

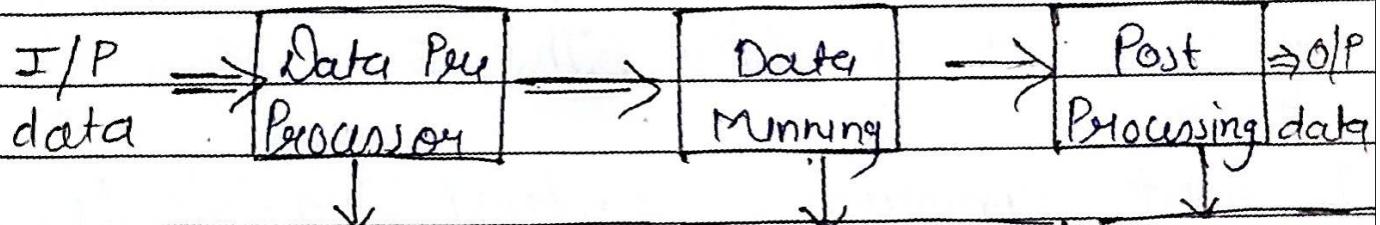
Data Science :-

Abstracting information from a source
is called data mining.

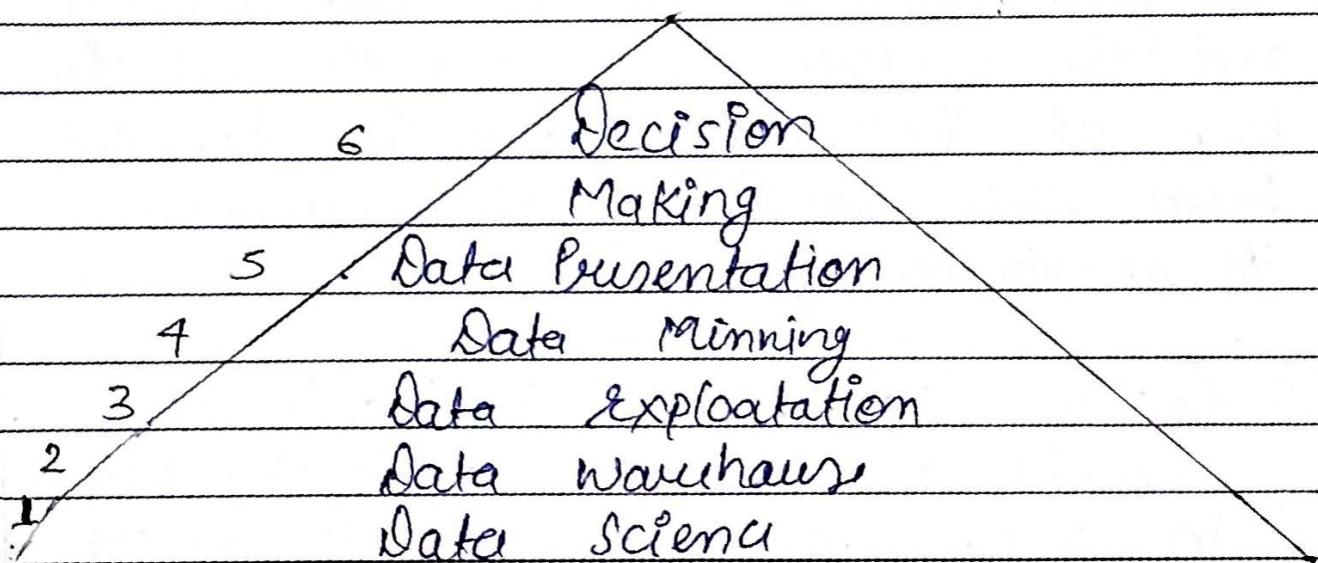
→ Compilation Process :-

1. Lexical analyser
2. Syntax analyser
3. Semantic
4. Intermediate
5. Code optimisation
6. Code generation

21/08/23

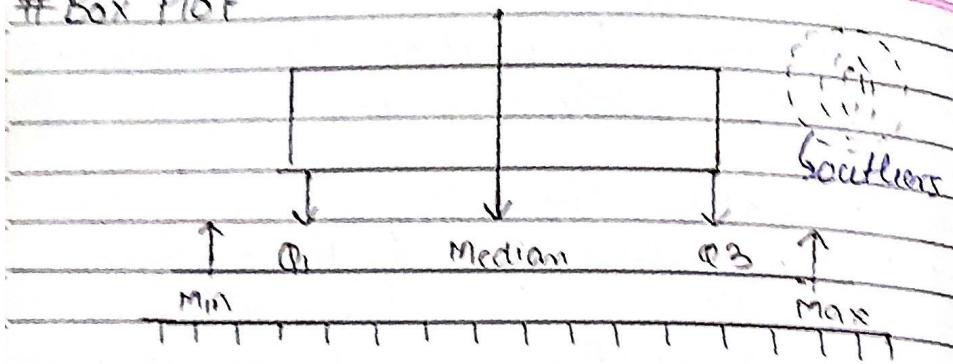


• Data interpretation	• Pattern visualisation	• Pattern visualisation
• clarity	• classification	• Data validation



6 D's

Box Plot



A box plot displays the 5 no. summary of a set of data. The 5 no. summary :-

1. first minimum
2. first Quartile (Q₁)
3. Minimum first Quartile
- 4.

In a box plot we draw a box from the first quartile to the 3rd quartile and the vertical line goes through the box at the median and the box goes from each quartile to the minimum to maximum for ex:-

- (Q1) finding the 5 no. summary. A sample of 10 boxes with the weight in gram i.e. 25g, 28g, 29g, 29g, 30g, 32g, 35g, 37g, 38g, 39g make a box plot of the data

Step 1 :- Order the data from smallest to largest

25, 28, 29, 29, 30, 31, 35, 35, 37, 38

Step 2 :- find the median

$$\frac{30+31}{2} = 32$$

Step 3 :- finding 1st Quartile :-

The first quartile is the median of the data points to the left of the median i.e. Q₁

