sin 3 yusec mberno sin

 $(z) = (1+z^2)^2$ Hylu: $Z = \pm i$ Towork: $Z = \pm 1$ $Z = \pm \infty$ 2 noprgok 2 noprgok z) = clg zKEH Hylle: Z = = + 17 K Fostock: Z = 17 K KEZ 3) f(z)=z·tg²z 3 nonxgka $k \in \mathbb{Z}$ $\not \ge 103$ 2 nonxgka $k \in \mathbb{Z}$ 2 nonxgka Ilynu: Z = 0 $Z = \frac{\pi}{2} + \pi k$ Touroco: $Z = \frac{\pi}{2} + \pi k$

 $=\sum_{n=0}^{\infty}\frac{(-1)^n}{9}\cdot\frac{1}{t^{n+1}}+\sum_{n=0}^{\infty}\left[\frac{1}{9}+\frac{n+1}{6}\right]\frac{t^n}{z^{n+1}}=\sum_{n=0}^{\infty}\frac{(-1)^n}{9}\cdot\frac{1}{(z-1)^{n+1}}+\sum_{n=0}^{\infty}\left[\frac{1}{9}+\frac{n+1}{6}\right]\cdot\frac{(z-1)^n}{z^{n+1}}$

5)
$$\frac{1}{z(z-1)(z-2)}$$
 $\alpha = 0 - \frac{3}{2} \in D$

$$\frac{1}{Z} \cdot \left(\frac{1}{Z - Z} - \frac{1}{Z - 1} \right) = \frac{1}{Z} \left(\frac{-1}{2} \frac{1}{1 - \frac{Z}{Z}} - \frac{1}{Z} \frac{1}{1 - \frac{1}{Z}} \right) = \frac{1}{Z} \left(\frac{-1}{Z} \sum_{h=0}^{\infty} \left(\frac{Z}{Z} \right)^h - \frac{1}{Z} \cdot \sum_{h=0}^{\infty} \left(\frac{1}{Z} \right)^h \right) = \frac{1}{Z} \cdot \left(\frac{1}{Z} \right)^{\frac{1}{N-2}} - \sum_{h=0}^{\infty} \frac{Z^{n-1}}{Z^{n+1}} - \sum_{h=0}^{\infty} \frac{Z^{n-1}}{Z^{n+1}} = 0$$

$$7) \frac{z^{3}}{(z+1)(z-2)} \qquad \alpha = -1 \qquad 0 : 0 < |z+1| < 3$$

$$t = z+1 \qquad \frac{(t-1)^{3}}{t \cdot (t-3)} = \frac{1}{t} \cdot \frac{(t-1)^{3}}{t-3} = \frac{1}{t} \left(1 + \frac{2}{t-3}\right) (t-1)^{2} =$$

$$= \frac{1}{t} \left[(t-1)^{2} + \frac{2(t-1)}{t-3} (t-1) \right] = \frac{1}{t} \left(t^{2} - 2t + 1 + \left(2 + \frac{4}{t-3}\right) (t-1) \right) =$$

$$= \frac{1}{t} \left(t^{2} - 1 + \frac{4t}{t-3} - \frac{4}{t-3} \right) = t - \frac{1}{t} + \frac{4}{t-3} - \frac{4}{t(t-3)} = t - \frac{1}{t} + \frac{4}{t-3} + \frac{4}{3} \left(\frac{1}{t} + \frac{1}{3-t} \right) =$$

$$= \frac{1}{t} \cdot \frac{1}{3} \cdot \frac{1}{t} + \frac{8}{3} \cdot \frac{1}{t-3} = t + \frac{1}{3} \cdot \frac{1}{t} - \frac{8}{9} \cdot \frac{1}{1-\frac{t}{3}} = t + \frac{1}{3} \cdot \frac{1}{t} - \frac{8}{9} \cdot \sum_{n=0}^{\infty} \left(\frac{t}{3} \right)^{n} =$$

$$= \frac{1}{3} \cdot \frac{1}{t} - \frac{8}{9} + \frac{19}{27} \cdot t - \frac{8}{9} \cdot \sum_{n=2}^{\infty} \left(\frac{t}{3} \right)^{n} =$$

$$= \frac{1}{3} \cdot \frac{1}{t-1} - \frac{8}{9} \cdot \frac{19}{27} \cdot (z+1) - \frac{8}{9} \cdot \sum_{n=2}^{\infty} \frac{(z+1)^{n}}{3^{n}}$$

