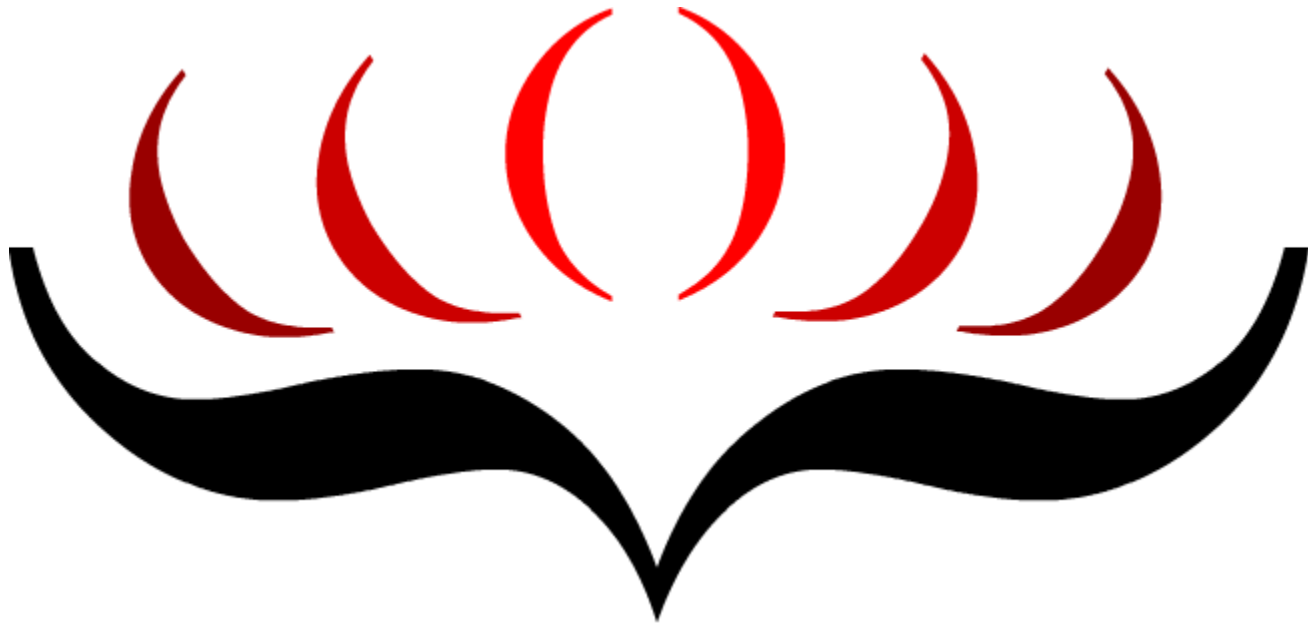


# The philosophy and history of functional programming



# Agenda

- Joseph Jacquard and Jacquard loom
- The theoretical basis of imperative programming
- The theoretical basis functional programming
- The first (electric) computer
- The LISP and other languages

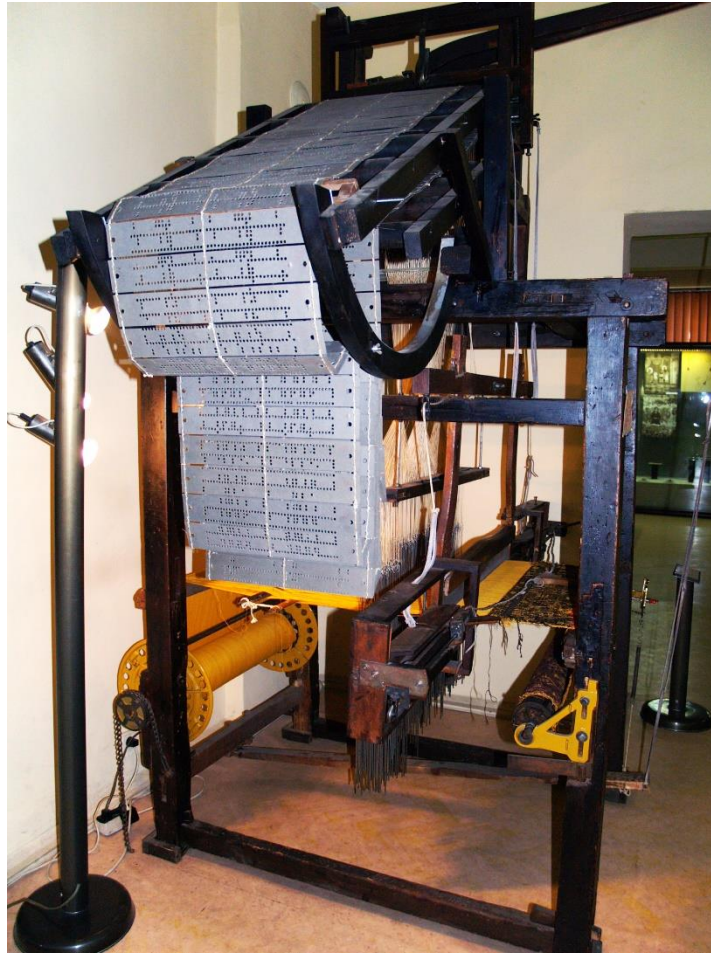
# Historical origins



# Joseph Marie Jacquard



# Jacquard loom (1805)



...

The theoretical basis of  
imperative programming  
was already founded in  
the 30s.

# Alan Turing





# John von Neumann



The theory of functions  
as a model for calculation  
comes also from the 20s  
and 30s.

