

**Lecture 24:**

# **Parallel Deep Neural Networks**

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**Parallel Computer Architecture and Programming  
CMU 15-418/15-618, Spring 2020**



# Training/evaluating deep neural networks

Technique leading to many high-profile AI advances in recent years

Speech recognition/natural language processing

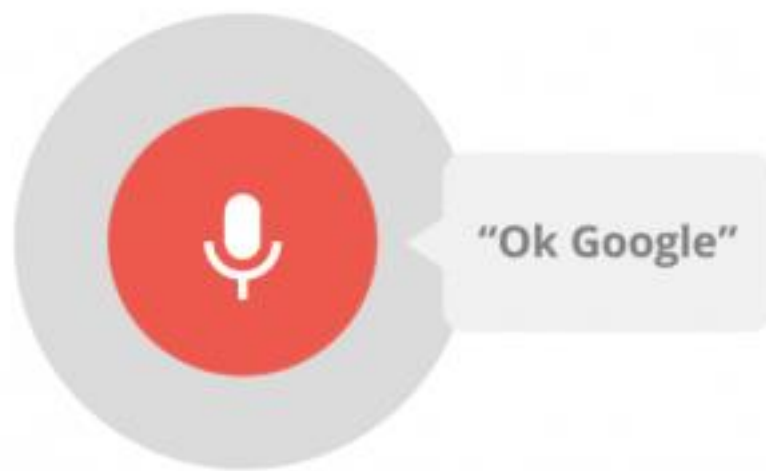
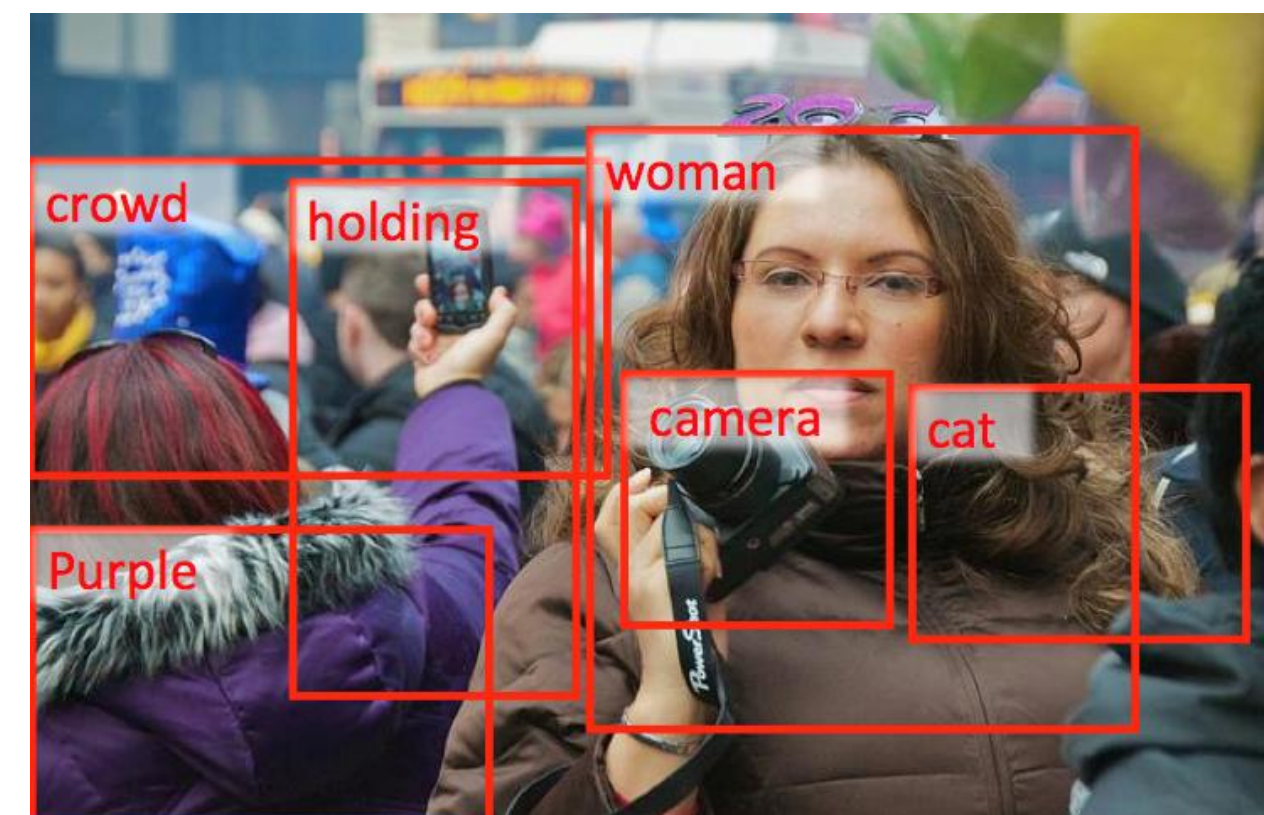
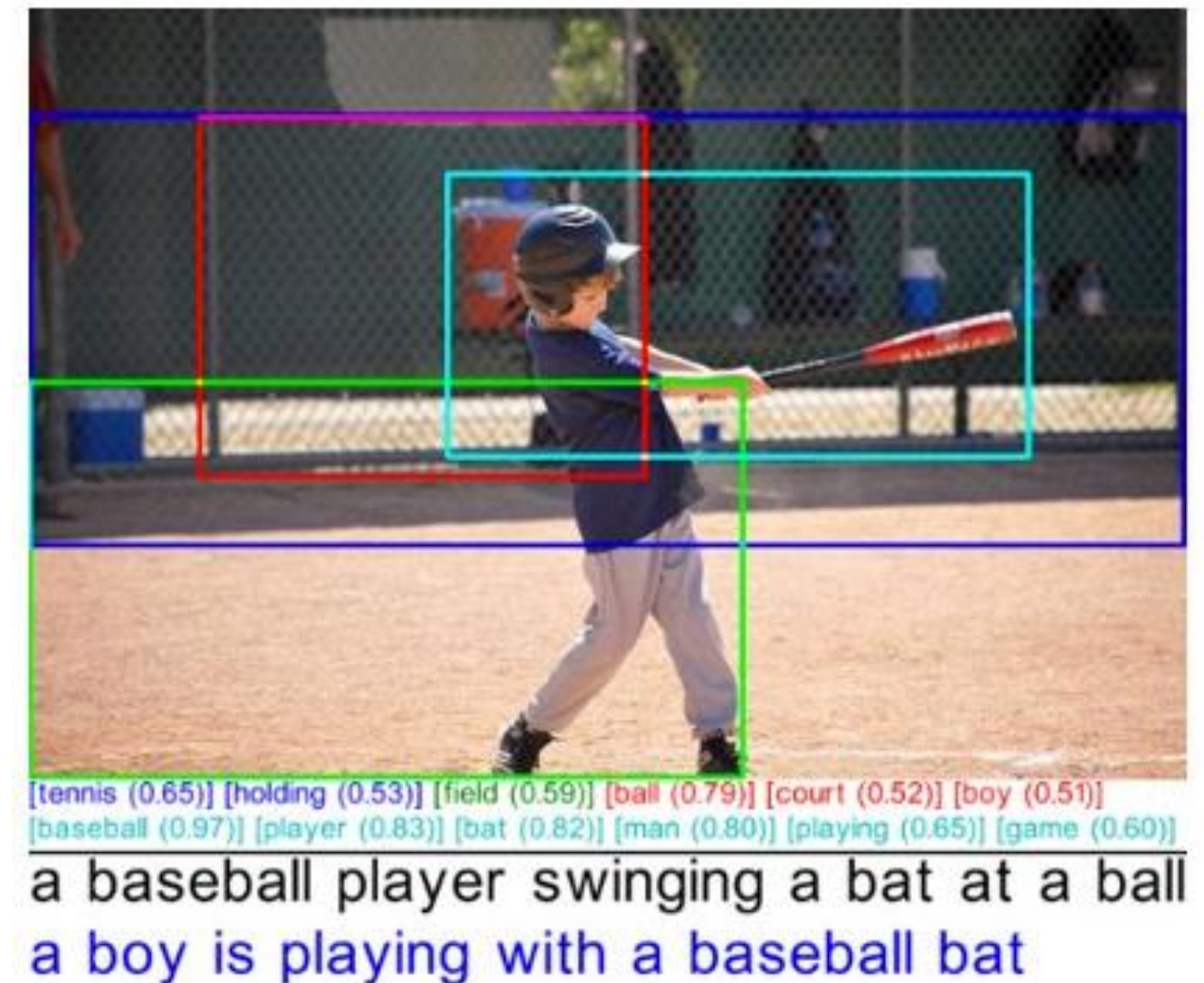


Image interpretation and understanding

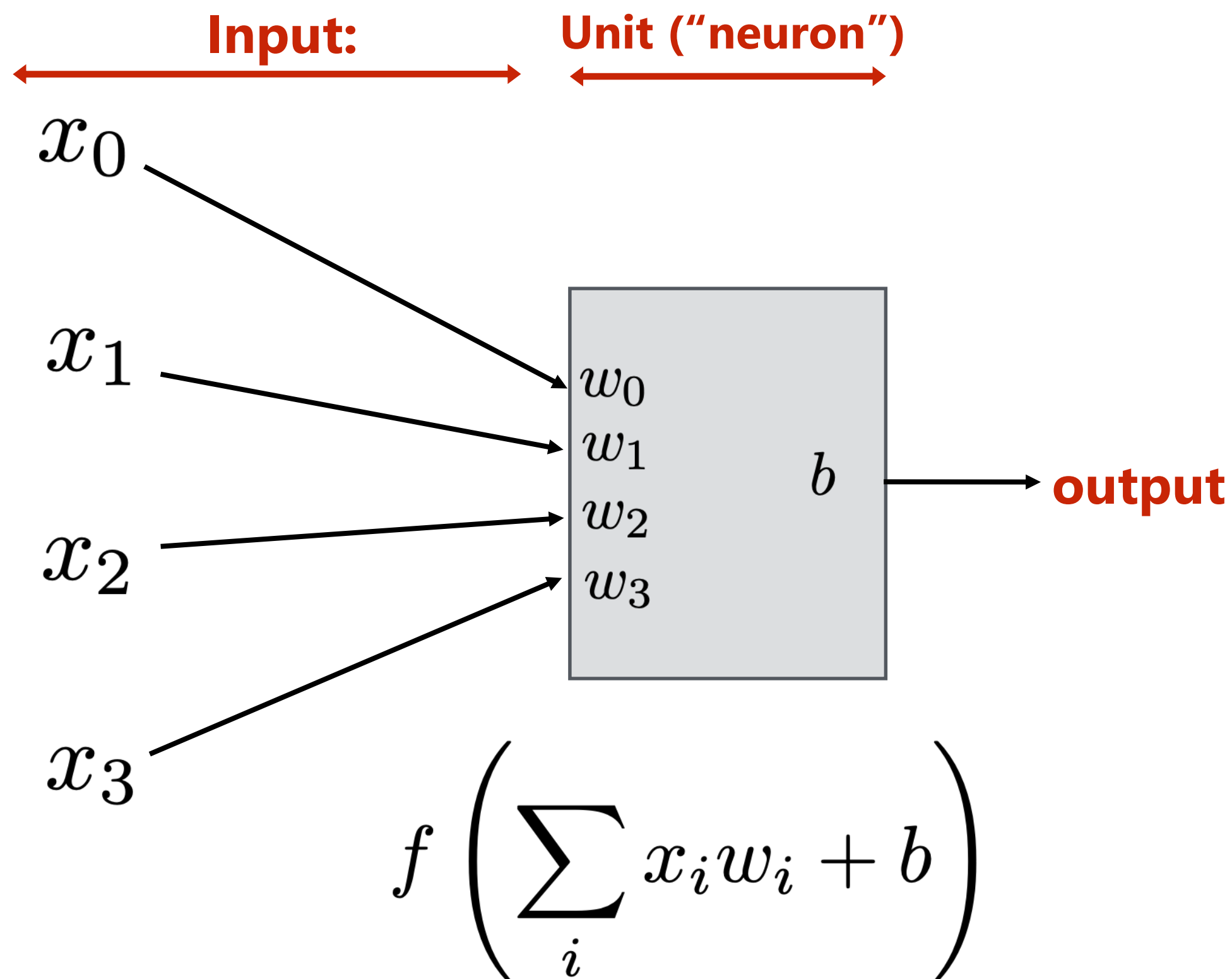




# What is a deep neural network?

## A basic unit:

Unit with  $n$  inputs described by  $n+1$  parameters (weights + bias)



**Example  $f$ : rectified linear unit (ReLU)**

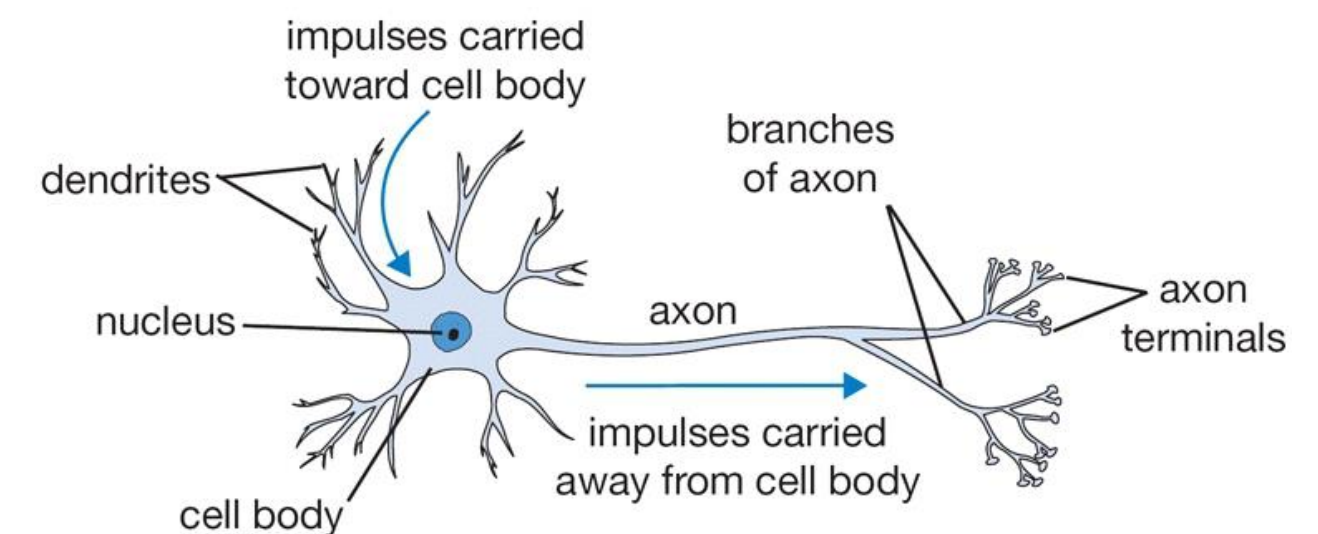
$$f(x) = \max(0, x)$$

**Basic computational interpretation:**

**It's just a circuit!**

**Biological inspiration:**

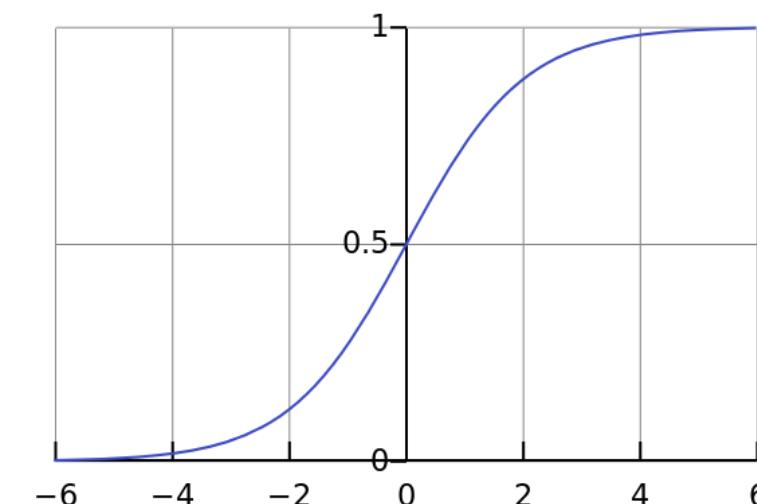
**unit output corresponds loosely to activation of neuron**



**Machine learning interpretation:**

**binary classifier:** interpret output as the probability of one class

$$f(x) = \frac{1}{1 + e^{-x}}$$



# Deep Learning Heros



Type to enter a caption.

