

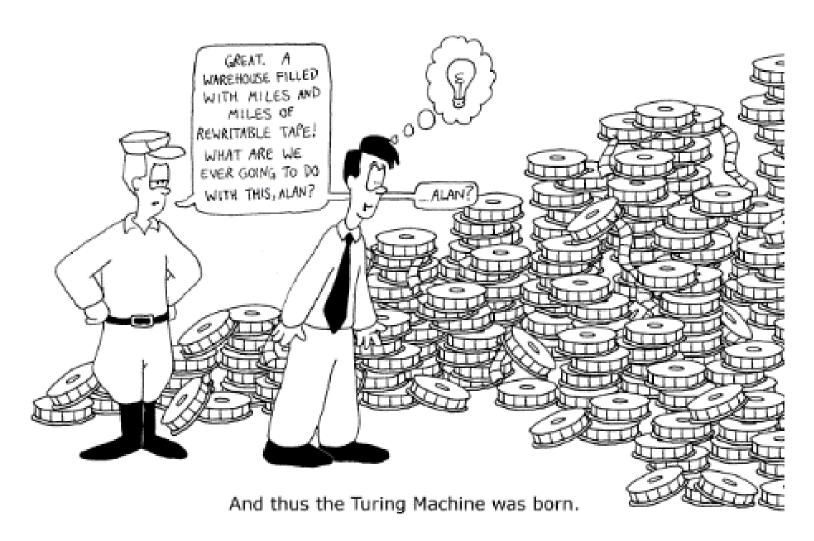
Agenda

- A brief history
- Basic commands
- Input/Output
- Control structures
- Some examples
- Program "Hello world!"

Alan Turing



Turing machine

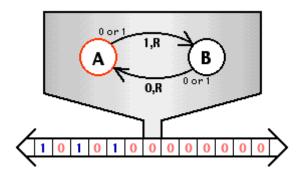


Turing machine

It's a hypothetical device that manipulates symbols on a strip of tape according to a table of rules.

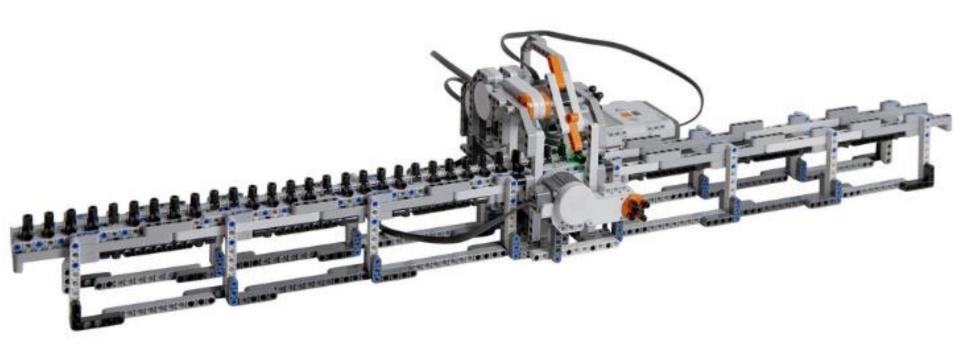
The "Turing" machine was invented in **1936** by **Alan Turing** who called it an "a-machine" (automatic machine).