$$\Rightarrow Q_1 = 29.$$

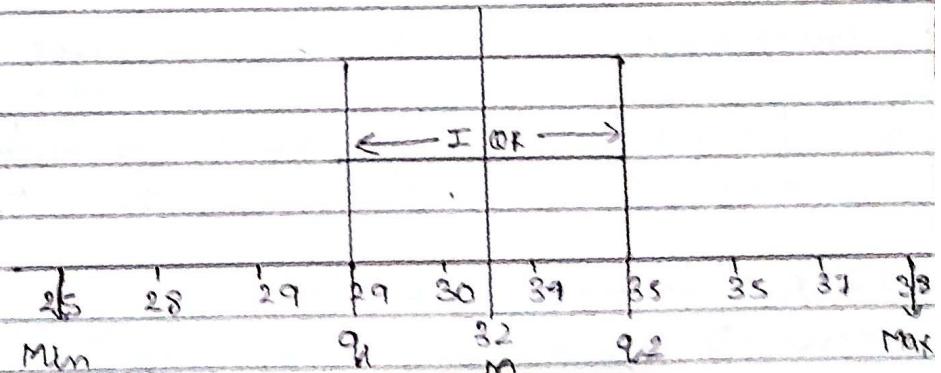
Step 4 :- find 3rd Quartile :-

The third quartile is the median of the data points that is right of the median

$$\Rightarrow Q_3 = 35$$

Step 5 :- find Min and Max

$$\Rightarrow \text{Min} = 25, \text{Max} = 38$$



$$\Rightarrow \text{Inter Quartile Range (IQR)} = Q_3 - Q_1$$

$$\Rightarrow IQR = 35 - 29 = 6$$

$$\Rightarrow \text{lower limit} = 236 - 97.5$$

$$\Rightarrow \text{lower limit} = 138.5$$

(Q) find out the 5 tuple summary with (IQR) let the data range be 199, 201, 236, 271, 278, 283, 291, 301, 303, 341
 $\therefore n = 11$

STEP 1 :- 199, 201, 236, 271, 278, 283, 291, 301, 303, 341,

STEP 2 :- $M = 278$

STEP 3 :- $Q_1 = 236$

STEP 4 :- $Q_3 = 301$

STEPS :- Min 199, Max 341

lower limit

upper limit

138.5 199 201 236 269 271 278 283 291 301 303 341
 Min Q_1 M Q_3 Max

$$\Rightarrow IQR = 301 - 236 = 65$$

$$\text{Min} \Rightarrow \text{lower limit} = Q_1 - 1.5(IQR)$$

$$\Rightarrow \text{upper limit} = Q_3 + 1.5(IQR) = 301 + 97.5$$

$$\Rightarrow \text{upper limit} = 398.5$$

Least Square Method

(Q) A producer believes that the sale of his product for that years is related to an economic index and the data for that period is shown in the following tables

