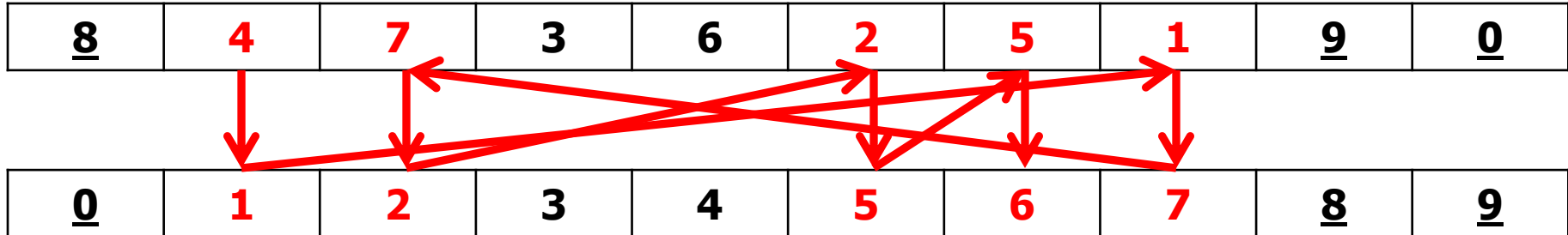
Cycle Crossover



8								9	0
---	--	--	--	--	--	--	--	---	---

0								8	9
---	--	--	--	--	--	--	--	---	---

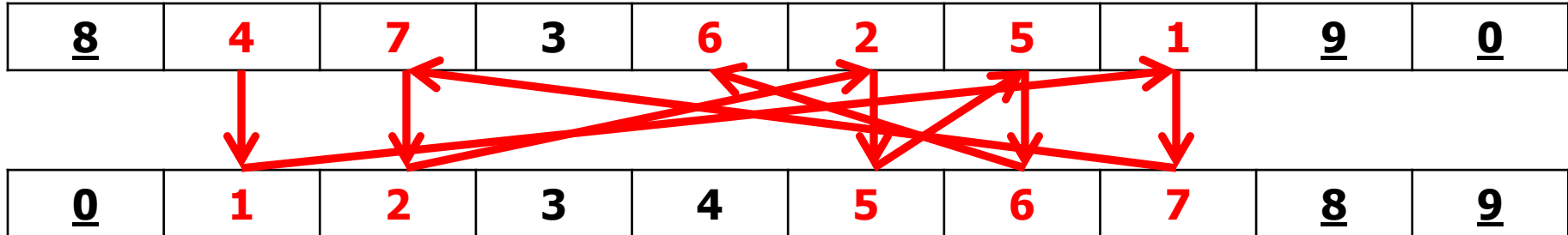
Cycle Crossover



8								9	0
---	--	--	--	--	--	--	--	---	---

0								8	9
---	--	--	--	--	--	--	--	---	---

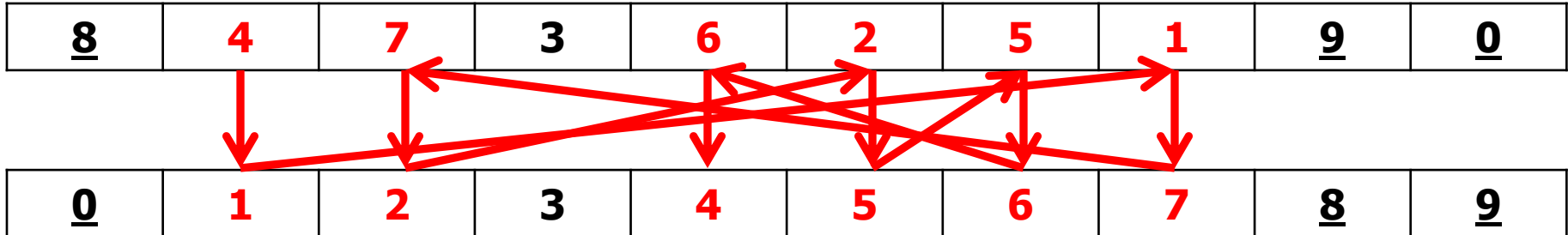
Cycle Crossover



8								9	0
---	--	--	--	--	--	--	--	---	---

0								8	9
---	--	--	--	--	--	--	--	---	---

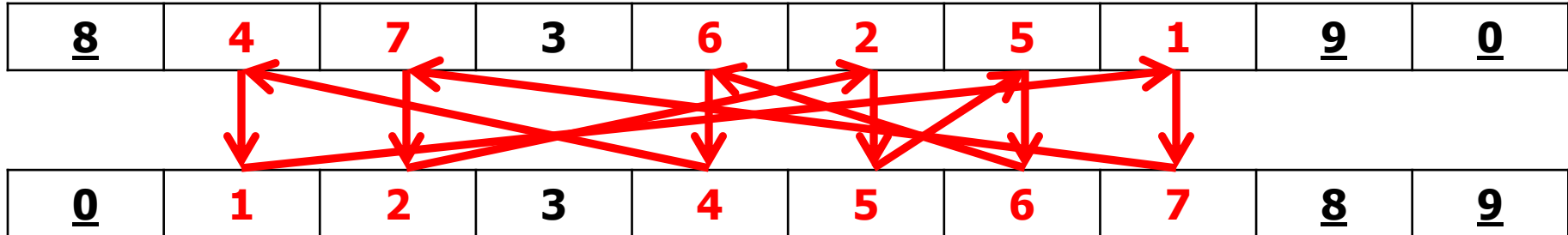
Cycle Crossover



8								9	0
---	--	--	--	--	--	--	--	---	---

0								8	9
---	--	--	--	--	--	--	--	---	---

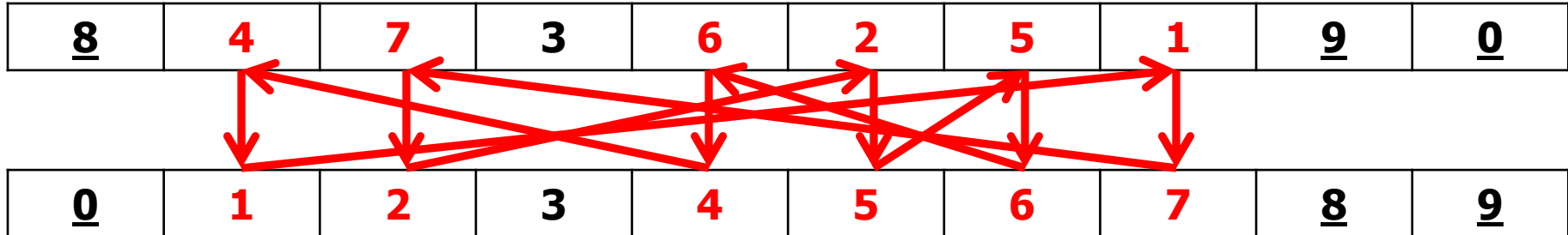
Cycle Crossover



8								9	0
---	--	--	--	--	--	--	--	---	---

0								8	9
---	--	--	--	--	--	--	--	---	---

Cycle Crossover



8	1	2		4	5	6	7	9	0
---	---	---	--	---	---	---	---	---	---

0	4	7		6	2	5	1	8	9
---	---	---	--	---	---	---	---	---	---

Cycle Crossover

<u>8</u>	<u>4</u>	<u>7</u>	3	<u>6</u>	<u>2</u>	<u>5</u>	<u>1</u>	<u>9</u>	<u>0</u>
----------	----------	----------	---	----------	----------	----------	----------	----------	----------

<u>0</u>	<u>1</u>	<u>2</u>	3	<u>4</u>	<u>5</u>	<u>6</u>	<u>7</u>	<u>8</u>	<u>9</u>
----------	----------	----------	---	----------	----------	----------	----------	----------	----------

8	1	2		4	5	6	7	9	0
---	---	---	--	---	---	---	---	---	---

0	4	7		6	2	5	1	8	9
---	---	---	--	---	---	---	---	---	---

Cycle Crossover

<u>8</u>	<u>4</u>	<u>7</u>	3	<u>6</u>	<u>2</u>	<u>5</u>	<u>1</u>	<u>9</u>	<u>0</u>
----------	----------	----------	---	----------	----------	----------	----------	----------	----------