- **2019 Turing Award Winners**
  - **Yoshua Bengio**
  - **Geoff Hinton**
  - **Yann LeCun**

# Two Distinct Issues with Deep Networks

- **Evaluation/Inference**
  - often takes milliseconds
- **Training**
  - often takes hours, days, weeks



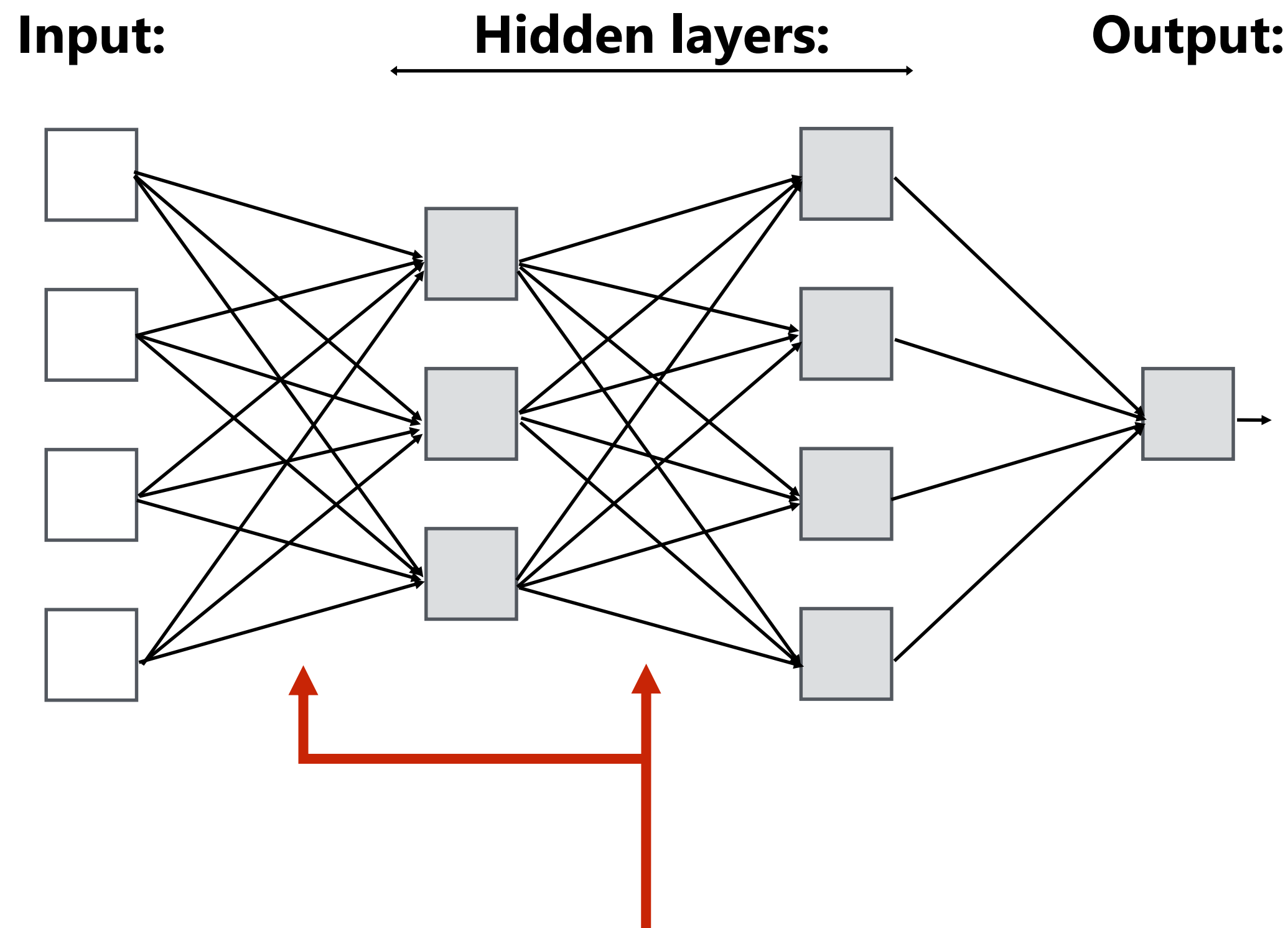
# What is a deep neural network? topology

This network has: 4 inputs, 1 output, 7 hidden units

“Deep” > one hidden layer

Hidden layer 1: 3 units x (4 weights + 1 bias) = 15 parameters

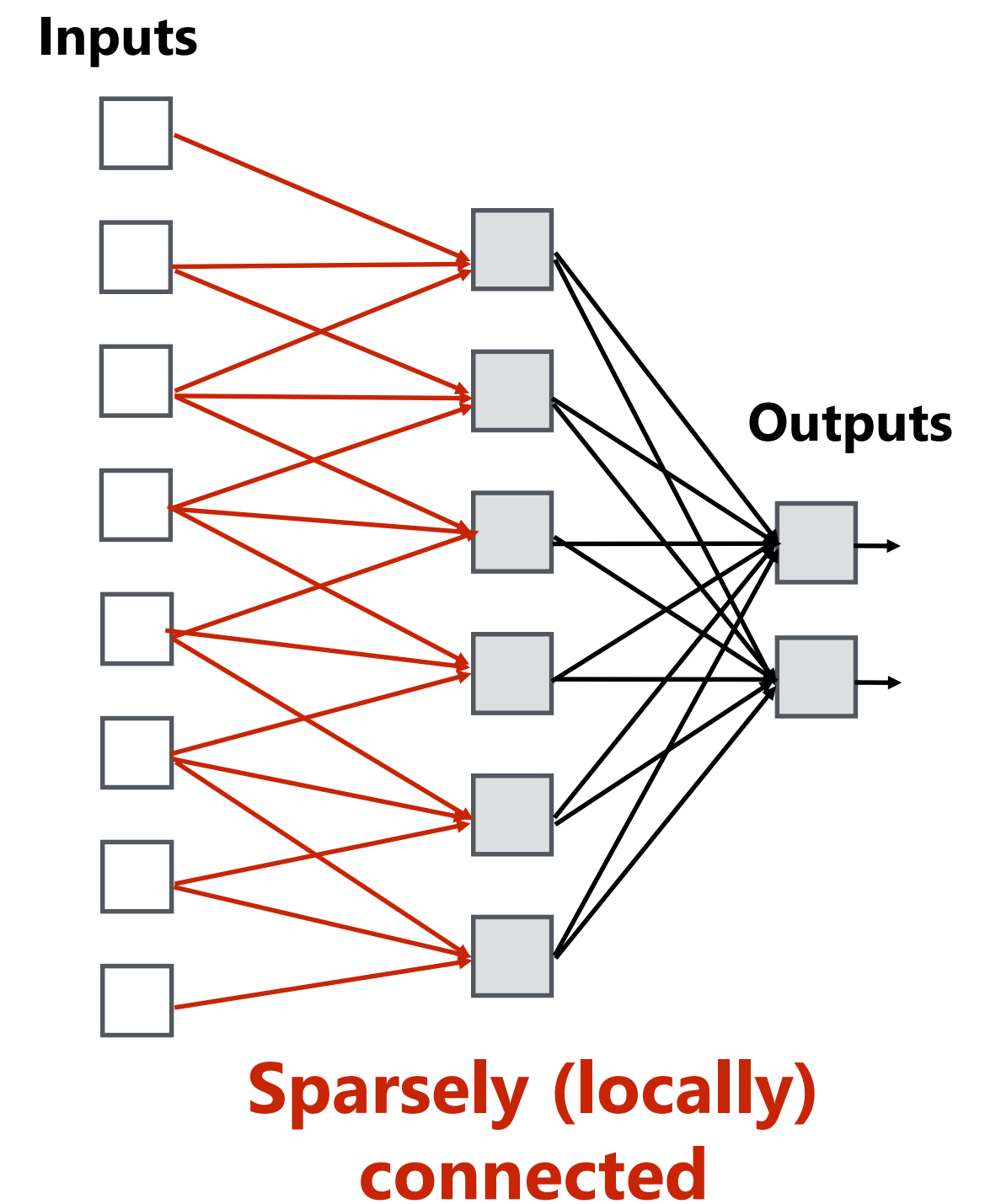
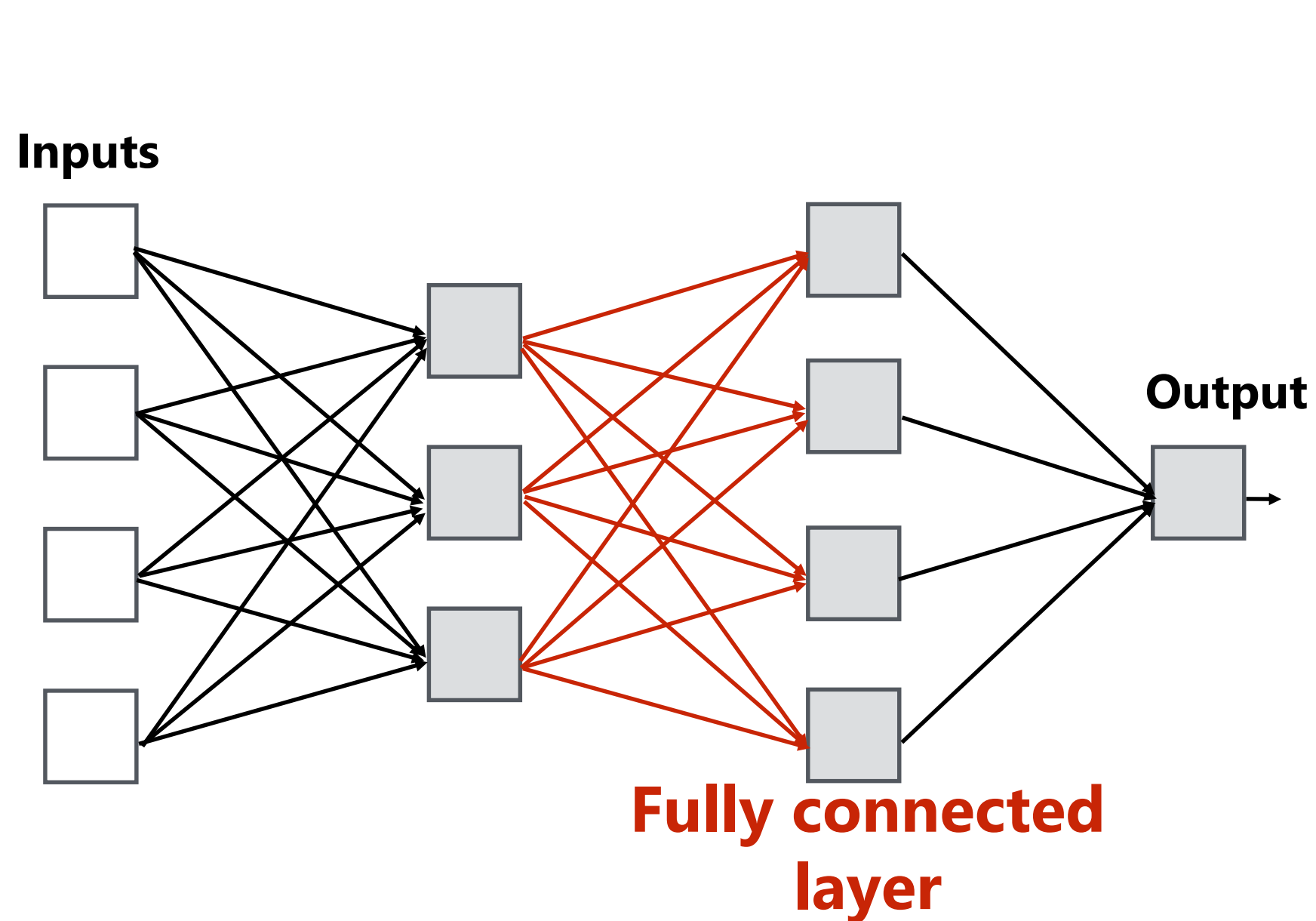
Hidden layer 2: 4 units x (3 weights + 1 bias) = 16 parameters



**Note fully-connected topology in this example**

# What is a deep neural network?

## topology

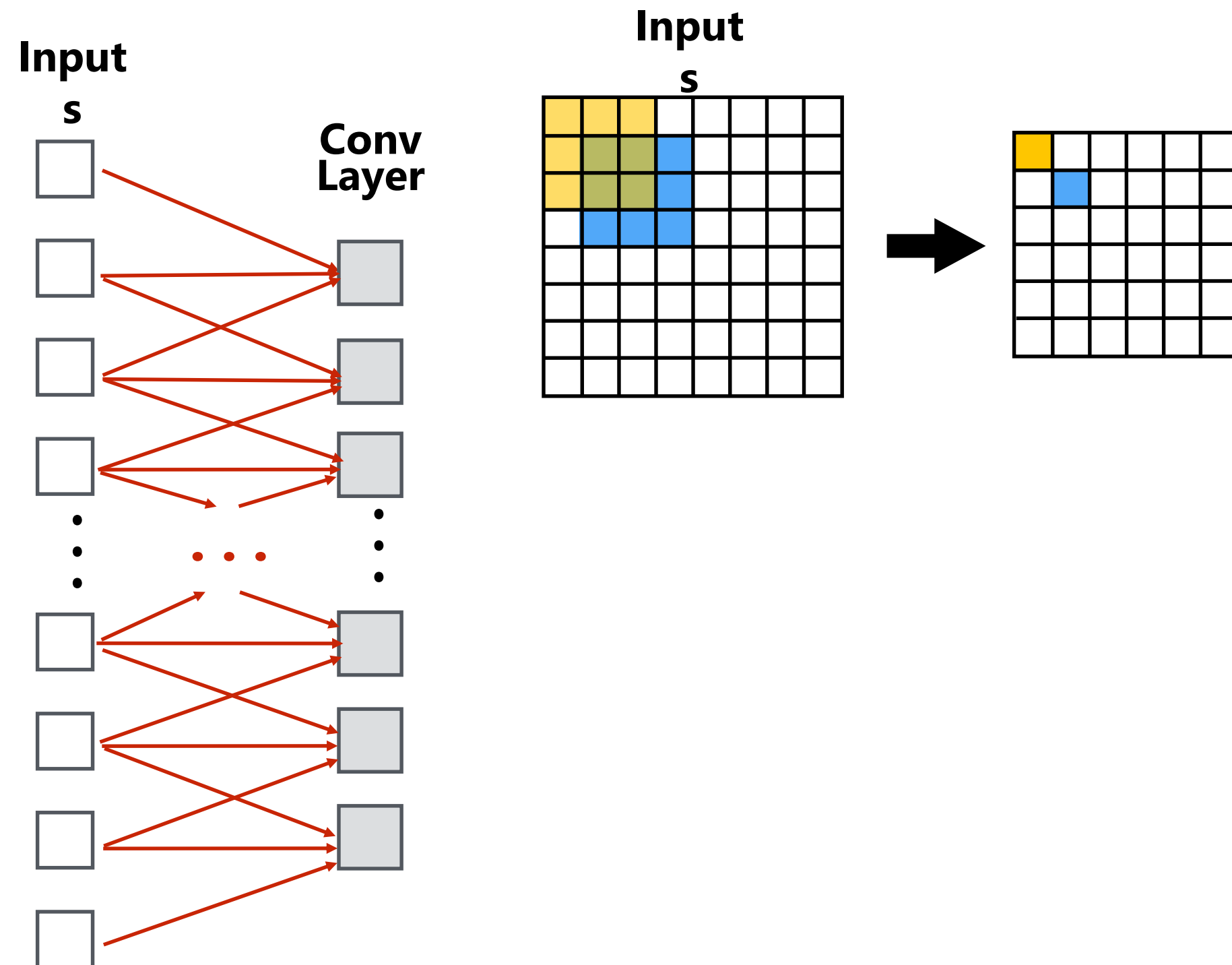


# Recall image convolution (3x3 conv)

```
int WIDTH = 1024;
int HEIGHT = 1024;
float input[(WIDTH+2) * (HEIGHT+2)];
float output[WIDTH * HEIGHT];

float bias = 0.f;
float weights[] = {1.0/9, 1.0/9, 1.0/9,
                  1.0/9, 1.0/9, 1.0/9,
                  1.0/9, 1.0/9, 1.0/9};
```

```
for (int j=0; j<HEIGHT; j++) {
    for (int i=0; i<WIDTH; i++) {
        float tmp = bias;
        for (int jj=0; jj<3; jj++)
            for (int ii=0; ii<3; ii++)
                tmp += input[(j+jj)*(WIDTH+2) + (i+ii)] * weights[jj*3 + ii];
        output[j*WIDTH + i] = tmp;
    }
}
```



**Convolutional layer: locally connected AND all units in layer share the same parameters (same weights + same bias):**  
 (note: network diagram only shows links due to one iteration of *ii* loop)