# Moisei Sheinfinkel

(Moses Schönfinkel)



# Haskell Curry



# Alonzo Church



# Lambda calculus

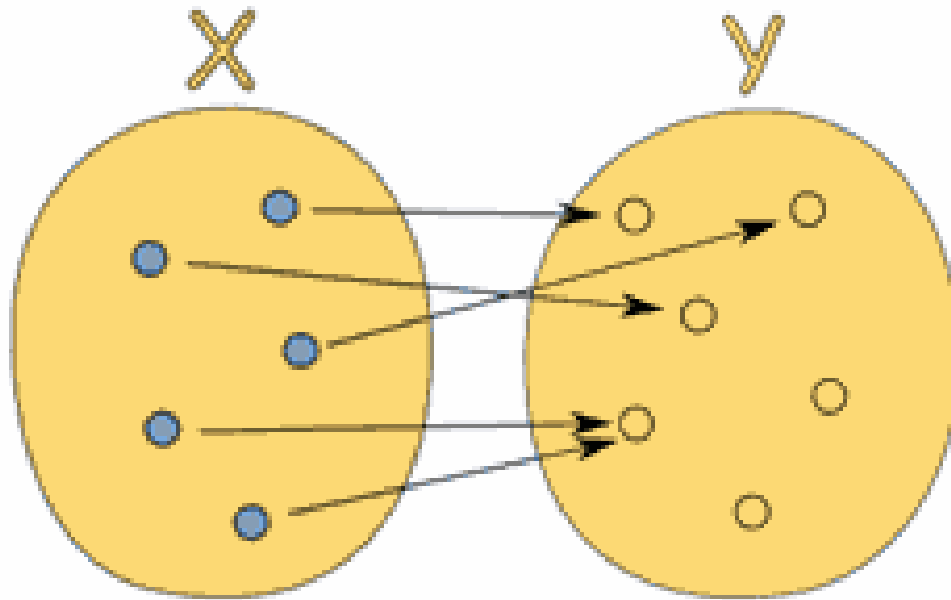
- It all began in the 1930's with Alonzo Church when he created the lambda calculus.

He wanted to describe the world in functions.

# Lambda ...



# Formal definition of a function





# The square

$$\text{square}(1) = 1 * 1 = 1$$

$$\text{square}(2) = 2 * 2 = 4$$

...

...

...

$$\text{square}(x) \equiv x * x$$

$$f(x) = x * x$$

# Lambda calculus

- $\text{square}(x) \equiv x * x$
- $f(x) = x * x$
- $\lambda(x) = x * x$

$\lambda x. x * x$

The diagram shows the lambda expression  $\lambda x. x * x$ . A red arrow points from the word 'argument' to the variable  $x$ . A red bracket points from the word 'body' to the expression  $x * x$ .

# Church encoding

- $0 := \lambda f. \lambda x. x$
  - $1 := \lambda f. \lambda x. f\ x$
  - $2 := \lambda f. \lambda x. f\ (f\ x)$
  - $3 := \lambda f. \lambda x. f\ (f\ (f\ x))$
- 
- $0 \rightarrow x$
  - $1 \rightarrow f(x)$
  - $2 \rightarrow f(f(x))$
  - $3 \rightarrow f(f(f(x)))$
  - $N+1 \rightarrow f(N)$

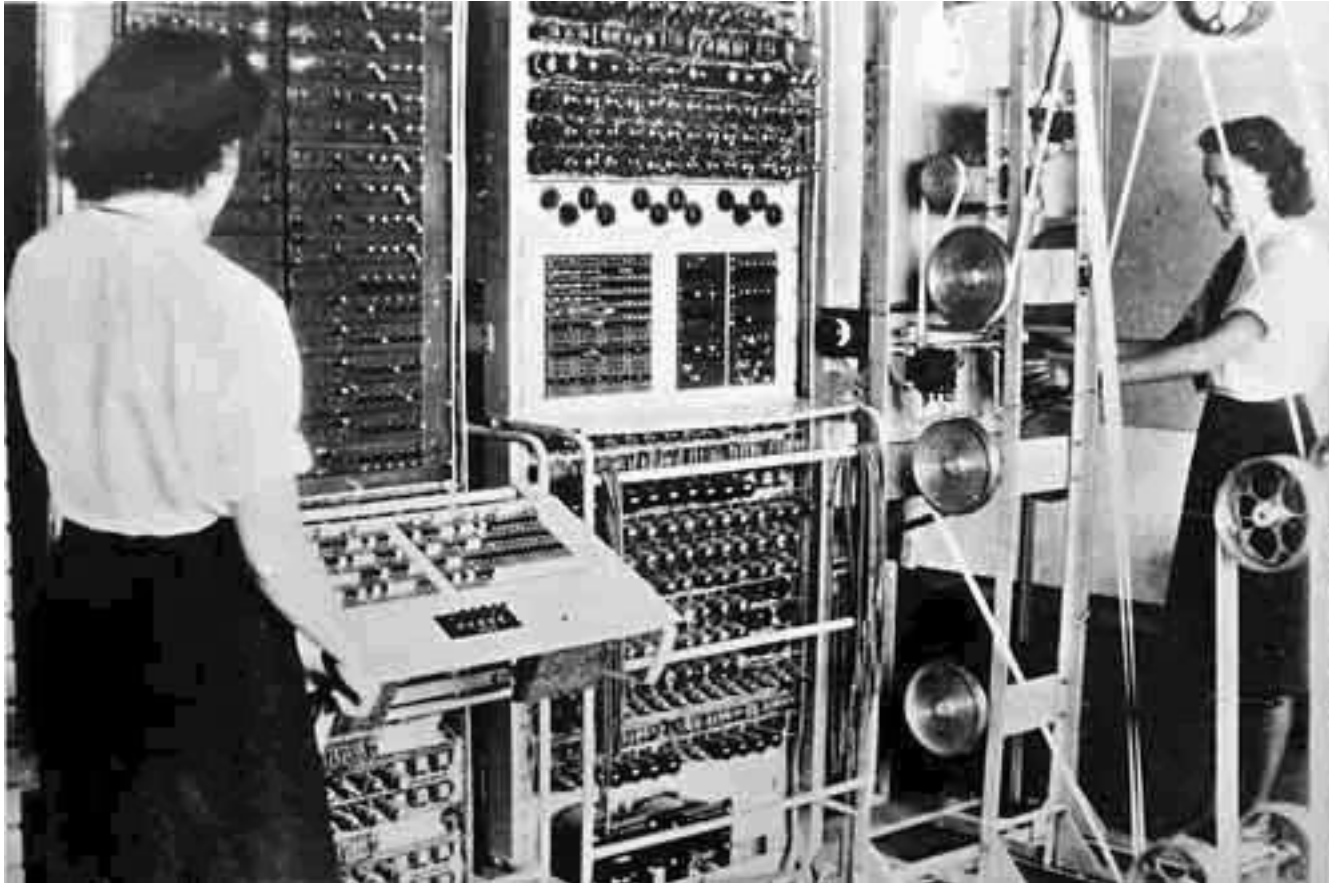
...