<u>0</u>	<u>1</u>	<u>2</u>	3	<u>4</u>	<u>5</u>	<u>6</u>	<u>7</u>	<u>8</u>	<u>9</u>
----------	----------	----------	---	----------	----------	----------	----------	----------	----------

8	1	2		4	5	6	7	9	0
---	---	---	--	---	---	---	---	---	---

0	4	7		6	2	5	1	8	9
---	---	---	--	---	---	---	---	---	---

Cycle Crossover

<u>8</u>	<u>4</u>	<u>7</u>	3	<u>6</u>	<u>2</u>	<u>5</u>	<u>1</u>	<u>9</u>	<u>0</u>
----------	----------	----------	----------	----------	----------	----------	----------	----------	----------



<u>0</u>	<u>1</u>	<u>2</u>	3	<u>4</u>	<u>5</u>	<u>6</u>	<u>7</u>	<u>8</u>	<u>9</u>
----------	----------	----------	----------	----------	----------	----------	----------	----------	----------

<u>8</u>	<u>1</u>	<u>2</u>		<u>4</u>	<u>5</u>	<u>6</u>	<u>7</u>	<u>9</u>	<u>0</u>
----------	----------	----------	--	----------	----------	----------	----------	----------	----------

<u>0</u>	<u>4</u>	<u>7</u>		<u>6</u>	<u>2</u>	<u>5</u>	<u>1</u>	<u>8</u>	<u>9</u>
----------	----------	----------	--	----------	----------	----------	----------	----------	----------

Cycle Crossover

<u>8</u>	<u>4</u>	<u>7</u>	3	<u>6</u>	<u>2</u>	<u>5</u>	<u>1</u>	<u>9</u>	<u>0</u>
----------	----------	----------	----------	----------	----------	----------	----------	----------	----------



<u>0</u>	<u>1</u>	<u>2</u>	3	<u>4</u>	<u>5</u>	<u>6</u>	<u>7</u>	<u>8</u>	<u>9</u>
----------	----------	----------	----------	----------	----------	----------	----------	----------	----------

8	1	2	3	4	5	6	7	9	0
----------	----------	----------	----------	----------	----------	----------	----------	----------	----------

0	4	7	3	6	2	5	1	8	9
----------	----------	----------	----------	----------	----------	----------	----------	----------	----------

Cycle Crossover

<u>8</u>	<u>4</u>	<u>7</u>	<u>3</u>	<u>6</u>	<u>2</u>	<u>5</u>	<u>1</u>	<u>9</u>	<u>0</u>
----------	----------	----------	----------	----------	----------	----------	----------	----------	----------

<u>0</u>	<u>1</u>	<u>2</u>	<u>3</u>	<u>4</u>	<u>5</u>	<u>6</u>	<u>7</u>	<u>8</u>	<u>9</u>
----------	----------	----------	----------	----------	----------	----------	----------	----------	----------