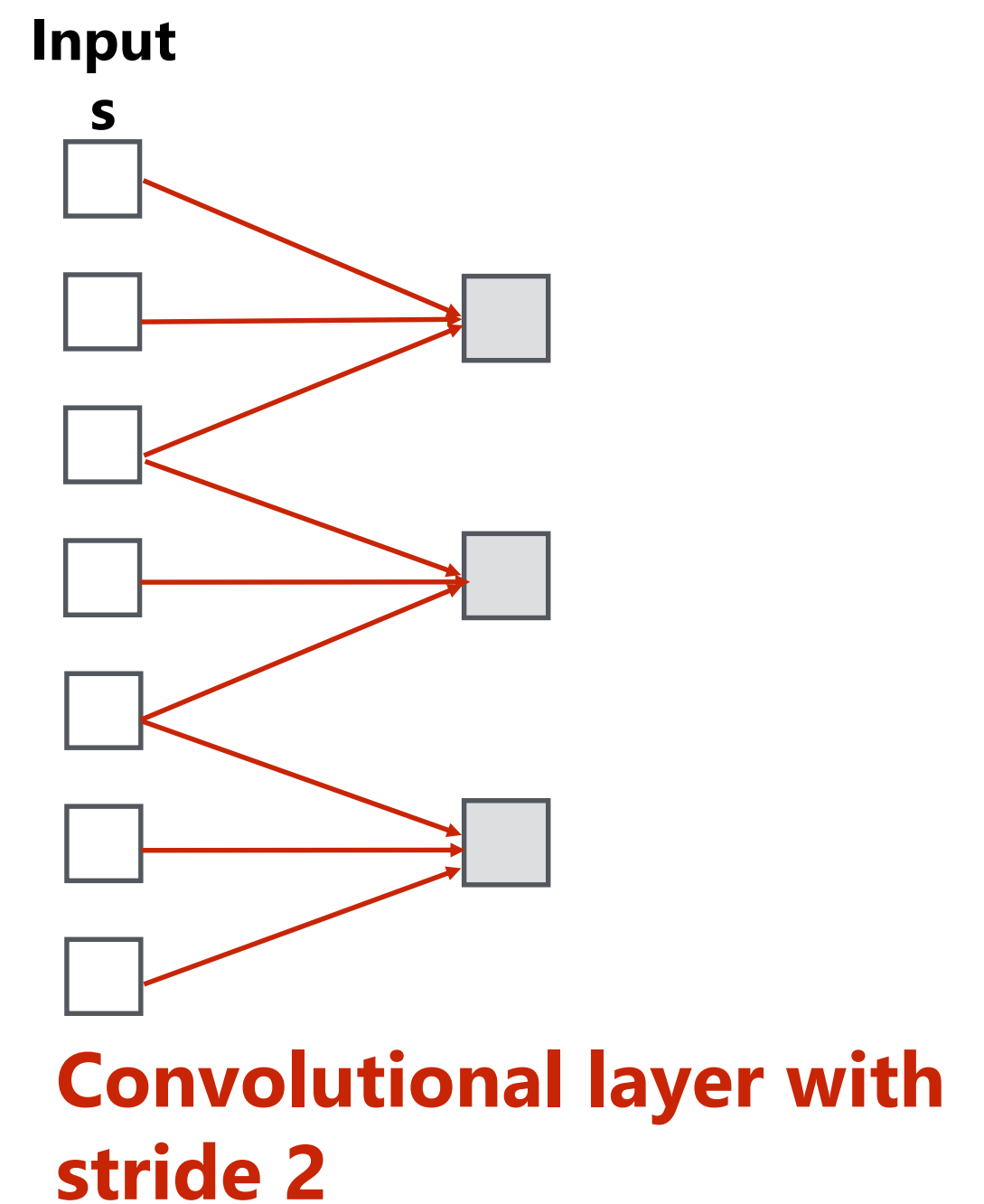
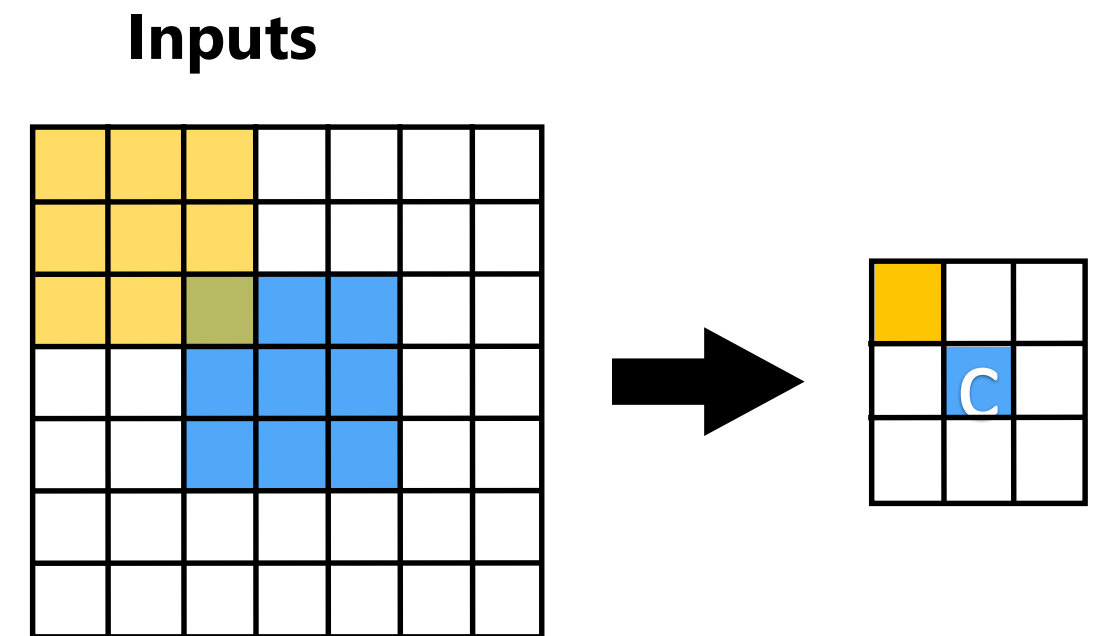
# Strided 3x3 convolution

```
int WIDTH = 1024;
int HEIGHT = 1024;
int STRIDE = 2;

float input[(WIDTH+2) * (HEIGHT+2)];
float output[(WIDTH/STRIDE) * (HEIGHT/STRIDE)];

float bias = 0.f;
float weights[] = {1.0/9, 1.0/9, 1.0/9,
                  1.0/9, 1.0/9, 1.0/9,
                  1.0/9, 1.0/9, 1.0/9};

for (int j=0; j<HEIGHT; j+=STRIDE) {
    for (int i=0; i<WIDTH; i+=STRIDE) {
        float tmp = bias;
        for (int jj=0; jj<3; jj++)
            for (int ii=0; ii<3; ii++) {
                tmp += input[(j+jj)*(WIDTH+2) + (i+ii)] * weights[jj*3 + ii];
            }
        output[(j/STRIDE)*WIDTH + (i/STRIDE)] = tmp;
    }
}
```



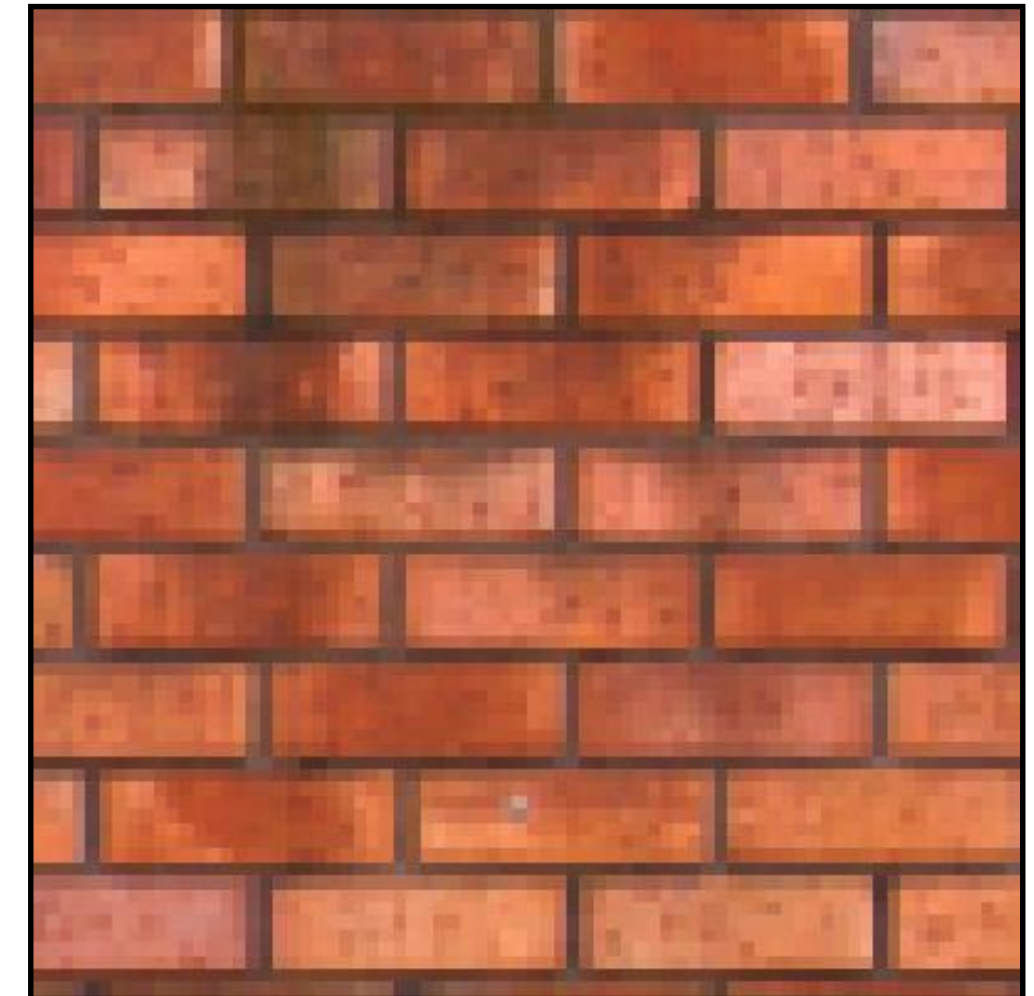
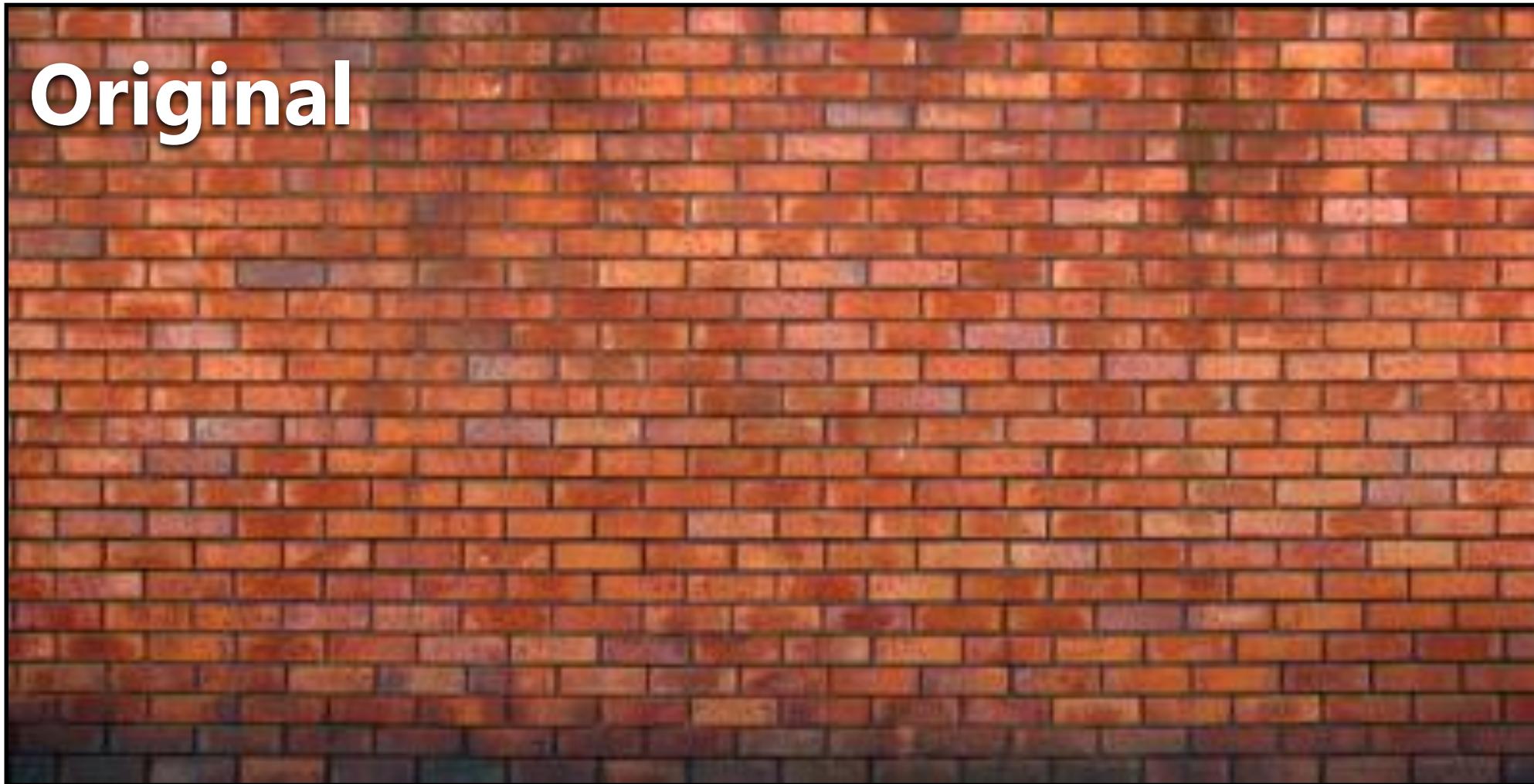


# What does convolution using these filter weights do?

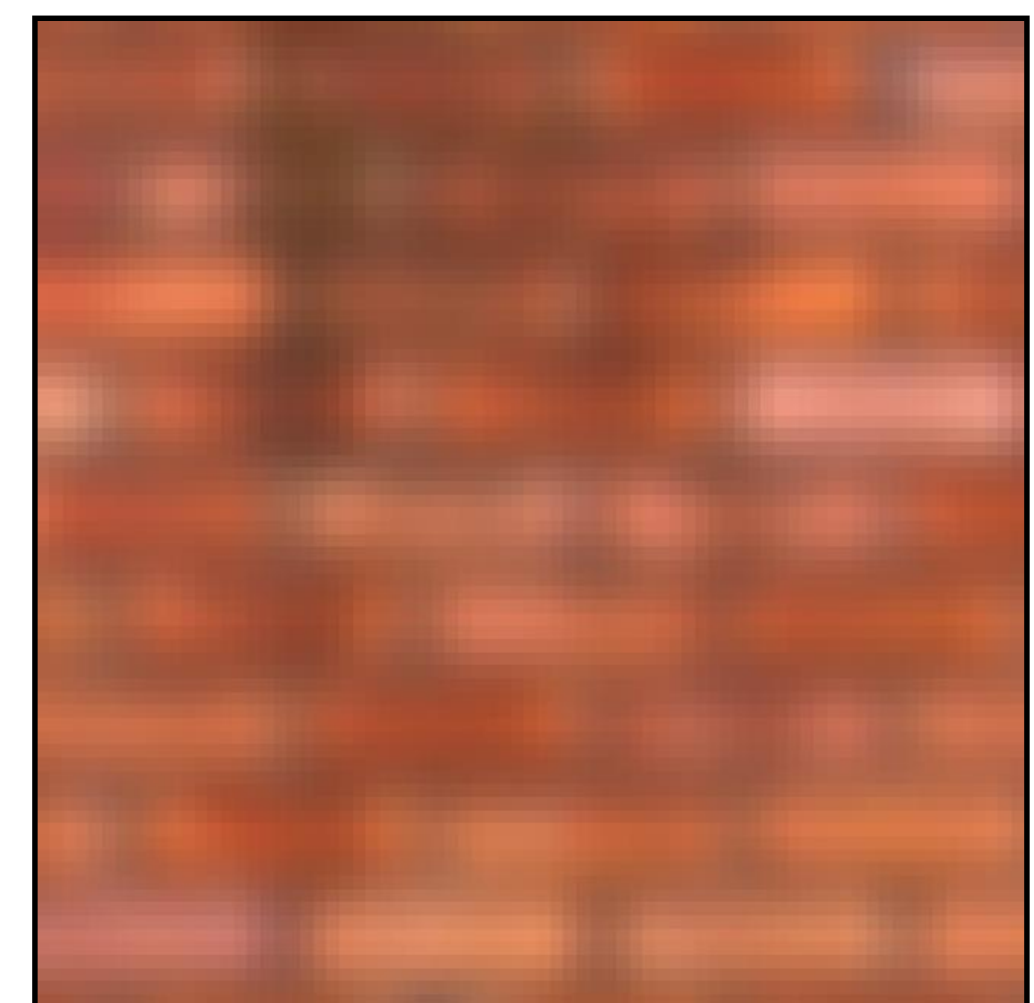
$$\begin{bmatrix} .075 & .124 & .075 \\ .124 & .204 & .124 \\ .075 & .124 & .075 \end{bmatrix}$$