Years	Economic Index (x)	Sales (Y_n) 1000 unit
1	104	2.0
2	100	2.3
3	111	2.1
4	129	2.6
5	126	2.3
6	115	2.4
7	152	2.5
8	161	2.8
9	143	2.6
10	170	3.0
$n = 10$	$\sum x = 1311$	$\sum Y_n = 24.6$

(Q) Determine the equation of the least square line that describe the relation

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b/w the rate and the economic indicator.

- ii) Determine the strength of the relation b/w the two variables by computing the value of coefficient of correlation
iii) If the value of the economic index for 11th year is 175 find out the sales in the 11th year

Soln $y = a + mx \Rightarrow Y_a = na + m \sum x$ — (1)

for for list

$$\sum xy_a = a \sum x + m \sum x^2 \quad \text{square method} — (2)$$

$$\Rightarrow 24.6 = 10.a + m \cdot 1311$$

Years	Economic Index (Y)	Sales (Y_a)
	10000 Units	
1	104	2.0
2	180	2.3
3	111	2.1
4	129	2.6
5	126	2.3
6	115	2.4
7	152	2.5
8	161	2.8
9	143	2.6
10	170	3.0
$\sum x = 1311$		$\sum y_a = 24.6$
$\sum xy_a = 177253$		61.36
$\sum x^2 = 32849$		

$$P = n \sum xy_a - (\sum x) \cdot (\sum y)$$

$$(2) \sqrt{n \sum x^2 - (\sum x)^2} \sqrt{n \sum y_a^2 - \sum y^2}$$

coefficient of relation

$$\Rightarrow 24.6 = 10.a + 1311m — (3)$$

$$\Rightarrow 3284.9 = 1311a + 177253m — (4)$$

Multiply with 1311 on eqn (3) and 10 on eqn (4)

$$\Rightarrow 32250.6 = 13110a + 1718721m$$

$$\Rightarrow 32849.0 = 13110a + 1772530m$$

$$+ 5984 = + 53809m$$

$$\Rightarrow m = 0.011$$

$$\Rightarrow 24.6 = 10a + 14.421$$

$$\Rightarrow a \approx 1.01 \text{ ans} //$$

$$1) Y_a = 1.002 + 0.011x$$

$$2) \sigma = \frac{n \sum xy_a - (\sum x) \cdot (\sum y)}{\sqrt{n \sum x^2 - (\sum x)^2} \sqrt{n \sum y_a^2 - (\sum y)^2}}$$

$$= 10 \times 3284.9 - (1311) \cdot (24.6)$$

$$\sqrt{10 \times 177253 - (1311)^2} \sqrt{(10 \times 61.36 - (24.6)^2)}$$

$$= 32849 - 32250.6 = 598.4$$

$$\sqrt{53809} \times \sqrt{8.44} = 673.84$$

$$\Rightarrow \sigma = 0.89 \text{ ans} //$$

$$3) Y_a = 1.002 + 0.011(x)$$

$$= 1.002 + 0.011(175)$$

$$\Rightarrow Y_a = 2.927$$

	15	70	105	225	
	16	40	64	256	
	$\sum x = 136$	$\sum Y_a = 54$	522	1496	

Time Series Analysis

Ques1) Find the Quarterly sales of the fifth year by suitable forecasting method/technique for the data given 4 years also make adjustment for expected seasonal variation

$$n = 16$$

\Rightarrow We know that

$$\sum Y_a = na + m \sum x$$

\Rightarrow putting values

$$54 = 16a + m \times 136$$

$$54 = 16a + 136m \quad \text{--- (1)}$$

\Rightarrow now,

$$\sum x Y_a = a \sum x + m \sum x^2$$

\Rightarrow putting values

$$522 = a \times 136 + m \times 1496$$

$$522 = 136a + 1496m \quad \text{--- (2)}$$

\Rightarrow multiplying eqn (1) with 11 and then eqn (1) - eqn (2)

$$594 = 176a + 1496m$$

$$522 = 136a + 1496m$$

$$- \quad - \quad -$$

$$72 = 40a$$

$$\Rightarrow a = \frac{72}{40} = 1.80$$

\Rightarrow put a in eqn (1)