8	1	2	3	4	5	6	7	9	0
---	---	---	---	---	---	---	---	---	---

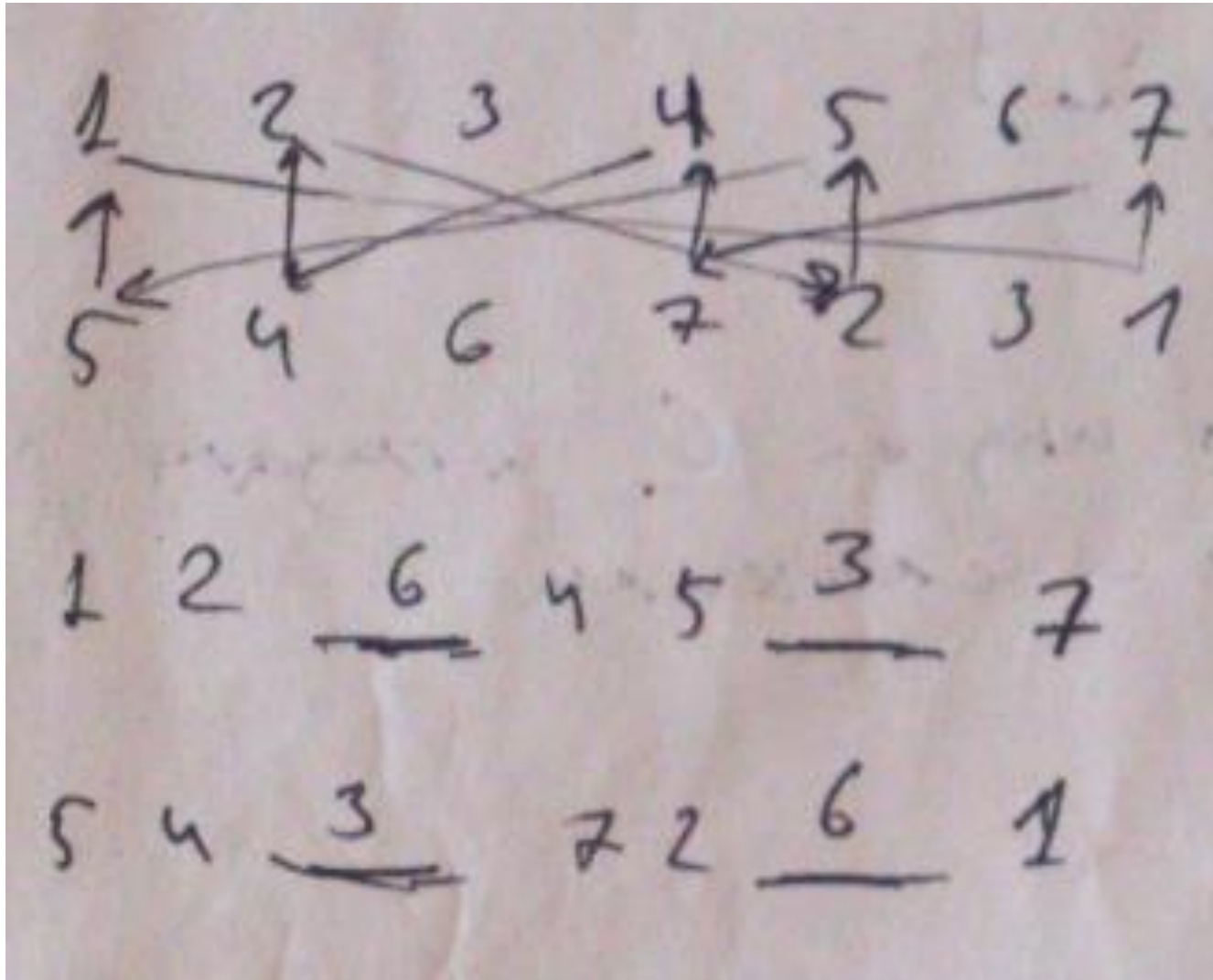
0	4	7	3	6	2	5	1	8	9
---	---	---	---	---	---	---	---	---	---

