



PARALLEL COMPUTING (CPA)

Lab 1: Parallelization with OpenMP

Curso 2018/19

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Introduction

This laboratory exercise comprises 3 sessions, corresponding to each of the 3 sections of this document. Next table shows the files needed to develop each one of the exercises.

Session 1	Numerical Integration	integral.c
Session 2	Image Processing	imagenes.c, Lenna.ppm
Session 3	Prime numbers	primo_grande.c, primo_numeros.c

The exercises of this subject are intended to be done on the computers of the laboratory, using Linux and using the kahan computing cluster when necessary.

You should use the remote folder <code>DiscoW</code> to store the files of the laboratory exercises (you should also create the necessary folders inside <code>DiscoW</code> to organise the content). In this way, the files will also be accessible from the <code>kahan</code> cluster.

Please avoid using blank spaces in file or folder names, since they may cause troubles when using the cluster.

You can use any conventional Linux computer for most of the laboratory exercises. However, you will need to run jobs on the kahan computing cluster. If you are outside of the laboratory, you can access kahan in either of these two ways:

Accessing the laboratory environment through the virtual desktop system, following the instructions in https://www.upv.es/entidades/DSIC/infoweb/dsic/info/1043006normali.html ("Acceso escritorios Linux"). Once in the virtual desktop, you can access kahan by means of ssh, as described in section 1.3.

The advantage of accessing through the virtual desktop is that you can edit your files in DiscoW and use them directly in kahan.

• Directly accessing the kahan computing cluster through ssh, like in:

```
$ ssh your_username@kahan.dsic.upv.es
```

There are also ssh clients for Windows, such as Putty. If you want to copy the files from your computer to kahan or viceversa, you can use the scp command. For example, if you want to copy a file named fich.c from your computer to the folder prac1/ in kahan (assuming that this folder already exists in kahan), you can use the command:

\$ scp fich.c your_username@kahan.dsic.upv.es:prac1/fich.c

1. Numerical Integration

In this first exercise, we will learn how to compile OpenMP parallel programs and how to parallelise simple loops. You will also learn how to run executable programs, both in your local machine and in the kahan computing cluster.

We consider here the integral of a given function f(x) in the interval [a, b]:

$$\int_{a}^{b} f(x)dx.$$

In this exercise we will compute an approximation of the integral by summing the area of a set of rectangles that occupy an area similar to the one of the integral. Figure 1 shows an example of the approximation. This approximation can be computed using the following expression:

$$\int_{a}^{b} f(x)dx \approx \sum_{i=0}^{n-1} f(x_i) \cdot h = h \cdot \sum_{i=0}^{n-1} f(x_i),$$
 (1)

where n is the number of rectangles used, h = (b-a)/n is the width of the rectangles and, $x_i = a+h\cdot(i+0.5)$ is the midpoint of each rectangle's base. The accuracy of the approximation depends on the number of rectangles used.

The sequential code of the program is available in the file integral.c. Figure 2 shows an extract of such code. In particular, we can see that there are two different functions for computing the integral. Both approximations are quite similar, and both include a loop that implements the summation of the equation (1).

The objective of this laboratory exercise is to parallelize using OpenMP the two variants for the computation of the integral.

First, you have to compile the source code. For this purpose, open a terminal on the folder where file integral.c is stored and run the command:

\$ gcc -Wall -o integral integral.c -lm

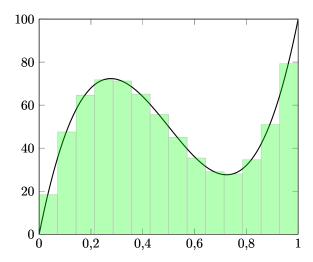


Figura 1: Geometric interpretation of the integral.

If successful, the compiler will have created an executable in the same folder with the name integral. The meaning of the compiler arguments are:

- -o executable_file: the name of the executable file (output).
- -lm: link the executable with the mathematical library of functions. This option is needed when using mathematical functions such as sin, cos, pow, exp...
- -Wall (optional): show all the compile warnings.

Then, run the program. At runtime, an argument can be used to select the variant to be used (1 or 2). For example, to use the first variant you can use:

```
$ ./integral 1
```

The result of the integral will be shown on the screen. The result should be the same regardless of the variant chosen. Optionally, the program accepts the value n (number of rectangles) as a second argument (by default it uses 1000 rectangles). For example:

```
$ ./integral 1 100000
```

1.1. Parallelization of the first variant

The first step will be to modify the code in the file integral.c to perform the computation of the integral in parallel using OpenMP. Instead of editing the original file, you should create a copy with a different name (e.g., pintegral.c).