$$54 = 16 \times 1.80 + 136m$$

$$54 = 28.8 + 136m$$

$$54 - 28.8 = 136m$$

$$25.2 = 136m$$

$$\Rightarrow m = \frac{25.2}{136} \Rightarrow 0.185$$

Years	Quarter(x)	Sales 1000 units	$x Y_a$	x^2	$x^3 = 1.80x$
1	1	1.0	1	1	$y_1 = 1.985$
	2	3.0	6	4	$y_2 = 2.17$
	3	4.0	12	9	$y_3 =$
	4	2.0	8	16	
2	5	1.0	5	25	
	6	3.0	18	36	
	7	5.0	35	49	
	8	3.0	24	64	
3	9	2.0	48	81	
	10	4.0	40	100	
	11	6.0	66	121	
	12	2.0	24	144	
4	13	2.0	26	169	
	14	5.0	70	196	

$$\text{So } y^1 = 1.80 + 0.185x$$

now for 5th year, we have to find quarterly sales of 5th year i.e for

$x = 17, 18, 19, 20$

$$\Rightarrow y^{17} = 1.80 + 0.18(17) = 4.945$$

$$\Rightarrow y^{18} = 1.80 + 0.18(18) = 5.13$$

$$\Rightarrow y^{19} = 1.80 + 0.18(19) = 5.315$$

$$y^{20} = 1.80 + 0.18(20) = 5.5$$

(Ques 2) A machine shop produces steel pins. The width of the 100 pins was checked after manufacturing and data was recorded as follows

width (in mm)	freq (f)	fx_f	x^2	f_x^2	cell mid point (x)
9.50 - 9.51	6	57.03	90.34	542.04	9.505
9.52 - 9.53	2	19.05	90.72	181.44	9.525
9.54 - 9.55	20	190.09	91.10	1822	9.545
9.56 - 9.57	32	306.08	91.48	2927	9.565
		36			
9.58 - 9.59	22	210.87	91.87	2021	9.585
		14			
9.60 - 9.61	8	76.14	92.25	738	9.605
9.62 - 9.63	6	57.75	92.64	555	9.625
		84			

9.64 - 9.65	4	38.58	93.02	372.08	9.645
$\Sigma f_i = 100$		957.1	733.42	9159.9	

→ find out arithmetic mean, standard deviation and variance (H.W)

$$\text{Formula :- 1) Mean : } \bar{x} = \frac{\sum f_i x_i}{\sum f_i}$$

$$2) \text{Standard deviation : } \sigma = \sqrt{\frac{\sum f_i x^2 - (\bar{x})^2}{n}}$$

$$3) \text{Variance} = \sigma^2$$

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$$\text{Solt} \quad 1) \text{Mean} = \bar{x} = \frac{\sum f_i x_i}{\sum f_i} = \frac{957.1}{100} = 9.571$$

$$\Rightarrow \text{Mean} = 9.571$$

$$2) \text{Standard deviation : } \sigma = \sqrt{\frac{\sum f_i x^2 - (\bar{x})^2}{n}}$$

$$\Rightarrow \sigma = \sqrt{\frac{9160.12 - (9.572)^2}{100}}$$

$$\Rightarrow \sigma = \sqrt{91.601 - 91.604}$$

$$\Rightarrow \sigma = \sqrt{-0.03} \Rightarrow \sigma = 0.031$$

$$3) \text{Variance} = \sigma^2 = 0.03$$

(Ans)

The measured values are ~~344°, 338°, 342°, 335° and 336°~~ their values are constitute the first sub group

frequency distribution:-

frequency distribution is a tabulation of data obtained from measurement arranged in ascending or descending

order acc. to size and find out

determine the range of the data,

arithmetic mean, mid point, median & mode

$$\Rightarrow \sigma = \sqrt{\frac{(335-339)^2 + (336-339)^2 + (338-339)^2 + (342-339)^2 + (344-339)^2}{5}}$$

$$\Rightarrow \sigma = \sqrt{\frac{16+9+1+9+25}{5}} = \sqrt{\frac{60}{5}}$$

$$\Rightarrow \sigma = \sqrt{12} \Rightarrow \sigma = 3.46 \text{ Std deviation}$$

$$\Rightarrow \sigma^2 = 12 \rightarrow \text{variance}$$

Ques 3) 5 theoretical control are listed Ques 4) The mean and the standard deviation of a sample of 100 observations were calculated as 40 and 5.1 respectively while comparing with the original data it was found that by mistake a figure of 40 was mis-copied as 50 for one observation