Cycle Crossover

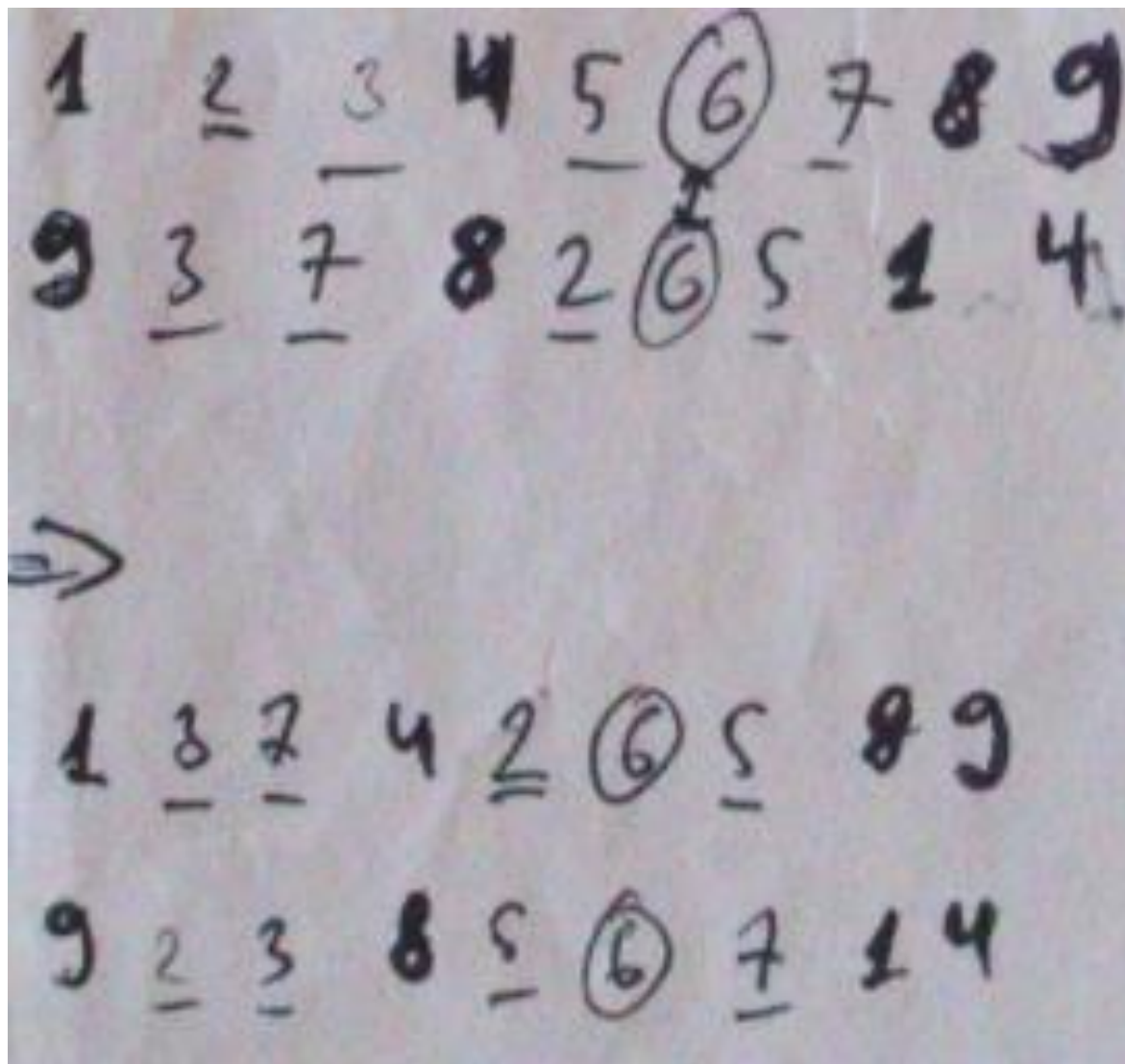
8 4 7 (3) 6 2 5 1 9 0
0 1 2 (3) 4 5 6 7 8 9

8 1 2 (3) 4 5 6 7 9 0
0 7 7 (3) 6 (2) 5 1 8 9

Cycle Crossover



Cycle Crossover



Uniform Crossover

1	2	3	4	5	6	7	8	9	1
----------	----------	----------	----------	----------	----------	----------	----------	----------	----------

2	3	4	5	5	7	7	9	9	0
----------	----------	----------	----------	----------	----------	----------	----------	----------	----------

Uniform Crossover

1	2	3	4	5	6	7	8	9	1
---	---	---	---	---	---	---	---	---	---

2	3	4	5	5	7	7	9	9	0
---	---	---	---	---	---	---	---	---	---

Getting a ***gene*** from one of the parents randomly!

Uniform Crossover

1	2	3	4	5	6	7	8	9	1
---	---	---	---	---	---	---	---	---	---

2	3	4	5	5	7	7	9	9	0
---	---	---	---	---	---	---	---	---	---

Getting a ***gene*** from one of the parents randomly!

--	--	--	--	--	--	--	--	--	--

Uniform Crossover

1	2	3	4	5	6	7	8	9	1
---	---	---	---	---	---	---	---	---	---

2	3	4	5	5	7	7	9	9	0
---	---	---	---	---	---	---	---	---	---

Getting a ***gene*** from one of the parents randomly!

2									
---	--	--	--	--	--	--	--	--	--

Uniform Crossover

1	2	3	4	5	6	7	8	9	1
---	---	---	---	---	---	---	---	---	---

2	3	4	5	5	7	7	9	9	0
---	---	---	---	---	---	---	---	---	---

Getting a ***gene*** from one of the parents randomly!