8)
$$a = 0$$
 0 : $|z| > 2$

$$\frac{1}{5} \left(z^{2} - 1 - z^{2} + 4 \right) = \frac{1}{5} \left[\frac{1}{2} \left(\frac{1}{z - 1} - \frac{1}{z + 1} \right) - \frac{1}{z + 2i} \right] z$$

$$= \frac{1}{10} z - 1 - \frac{1}{10} z + 1 + \frac{1}{20} z - 2i - \frac{1}{20} z + 2i$$

$$= \frac{1}{10} z - \frac{1}{10} z -$$

$$20.16$$
1) $z^{3}e^{\frac{1}{z}}$ $\alpha = 0$ $0 < |z| < \infty$

$$z^{3} \cdot e^{\frac{1}{z}} = z^{3} \cdot \sum_{n=0}^{\infty} \frac{1}{n! \cdot z^{n}} = \sum_{h=0}^{\infty} \frac{1}{n! \cdot z^{n-3}}$$
2) $z^{2} \cdot \sin(n\frac{z+1}{z}) = -z^{2} \cdot \sin(\frac{\pi}{z}) = -z^{2} \cdot \sum_{n=0}^{\infty} \frac{(-1)^{n}}{(z+1)!} (\frac{\pi}{z})^{2n+1} = \sum_{n=0}^{\infty} \frac{(-1)^{n}}{(2h+1)!} (\frac{\pi}{z})^{2n+1} = \sum_{n=0}^{\infty} \frac{(-1)^{n}}{(2h+1)!} (\frac{\pi}{z})^{2n+1} = \sum_{n=0}^{\infty} \frac{(-1)^{n}}{(2h+1)!} (\frac{\pi}{z})^{2n+1} (\frac{\pi}{z})^{2n+1} = \sum_{n=0}^{\infty} \frac{(-1)^{n}}{(2n)!} t^{-2n+1} + 2 \cdot \sum_{n=0}^{\infty} \frac{(-1)^{n}}{(2n)!} t^{-2n} = \sum_{n=0}^{\infty} \frac{(-1)^{n}}{(2n)!} t^{-2n+3} + 6 \cdot \sum_{n=0}^{\infty} \frac{(-1)^{n}}{(2n)!} t^{-2n+2} + 12 \cdot \sum_{n=0}^{\infty} \frac{(-1)^{n}}{(2n)!} t^{-2n+1} + 8 \cdot \sum_{n=0}^{\infty} \frac{(-1)^{n}}{(2n)!} t^{-2n} = \sum_{n=0}^{\infty} \frac{(-1)^{n}}{(2n)!} t^{-2n+2} + 12 \cdot \sum_{n=0}^{\infty} \frac{(-1)^{n}}{(2n)!} t^{-2n+1} + 8 \cdot \sum_{n=0}^{\infty} \frac{(-1)^{n}}{(2n)!} t^{-2n} = \sum_{n=0}^{\infty} \frac{t^{2}}{(2n)!} (\frac{t}{t}) = \frac{t^{2}}{t} \cdot (\frac{t}{t+1} - \frac{t}{t+2}) = e^{\frac{t}{t}} \cdot (\frac{t}{t} \frac{t}{1 - (-\frac{t}{t})}) = \sum_{n=0}^{\infty} \frac{t}{k!} t^{2n} \cdot \sum_{n=0}^{\infty} (-1)^{n} \frac{t^{2n+1}}{t^{2n+1}} + \sum_{n=0}^{\infty} \frac{t}{k!} \frac{t^{2n}}{t^{2n}} \cdot \sum_{n=0}^{\infty} (-1)^{n} \frac{t^{2n+1}}{t^{2n+1}} = \sum_{n=0}^{\infty} \frac{t}{k!} \frac{t^{2n}}{t^{2n}} \cdot \sum_{n=0}^{\infty} (-1)^{n} \frac{t^{2n+1}}{t^{2n+1}} + \sum_{n=0}^{\infty} \frac{t}{k!} \frac{t^{2n}}{t^{2n}} \cdot \sum_{n=0}^{\infty} (-1)^{n} \frac{t^{2n+1}}{t^{2n+1}} = \sum_{n=0}^{\infty} \frac{t}{k!} \frac{t^{2n}}{t^{2n}} \cdot \sum_{n=0}^{\infty} (-1)^{n} \frac{t^{2n+1}}{t^{2n+1}} + \sum_{n=0}^{\infty} \frac{t}{k!} \frac{t^{2n}}{t^{2n}} \cdot \sum_{n=0}^{\infty} (-1)^{n} \frac{t^{2n+1}}{t^{2n+1}}$
6) $e^{\frac{t}{2}} (z - \frac{t}{z})$ $\alpha = 0$ $0 < |z| < \infty$