Turing machine

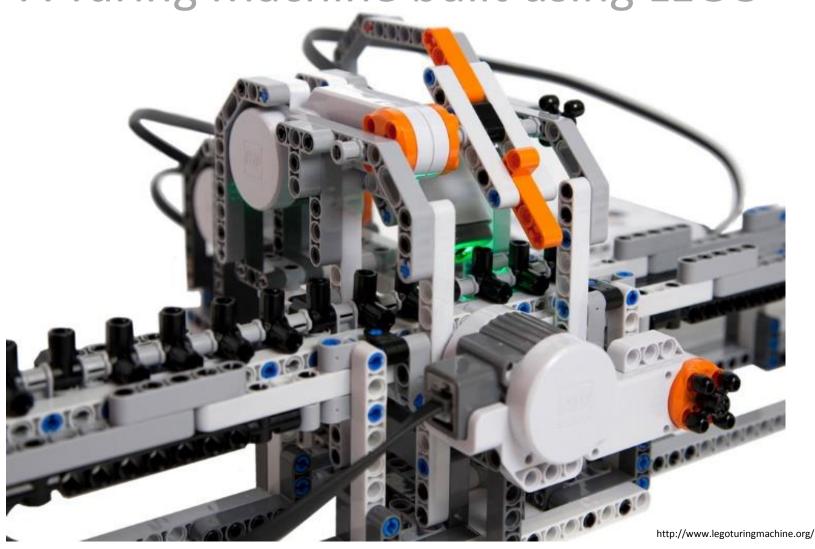


A Turing Machine built using LEGO

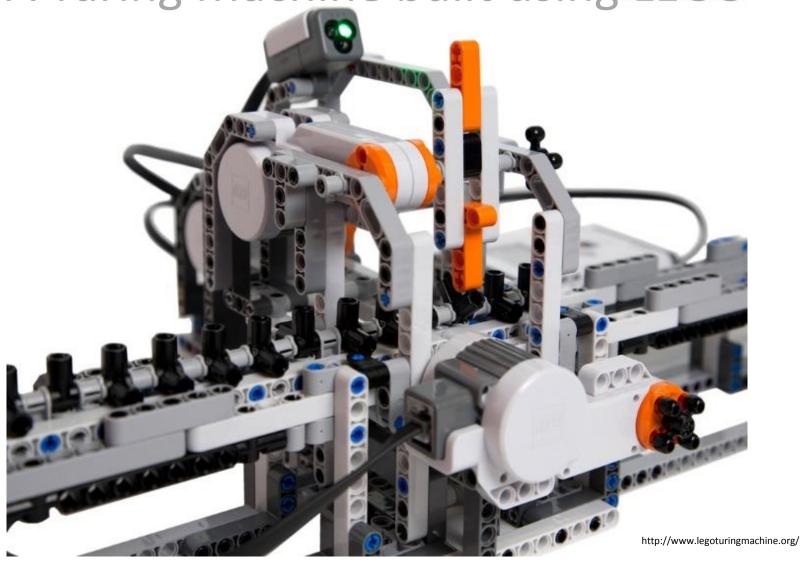
To honor Alan Turing, we built a simple LEGO Turing Machine, to show everyone how simple a computer actually is.