2	2								
---	---	--	--	--	--	--	--	--	--

Uniform Crossover

1	2	3	4	5	6	7	8	9	1
---	---	---	---	---	---	---	---	---	---

2	3	4	5	5	7	7	9	9	0
---	---	---	---	---	---	---	---	---	---

Getting a ***gene*** from one of the parents randomly!

2	2	4							
---	---	---	--	--	--	--	--	--	--

Uniform Crossover

1	2	3	4	5	6	7	8	9	1
---	---	---	---	---	---	---	---	---	---

2	3	4	5	5	7	7	9	9	0
---	---	---	---	---	---	---	---	---	---

Getting a ***gene*** from one of the parents randomly!

2	2	4	4						
---	---	---	---	--	--	--	--	--	--

Uniform Crossover

1	2	3	4	5	6	7	8	9	1
---	---	---	---	---	---	---	---	---	---

2	3	4	5	5	7	7	9	9	0
---	---	---	---	---	---	---	---	---	---

Getting a ***gene*** from one of the parents randomly!

2	2	4	4	5					
---	---	---	---	---	--	--	--	--	--

Uniform Crossover

1	2	3	4	5	6	7	8	9	1
---	---	---	---	---	---	---	---	---	---

2	3	4	5	5	7	7	9	9	0
---	---	---	---	---	---	---	---	---	---

Getting a ***gene*** from one of the parents randomly!

2	2	4	4	5	7				
---	---	---	---	---	---	--	--	--	--

Uniform Crossover

1	2	3	4	5	6	7	8	9	1
---	---	---	---	---	---	---	---	---	---

2	3	4	5	5	7	7	9	9	0
---	---	---	---	---	---	---	---	---	---

Getting a ***gene*** from one of the parents randomly!

2	2	4	4	5	7	7			
---	---	---	---	---	---	---	--	--	--

Uniform Crossover

1	2	3	4	5	6	7	8	9	1
---	---	---	---	---	---	---	---	---	---

2	3	4	5	5	7	7	9	9	0
---	---	---	---	---	---	---	---	---	---

Getting a ***gene*** from one of the parents randomly!

2	2	4	4	5	7	7	9		
---	---	---	---	---	---	---	---	--	--

Uniform Crossover

1	2	3	4	5	6	7	8	9	1
---	---	---	---	---	---	---	---	---	---

2	3	4	5	5	7	7	9	9	0
---	---	---	---	---	---	---	---	---	---

Getting a ***gene*** from one of the parents randomly!

2	2	4	4	5	7	7	9	9	
---	---	---	---	---	---	---	---	---	--

Uniform Crossover

1	2	3	4	5	6	7	8	9	1
---	---	---	---	---	---	---	---	---	---

2	3	4	5	5	7	7	9	9	0
---	---	---	---	---	---	---	---	---	---

Getting a ***gene*** from one of the parents randomly!

2	2	4	4	5	7	7	9	9	0
---	---	---	---	---	---	---	---	---	---

Uniform Crossover

1	2	3	4	5	6	7	8	9	1
---	---	---	---	---	---	---	---	---	---

2	3	4	5	5	7	7	9	9	0
---	---	---	---	---	---	---	---	---	---

Getting a ***gene*** from one of the parents randomly!

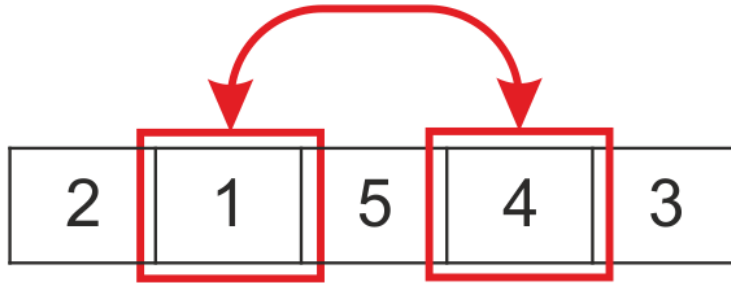
2	2	4	4	5	7	7	9	9	0
---	---	---	---	---	---	---	---	---	---