**“Gaussian Blur”**

**Original**



**Blurred**



# What does convolution with these filters do?

$$\begin{bmatrix} -1 & 0 & 1 \\ -2 & 0 & 2 \\ -1 & 0 & 1 \end{bmatrix}$$

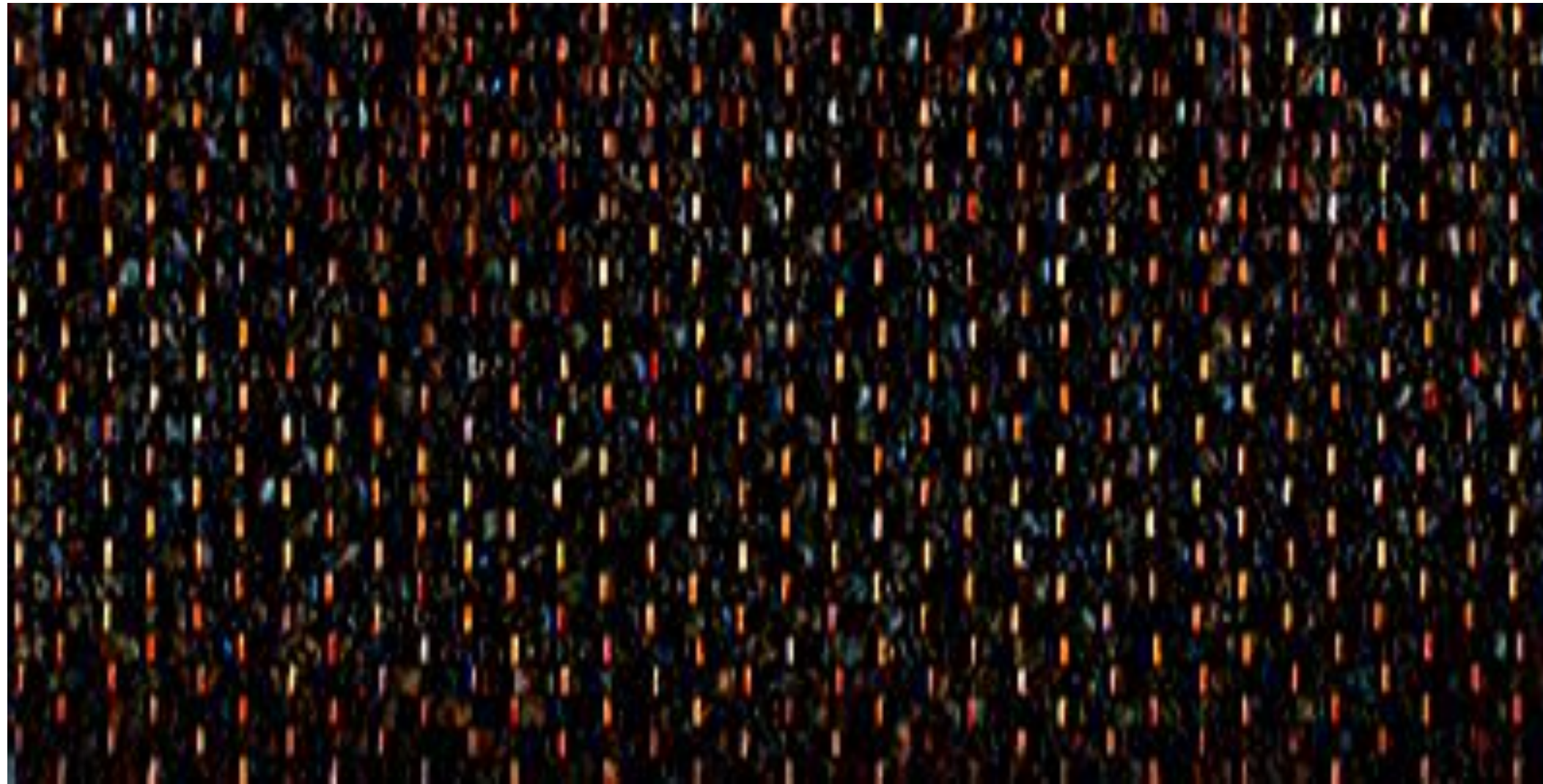
**Extracts horizontal  
gradients**

$$\begin{bmatrix} -1 & -2 & -1 \\ 0 & 0 & 0 \\ 1 & 2 & 1 \end{bmatrix}$$

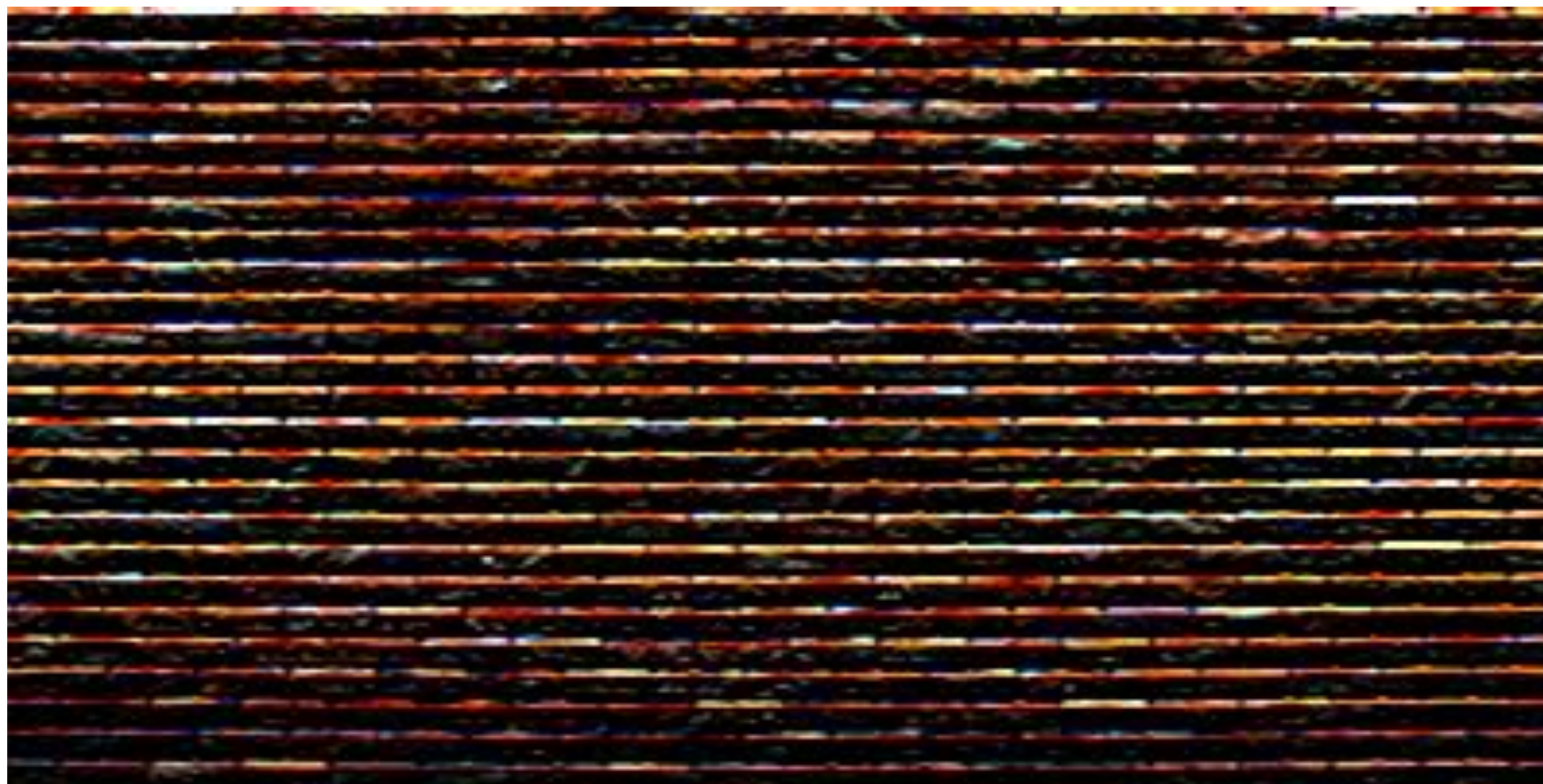
**Extracts vertical  
gradients**



# Gradient detection filters



**Horizontal gradients**

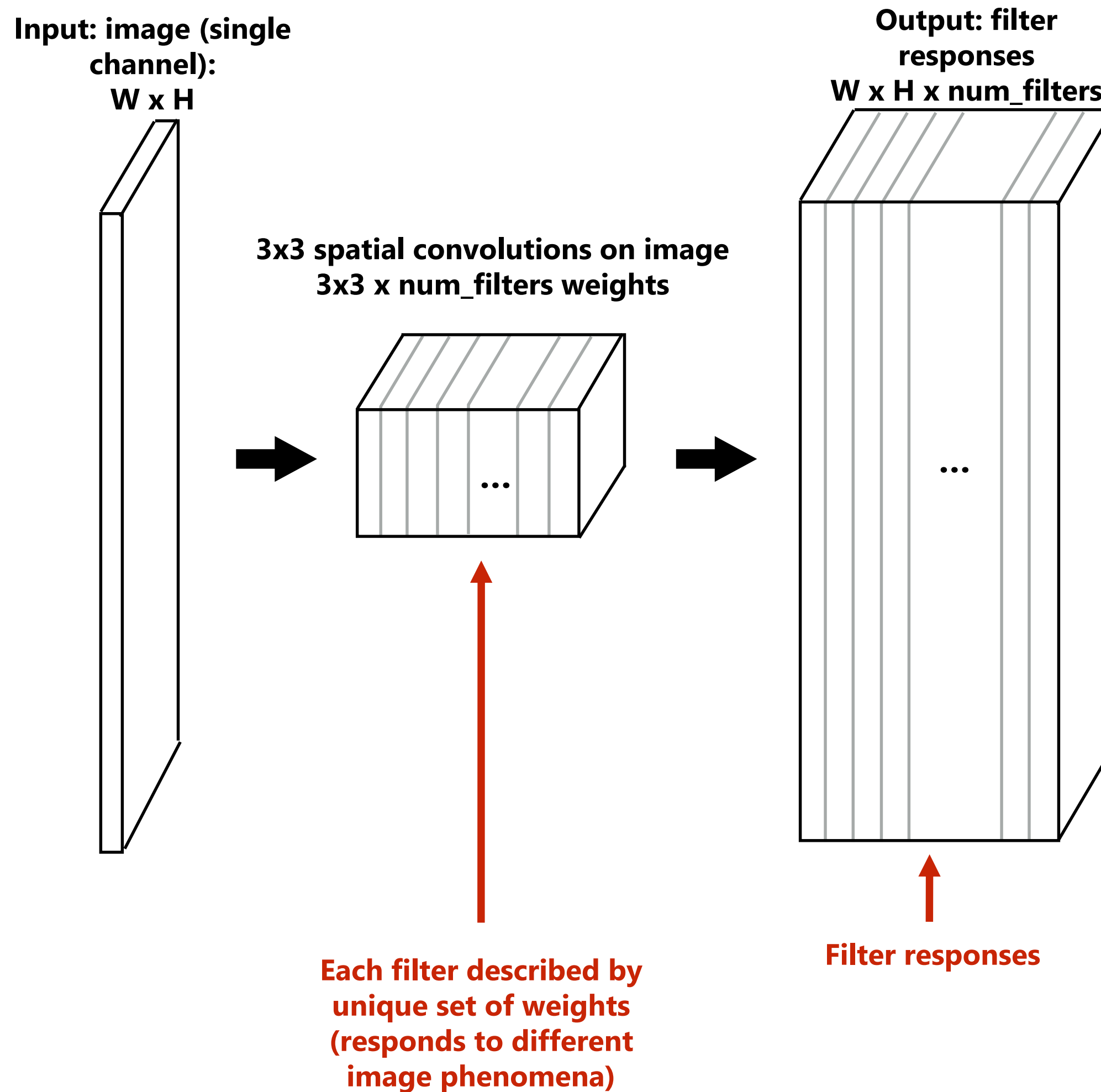


**Vertical gradients**

**Note: You can think of a filter as a “detector” of a pattern, and the magnitude of a pixel in the output image as the “response” of the filter to the region surrounding each pixel in the input image**