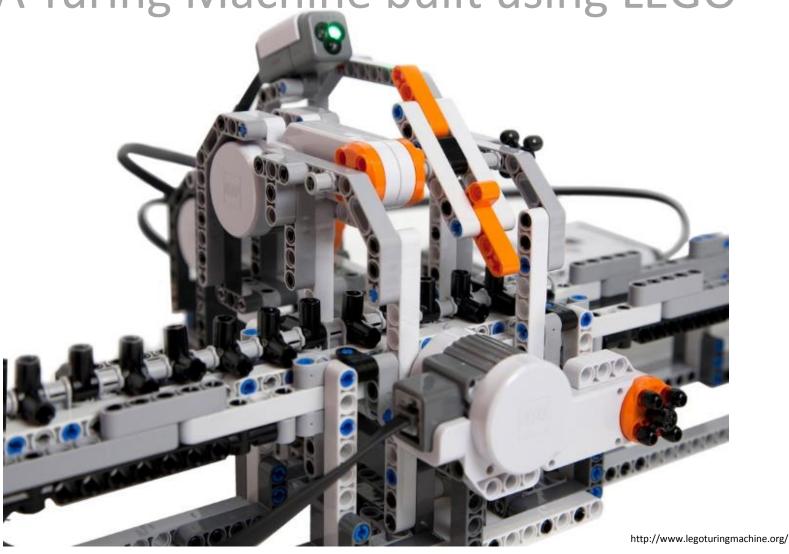
Reading the memory



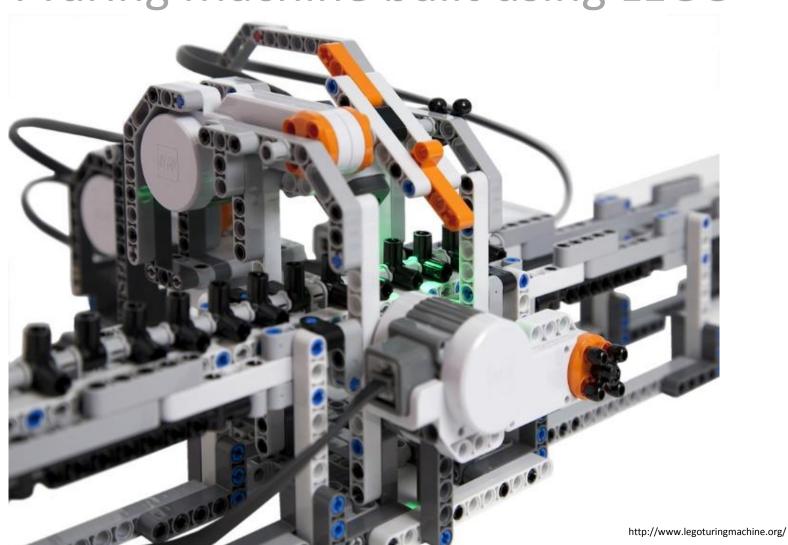
Writing the memory



Moving the memory



Detail shot



Turing completeness

Turing complete or computationally universal if it can be used to simulate any single-taped Turing machine.

A classic example is lambda calculus.

Corrado Böhm



P"

P" is a primitive computer programming language created by Corrado Böhm in 1964 to describe a family of Turing machines.

P"

- P" was the **first** "GOTO-less" imperative structured programming language to be proven Turing-complete.
- The brainfuck language (apart from its I/O commands) is a minor informal variation of P".

Urban Dominik Müller



BrainFuck

```
]<<<<>>></></>
| [-]</br/>
| [-
>>>>>]</>
```

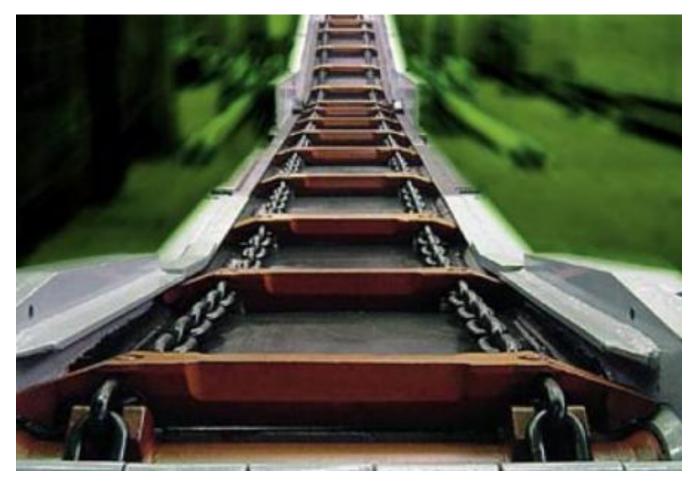
The name

Sometimes also called:

- Brainf * ck
- Brainf ***
- BF

BF

Tape with compartments



http://www.hombiz.ru/idei-texnicheskix-novinok/skrebkovyj-konvejer-cepnye-skrebkovye-konvejery.html

Commands (1)



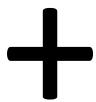
Step to the right

Commands (2)



Step to the left

Commands (3)



Increment the value

(increase by one)

Commands (4)

Decrement the value

(decrease by one)

Input/Output (1)

Write a sybmol

Input/Output (2)

Read a symbol

Control structures (1)

The begin loop

Control structures (2)