Uniform Crossover

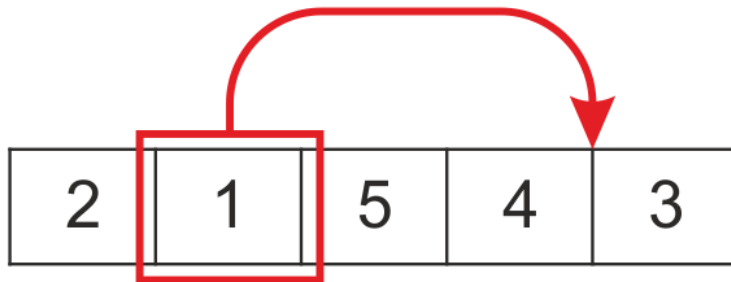
→ 1 2 3 4 5 6 7 8 9 1
→ 2 3 4 5 5 7 7 8 9 0

!
rand(2) → na k-trenku na random uzdu parne 1 om 2 re:
1 na 2; 2 na 3; 3 na 4 ...

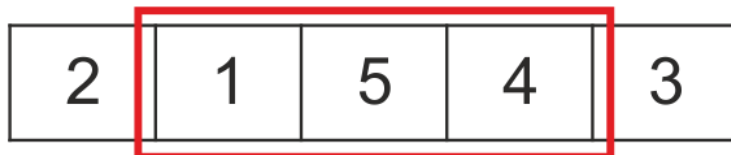
Mutation



swap



insertion

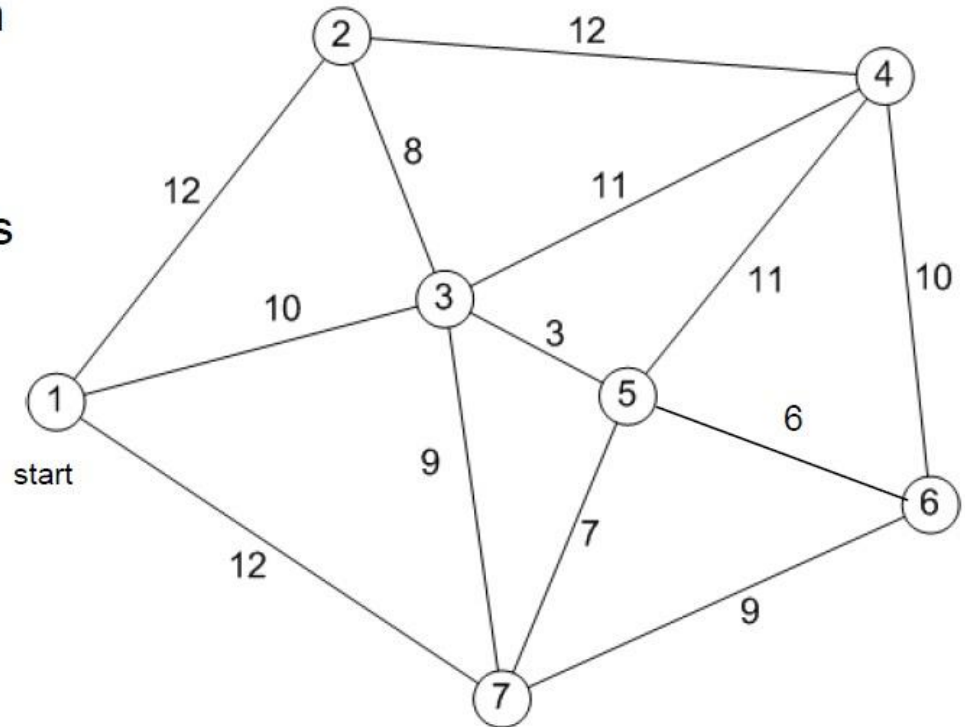


reverse

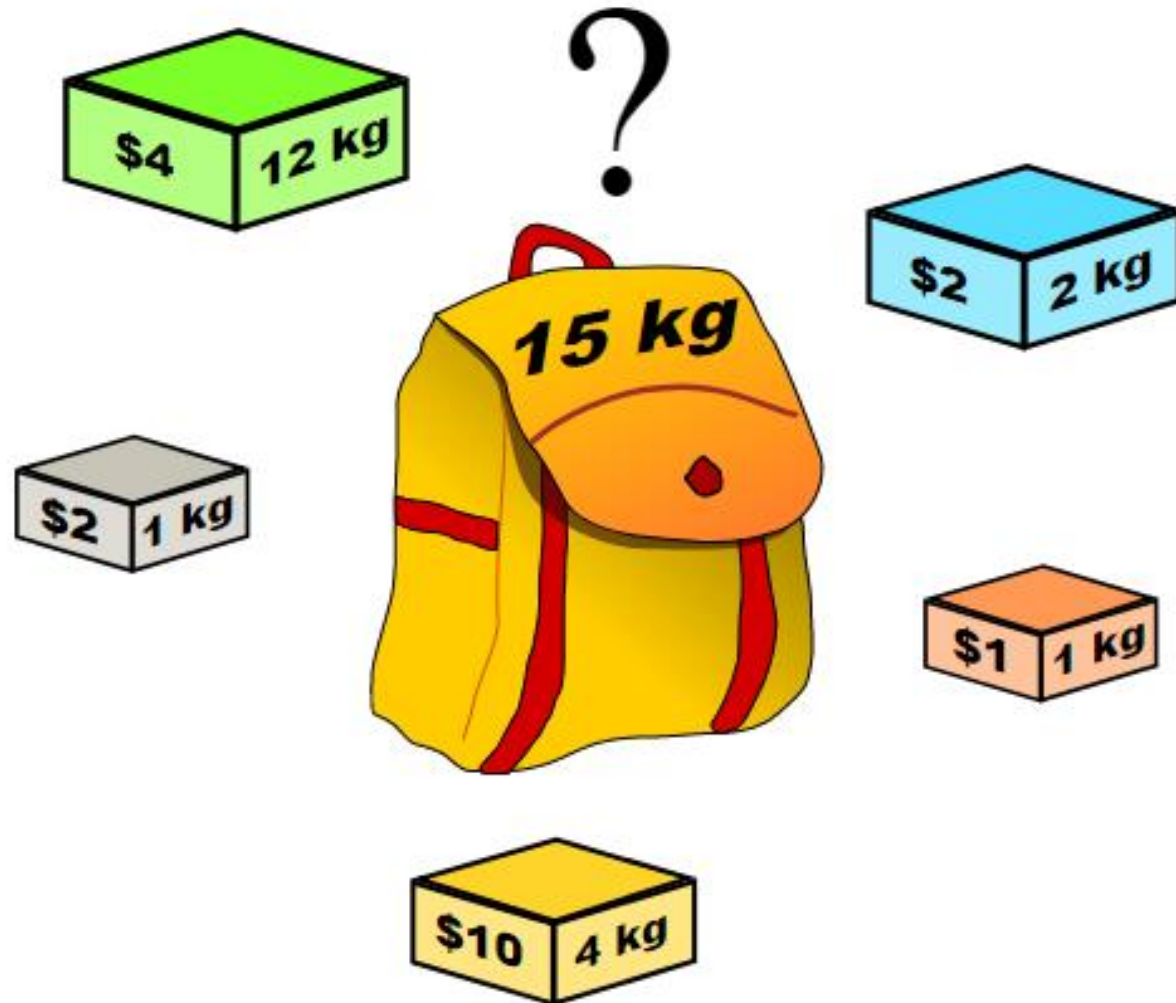
Travelling salesman problem

The Traveling Salesman Problem

- Starting from city 1, the salesman must travel to all cities once before returning home
- The distance between each city is given, and is assumed to be the same in both directions
- Only the links shown are to be used
- Objective - Minimize the total distance to be travelled



Knapsack problem



```
t = 0;
initialize(P(t=0));
evaluate(P(t=0));
while isNotTerminated() do
     $P_p(t) = P(t).selectParents();$ 
     $P_c(t) = reproduction(P_p);$ 
    mutate( $P_c(t)$ );
    evaluate( $P_c(t)$ );
     $P(t+1) = buildNextGenerationFrom(P_c(t), P(t));$ 
    t = t + 1;
end
```