You can start by making the program show the number of threads used for its execution. To do so, edit the program as figure 3 describes. That is, add a printf sentence in the main function to show the number of threads by calling the proper OpenMP function. Take into account that you must include the omp.h header file.

To compile an OpenMP program, you must add the option -fopenmp, such as:

```
$ gcc -fopenmp -Wall -o pintegral pintegral.c -lm
```

```
/* Computation of the integral for a function f. Variant 1 */
double calcula_integral1(double a, double b, int n)
   double h, s=0, result;
   int i;
  h=(b-a)/n;
  for (i=0; i<n; i++) {
      s+=f(a+h*(i+0.5));
   result = h*s;
   return result;
/* Computation of the integral for a function f. Variant 2 */
double calcula_integral2(double a, double b, int n)
   double x, h, s=0, result;
   int i;
  h=(b-a)/n;
   for (i=0; i<n; i++) {
      x=a:
      x+=h*(i+0.5);
      s+=f(x);
  }
   result = h*s;
   return result;
}
```

Figura 2: Sequential code for the computation of the integral.

To run the program using several threads (e.g. 4), you can use the OMP_NUM_THREADS environment variable, such as:

```
$ OMP_NUM_THREADS=4 ./pintegral 1
```

Bear in mind that there must be no blank space in "OMP_NUM_THREADS=4".

The program will show the number of threads on the screen. Does it display 1 thread instead of 4? If it does, take into account that the OpenMP function returns the number of **active** threads, and if it is called outside of a parallel region, the number of active threads is just 1. You have to solve this issue so that the program works as expected. Additionally, take into account that the number of threads should only appear on the screen once.

The next step will be to modify the code in the file integral.c to actually perform the computation of the integral in parallel using OpenMP. We will start with the first variant (calcula_integral1). A first approach could be to use the directive parallel for without considering if variables should be private, shared or some other type. After this change, you can compile and execute the program.

We can check that the result obtained is incorrect. The problem is that the scope of the variables may be incorrect, resulting in race conditions. To solve this, we should correctly indicate the scope of the variables within the loop, by using clauses such as private or reduction, if necessary.

Once the code has been corrected, it can be compiled and executed again. We should check that the result is the same as that of the original sequential code, and that it does not vary when using different numbers of threads. Execution should be repeated several times.

```
#include <omp.h>
...
int main(int argc, char *argv[]) {
    ...
    printf("Number of threads: %d\n", proper_openmp_function());
    ...
}
```

Figura 3: (Incomplete) update to show the number of threads.

1.2. Parallelisation of the second variant

We will proceed next with the parallelisation of the second variant (calcula_integral2). As we can see in Figure 2, the code is practically identical to the first version, except for the use of an auxiliary variable x. Of course, that change should not affect the result of the computation.

You should parallelise this second version. Check again that the result is the same as that of the original sequential code, and that it does not vary when changing the number of threads.

1.3. Execution in the cluster

In this section we will use the kahan computing cluster to run the program, which will enable us to use a larger number of *cores*.

kahan is a cluster comprising 6 compute nodes, each one provided of 32 cores, and a *front-end* node where the users will log to compile and submit the runs. All the *cores* within a node share the memory of that node, but cannot access the memory of any other node. There is more information about kahan in the resources area at *Poliformat*.

To work with kahan, you should log into the front-end node by means of ssh:

```
$ ssh your_user@kahan.dsic.upv.es
```

The home directory in kahan is the DiscoW folder in the local machine. You can easily check this by using the ls command.

Change to the folder that holds the files of the laboratory exercise (e.g. cpa/prac1) using the cd command, such as:

```
$ cd cpa/prac1
```

and compile the program in kahan as you did it previously in your local machine. You must recompile the program in kahan to link the executable to the specific libraries and environment of kahan, instead of those from our local machine.

Then check that you can run the program on the *front-end*, executing it just like you did previously on the local machine.

Although you can run the programs on the *front-end*, you should do it for very short runs only. The *front-end* node is not a compute node and can run out of resources, affecting other users who are editing and compiling the programs.