The end loop

Brainfuck in hardware



The first example

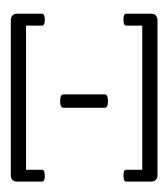


Reset in C#

```
while (tape[0] != 0)
{
   tape[0]--;
}
```



Reset in BF



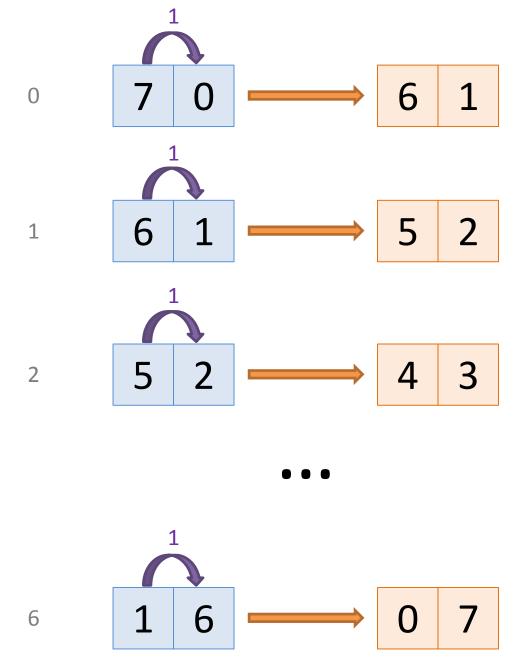
7 ----- 0

The second example



Move in C#

The second way The first way while (tape[0] != 0) while (tape[0] != 0) { tape[1]++; ____ → tape[0]--; tape[0]--; -→ tape[1]++; } }



Move in BF

The first way	The second way
[>+<-]	[->+<]



The third example





```
var tape = new Dictionary<int, byte>();
var index = 0;
while (tape[index] != 0)
   tape[index]--;
   index++;//1
   tape[index]++;
   index++;//2
   tape[index]++;
   index--;//1
   index--;//0
```

```
var tape = new Dictionary<int, byte>();
var index = 0;
while (tape[index] != 0)
   tape[index]--;
   index++;//1
   tape[index]++;
   index++;//2
   tape[index]++;
   index--;//1
   index--;//0
```

```
var tape = new Dictionary<int, byte>();
var index = 0;
while (tape[index] != 0)
  tape[index]--;
   index++;//1
   tape[index]++;
   index++;//2
   tape[index]++;
   index--;//1
   index--;//0
```

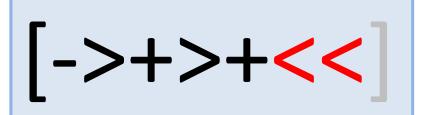
```
var tape = new Dictionary<int, byte>();
var index = 0;
while (tape[index] != 0)
   tape[index]--;
   index++;//1
   tape[index]++;
   index++;//2
   tape[index]++;
   index--;//1
   index--;//0
```

```
var tape = new Dictionary<int, byte>();
var index = 0;
while (tape[index] != 0)
   tape[index]--;
   index++;//1
   tape[index]++;
   index++;//2
   tape[index]++;
   index--;//1
   index--;//0
```

```
var tape = new Dictionary<int, byte>();
var index = 0;
while (tape[index] != 0)
   tape[index]--;
   index++;//1
   tape[index]++;
   index++;//2
   tape[index]++;
   index--;//1
   index--;//0
```

```
var tape = new Dictionary<int, byte>();
var index = 0;
while (tape[index] != 0)
   tape[index]--;
   index++;//1
   tape[index]++;
   index++;//2
   tape[index]++;
   index--;//1
   index--;//0
```

```
var tape = new Dictionary<int, byte>();
var index = 0;
while (tape[index] != 0)
   tape[index]--;
   index++;//1
   tape[index]++;
   index++;//2
   tape[index]++;
   index--;//1
   index--;//0
```



```
var tape = new Dictionary<int, byte>();
var index = 0;
while (tape[index] != 0)
  tape[index]--;
  index++;//1
  tape[index]++;
                      ->+>+<
  index++;//2
  tape[index]++;
  index--;//1
  index--;//0
```

```
var tape = new Dictionary<int, byte>();
var index = 0;
while (tape[index] != 0)
  tape[index]--;
  index++;//1
  tape[index]++;
                      ->+<
  index++;//2
  tape[index]++;
  index--;//1
  index--;//0
```

```
index++;//1
index++;//2
while (tape[index] != 0)
   tape[index]--;
   index--;//1
   index--;//0
   tape[index]++;
   index++;//1
   index++;//2
```

```
index++;//1
index++;//2
while (tape[index] != 0)
   tape[index]--;
   index--;//1
   index--;//0
   tape[index]++;
   index++;//1
   index++;//2
```

```
index++;//1
index++;//2
while (tape[index] != 0)
   tape[index]--;
   index--;//1
   index--;//0
   tape[index]++;
   index++;//1
   index++;//2
```

```
index++;//1
index++;//2
while (tape[index] != 0)
  tape[index]--;
   index--;//1
   index--;//0
   tape[index]++;
   index++;//1
   index++;//2
```

```
>> -<<+>>
index++;//1
index++;//2
while (tape[index] != 0)
  tape[index]--;
  index--;//1
  index--;//0
  tape[index]++;
  index++;//1
  index++;//2
```