# World War II



In the 40s the first  
(electric programmable)  
computers were built.

# Colossus computer



# Colossus computer

It were used by British codebreakers  
during World War II

to help in the  
cryptanalysis of the  
Lorenz cipher.



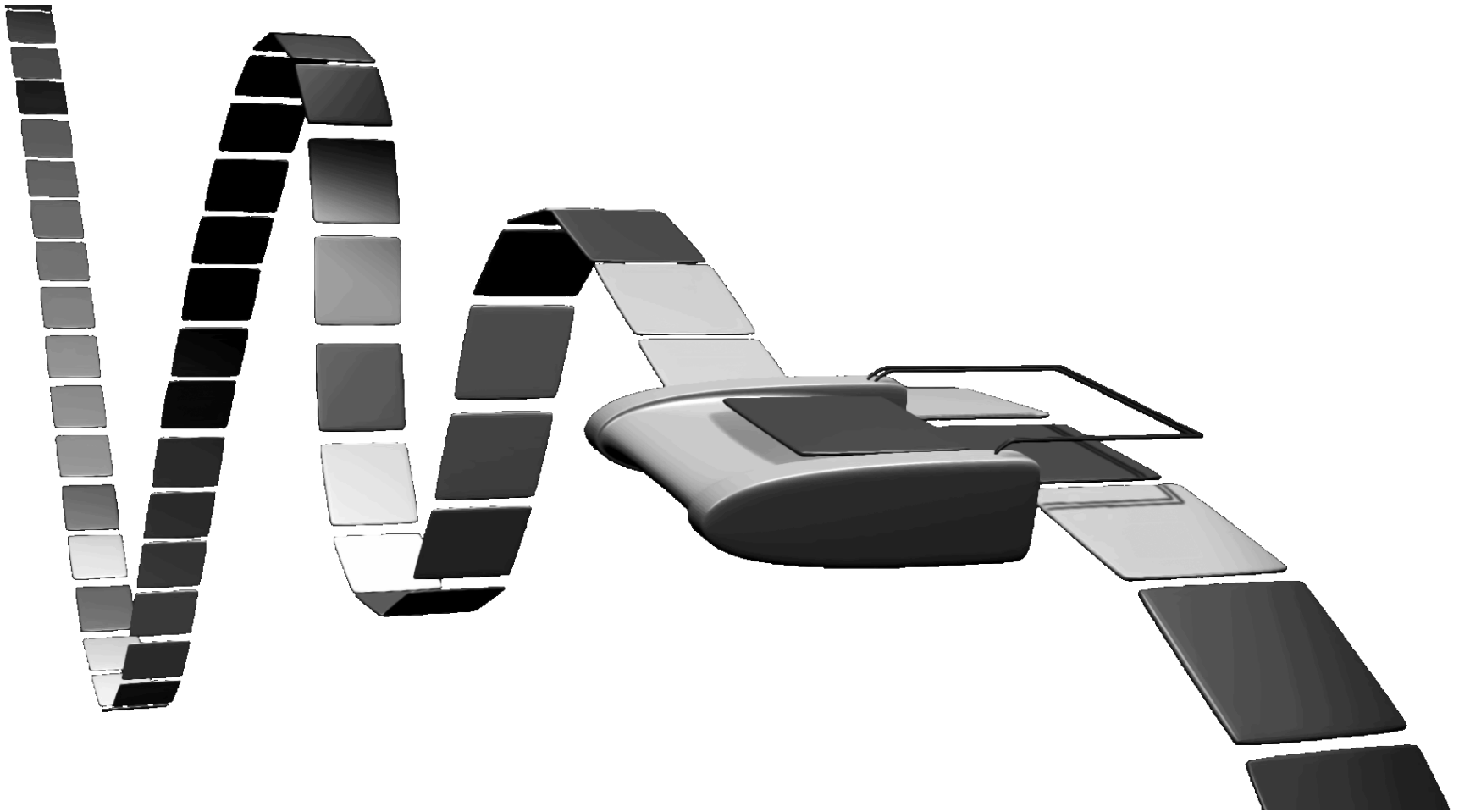
The first computers

In those days computer  
use was very expensive.

It was obvious to have the  
programming language resemble the  
architecture of the computer  
as close as possible.