Jobs must be run on kahan using the **queue system** only. In order to do that, we have to create a **job file**, which is basically a script with the options of the queue system followed by the commands that we want to execute. Figure 4 shows an example in which an OpenMP program is launched with 3 execution threads (see the last line in the script file). Lines starting by **#PBS** define different options of the queue system, namely:

■ -1: resources needed for the job to run. This case, the job will use one full node of the cluster (the 32 cores) and will run for a maximum of 5 minutes (walltime). Do not include blank spaces in the list of resources.

```
#!/bin/sh
#PBS -l nodes=1,walltime=00:05:00
#PBS -q cpa
#PBS -d .

OMP_NUM_THREADS=3 ./pintegral 1
```

Figura 4: Script file for submitting the job in the queue system.

- -q: queue to which the job will be submitted. A queue system can manage different queues for different
 job types or user privileges. In the laboratory exercises of this subject, we will always use the queue
 cpa.
- -d: execution directory for the job. By default, the execution directory is home. In this example, we set the execution directory to the current directory (.).

Write the text of figure 4 in a file (e.g. jobopenmp.sh) and change the number of threads. Would it make sense to change the number of nodes to a value greater than one?

Then, you can launch the job to the queue system by using the command qsub. Assuming that the job file is named jobopenmp.sh, the job can be submitted by executing the following command on the *front-end*:

```
$ qsub jobopenmp.sh
```

The job identifier will be displayed on the terminal.

Once submitted, the queue system will assign the necessary resources (one full node in our case) to the job, when those resources become available, keeping the job in a waiting status until then. In this way, the system ensures that the nodes allocated to a job will not be used by any other job.

What happens with the messages that the program should display? Those messages are not shown on the terminal, but they are stored in a file instead. For example, if the script file is jobopenmp.sh and the job id is 1485, two files will appear after its execution: jobopenmp.sh.o1485 (standard output) and jobopenmp.sh.e1485 (standard error output). We can see their contents using the cat command, like:

```
$ cat jobopenmp.sh.o1485
Valor de la integral = 1.000000411234
```

You can check the status of the queues using the command qstat, such as:

For each job, the status (S) of the job is displayed, which could be: queued (Q), running (R) or Ended (E). A job can be cancelled using the qdel command and the job identifier:

```
$ qdel 1485
```

1.4. Execution time measuring

When developing parallel algorithms, it is important to measure the execution time of the program, or a part of it, to compare it to the sequential time and evaluate the speed-up obtained.

To measure the execution time of a program fragment we will use the <code>omp_get_wtime()</code> function from OpenMP, which returns the time spent (in seconds) since a fixed point in time. Figure 5 shows how to use this function.

```
#include <omp.h>
...

int main(int argc, char *argv[]) {
   double t1, t2;
   ...
   t1 = omp_get_wtime();
   ... /* Fragment of code to measure */
   t2 = omp_get_wtime();
   printf("Tiempo: %f:\n", t2-t1);
}
```

Figura 5: Measuring the execution time of a code fragment.

Compute the execution time of the parallel program running in the cluster for 1,000,000 rectangles, using first 1 thread and then 16 threads. Obtain the speed-up achieved.

Can we increase the number of threads indefinitely, reducing the execution time forever? If not, which could be the maximum number of threads that could improve the performance?.

2. Image processing

This practice exercise focuses on the implementation in parallel of an image filtering process using OpenMP. The objective of this practice exercise is to deepen your knowledge of OpenMP and the solution of dependencies among threads. The exercises should be implemented on the computers of the lab. The exercise will be based on the sequential version of a program that reads an image in PPM format (a portable text-based format), applies several filtering steps based on a weighted average with variable radius and writes the resulting image in a file using the same format. The result of the exercise will be a parallel code using OpenMP that exploits the parallelism of the different loops into which the method is structured.

2.1. Problem description

Image filtering consists on substituting the values of the pixels in an image by values depending on the values of the neighbours. Image filtering can be used to reduce noise, focusing or blurring an image, etc. The neighbours of a pixel are the pixels located, in both directions, not further than a maximum distance called radius. Average filtering reduces notably white noise, but introduces a blurring effect. In a weighted average filter, a mask is used to weight the different values of the pixel neighbours, following a parabolic or linear adjustment. This filtering provides better results than a simple average, but it has a higher computational cost. Finally, the filtering is an iterative process that may involve several sequential steps.

2.2. Sequential version

The material for the student includes the file imagenes.c with the sequential implementation of the filtering. The filtering used gives a weight of one to the pixels further from the centre and increases the values as they get closer to the centre. Figure 6 shows a schema of the filter.