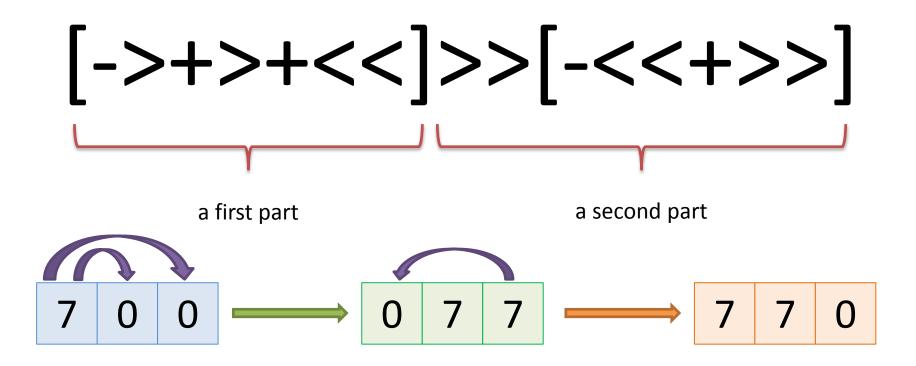
```
>> -<<+>>
index++;//1
index++;//2
while (tape[index] != 0)
  tape[index]--;
  index--;//1
  index--;//0
  tape[index]++;
  index++;//1
  index++;//2
```

```
>> -<<+>>
index++;//1
index++;//2
while (tape[index] != 0)
  tape[index]--;
  index--;//1
  index--;//0
  tape[index]++;
  index++;//1
  index++;//2
```

```
>> -<<+>>
index++;//1
index++;//2
while (tape[index] != 0)
  tape[index]--;
  index--;//1
  index--;//0
  tape[index]++;
  index++;//1
  index++;//2
```

```
|-<<+>>
index++;//1
index++;//2
while (tape[index] != 0)
  tape[index]--;
   index--;//1
   index--;//0
  tape[index]++;
   index++;//1
   index++;//2
```

Copy in BF



The fourth example



```
var tape = new Dictionary<int, byte>();
var index = 0;

tape[index] = (byte)Console.Read();
while (tape[index] != 0)
{
   Console.Write((char)tape[index]);
   tape[index] = (byte)Console.Read();
}
```

```
var tape = new Dictionary<int, byte>();
var index = 0;

tape[index] = (byte)Console.Read();
while (tape[index] != 0)
{
   Console.Write((char)tape[index]);
   tape[index] = (byte)Console.Read();
}
```

```
var tape = new Dictionary<int, byte>();
var index = 0;

tape[index] = (byte)Console.Read();
while (tape[index] != 0)
{
   Console.Write((char)tape[index]);
   tape[index] = (byte)Console.Read();
}
```

```
var tape = new Dictionary<int, byte>();
var index = 0;

tape[index] = (byte)Console.Read();
while (tape[index] != 0)
{
    Console.Write((char)tape[index]);
    tape[index] = (byte)Console.Read();
}
```

```
var tape = new Dictionary<int, byte>();
var index = 0;

tape[index] = (byte)Console.Read();
while (tape[index] != 0)
{
    Console.Write((char)tape[index]);
    tape[index] = (byte)Console.Read();
}
```

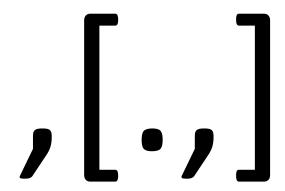
```
var tape = new Dictionary<int, byte>();
var index = 0;

tape[index] = (byte)Console.Read();
while (tape[index] != 0)
{
   Console.Write((char)tape[index]);
   tape[index] = (byte)Console.Read();
}
```

```
var tape = new Dictionary<int, byte>();
var index = 0;

tape[index] = (byte)Console.Read();
while (tape[index] != 0)
{
   Console.Write((char)tape[index]);
   tape[index] = (byte)Console.Read();
}
```