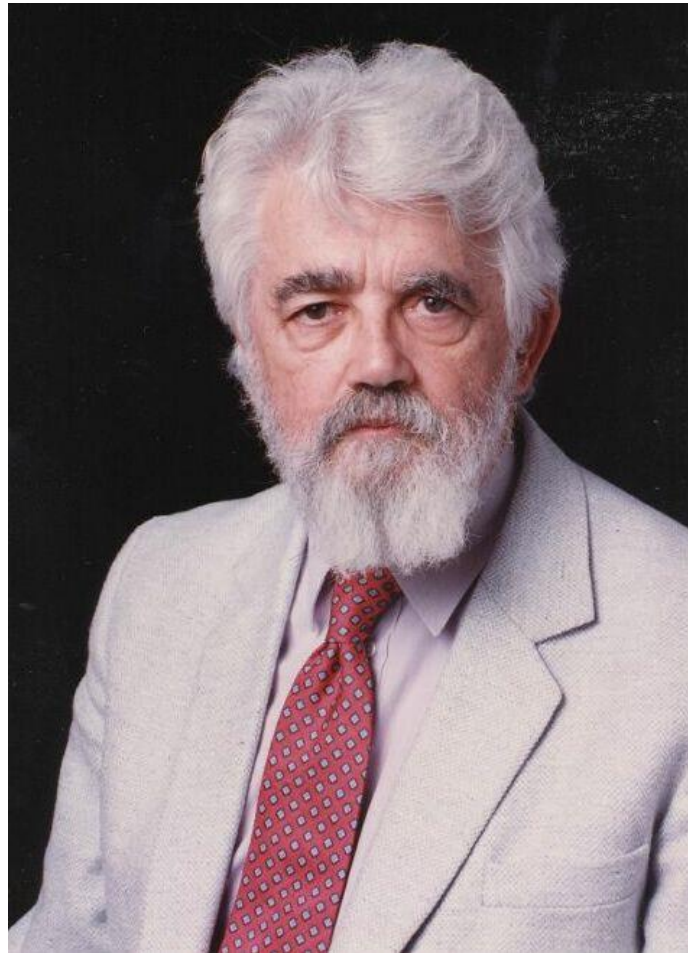
Focused only on the  
works of Alan Turing.

# The turing machine



...

# John McCarthy



## LISP (1958)

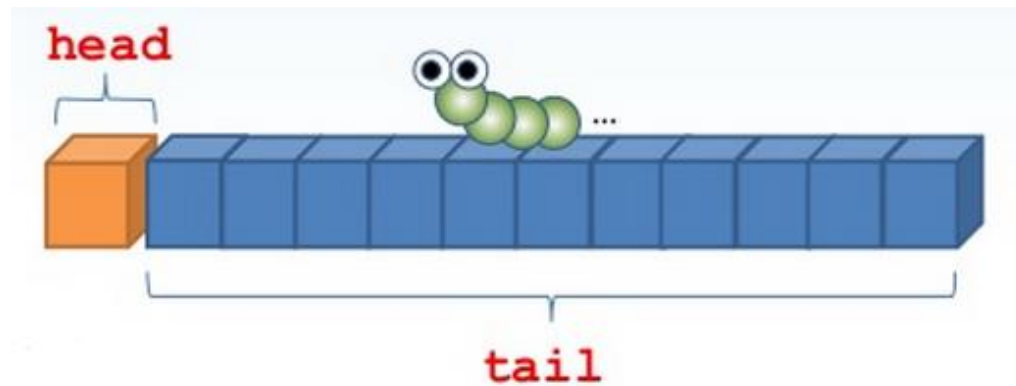
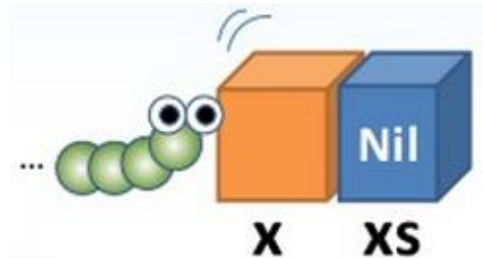
The name LISP derives from "LISt Processing".