Soln arranging f in ascending order

$$\Rightarrow 335, 336, 338, 339, 342, 344$$

$$\Rightarrow \text{Median} = 338$$

$$\Rightarrow AM(\bar{x}) = \frac{335 + 336 + 338 + 342 + 344}{5} = 339$$

$$\Rightarrow \text{Range} = 344 - 335 = 9$$

$$\Rightarrow \text{std deviation} = \sqrt{\frac{(x_1-\bar{x})^2 + (x_2-\bar{x})^2 + \dots + (x_n-\bar{x})^2}{N}}$$

-ation was calculated as 40 and S.D respectively while comparing with the original data it was found that by mistake a figure of 40 was mis-copied as 50 for one observation calculate the correct mean and std. deviation.

$$\left. \begin{aligned} \text{Soln} \quad & \because AM(\bar{x}) = \frac{\sum x}{N} \\ & \therefore \sigma = \sqrt{\frac{\sum x^2 - (\bar{x})^2}{N}} \end{aligned} \right\}$$

$$\textcircled{1} \quad \bar{x} = \frac{\sum x}{N} \Rightarrow 40 = \frac{\sum x}{100}$$

$$\Rightarrow \sum x = 4000$$

$$\Rightarrow \sum x = 4000 - 50 + 40 = 3990$$

$$\Rightarrow \sum x = 3990$$

$$\bar{x} = 39.90$$

$$\Rightarrow \text{std deviation } (\sigma) = \sqrt{\frac{\sum x^2 - (\bar{x})^2}{N}}$$

$$\Rightarrow s \cdot 1 = \sqrt{\frac{\sum x^2 - (40)^2}{100}}$$

$$\Rightarrow (s \cdot 1)^2 = \frac{\sum x^2}{100} - 1600$$

$$\Rightarrow 26.01 = \frac{\sum x^2}{100} - 1600$$

$$\Rightarrow (26.01 + 1600) \times 100 = \sum x^2$$

$$\Rightarrow \sum x^2 = 162601 \times 100$$

$$\Rightarrow \sum x^2 = 162601 - 50^2 + 40^2 \\ 162601 - 2500 + 1600$$

$$\sum x^2 = 162601 - 900$$

$$\sum x^2 = 161701 \rightarrow \text{correct}$$

$$\text{Correct std. dev.} = \sqrt{\frac{\sum x^2 - (\bar{x})^2}{100}}$$

$$= \sqrt{\frac{161701 - (39.90)^2}{100}}$$

$$= \sqrt{\frac{161701 - 1592.01}{100}}$$

$$\Rightarrow \sqrt{1617.01 - 1592.01}$$

$$\Rightarrow \sqrt{25}$$

$$\Rightarrow r \rightarrow 5 // \rightarrow \text{correct}$$

Hypothesis Testing

→ state H_0 as well as H_a

→ specify the value of significant (α or the χ value)

→ Decide the correct Sampling Distribution

→ Sample a ~~regular~~ random sample & work out an appropriate value for sample data

→ Calculate the probability if H_0 is true

→ Is this probability equal to or similar

	↓ Yes	↓ No
Reject		Accept
H_0		H_0

run this risk
of committing
Type I error run this risk
of committing
Type II error

Flow diagram of Hypothesis testing

To test a hypothesis testing to tell on the basis of the data the researchers are collected whether or not the hypothesis seems to be valid.

In hypothesis testing the main question is whether to accept the null hypothesis or not to accept the null hypothesis. Hypothesis testing can also be defined in the following flow diagram for better understanding.

where H_0 is a null hypothesis and H_a denoted as alternative hypothesis

→ A tentative assumption is made

about the parameter or distribution

This assumption is called Null hypothesis and is denoted by (H_0)

→ An alternative hypothesis which the opposite of null hypothesis. In alternative hypothesis maintain the relation b/w two measured variables.

The hypothesis of testing procedure

involves using sampling data to determine whether or not H_0 can

be rejected. The ideal procedure is in hypothesis testing leads to acceptance of

H_0 when H_0 is true, and the rejection of H_0 when H_0 is false. The hypothesis testing is based on the sampling information and possibilities of error must be considered.