Echo in BF



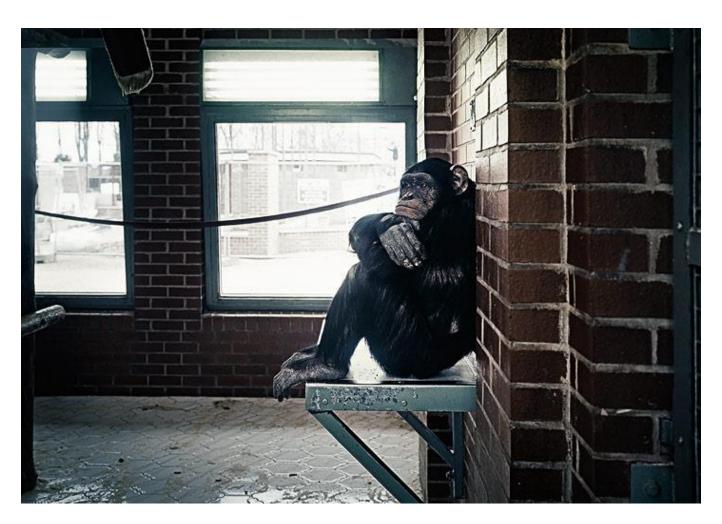
The fifth example



"Hello world!" in C# (1)

```
class Program
{
    static void Main()
    {
        Console.Write("Hello world!");
    }
}
```

Really, it works... but it's so boring



"Hello world!" in C# (2)

```
class Program
   static void Main()
      var tape = new char[]
            'H', 'e', 'l', 'l', 'o',
            'w', 'o', 'r', 'l', 'd',
         };
      Console.Write(tape);
```

The American Standard Code for Information Interchange (ASCII)

It's a character-encoding scheme originally based on the English alphabet that encodes 128 specified characters.

ASCII

re Z			~~~ <u>~</u> ~	<u> </u>	T. / " ~ ~ ~ ~			~~~~	49.41	~ <u> </u>	المسترسين	_~~_	and the second	<u> </u>
010 0001	041	33	21	!	100 0001	101	65	41	Α	110 0001	141	97	61	a
010 0010	042	34	22	"	100 0010	102	66	42	В	110 0010	142	98	62	b
010 0011	043	35	23	#	100 0011	103	67	43	С	110 0011	143	99	63	С
010 0100	044	36	24	\$	100 0100	104	68	44	D	110 0100	144	100	64	d
010 0101	045	37	25	%	100 0101	105	69	45	Е	110 0101	145	101	65	е
010 0110	046	38	26	&	100 0110	106	70	46	F	110 0110	146	102	66	f
010 0111	047	39	27	•	100 0111	107	71	47	G	110 0111	147	103	67	g
010 1000	050	40	28	(100 1000	110	72	48	Н	110 1000	150	104	68	h
010 1001	051	41	29)	100 1001	111	73	49	I	110 1001	151	105	69	i
010 1010	052	42	2A	*	100 1010	112	74	4A	J	110 1010	152	106	6A	j
010 1011	053	43	2B	+	100 1011	113	75	4B	K	110 1011	153	107	6B	k
010 1100	054	44	2C	,	100 1100	114	76	4C	L	110 1100	154	108	6C	I
010 1101	055	45	2D	-	100 1101	115	77	4D	М	110 1101	155	109	6D	m

```
class Program
   static void Main()
      var tape = new int[]
            72/*'H'*/, 101/*'e'*/, 108/*'l'*/, 108/*'l'*/, 111/*'o'*/,
            32/*' '*/,
            119/*'w'*/, 111/*'o'*/, 114/*'r'*/, 108/*'l'*/, 100/*'d'*/,
            33/*'!'*/
         };
      foreach (var value in tape)
         Console.Write((char)value);
```

```
class Program
   static void Main()
     var tape = new int[12];
      tape[0] = 72; /*'H'*/ tape[1] = 101; /*'e'*/
     tape[2] = 108; /*'l'*/ tape[3] = 108; /*'l'*/
      tape[4] = 111; /*'o'*/ tape[5] = 32; /*' '*/
     tape[6] = 119; /*'w'*/ tape[7] = 111; /*'o'*/
      tape[8] = 114; /*'r'*/ tape[9] = 108; /*'l'*/
      tape[10] = 100; /*'d'*/ tape[11] = 33; /*'!'*/
      foreach (var value in tape)
         Console.Write((char)value);
```

"Hello world!" in ASCII

0	1	2	3	4	5	6	7	8	9	10	11
72	101	108	108	111	32	119	111	114	108	100	33
Η	e			0		W	0	r		d	!