- Lots of Irritating Superfluous Parentheses
- Lost In Stupid Parentheses

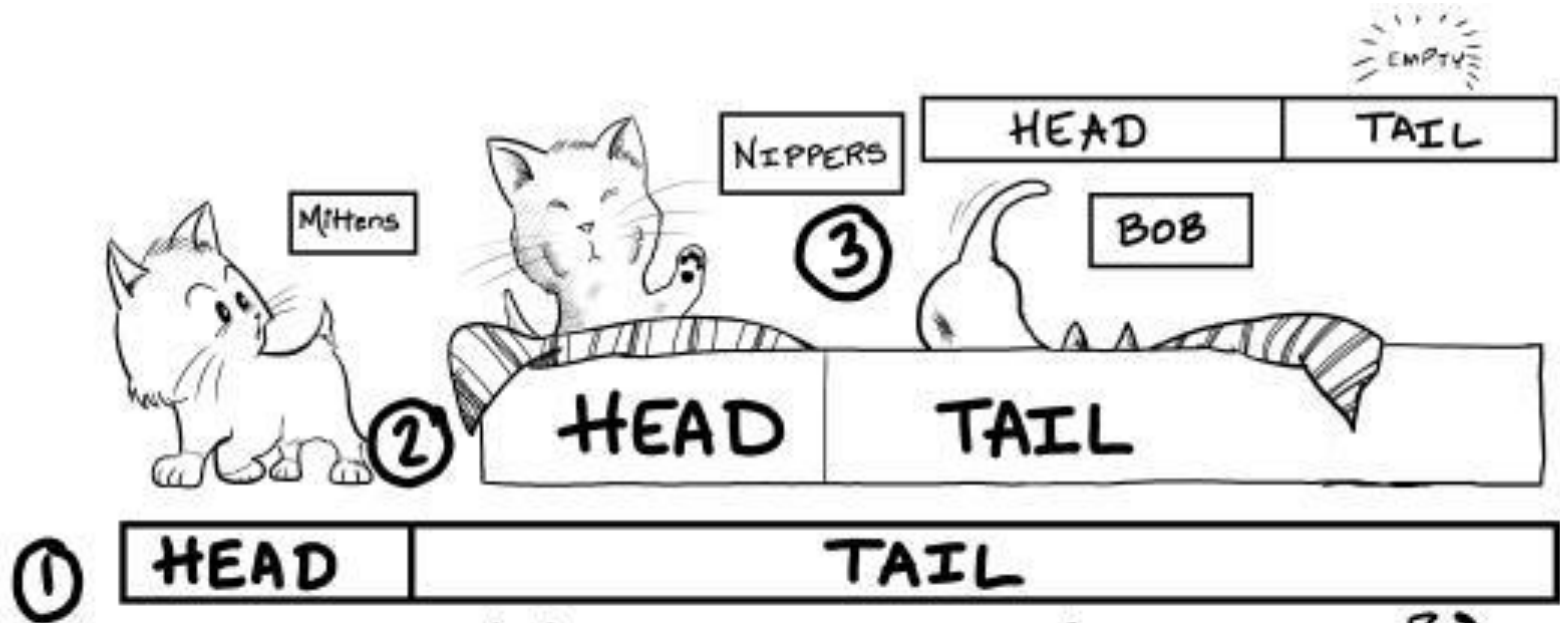
## A linked lists

Linked lists are one of Lisp language's major data structures, and Lisp source code is itself made up of lists.

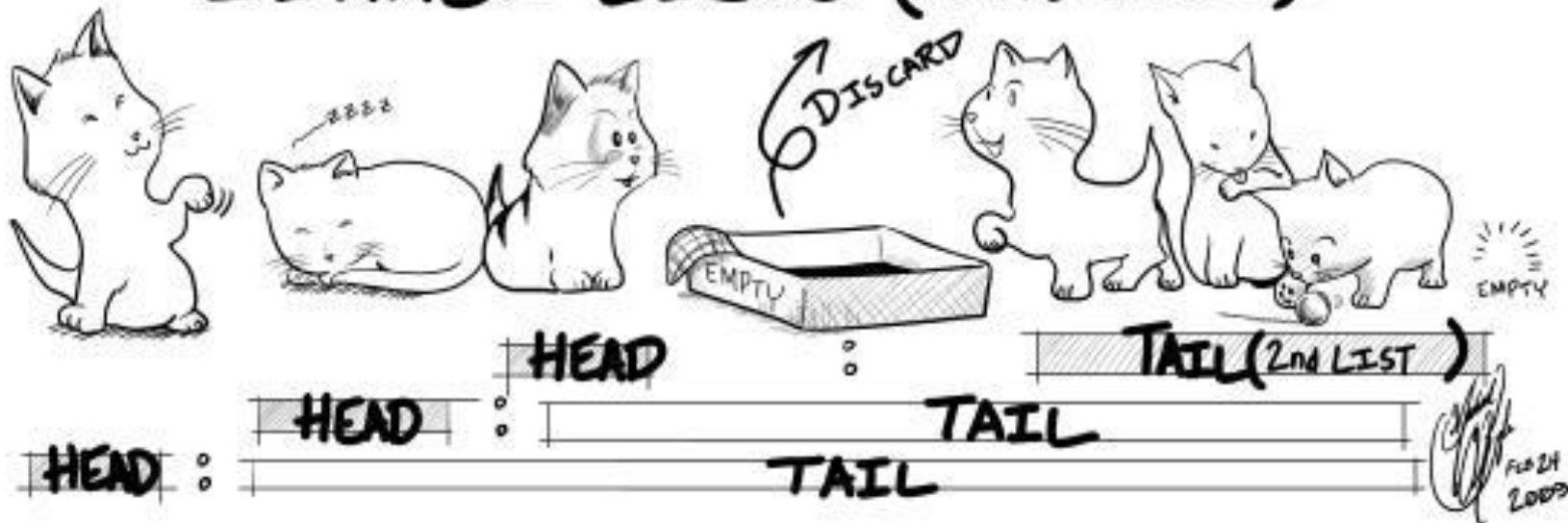
# A linked lists







## LINKED LISTS (with Cats?)



# Jan Łukasiewicz



A polish notation

It's a form of notation for  
logic, arithmetic, and  
algebra.

+ 3 4

Symbolic expressions (S-expressions)

A code in LISP  
is written  
as  
S-expressions.

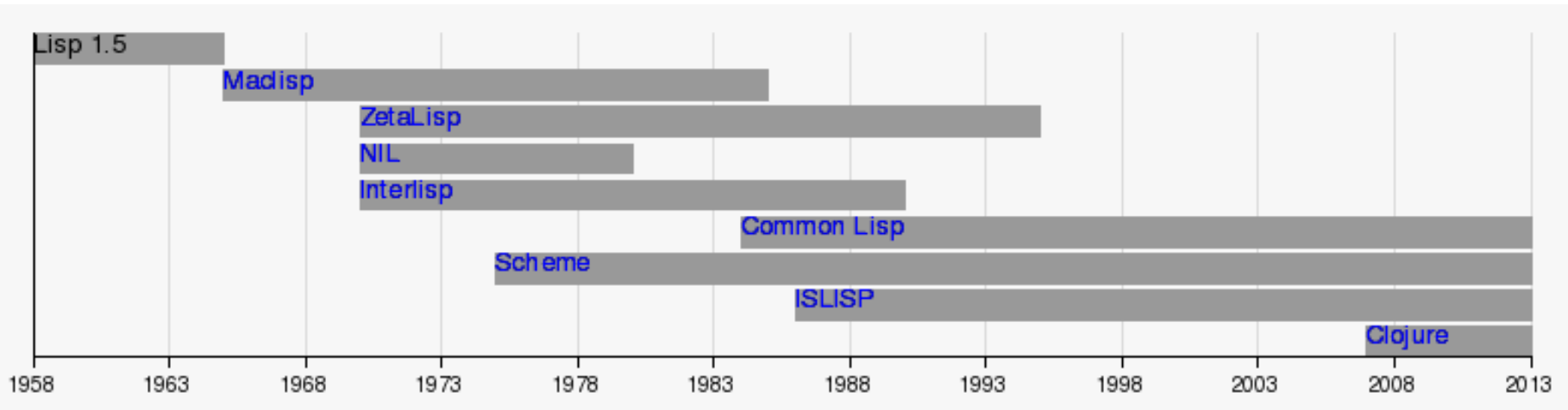
# S-expressions

- (A B C)
- (VeryLongLongName)
- (A (B C))

# Lisp pioneered many ideas

- tree data structures
- automatic storage management
- dynamic typing
- conditionals
- higher-order functions
- recursion
- the self-hosting compiler
- ...