- A Type I error corresponds to rejecting H_0 , where H_0 is actually true.
- And a Type II error corresponds to accepting H_0 , where H_0 is false.

The probability of making a Type I error is denoted by α , and a probability of making a Type II error is denoted by β .

★ Z test :-

$$Z = \frac{\bar{X} - \mu_{H_0}}{\sigma_p / \sqrt{n}}$$

→ Population normal infinite

• Sample size may be large or small but variance of the population is known.

• H_a may be one sided or two sided

in such cases Z test is used

→ Population normal finite

- sample size may be large or small but variance of the population is known
- H_0 may be one sided or two sided
in such case the z test is called finite population multiplier

$$Z = \frac{\bar{x} - \mu_{H_0}}{\left(\sigma_p / \sqrt{n}\right) - (\sqrt{(N-n)/(N-1)})}$$

→ Population normal infinit

- sample size small, variance of the population unknown
- H_0 maybe one sided or two sided.

in such cases T test is used

$$t = \frac{\bar{x} - \mu_{H_0}}{\sigma_s / \sqrt{n}}$$

→ Population normal finite

- sample size small, variance of the population unknown
- H_0 may be one sided or two sided
in such cases t test is used

$$t = \frac{\bar{x} - \mu_{H_0}}{\left(\sigma_s / \sqrt{n}\right) / \sqrt{(N-n)/(N-1)}}$$

$$\left(\sigma_s / \sqrt{n}\right) / \sqrt{(N-n)/(N-1)}$$

→ Population may not be normal but

- same size, large variance of the population
- population may be unknown ~~or~~ known and H_0 maybe one sided or two side

in such situation, z test is used.

(we can use either case 1 or case 2 formula)

$$\text{for variance: } \sigma_s^2 = \frac{\sum (x_i - \bar{x})^2}{(n-1)}$$

Ques) A sample of 400 male students is found to have a mean height is 67.47 inches can it be reason regarded as a sample from a large population with mean height 67.39 inches and standard deviation is 1.30 inches test at 5% level of significance

Soln $H_0 = \mu_{H_0} = 67.39''$

$H_a = \mu_{H_0} \neq 67.39''$

$\bar{x} = 67.47'', \sigma_p = 1.30, n = 400$

$$Z = \frac{67.47 - 67.39}{1.31 / \sqrt{400}} = \frac{0.08}{0.065}$$

$$Z = 1.23$$

Considering H_0 is two sided for given question

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554 test using student whether the breaking strength of any lot may be taken to be 578 kg. With 5% level of significance. Verify degree of freedom, arithmetic mean, standard deviation and t test result.

Ques

Ques) The specimen of a copper wire drawn from a large set and have the following breaking strength in (weight in kg) 570, 572, 578, 568, 572, 578, 570, 572, 596,

Data warehousing :- Data warehousing governing all the data, and control multidimensional space data. The construction of data warehouse involves

- Data cleaning
- Data integration
- Data transformation

Data warehouse provides online analytical processing tool (OLAP) for interactive analysis of multidimensional data which facilitate effective data generalisation and data mining.

Many other data mining functions such as association, classification, prediction and clustering can be integrated with OLAP operation to enhance interactive mining of knowledge in multiple level of abstraction.

Data warehousing providing architecture and tool for business execution to systematically organising understand and use their data to make strategic decision. It is a subject oriented, integrated, and time variant and non volatile collection of data in support and management decision marketing process.

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Compare OLAP & OLTP processing
The major distinguish feature of OLAP and OLTP are summarised as follows