# Applying many filters to an image at once

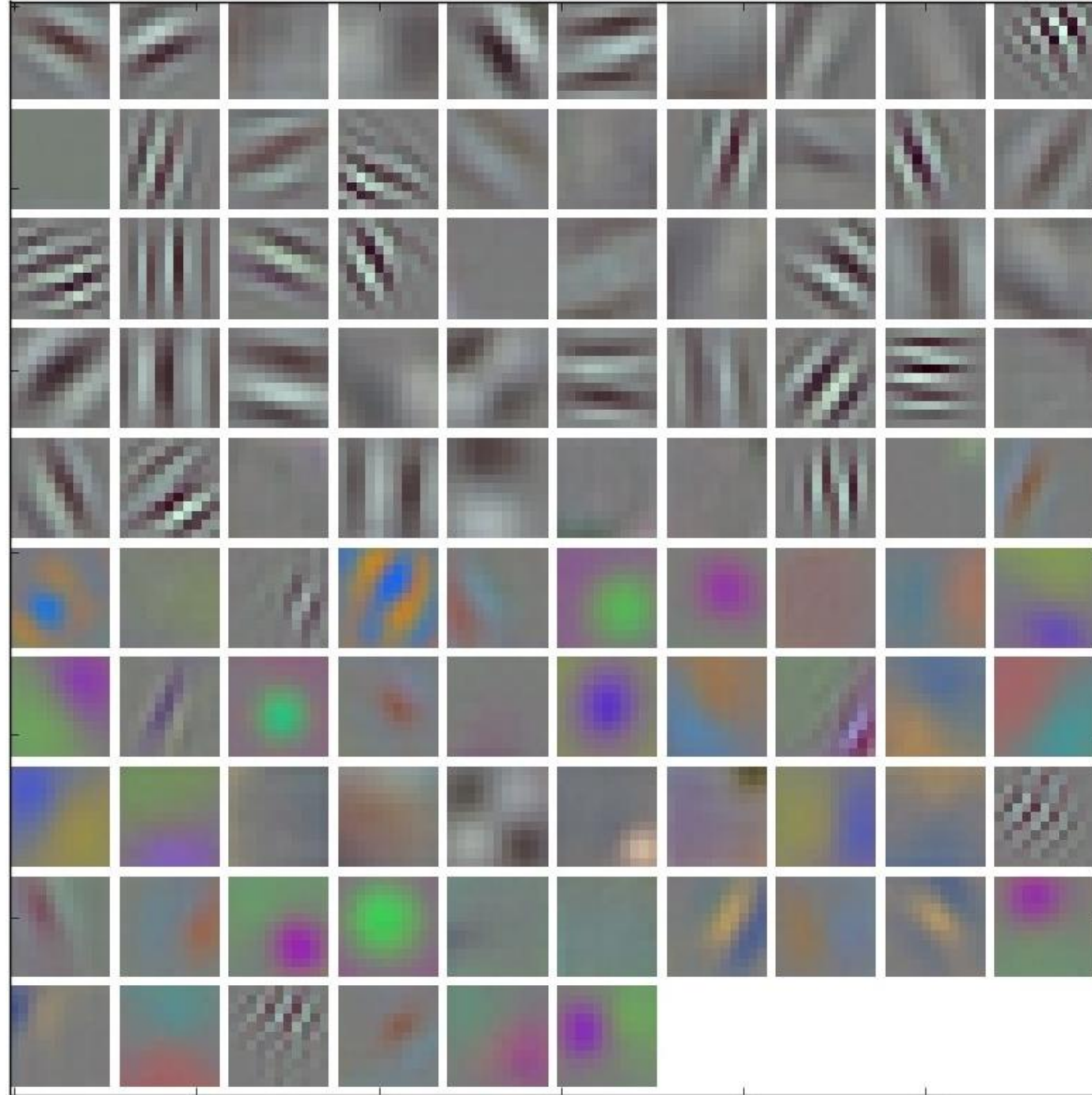


# Applying many filters to an image at once

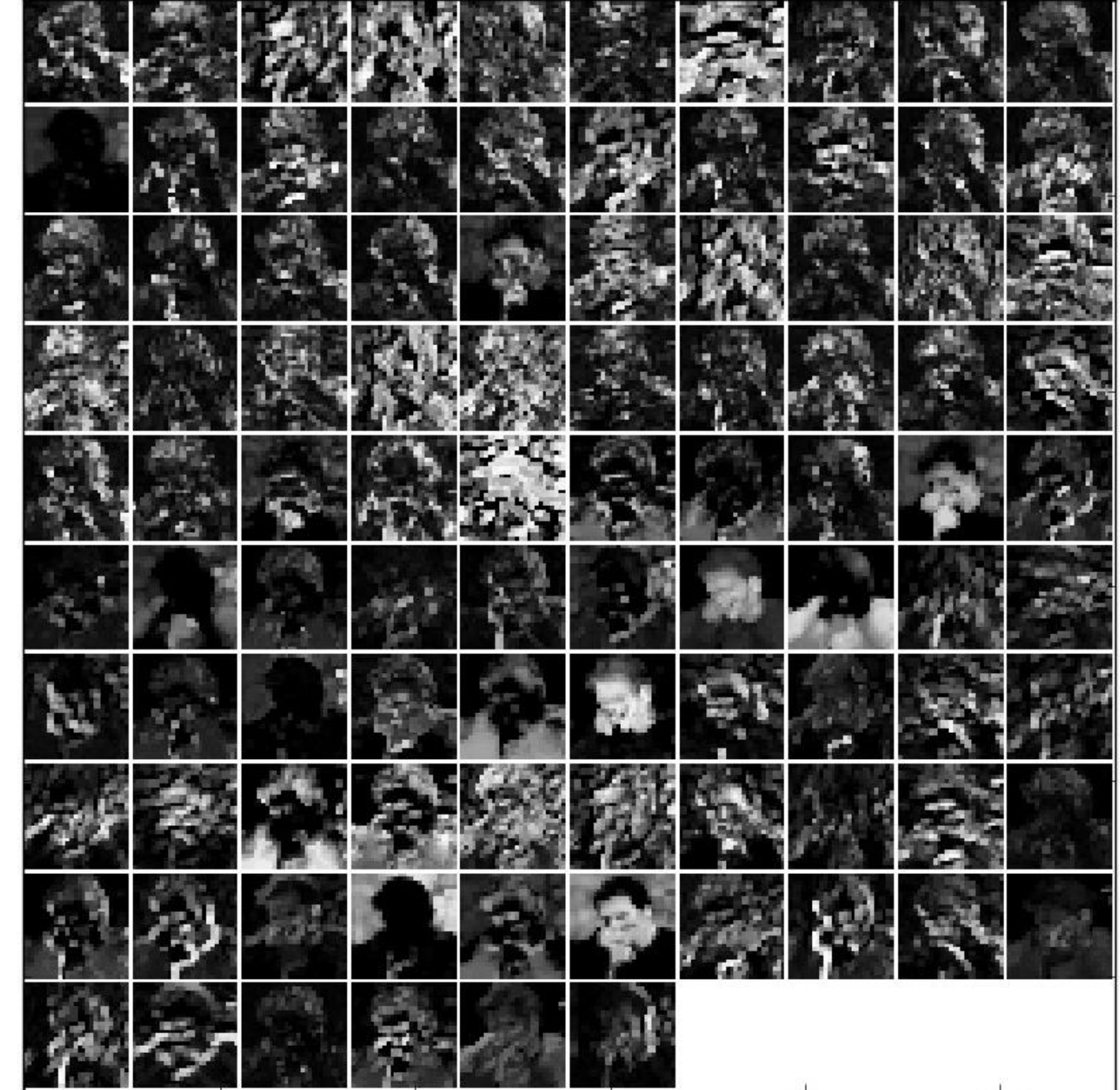
Input RGB image (W x H x 3)



96 11x11x3 filters  
(operate on RGB)

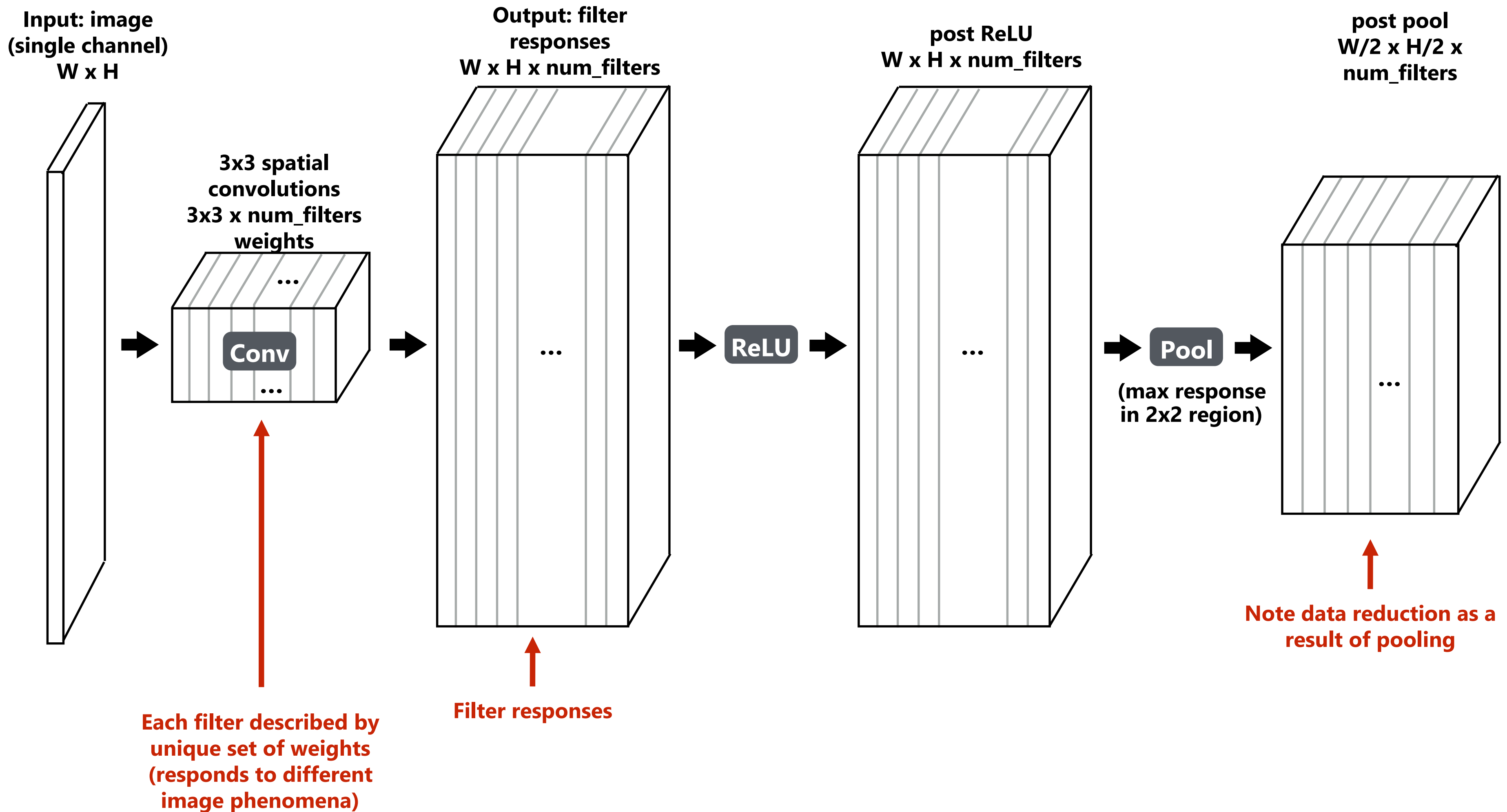


96 responses (normalized)





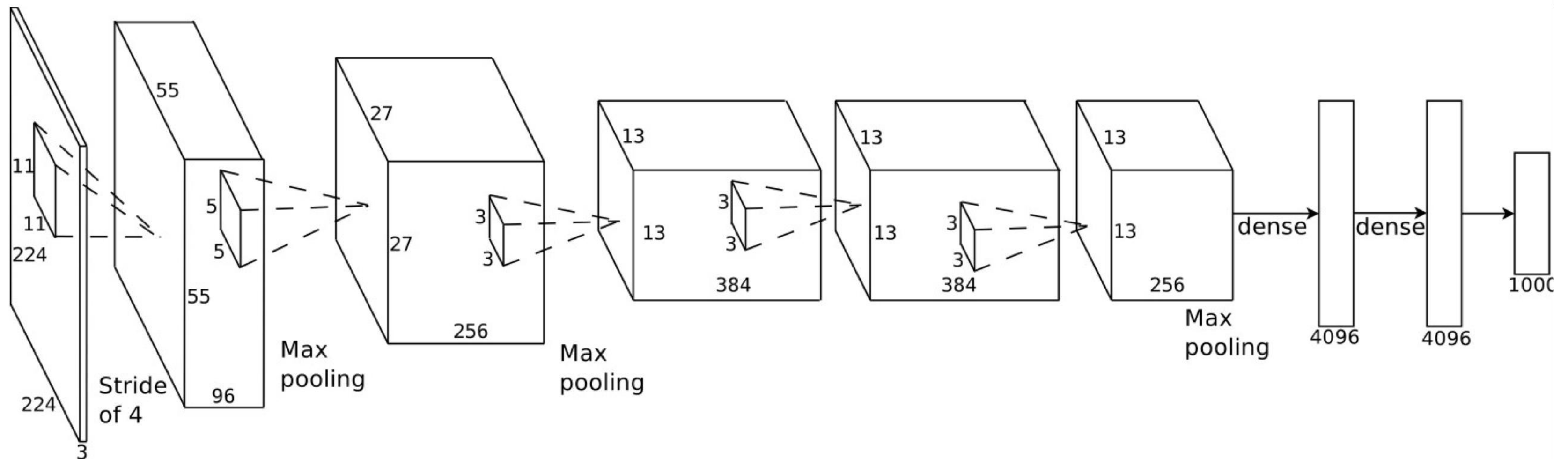
# Adding additional layers



# Modern object detection networks

Sequences of conv + relu + (optional) pool layers

AlexNet [Krizhevsky12]: 5 convolutional layers + 3 fully connected



## VGG-16 [Simonyan15]: 13 convolutional layers

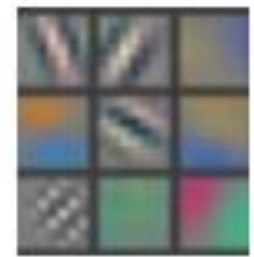
input: 224 x 224 RGB  
conv/relu: 3x3x3x64  
conv/relu: 3x3x64x64  
maxpool  
conv/relu: 3x3x64x128  
conv/relu: 3x3x128x128  
maxpool

conv/relu: 3x3x128x256  
conv/relu: 3x3x256x256  
conv/relu: 3x3x256x256  
maxpool  
conv/relu: 3x3x256x512  
conv/relu: 3x3x512x512  
conv/relu: 3x3x512x512  
maxpool

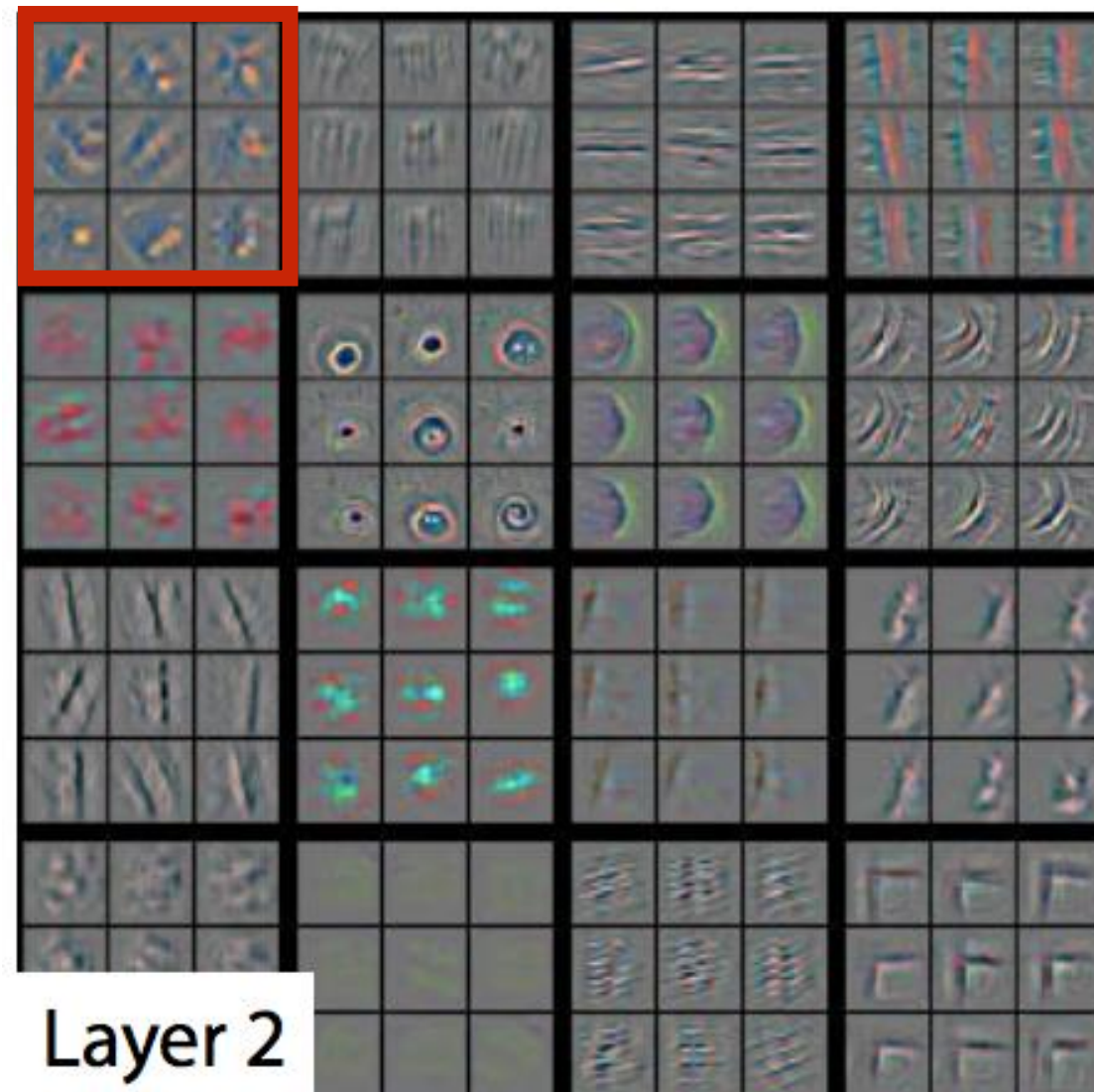
conv/relu: 3x3x512x512  
conv/relu: 3x3x512x512  
conv/relu: 3x3x512x512  
maxpool  
fully-connected 4096  
fully-connected 4096  
fully-connected 1000  
soft-max