# The LISP dialects



# Peter Landin





Peter Landin's work in the mid 60's was the next significant impetus to the functional programming paradigm.

ISWIM (1966)

If you See What I Mean.

- Also said to have stood for "I See What You Mean", but ISWYM was mistyped as ISWIM.

PAL (1968)

# Pedagogic Algorithmic Language

- The PAL language is a direct descendent of Peter Landin's ISWIM, although there are important differences, particularly in the imperatives.

# David Turner



# SASL (1973)

The name SASL stands for  
"St Andrews Static  
Language"

- SASL is a mathematical notation for describing certain kinds of data structure.

# SASL (1973)

- In SASL a "program" is an expression describing some data object.

2+3?

is a SASL program, to which the system responds by printing:

5

# SASL (1973)

A slightly more complicated example will serve better to convey the flavour of the language

fac 4

where fac 0 = 1

fac n = n \* fac (n - 1)

?

# SASL (1973)

"fac 4" yields in succession the expressions:

$4 * \text{fac } 3$

$4 * (3 * \text{fac } 2)$

$4 * (3 * (2 * \text{fac } 1))$

$4 * (3 * (2 * (1 * \text{fac } 0)))$

$4 * (3 * (2 * (1 * 1)))$

which gives the value 24



# Robin Milner



## ML (1973)

ML is a general-purpose  
functional programming  
language.

- Syntax is inspired by ISWIM.

## ML (1973)

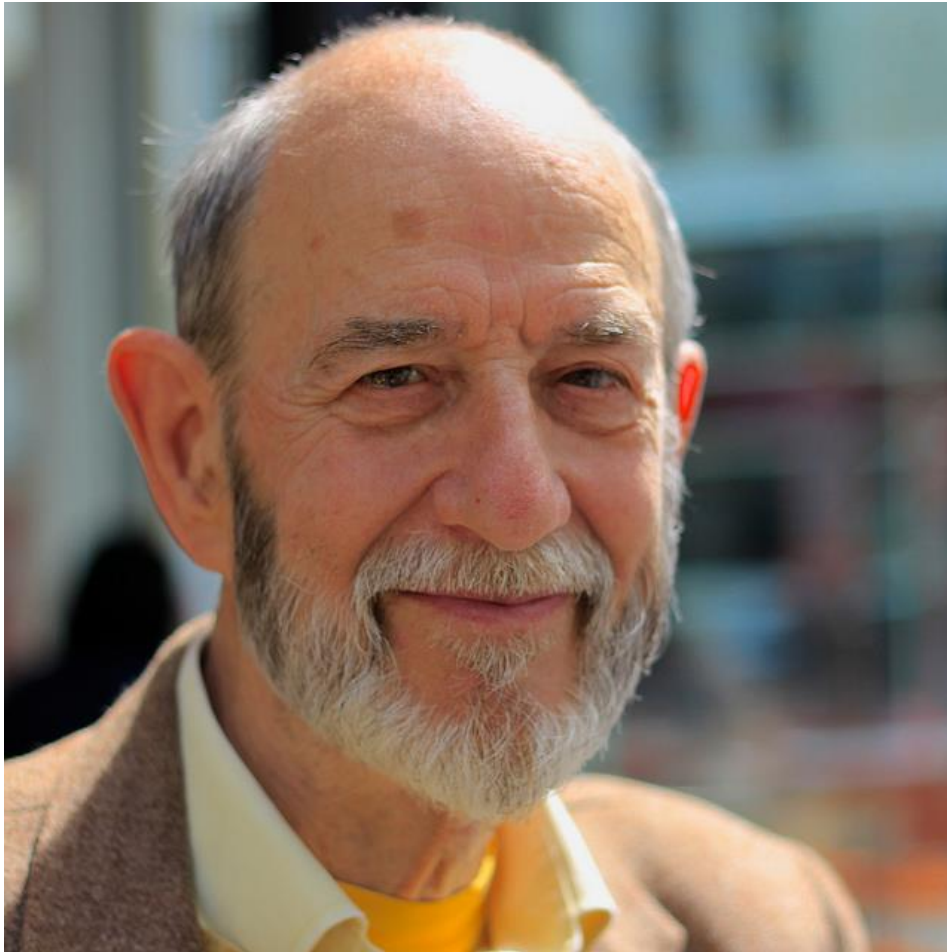
It was conceived to develop  
proof tactics in the LCF  
theorem prover.

- ML is often referred to as an impure functional language

# ML influenced

- Miranda
- Haskell
- Cyclone
- C++
- F#
- Clojure
- Erlang
- ...

# Rod Burstall



NPL (1977)

NPL was a functional programming language with pattern matching.

Hope (~80)

The name may have been  
derived from Hope Park  
Square in Edinburgh,

at one time the location of the Department of  
Artificial Intelligence.

# Hope (~80)

Language with polymorphic typing, algebraic types, pattern matching and higher-order functions.

- It predates Miranda and Haskell and is contemporaneous with ML.