This figure shows an original image (left) where filtering is applied to the central pixel (with a colour value of 138). The filtering is based on the quadratic mask shown on the right side of the figure. Applying the filter implies performing the computations shown in the figure, obtaining the resulting image shown on the right side. This filtering is performed at every pixel of the image.

The algorithm follows the two dimensions of the image, and for each pixel, two inner loops are applied that go through the pixels that are located not further than the radius for both dimensions. The limits of the image are checked to avoid surpassing the lower and upper limits of the image. The image filtering is repeated

125	123	124		1	2	1	(125+2*123+124+	125	123	124
110	138	130	*	2	4	2	$ \begin{array}{ccc} 2*110+4*138+2*130+\\ \rightarrow & 108+2*124+132) & \rightarrow\\ & / (1+2+1+2+4+) \end{array} $	110	126	130
108	124	132		1	2	1	2+1+2+1)	108	124	132

Figura 6: Model for the application of the weighted average in the image filtering. From left to right, original values, filtering mask, weighting operation and in bold face final value.

several times over the whole image, therefore requiring five nested loops: steps, rows, columns, radius per rows, radius per columns, as depicted in figure 7.

For reading and writing the image, the PPM format is used. This format is simple and images can be displayed using different programs, such as <code>irfanview1</code> or <code>display</code> (available in Linux). The image format is shown in figure 8 and can be displayed using the commands <code>head</code>, <code>more</code> or <code>less</code>.

Therefore, the program reads the contents of a file whose name is indicated by the constant IMAGEN_ENTRADA, and it will apply the filtering as many times as the constant NUM_PASOS specifies, using the value of VAL_RADIO for the radius. Finally, it will write the filtered image in the file indicated in IMAGEN_SALIDA. Memory allocation is performed by the reading function, ensuring that all the pixels of the image are consecutively stored in memory.

You are asked to verify the correct performance of the program. Compile and run the program on the local machine. You will see the program creates the output file lenna-fil.ppm (the name specified in IMAGEN_SALIDA), which is the result of applying the filter to the file Lenna.ppm, a well-known test image from a popular benchmark² (see Figure 9).

Copy the file lenna-fil.ppm to a file named ref.ppm. This file is the output of the original program, which will be used as the reference to be compared to the output of the modified programs that will be requested later on, in order to check their correct behaviour.

Finally, modify the program to show the number of threads, as you did in the previous session, and also the execution time of the function that performs the filtering. Compile and execute the program on the cluster (using the queue system as explained in section 1.3) and check that the modification works as expected.

2.3. Parallel implementation

There are different approximations for the parallel implementation using OpenMP, depending on which loop is chosen for its parallelization. The work in this laboratory exercise will focus on analysing the five loops and deciding (and testing) which loops can be parallelized. Each parallelization will require identifying the variables that must be shared or private. To do so, the student must do the following steps for each loop:

- 1. Analyse if the different iterations of a loop have any inter-dependency (e.g. if the second iteration uses as input results produced in the first iteration), and in that case, if those dependencies can be overcome or solved using an OpenMP clause (e.g. in the case of summations). If the loop cannot be parallelised, skip the next steps.
- 2. Write the directives required to parallelise the loop, paying attention to the scope of the variables (which variables should be private to each thread and which ones should be shared among the threads).
- 3. Run the modified program (preferably on the cluster).
- 4. Check that the file generated by the modified program(lenna-fil.ppm) is exactly the same as the one produced by the original program (ref.ppm). To do so, run the command:

¹http://www.irfanview.com

²http://en.wikipedia.org/wiki/Standard_test_image

```
for (p=0;p<pasos;p++) {
 for (i=0;i<n;i++) {
   for (j=0; j \le m; j++) {
     resultado.r = 0;
      resultado.g = 0;
      resultado.b = 0;
      tot=0;
      for (k=max(0,i-radio);k\leq min(n-1,i+radio);k++) {
         for (l=max(0,j-radio);l<=min(m-1,j+radio);l++) {</pre>
           v = ppdBloque[k-i+radio][l-j+radio];
           resultado.r += ppsImagenOrg[k][1].r*v;
           resultado.g += ppsImagenOrg[k][1].g*v;
           resultado.b += ppsImagenOrg[k][1].b*v;
           tot+=v;
         }
      }
      resultado.r /= tot;
      resultado.g /= tot;
      resultado.b /= tot;
      ppsImagenDst[i][j].r = resultado.r;
      ppsImagenDst[i][j].g = resultado.g;
     ppsImagenDst[i][j].b = resultado.b;
 }
 memcpy(ppsImagenOrg[0],ppsImagenDst[0],n*m*sizeof(struct pixel));
```

Figura 7: Main loops in the image processing.

```
P3 <- Identifier for the format (ppm, colour RGB)
512 512 <- Image size (number of columns and number of rows)
255 <- Intensity depth
224 137 125 225 135 ... <- 512x512x3 values. Each pixel is coded with three consecutive values (R,G,B)
```

Figura 8: PPM image file format.