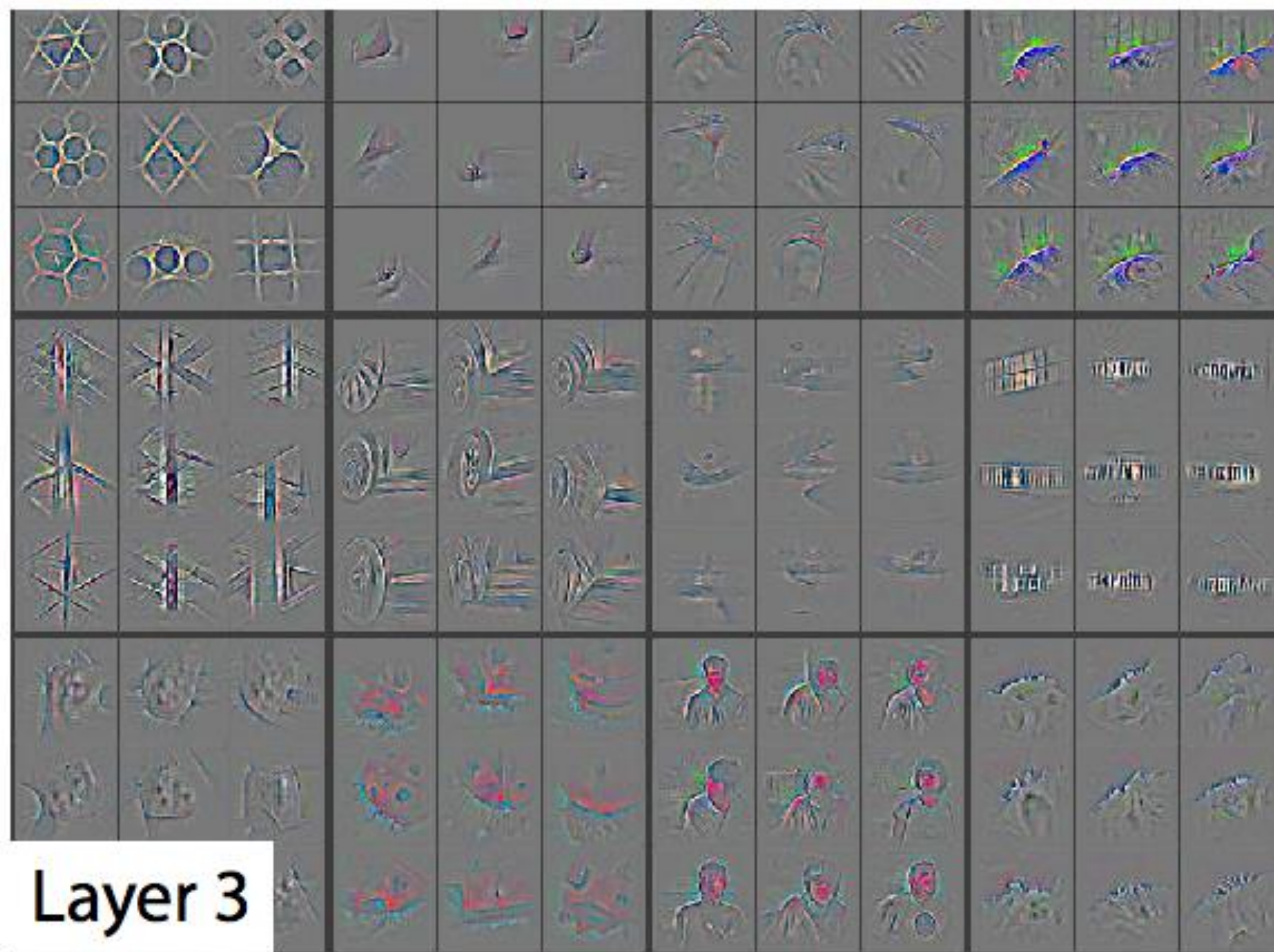
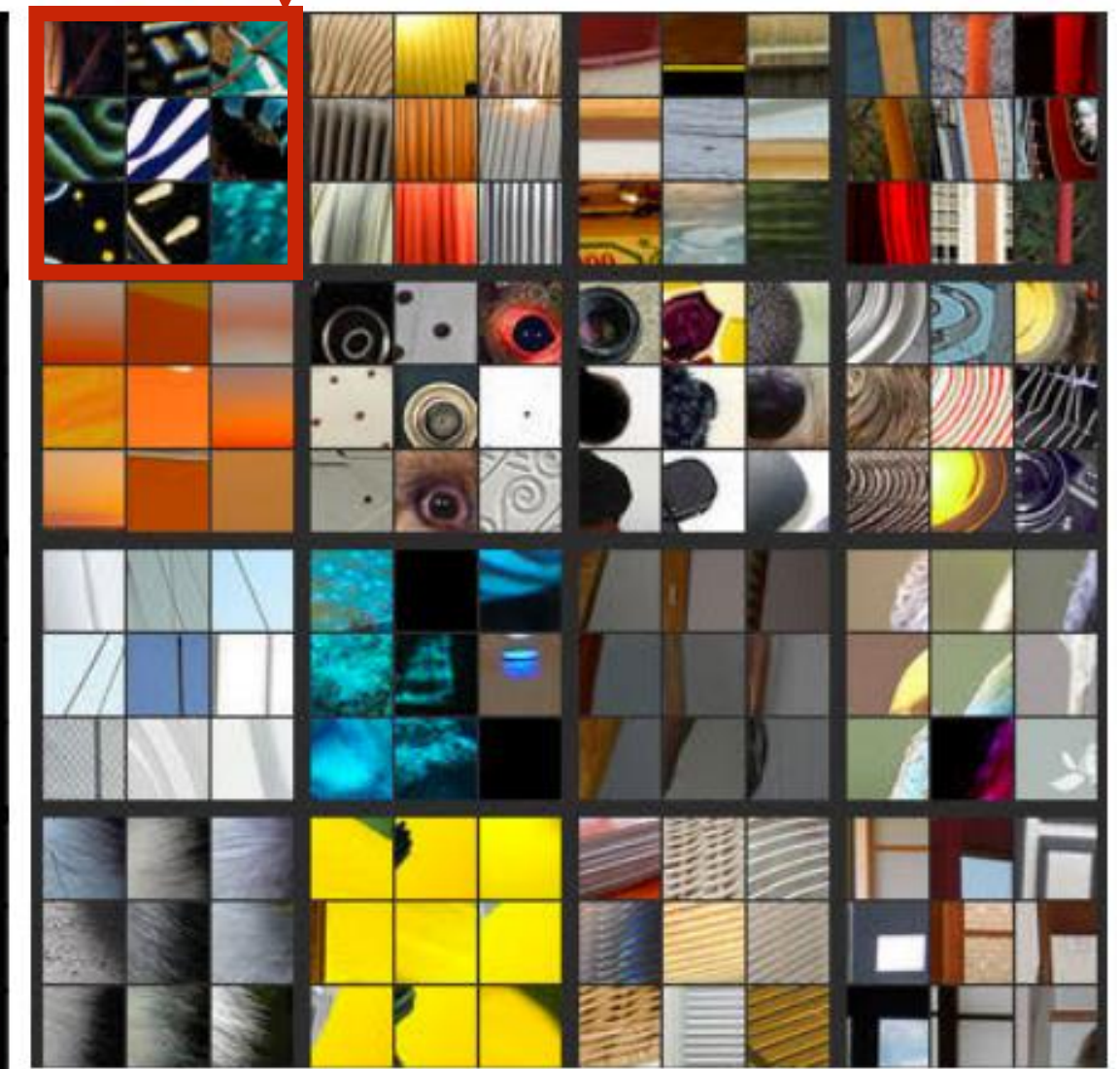
# Why deep?



Layer 1



Layer 2



Layer 3

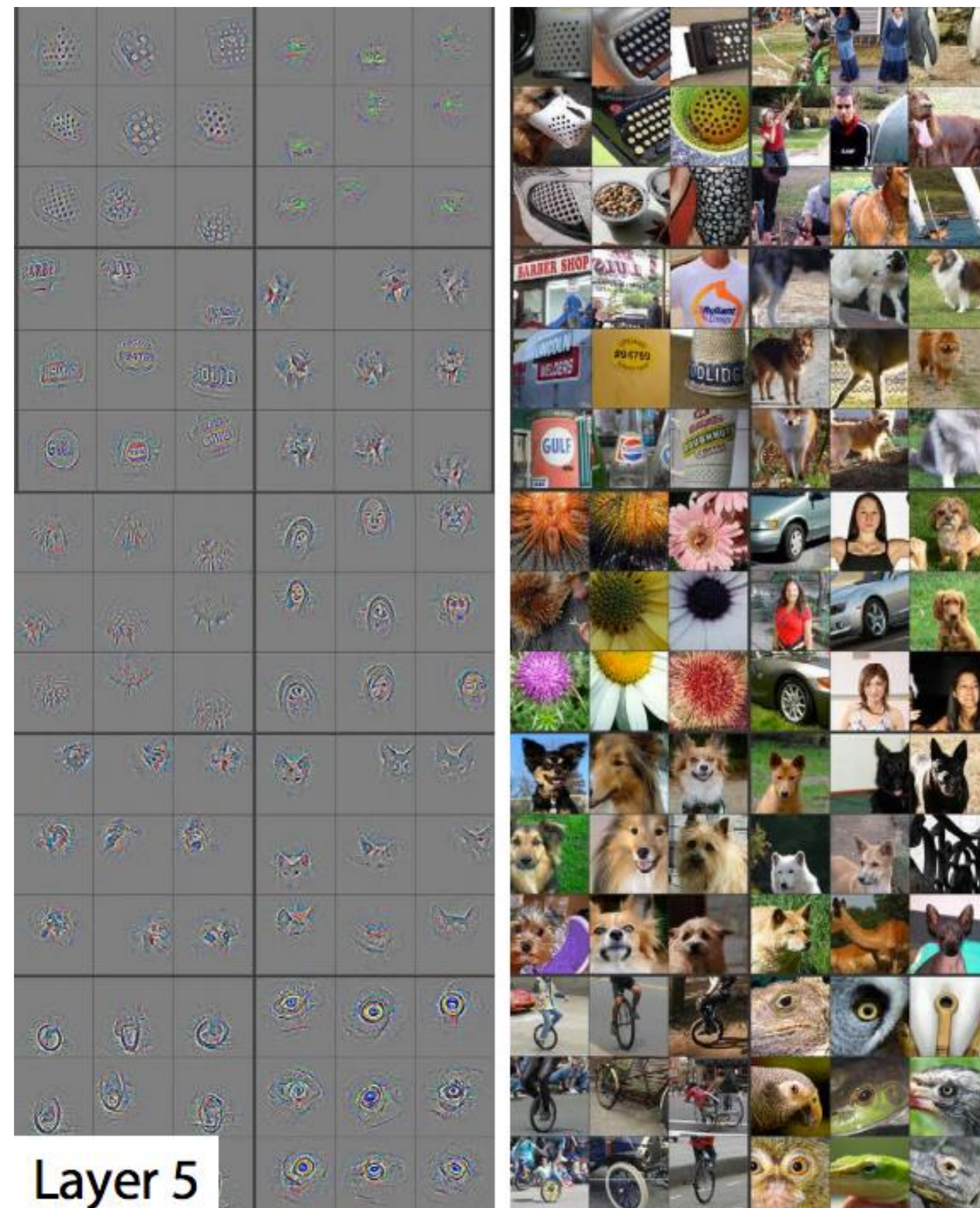
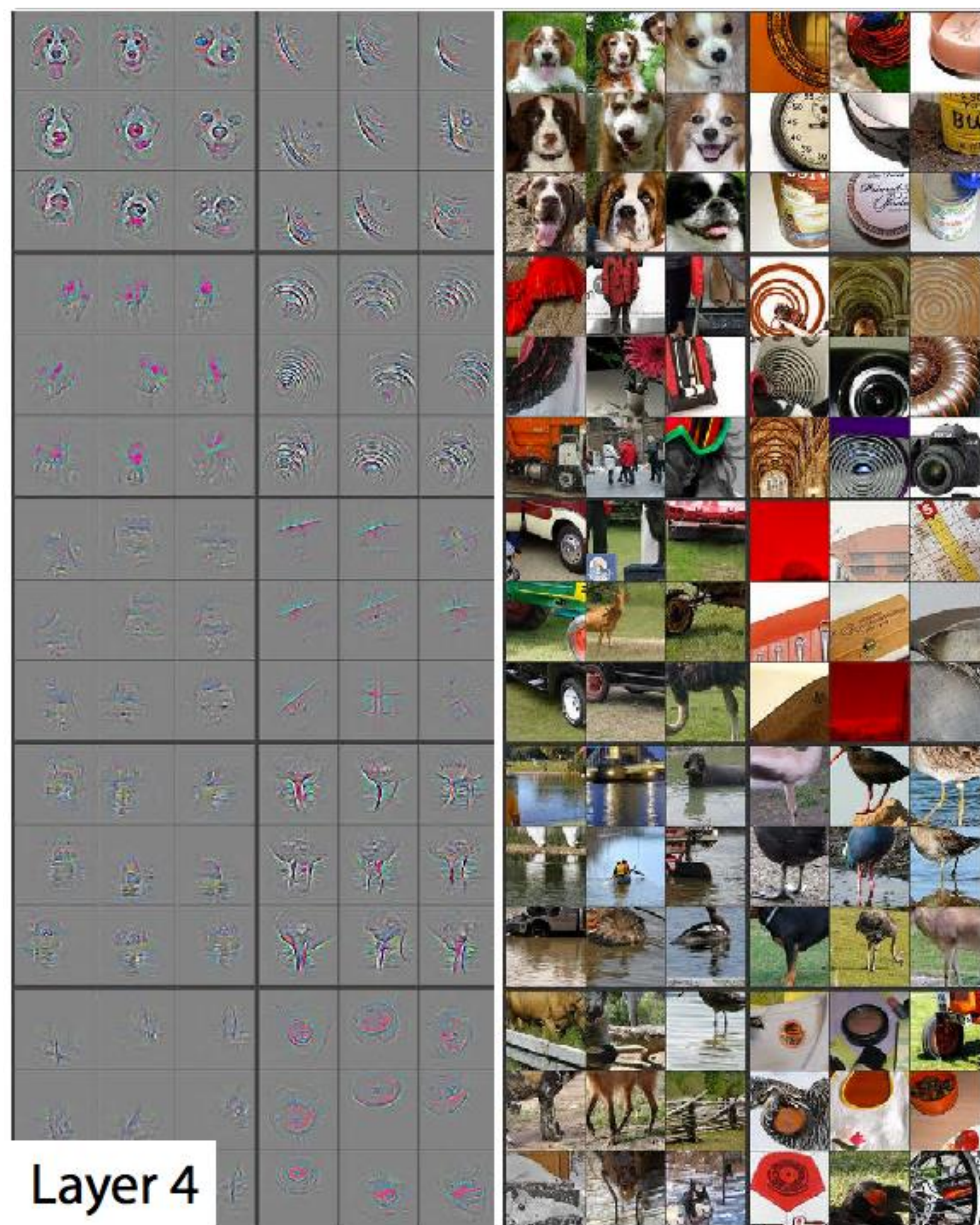


Left: what pixels trigger the response

Right: images that generate strongest response for filters at each layer



# Why deep?





# **Efficiently implementing convolution layers**

# Direct implementation of conv layer

```
float input[INPUT_HEIGHT][INPUT_WIDTH][INPUT_DEPTH];
float output[INPUT_HEIGHT][INPUT_WIDTH][OUTPUT_DEPTH];
float layer_weights[OUTPUT_DEPTH][INPUT_DEPTH][LAYER_CONVY][LAYER_CONVX];
float layer_biases[OUTPUT_DEPTH];
// assumes convolution stride is 1
// Note that code does not handle boundary conditions
for (int img=0; img<IMAGE_BATCH_SIZE; img++) // Optional outer loop for multiple images
    for (int j=0; j<INPUT_HEIGHT; j++)
        for (int i=0; i<INPUT_WIDTH; i++)
            for (int f=0; f<OUTPUT_DEPTH; f++) {
                float tmp = layer_biases[f];
                for (int kk=0; kk<INPUT_DEPTH; kk++) // sum over filter responses of input channels
                    for (int jj=0; jj<LAYER_CONVY; jj++) // spatial convolution
                        for (int ii=0; ii<LAYER_CONVX; ii++) // spatial convolution
                            tmp += layer_weights[f][kk][jj][ii] * input[j+jj][i+ii][kk];
                output[j][i][f] = tmp; // Use Max(0.f, tmp) for ReLU
            }
```

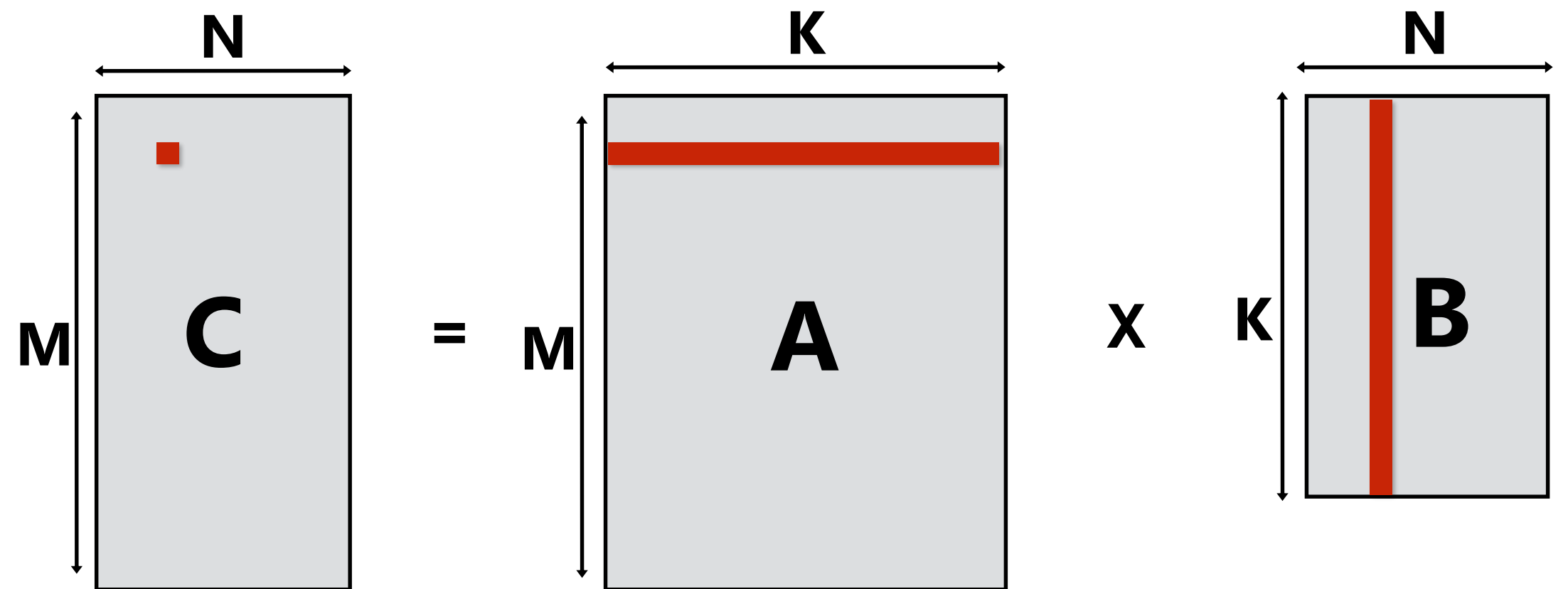
**Seven loops with significant input data reuse: reuse of filter weights (during convolution), and reuse of input values (across different filters)**