# David Turner



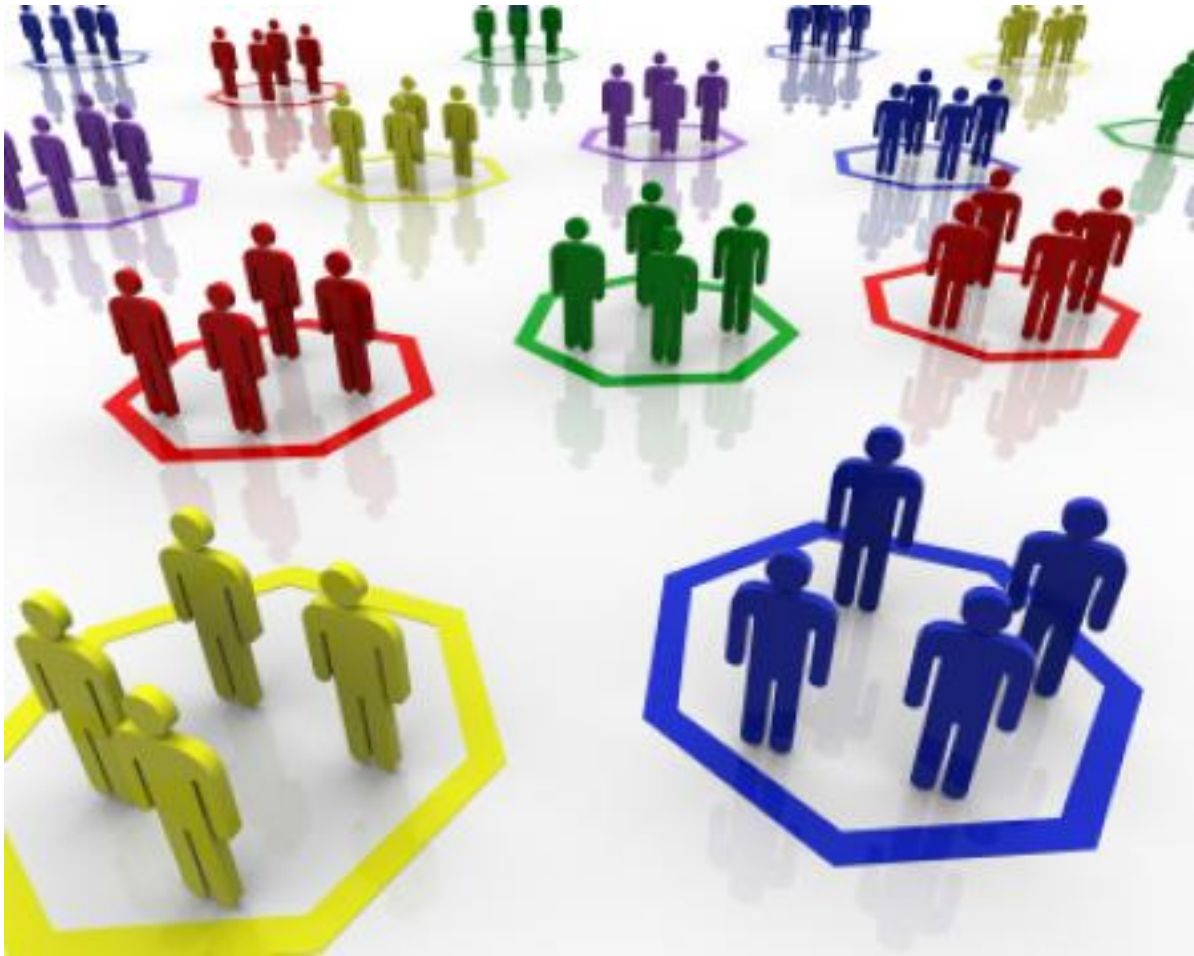
## Miranda (1985)

Miranda is a lazy, purely functional programming language.

- The later Haskell programming language is similar in many ways to Miranda.

...

# Each group develops its own language



# Haskell (1987)

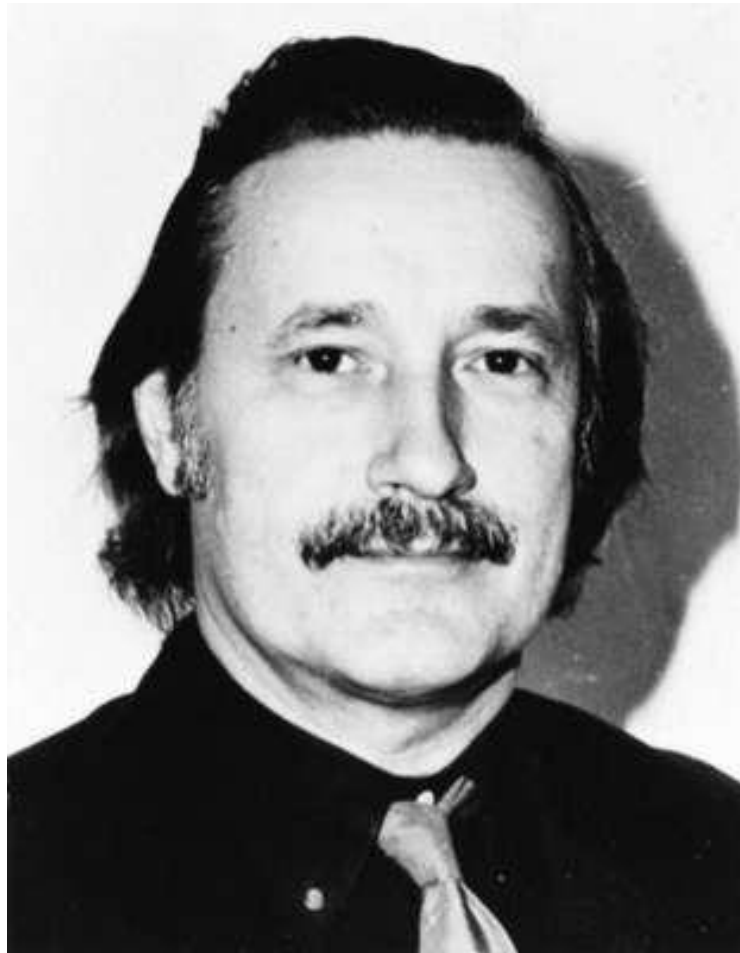
It's a standardized, general-purpose purely functional programming language, with non-strict semantics and strong static typing.