Figura 9: Reference image (Lenna.ppm) before (left) and after (right) de applying a one-step filtering with a radius of 0.5.

\$ cmp lenna-fil.ppm ref.ppm

If both files are the same, the previous command will not show any message.

Take these pieces of advice into account:

- Start from the innermost loop. As there are fewer variables involved, it may be simpler to start from this loop, and progressively consider the outer loops successively until you reach the outermost loop.
- The reduction clause cannot be applied to a variable of type struct. In case that you need so, substitute the struct by one variable per each one of the members.
- A parallel version may produce correct results but be inefficient and slow, even taking longer when the number of threads is increased. Therefore, we suggest using only 2 threads when running the parallel versions for now.
- Take into account that the cluster is shared among all the students, so you should not fill up the queue with your jobs. You may run several commands in the same script file.

Would parallelising two loops at the same time make sense?

Obtain a set of results similar to the ones shown in Figure 10, in which we obtain the execution time of the sequential time and the execution time of each parallel version for different numbers of threads. Take into account that if a parallel version takes longer with 2 threads than the sequential version, it will get even worse with more threads, so you should not execute it with more than 2 threads.

It can be seen that there are parallel versions that are more efficient than others. Which are the most efficient ones? Why?

Figura 10: Time measuring

```
Function prime (n)
  If n is even and it is not number 2 then
   p <- false
  else
   p <- true
 End
  If p then
   s <- square root of n
    i <- 3
   While p and i <= s
      If remainder of n divided by i is 0 then
        p <- false
      End
      i <- i + 2
   End
 End
 return p
End
```

Figura 11: Sequential algorithm to determine if n is prime.

3. Prime numbers

The objective of this lab exercise is to solve in parallel the well-known problem of checking whether a number is prime or not. Although other more efficient versions do exist, we will use in this case the typical sequential approach.

In this case, the parallelisation will not be "trivial". Sometimes, using OpenMP is not as straightforward as including a pair of directives. When possible, this is desirable since it brings clarity, simplicity and platform independence. However, sometimes we must carefully think about the problem and explicitly indicate the distribution of the work (loop iterations) among the threads. This is what we should do in this exercise.

3.1. Sequential Algorithm

The classic sequential algorithm to find out if a number is prime is shown in figure 11. It involves checking if the number can be exactly divided by any number below it (different from 1). In this case, the number is not prime.

Checking whether a number is prime or not using this algorithm has a low computing cost for small numbers. Note that the loop ends as soon as an exact divisor is found. Therefore, the larger computational cost will be when the number to be checked is large and either prime or not prime but composed of large factors.

With the objective of working with code with a higher computational cost, we will extend the problem to find the largest prime number that can be stored in an integer variable of 8 bytes. Parallelising problems with low computational cost is not useful except for basic learning and typically leads to low performance and efficiency.

```
Function largest_prime
  n <- largest integer
While n is not a prime
  n <- n - 2
End
  return n
End</pre>
```

Figura 12: Algorithm to be parallelised: It searches the largest prime that can be stored in an unsigned integer of 8 bytes.

```
#pragma omp parallel ...
{
   for (i = ...; p && i <= ...; i += ...)
      if (n % i == 0) p = 0;
}</pre>
```

Figura 13: Parallelisation schema for function prime.

The process will start with the largest number that can be stored in an unsigned integer of 8 bytes and will decrease it until a prime number is found, using the previous algorithm to check if each number is prime. The largest prime will be odd, so we can decrease it by two in each iteration in order to skip even numbers, which are obviously not prime. The algorithm is shown in figure 12.

The student should read and analyse the program provided in the file primo_grande.c. This program uses the previous algorithms to search and show on the screen the largest prime number that can be stored in an unsigned integer variable (8 bytes).