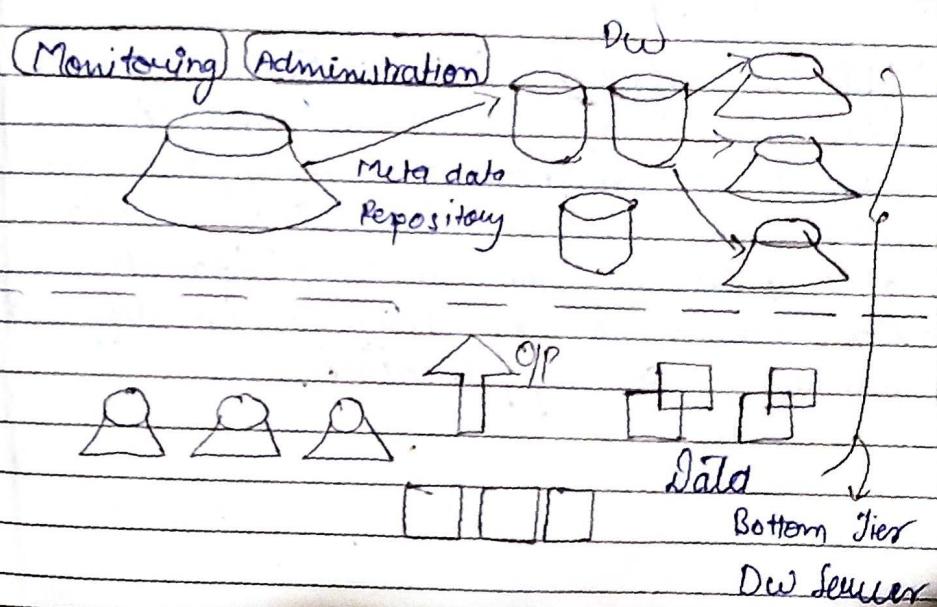
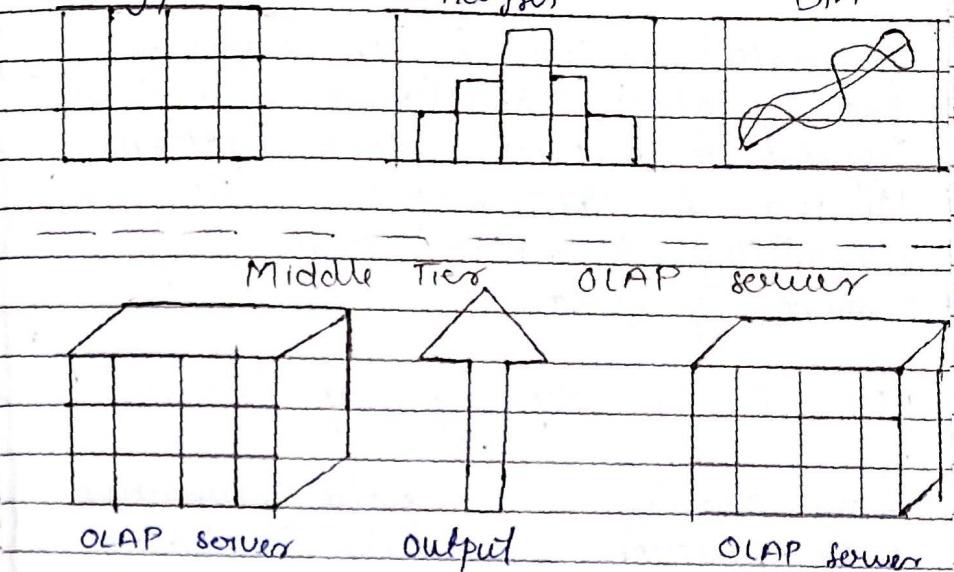
features	OLTP	OLAP
user and system oriented	customer oriented and used for transaction & query processing	market oriented and used for data analysis
Data contained	manages current data and easily used for decision making	large amount of data management, historical data summarisation, aggregation facility
Database design	E-R diagram, data model, application oriented and DP design	star & snow fall model and subject oriented database design
Access pattern	Atomic transaction, concurrency control	read only operations and complex queries
Users	Customer Oriented	Analyst, manager, it is market oriented