- Suppose, in our set of tools no ready-numeric value.
- We have only a zero value and the ability to increase it by one (or decrease by one)

```
tape[0]++;
.
. 72 times == ,H'
.
tape[0]++;
```

```
tape[1]++;
.
.
.
.
tape[1]++;

101 times == ,e'
.
tape[1]++;
```

```
for (int i = 0; i < 72; i++)
  tape[0]++;</pre>
```

```
for (int i = 0; i < 101; i++)
  tape[1]++;</pre>
```

Suppose we do not have a predefined value...

```
tape[0]++;
.
.
.
.
tape[0]++;
```

```
var tape = new int[3];
tape[0] += 10;
for (int i = 0; i < tape[0]; i++)</pre>
   tape[1] += 7;
   tape[2] += 10;
   tape[3] += 3;
```

```
var tape = new int[3];
tape[0] (+= 10;)
for (int i = 0; i < tape[0]; i++)</pre>
   tape[1] (+= 7;
   tape[2] += 10;
   tape[3] (+= 3;
```

```
var tape = new int[3];
tape[0] += 1; tape[0] += 1; tape[0] += 1;
tape[0] += 1; tape[0] += 1; tape[0] += 1;
                                            10 times
tape[0] += 1; tape[0] += 1; tape[0] += 1;
tape[0] += 1;
for (int i = 0; i < tape[0]; i++)
                                    7 times
   tape[1] += 1; tape[1] += 1; tape[1] += 1; tape[1] += 1;
   tape[1] += 1; tape[1] += 1; tape[1] += 1;
                                              10 times
   tape[2] += 1; tape[2] += 1; tape[2] += 1; tape[2] += 1;
   tape[2] += 1; tape[2] += 1; tape[2] += 1; tape[2] += 1;
   tape[2] += 1; tape[2] += 1;
                                   3 times
   tape[3] += 1; tape[3] += 1; tape[3] += 1;
```

```
var tape = new int[3];
int position = 0;
tape[position] += 10;
for (int i = 0; i < tape[position]; i++)</pre>
   position++; //1
   tape[position] += 7;
   position++;//2
   tape[position] += 10;
   position++;//3
   tape[position] += 3;
   position--;//2
   position--;//1
   position--;//0
```

Four cells

0	1	2	3
0	0	0	0
10	0	0	0
9	7	10	3
8	14	20	6
7	21	30	9
6	28	40	12
5	35	50	15
4	42	60	18
3	49	70	21
2	56	80	24
1	63	90	27
0	70	100	30

++++++++ p0v10

\Rightarrow	0	10						
	0	0						
	0	0						
	0	0						

72	101	108	108	111	32	119	111	114	108	100	33
Н	e			O		W		r		d	

\Rightarrow	0	10	0						
	0	0	70						
	0	0	100						
	0	0	30						

72	101	108	108	111	32	119	111	114	108	100	33
Н	e			O		W	O	r		d	

	0	10	0	0					
⇒	0	0	70	72					
	0	0	100	100					
	0	0	30	30					

72	101	108	108	111	32	119	111	114	108	100	33
Н	e					W		r		d	

	0	10	0	0					
	0	0	70	72					
>	0	0	100	101					
	0	0	30	30					

72	101	108	108	111	32	119	111	114	108	100	33
Η	e			O		W		r		d	

	0	10	0	0	0					
	0	0	70	72	72					
\Rightarrow	0	0	100	101	108					
	0	0	30	30	30					