**But must roll your own highly optimized implementation of a complicated loop nest.**



# Dense matrix multiplication

```
float A[M][K];  
float B[K][N];  
float C[M][N];  
  
// compute C += A * B  
#pragma omp parallel for  
for (int j=0; j<M; j++)  
    for (int i=0; i<N; i++)  
        for (int k=0; k<K; k++)  
            C[j][i] += A[j][k] * B[k][i];
```



**What is the problem with this implementation?**

**Low arithmetic intensity (does not exploit temporal locality in access to A and B)**

# Blocked dense matrix multiplication

```
float A[M][K];
```

```
float B[K][N];
```

```
float C[M][N];
```

```
// compute C += A * B
```

```
#pragma omp parallel for
```

```
for (int jblock=0; jblock<M; jblock+=BLOCKSIZE_J)
```

```
    for (int iblock=0; iblock<N; iblock+=BLOCKSIZE_I)
```

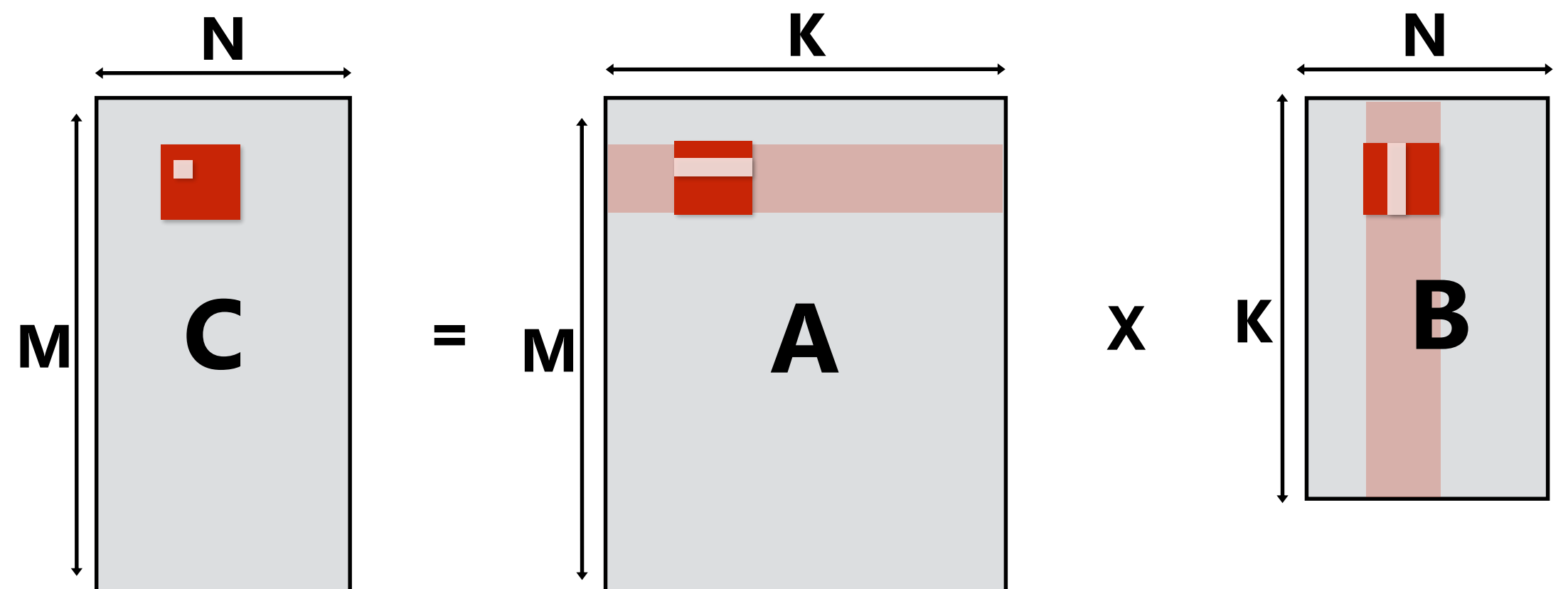
```
        for (int kblock=0; kblock<K; kblock+=BLOCKSIZE_K)
```

```
            for (int j=0; j<BLOCKSIZE_J; j++)
```

```
                for (int i=0; i<BLOCKSIZE_I; i++)
```

```
                    for (int k=0; k<BLOCKSIZE_K; k++)
```

```
                        C[jblock+j][iblock+i] += A[jblock+j][kblock+k] * B[kblock+k][iblock+i];
```



**Idea: compute partial result for block of C while required blocks of A and B remain in cache**

**(Assumes BLOCKSIZE chosen to allow block of A, B, and C to remain resident)**

**Self check: do you want as big a BLOCKSIZE as possible? Why?**



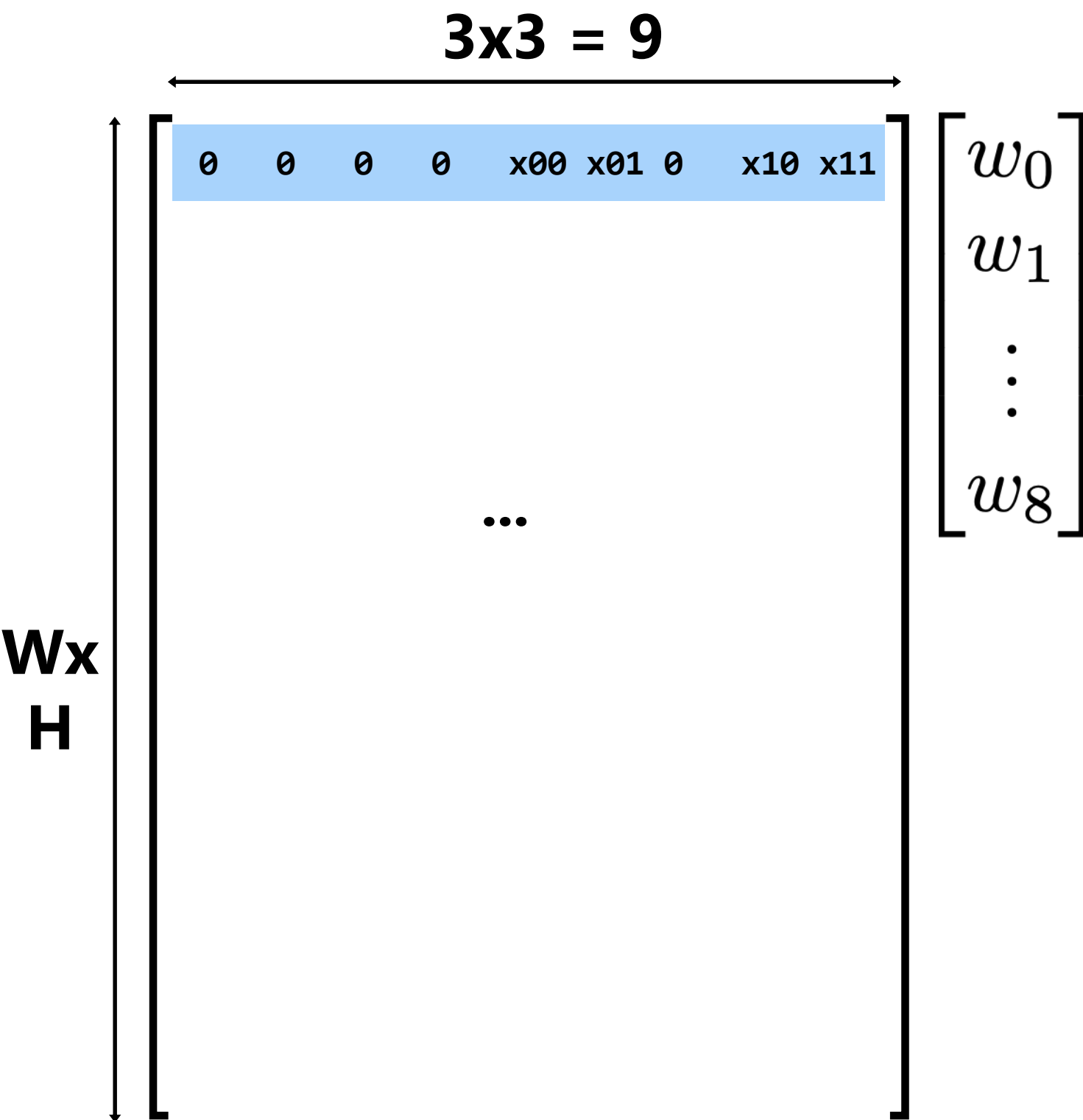
# Convolution as matrix-vector product

Construct matrix from elements of input image

$X_0$ 0	$X_0$ 1	$X_0$ 2	$X_0$ 3	...			
$X_1$ 0	$X_1$ 1	$X_1$ 2	$X_1$ 3	...			
$X_2$ 0	$X_2$ 1	$X_2$ 2	$X_2$ 3	...			
$X_3$ 0	$X_3$ 1	$X_3$ 2	$X_3$ 3	...			
...	...	...	...				

$O(N)$  storage overhead for filter with  $N$  elements

Must construct input data matrix



Note: 0-pad matrix

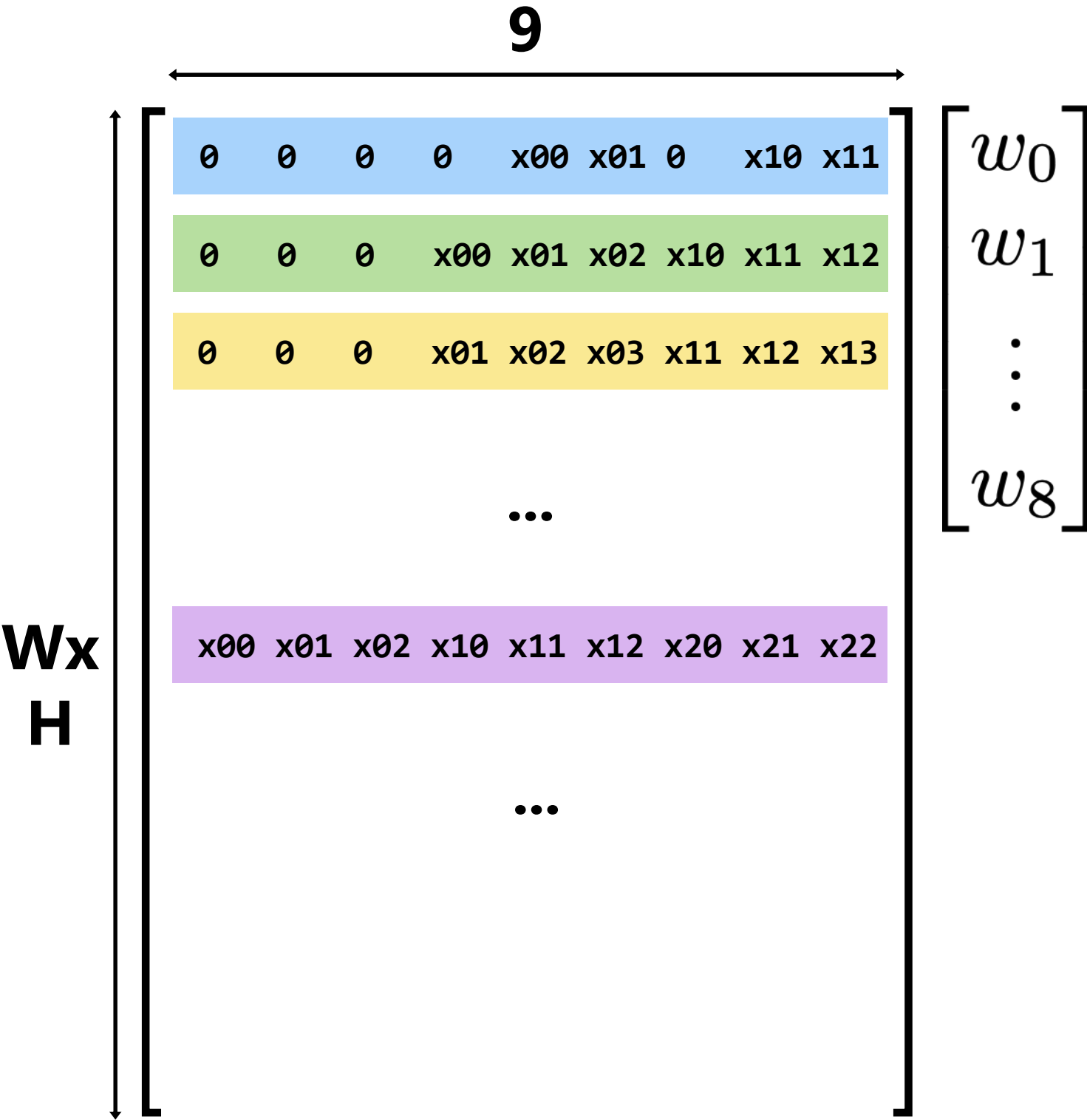
# 3x3 convolution as matrix-vector product

Construct matrix from elements of input image

	$X_0$ 0	$X_0$ 1	$X_0$ 2	$X_0$ 3	...			
	$X_1$ 0	$X_1$ 1	$X_1$ 2	$X_1$ 3	...			
	$X_2$ 0	$X_2$ 1	$X_2$ 2	$X_2$ 3	...			
	$X_3$ 0	$X_3$ 1	$X_3$ 2	$X_3$ 3	...			
	...	...	...	...				