...

# Concepts of functional programming

- First-class and higher-order functions
- Pattern matching
- Single assignment
- Lazy evaluation
- Garbage collection
- List comprehensions
- ...

# Christopher Strachey





# First-class function

The term was coined by Christopher Strachey in the context of “functions as first-class citizens” in the mid-1960s

# First-class function

Features can be stored in variables, passed as arguments to functions, created within functions and returned from functions.

# First-class function

- $\text{map} :: (a \rightarrow b) \rightarrow [a] \rightarrow [b]$
- $\text{map } f [] = []$
- $\text{map } f (x:xs) = f x : \text{map } f xs$

# Higher order function

The complete concept of higher-order functions is based two ideas:

- functions can be passed as arguments
- a normal function (or even nested functions) can be returned from a function.

# Higher order function

Language		Higher-order functions		Non-local variables			Partial application	Notes
		Arguments	Results	Nested functions	Anonymous functions	Closures		
Algol family	ALGOL 60	Yes	No	Yes	No	No	No	Have <a href="#">function types</a> .
	ALGOL 68	Yes	Yes <sup>[8]</sup>	Yes	Yes	No	No	
	Pascal	Yes	No	Yes	No	No	No	
	Oberon	Yes	Non-nested only	Yes	No	No	No	
C family	C	Yes	Yes	No	No	No	No	Has <a href="#">function pointers</a> .
	C++	Yes	Yes	No	C++11 <sup>[9]</sup>	C++11 <sup>[9]</sup>	No	Has <a href="#">function pointers</a> , <a href="#">function objects</a> . (Also, see below.)
	<u>C#</u>	Yes	Yes	No	2.0 / 3.0	2.0	No	Has <a href="#">delegates</a> (2.0) and <a href="#">lambda expressions</a> (3.0).
	Objective-C	Yes	Yes	No	2.0 + Blocks <sup>[10]</sup>	2.0 + Blocks	No	Has <a href="#">function pointers</a> .
	<u>Java</u>	Partial	Partial	No	No	8	No	Has <a href="#">anonymous inner classes</a> .
<u>Functional languages</u>	Lisp	Syntax	Syntax	Yes	Yes	Common Lisp	No	(see below)
	Scheme	Yes	Yes	Yes	Yes	Yes	SRFI 26 <sup>[11]</sup>	
	Clojure	Yes	Yes	Yes	Yes	Yes	Yes	
	ML	Yes	Yes	Yes	Yes	Yes	Yes	
	Haskell	Yes	Yes	Yes	Yes	Yes	Yes	
	Scala	Yes	Yes	Yes	Yes	Yes	Yes	
Scripting languages	JavaScript	Yes	Yes	Yes	Yes	Yes	ECMAScript 5	Partial application possible with user-land code on ES3 <sup>[12]</sup>
	PHP	Yes	Yes	Unscoped	5.3	5.3	No	(see below)
	Perl	Yes	Yes	anonymous, 6	Yes	Yes	6 <sup>[13]</sup>	(see below)
	Python	Yes	Yes	Yes	Partial	Yes	2.5 <sup>[14]</sup>	(see below)
	Ruby	Syntax	Syntax	Unscoped	Yes	Yes	1.9	(see below)
Other languages	Mathematica	Yes	Yes	Yes	Yes	Yes	No	
	Smalltalk	Yes	Yes	Yes	Yes	Yes	Partial	Partial application possible through library.
	Fortran	Yes	Yes	Yes	No	No	No	

# A lexical closures

- It's a function that can refer to and alter the values of bindings established by binding forms that textually include the function definition.
- It's often referred to just as a closure

# A pattern matching



# A pattern matching

It's a dispatch mechanism:  
choosing which variant of a  
function is the correct one to call.

- The patterns generally have the form of either sequences or tree structures.
- Inspired by standard mathematical notations.
- Pattern matching is not a switch.



# A single assignment

When a variable is assigned  
once, at most.

- It's also called *initialization*.
- It does not make sense in an **imperative programming**.

# A lazy evaluation



# A lazy evaluation

An evaluation should be delayed as long as they do not need the result.

- It's also known as **call-by-need**.
- It's opposite a **strict evaluation**.

# A lazy evaluation

- lazy evaluation frees a programmer from concerns about evaluation order
- the ability to compute with unbounded (“infinite”) data structures

# A garbage collection

It's a form of automatic memory management.

- It attempts to reclaim memory occupied by objects that are no longer in use by the program.
- It was invented by John McCarthy around 1959 to solve problems in Lisp

# A garbage collection

There are three main techniques for automatic memory management:

- reference counting
- mark-and-sweep
- copying.

## A list comprehensions

It's *syntactic sugar* for a combination of applications of the functions concat, map and filter.

# A list comprehensions in Haskell

```
pyth n = [ ( a, b, c ) | a <- [1..n],  
                        b <- [1..n-a+1],  
                        c <- [1..n-a-b+2],  
                        a + b + c <= n,  
                        a^2 + b^2 == c^2 ]
```



# The key idea

Do everything by composing functions:

- no mutable state
- no side effects

# In summary

This is a way to create a program in which:

- the only one action is to call a function
- the only one way partition is a function
- the only one rule of composition - the composition of functions

No memory nor assignment operators nor cycle  
nor block diagrams nor flow control ...

# Resource

## Books and papers

- **Functional Programming Application and Implementation** by *Peter Henderson*
- **A Unification of Functional and Imperative Languages** by *Ben Zhang*
- **The Conception, Evolution, and Application of Functional Programming Languages** by *Paul Hudak (Yale University)*
- **SASL LANGUAGE MANUAL** by *David Turner*
- **PAL -- A Reference Manual and a Primer** by *A. Evans*