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Multitier Architecture

TOP tier fronted tool

Analytical / Analysis DM

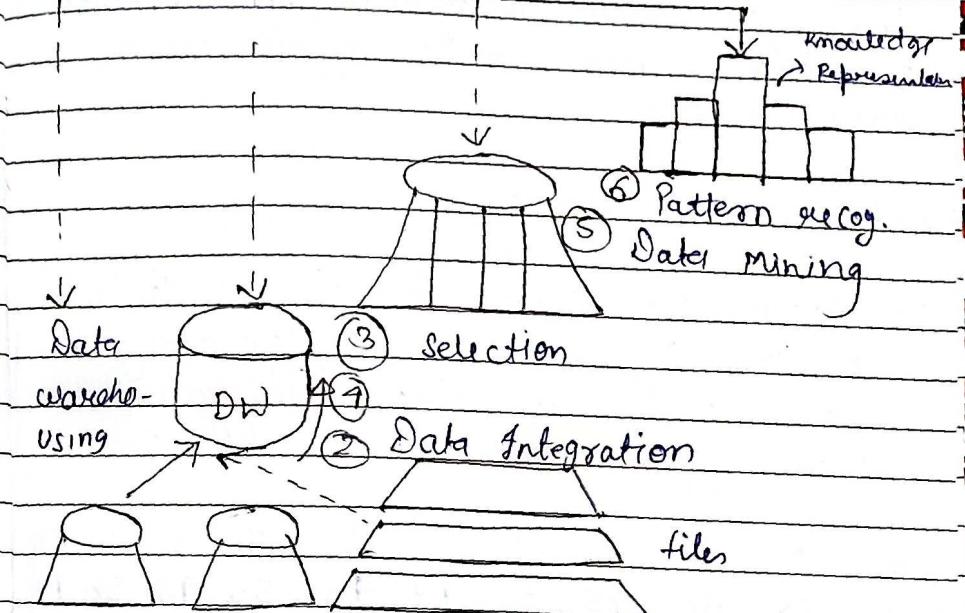


KDD Process (Knowledge Discovery from Data)

A data mining is an essential process where intelligence method are applied to extract data patterns. Mining is the process of discovering interesting knowledge from large amount of data.

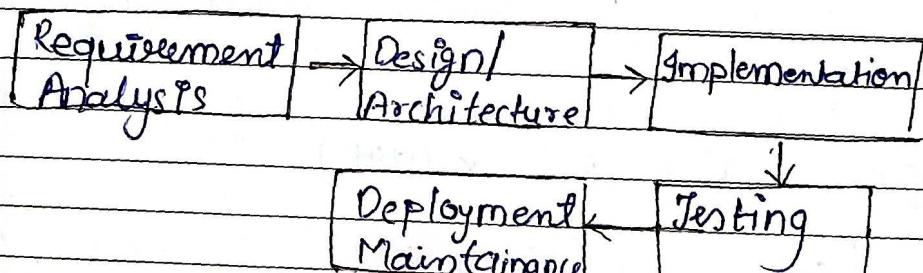
KDD is a step by step processing

1. Data cleaning
2. Data Integration
3. Data selection
4. Data Transformation
5. Data mining
6. Pattern evaluation
7. Knowledge Representation



05/09/2023

\Rightarrow 5 phases of Software development



SDLC

* Internal 1st topic :- KDD process, Numerical on time series, Numerical on least square method, Theory on

box plot with Numerical, Introduction of data science with application of data science

7	55	8
8	48	1
9	52	5
10	49	2

Chi-square Test:-

(Ques) Apply chi-square test in the context of sampling analysis for comparing a variance to a theoretical variance weight of 10 students as follows:-

s.no	1	2	3	4	5	6	7	8	9	10
weight	38	40	45	53	47	43	55	48	52	49

Can we say that the variance of the distribution of weight for all students from which above sample of 10 students was = 20 kgs. Test this at 5% level of significance.

$$\text{SOLN} \quad \chi^2 = \frac{\sigma_s^2}{\sigma_p^2} \times (\text{dof})$$

S.No.	Weight(x_i) in Kg	$(x_i - \bar{x})$
1	38	-9
2	40	-7
3	45	-2
4	53	6
5	47	0
6	43	-4

$$\sum x_i = 470$$

$$\bar{x} = \frac{\sum x_i}{n} = \frac{470}{10} = 47$$

$$\Rightarrow \sigma_s = \sqrt{\frac{(x_i - \bar{x})^2}{n-1}}$$

$$\Rightarrow \sigma_s = \sqrt{\frac{(47)^2 + (-7)^2 + (-2)^2 + (6)^2 + (0)^2 + (-4)^2 + (8)^2 + (1)^2}{9}} = \sqrt{\frac{280}{9}} = 16.67$$

$$\Rightarrow \sigma_s = \sqrt{\frac{280}{9}} \Rightarrow \sigma_s = \sqrt{31.11}$$

Now,

$$\sigma_s^2 = \text{variance} = 31.11$$

Now,

$$\chi^2 = \frac{31.11 \times 9}{20} = 13.99$$

$$\text{dof} = 9$$

$$\text{at } 5\% \quad \chi^2 = 16.928$$

Null hypothesis accepted