3.2. Parallel Algorithm

The student should implement a parallel version of the function that checks whether a number is prime or not, using OpenMP. Since part of the function is a for loop, it seems straightforward to use a parallel for directive. Let's try. What happens?

Actually, OpenMP does not allow the use of the parallel for directive in this case. Bear in mind that the parallel for directive stands for a parallel directive followed by a for directive. This second directive automatically splits the loop iterations among the threads, but it needs that the start, end and increment of the loop are perfectly defined. In the prime function, the start value and the increment of the loop variable (i) are well defined, but the final value is not known a priori. It may reach value s or it can end before if p is set to false. Therefore, we can use neither the for nor the parallel for directives.

Actually, the impossibility to use the for directive is because the loop termination condition contains an element that checks if the number is prime. What would happen if we remove this verification? The function will still be correct, but which problem will arise? (N.B. If you cannot realise where the problem is, you may remove this condition and run the program in parallel, but it is advisable to start on a smaller factor, as the execution time will very much increase).

Once the need of keeping such condition in the termination loop is understood, we must find an alternative way to implement the parallelism.

Our approach will be to implement an explicit splitting of the iterations of the loop among the threads. That is, we will perform explicitly what the for directive does automatically.

The parallelisation of the loop with look like in figure 13, where each loop in the parallel region must do a subset of the iterations of the original loop. The iterations assigned to each thread are defined by the initial value of i, the increment and the final value. Therefore, you need to modify some of these elements to ensure that each thread processes a different subset of iterations.

For example, assuming s=19, the values that the variable i will take along the loop are: 3, 5, 7, 9, 11, 13,

Figura 14: Algorithm that counts the number of prime numbers between 1 and a given value.

15, 17, 19. A way to split the iterations could be to assign a consecutive block of iterations to each thread. Given 3 threads, the distribution will be:

Thread 0	3	5	7
Thread 1	9	11	13
Thread 2	15	17	19

However, another way to split the iterations would be using a cyclic distribution:

Thread 0	3	9	15
Thread 1	5	11	17
Thread 2	7	13	19

In this case, cyclic distribution is easier to implement than block distribution, so we recommend it. Obviously, your implementation must work correctly for any value of **s** and number of threads. You will need to use OpenMP functions to get the number of threads and the thread identifier. For the sake of efficiency, do not call those functions in each loop iteration. Write the new parallel version and measure the execution time.

It is important to keep the exit condition in the loop when an exact divisor is found. In this way, if implemented correctly, when any thread discovers that a number is not prime, all other threads will eventually stop.

<u>Note</u>: It is advisable to add the volatile modifier to the variable that is used for loop control: volatile int p; The volatile modifier in the C language indicates that the compiler must not optimise the access to that variable (i.e., it must not load it in registers so that any access to it is done effectively on memory), in such a way that its modification from one thread will be visible earlier in the rest of threads³.

3.3. Counting primes

The final exercise for this problem will be to compute the total number of prime numbers between 1 and a large number, such as 100,000,000. [N.B.: If the program takes too long, a smaller limit can be chosen. In order to obtain a good performance improvement, the sequential version should take around 1 or 2 minutes at least.]

The algorithm to implementing this process is described in Figure 14. Check the sequential version of this algorithm, measuring its execution time.

Given that a parallel version of the algorithm for checking if a number is prime is already available, it is trivial to solve this problem in parallel by just using that parallel version.

However, this approach has low performance. The reason is that the initial prime numbers are very small and computing each one of them requires very little processing time, so there is no gain in splitting the workload among the threads.

³This behaviour can also be accomplished using the flush sentence in OpenMP.

A better strategy is to parallelise the loop on the main program (which is straightforward using OpenMP directives) and directly use the sequential version of the function prime. You should develop a parallel version based on that idea and measure the execution time. Finally, different scheduling strategies for the loop should be checked, using at least the following ones:

- Static without specifying the *chunk* size.
- Static with *chunk* size of 1.
- Dynamic.

Remember that the scheduling can be defined using two different ways:

- 1. Directly defining the scheduling in the OpenMP for directive using the clause schedule (such as schedule(static,6)).
- 2. Using the clause schedule(runtime) in the for directive, and giving a value to the environment variable OMP_SCHEDULE (e.g. OMP_SCHEDULE="static,6"). In this way you can change the scheduling without recompiling the program.
 - When using this option in kahan, you must indicate OMP_SCHEDULE="static,0" if you want static scheduling without specifying the *chunk* size.