72	101	108	108	111	32	119	111	114	108	100	33
Н	e	I				W		r		d	

	0	10	0	0	0	0
	0	0	70	72	72	72
⇒	0	0	100	101	108	108
	0	0	30	30	30	30

72	101	108	108	111	32	119	111	114	108	100	33
Н	e		1	O		W		r		d	

	0	10	0	0	0	0	0	
	0	0	70	72	72	72	72	
⇒	0	0	100	101	108	108	111	
	0	0	30	30	30	30	30	

72	101	108	108	111	32	119	111	114	108	100	33
Η	e			0		W		r		d	

	0	10	0	0	0	0	0	0				
	0	0	70	72	72	72	72	72				
	0	0	100	101	108	108	111	111				
>	0	0	30	30	30	30	30	32				

72	101	108	108	111	32	119	111	114	108	100	33
Н	e			0		W		r		d	

<+++++++. p2v+8

	0	10	0	0	0	0	0	0	0			
	0	0	70	72	72	72	72	72	72			
⇒	0	0	100	101	108	108	111	111	119			
	0	0	30	30	30	30	30	32	32			

72	101	108	108	111	32	119	111	114	108	100	33
Н	e			0		W		r		d	

----- p2v-8

	0	10	0	0	0	0	0	0	0	0		
	0	0	70	72	72	72	72	72	72	72		
⇒	0	0	100	101	108	108	111	111	119	111		
	0	0	30	30	30	30	30	32	32	32		

72	101	108	108	111	32	119	111	114	108	100	33
Н	e			0		W	0	r		d	ļ

+++. p2v+3

	0	10	0	0	0	0	0	0	0	0	0		
	0	0	70	72	72	72	72	72	72	72	72		
⇒	0	0	100	101	108	108	111	111	119	111	114		
	0	0	30	30	30	30	30	32	32	32	32		

72	101	108	108	111	32	119	111	114	108	100	33
Н	e			0		W	0	r		d	ļ

----- p2v-6

	0	10	0	0	0	0	0	0	0	0	0	0	
	0	0	70	72	72	72	72	72	72	72	72	72	
⇒	0	0	100	101	108	108	111	111	119	111	114	108	
	0	0	30	30	30	30	30	32	32	32	32	32	

72	101	108	108	111	32	119	111	114	108	100	33
Н	e			0		W	0	r	1	d	

----- p2v-8

	0	10	0	0	0	0	0	0	0	0	0	0	0	
	0	0	70	72	72	72	72	72	72	72	72	72	72	
⇒	0	0	100	101	108	108	111	111	119	111	114	108	100	
	0	0	30	30	30	30	30	32	32	32	32	32	32	

72	101	108	108	111	32	119	111	114	108	100	33
Н	e			0		W	0	r		d	ļ

	0	10	0	0	0	0	0	0	0	0	0	0	0	0
	0	0	70	72	72	72	72	72	72	72	72	72	72	72
	0	0	100	101	108	108	111	111	119	111	114	108	100	100
>	0	0	30	30	30	30	30	32	32	32	32	32	32	33

72	101	108	108	111	32	119	111	114	108	100	33
Н	e			0		W	0	r		d	İ



0	10	0	0	0	0	0	0	0	0	0	0	0	0
0	0	70	72	72	72	72	72	72	72	72	72	72	72
0	0	100	101	108	108	111	111	119	111	114	108	100	100
0	0	30	30	30	30	30	32	32	32	32	32	32	33

72	101	108	108	111	32	119	111	114	108	100	33
Н	e			0		W	0	r		d	ļ

"Hello world!" in BF

```
+++++++++
|>++++++>++++++++++>+
<<<-|
>++.>+.++++++..+++.>++.
<<+++++++++++++++-><sub>1</sub>+++<sub>1</sub>-----
.----.>+.>.
```

"Hello world!" in BF

```
+++++++++
|>++++++>+++++++++>+
<<<<-
>++.>+.++++++..+++.>++.
<<+++++++++++++++->.+++.
.----.>+.>.
```

How to do well?



"Hello world!" in BF

```
+++++++++
|>++++++>++++++++++>+
<<<<-
>++.>+.+++++..+++.>++.
--.>+.
```

Resources

- The Brainfuck Programming Language
- http://esolangs.org/wiki/Brainfuck
- http://www.hevanet.com/cristofd/brainfuck/
- http://www.iwriteiam.nl/Ha bf Turing.html