 $e^{\frac{t}{z}z} \cdot e^{\frac{t}{z}z} = \sum_{n=1}^{\infty} \frac{(tz)^n}{z^n \cdot n!} \cdot \sum_{m=1}^{\infty} (-1)^m \frac{t^m}{z^m \cdot m!} z^m$

$f(z) = \sum_{n=f_1}^{f_2} c_n z^n \qquad f_1 < f_2$ $g(z) = \sum_{n=g_1}^{g_2} \alpha_n z^n \qquad h(z) = \sum_{n=h_1}^{h_2} \beta_n z^n$	f(z)-Heuzbecm- Ha g(z), h(z)- -uzbecmxvi
$g_1 < g_2$ $h_1 < h_2$ $g(z)$	$f_1 + h_1 = g_1$ $f_2 + h_2 = g_2$
$f(z) = \frac{1}{h(z)} \qquad f(z) \qquad h(z) = g(z)$	
$a_n = \lambda \cdot \delta(t+1-n) fi hj$ $i = f, \delta(x) = \begin{cases} i & x = 0 \\ 0 & x \neq 0 \end{cases}$ $j = h, \delta(x) = \begin{cases} i & x \neq 0 \\ 0 & x \neq 0 \end{cases}$	

2)
$$f(z) = \frac{e^{z} + 1}{e^{z} - 1} = \frac{g(z)}{h(z)}$$
 $z_0 = 2\pi i k$ $k \in \mathbb{Z}$

$$g(z) = e^{z} + 1 = 2 + z + \frac{z^2}{2} + \frac{z^3}{6} + \dots \Rightarrow f_2 = +\infty$$

$$h(z) = e^{z} - 1 = z + \frac{z^2}{2} + \frac{z^3}{6} + \dots \Rightarrow f_2 = +\infty$$

$$\alpha_0 = 2 = 1 \cdot f_{-1} + 1 \cdot f_0 = 0$$

$$\alpha_1 = 1 = \frac{1}{2} \cdot f_{-1} + 1 \cdot f_0 = 0$$

$$1 \cdot \alpha = 1 \cdot \frac{1}{2} \cdot f_{-1} + 1 \cdot f_0 = 0$$

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3)
$$f(z) = \frac{z-1}{\sin^2 z} = \frac{z}{\sin^2 z} - \frac{z}{\sin^2 z}$$
 $z_0 = 0$
 $\sin^2 z = z^2 \left(1 - \frac{z^2}{6} + \frac{z^4}{120} - \dots\right)^2$
 $f(z) = \frac{1}{z} \left(\alpha_0 + \alpha_1 z + \alpha_2 z^2 + \dots\right) - \frac{1}{z^2} \left(\alpha_0 + \alpha_1 z + \alpha_2 z^2 + \dots\right)^2$
 $= \left(\frac{\alpha_0}{z} + \alpha_1 + \alpha_2 z z + \dots\right) - \left(\frac{\alpha_0}{z^2} + \frac{\alpha_1}{z} + \alpha_2 z^2 + \dots\right)^2$
 $\alpha_0 = 1$ $\alpha_1 = 0$
Thabkax tacms $f(z) : -\frac{1}{z^2} + \frac{1}{z}$

4)
$$f(z) = \frac{e^{iz}}{z^2 + 6^2}$$
 $z_0 = ib$ $b > 0$
 $f(z) = e^{iz}$
 $f(z) = e^{iz}$