$O(N)$  storage overhead for filter with  $N$  elements

Must construct input data matrix

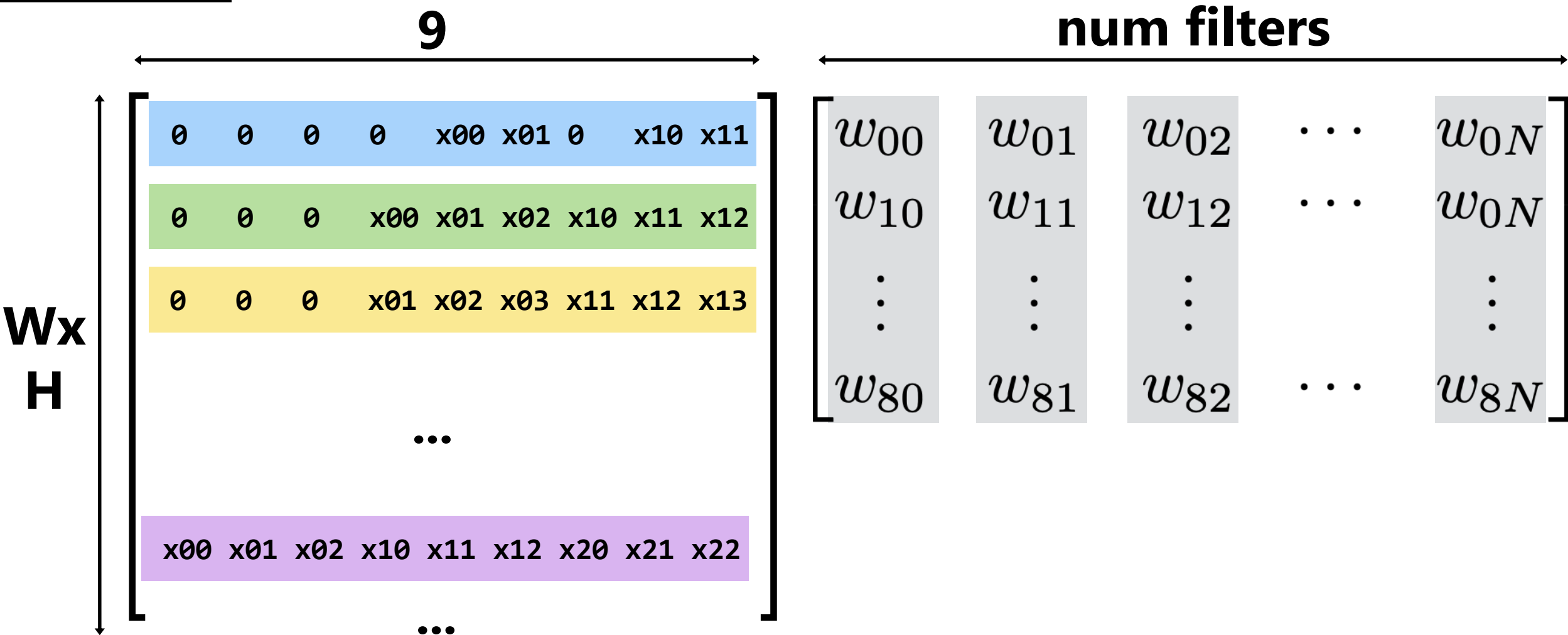


Note: 0-pad matrix

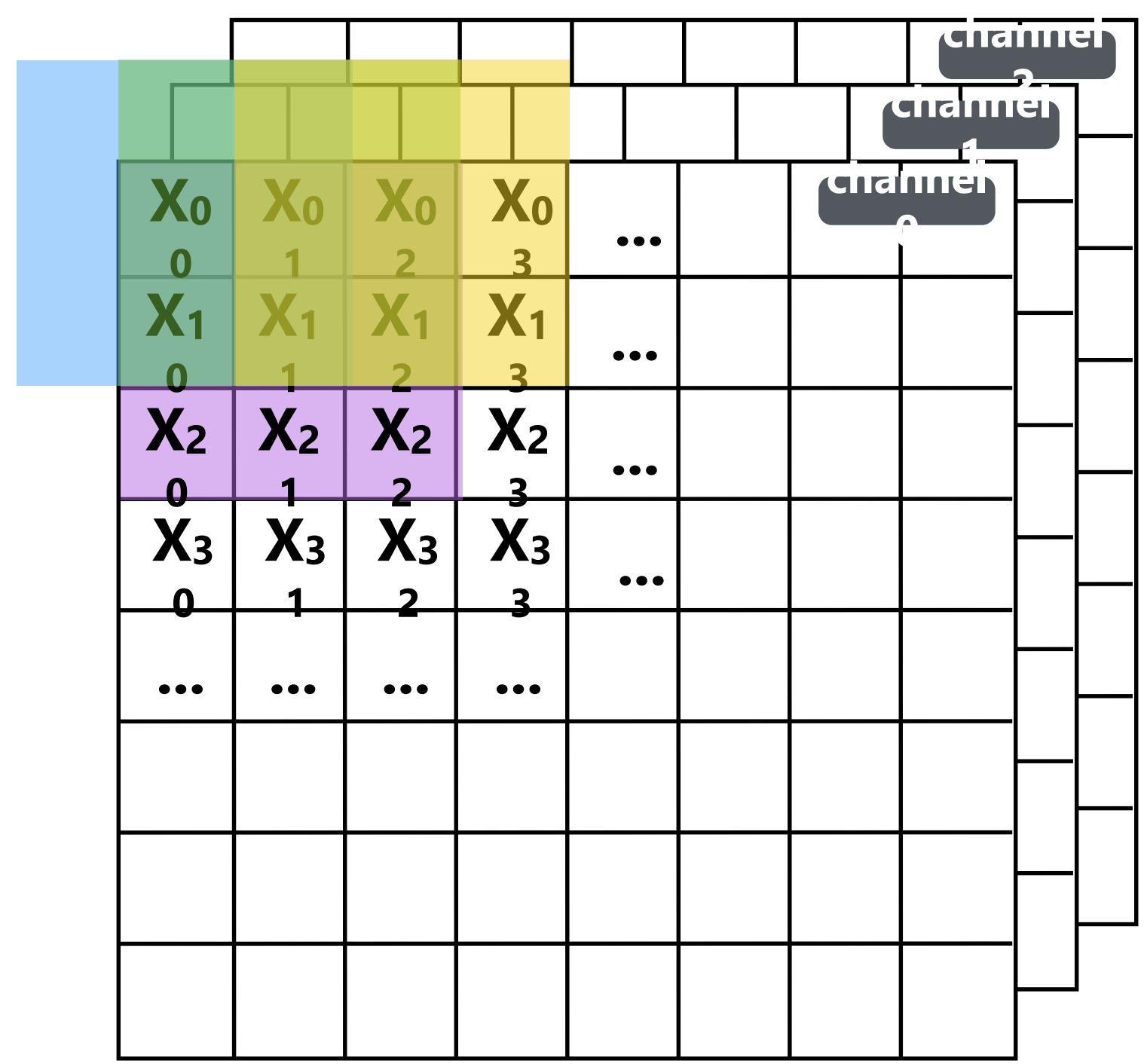


# Multiple convolutions as matrix-matrix mult

	$X_0$ 0	$X_0$ 1	$X_0$ 2	$X_0$ 3	...			
	$X_1$ 0	$X_1$ 1	$X_1$ 2	$X_1$ 3	...			
	$X_2$ 0	$X_2$ 1	$X_2$ 2	$X_2$ 3	...			
	$X_3$ 0	$X_3$ 1	$X_3$ 2	$X_3$ 3	...			
	...	...	...	...				

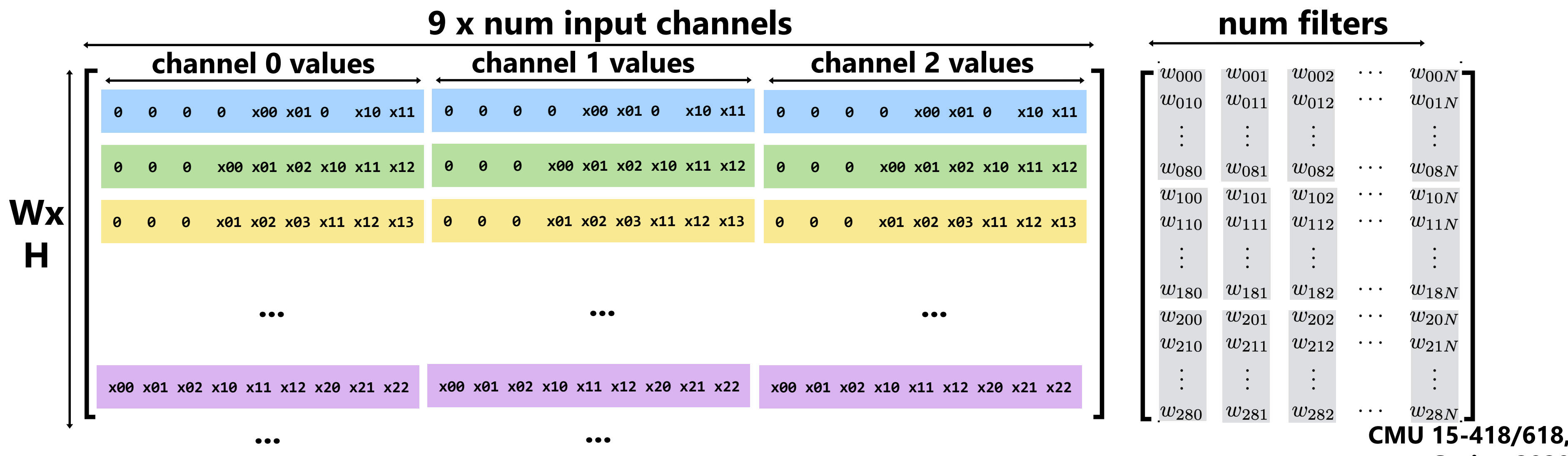


# Multiple convolutions on multiple input channels



For each filter, sum responses over input channels

Equivalent to (3 x 3 x num\_channels) convolution on (W x H x num\_channels) input data





# VGG memory footprint

inputs/outputs get multiplied by image batch size

multiply by next layer's conv window size to form input matrix to next conv layer!!! (for VGG, this is a 9x data amplification)

Calculations assume 32-bit values (image batch size = 1)

	weights mem:	output size (per image)	(mem)
input: 224 x 224 RGB image	—	224x224x3	150K
conv: (3x3x3) x 64	6.5 KB	224x224x64	12.3 MB
conv: (3x3x64) x 64	144 KB	224x224x64	12.3 MB
maxpool	—	112x112x64	3.1 MB
conv: (3x3x64) x 128	228 KB	112x112x128	6.2 MB
conv: (3x3x128) x 128	576 KB	112x112x128	6.2 MB
maxpool	—	56x56x128	1.5 MB
conv: (3x3x128) x 256	1.1 MB	56x56x256	3.1 MB
conv: (3x3x256) x 256	2.3 MB	56x56x256	3.1 MB
conv: (3x3x256) x 256	2.3 MB	56x56x256	3.1 MB
maxpool	—	28x28x256	766 KB
conv: (3x3x256) x 512	4.5 MB	28x28x512	1.5 MB
conv: (3x3x512) x 512	9 MB	28x28x512	1.5 MB
conv: (3x3x512) x 512	9 MB	28x28x512	1.5 MB
maxpool	—	14x14x512	383 KB
conv: (3x3x512) x 512	9 MB	14x14x512	383 KB
conv: (3x3x512) x 512	9 MB	14x14x512	383 KB
conv: (3x3x512) x 512	9 MB	14x14x512	383 KB
maxpool	—	7x7x512	98 KB
fully-connected 4096	392 MB	4096	16 KB
fully-connected 4096	64 MB	4096	16 KB
fully-connected 1000	15.6 MB	1000	4 KB
soft-max		1000	4 KB

# Reducing network footprint

- Large storage cost for model parameters
  - AlexNet model: ~200 MB
  - VGG-16 model: ~500 MB
  - This doesn't even account for intermediates during evaluation
- Footprint: cumbersome to store, download, etc.
  - 500 MB app downloads make users unhappy!
- Consider energy cost of 1B parameter network
  - Running on input stream at 20 Hz
  - 640 pJ per 32-bit DRAM access
  - $(20 \times 1\text{B} \times 640\text{pJ}) = 12.8\text{W}$  for DRAM access

(more than power budget of any modern smartphone)





# Compressing a network

**Step 1: prune low-weight links (iteratively retrain network, then prune)**

- Over 90% of weights can be removed without significant loss of accuracy
- Store weight matrices in compressed sparse row (CSR) format

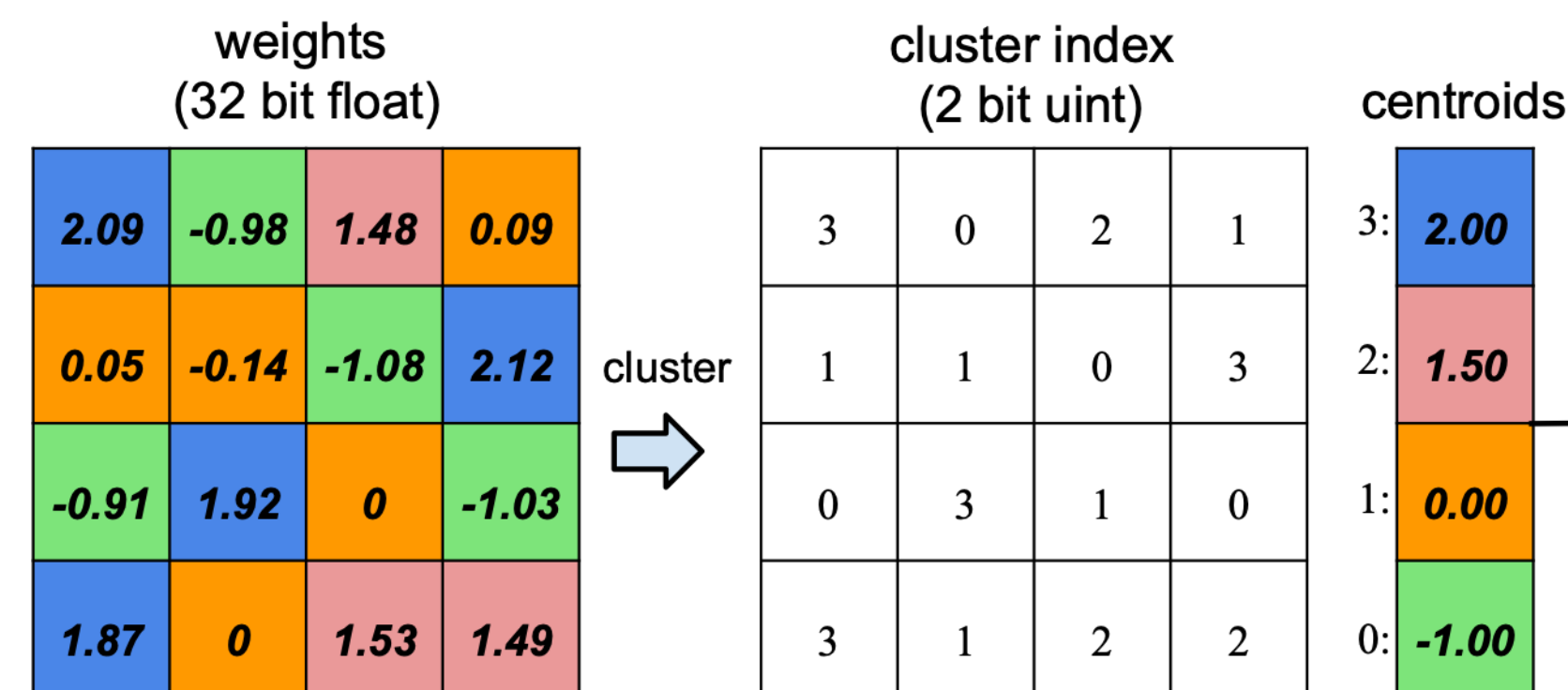
Indicies      1      4      9      ...  
Value      1.8    0.5    2.1

0	1.8	0	0	0.5	0	0	0	0	1.1	...
---	-----	---	---	-----	---	---	---	---	-----	-----

**Step 2: weight sharing: make surviving connects share a small set of weights**

- Cluster weights via k-means clustering (irregular (“learned”) quantization)
- Compress weights by only storing cluster index ( $\lg(k)$  bits)
- Retrain network to improve quality of cluster centroids

**Step 3: Huffman encode quantized weights and CSR indices**



# VGG-16 compression

Substantial savings due to combination of pruning, quantization, Huffman encoding

Layer	#Weights	Weights% (P)	Weigh bits (P+Q)	Weight bits (P+Q+H)	Index bits (P+Q)	Index bits (P+Q+H)	Compress rate (P+Q)	Compress rate (P+Q+H)
conv1_1	2K	58%	8	6.8	5	1.7	40.0%	29.97%
conv1_2	37K	22%	8	6.5	5	2.6	9.8%	6.99%
conv2_1	74K	34%	8	5.6	5	2.4	14.3%	8.91%
conv2_2	148K	36%	8	5.9	5	2.3	14.7%	9.31%
conv3_1	295K	53%	8	4.8	5	1.8	21.7%	11.15%
conv3_2	590K	24%	8	4.6	5	2.9	9.7%	5.67%
conv3_3	590K	42%	8	4.6	5	2.2	17.0%	8.96%
conv4_1	1M	32%	8	4.6	5	2.6	13.1%	7.29%
conv4_2	2M	27%	8	4.2	5	2.9	10.9%	5.93%
conv4_3	2M	34%	8	4.4	5	2.5	14.0%	7.47%
conv5_1	2M	35%	8	4.7	5	2.5	14.3%	8.00%
conv5_2	2M	29%	8	4.6	5	2.7	11.7%	6.52%
conv5_3	2M	36%	8	4.6	5	2.3	14.8%	7.79%
fc6	103M	4%	5	3.6	5	3.5	1.6%	1.10%
fc7	17M	4%	5	4	5	4.3	1.5%	1.25%
fc8	4M	23%	5	4	5	3.4	7.1%	5.24%
Total	138M	7.5%(13×)	6.4	4.1	5	3.1	3.2% (31×)	2.05% (49×)

**P = connection pruning (prune low weight connections)**

**Q = quantize surviving weights (using shared weights)**

**H = Huffman encode**

## ImageNet Image Classification Performance

	Top-1 Error	Top-5 Error	Model size	
VGG-16 Ref	31.50%	11.32%	552 MB	
VGG-16 Compressed	31.17%	10.91%	<b>11.3 MB</b>	<b>49×</b>



# Deep neural networks on GPUs

- **High-performance DNN implementations target GPUs**
  - **High arithmetic intensity computations (computational characteristics similar to dense matrix-matrix multiplication)**
  - **Benefit from flop-rich architectures**
  - **Highly-optimized library of kernels exist for GPUs (cuDNN)**



**Facebook's Big  
Sur**

# Emerging architectures for deep learning

- **NVIDIA Pascal (most recent GPU)**
  - Adds double-throughput 16-bit floating point ops
  - Feature that is already common on mobile GPUs
- **Google TensorFlow Processing Unit**
  - Hardware accelerator for array computations
  - Used in Google data centers
- **Apple Neural Engine**
  - On A11 & A12 processor chips in iPhones & iPads
- **XNOR Networks**
  - Reduce weights & data to single bits
- **FPGAs, ASICs?**
  - Microsoft “BrainWave” on FPGAs within data centers
  - Not new: FPGA solutions have been explored for years
- **...A million startups...**



# Programming frameworks for deep learning

- **Heavyweight processing (low-level kernels) carried out by target-optimized libraries (NVIDIA cuDNN, Intel MKL)**
- **Popular frameworks use these kernel libraries**
  - **Caffe, Torch, Theano, TensorFlow, MxNet**
- **DNN application development = constructing novel network topologies**
  - **Programming by constructing networks**
  - **Significant interest in new ways to express network construction**

# Summary: efficiently evaluating convnets

- **Computational structure**
  - **Convlayers: high arithmetic intensity, significant portion of cost of evaluating a network**
  - **Similar data access patterns to dense-matrix multiplication (exploiting temporal reuse is key)**
  - **But straight reduction to matrix-matrix multiplication is often sub-optimal**
  - **Work-efficient techniques for convolutional layers (FFT-based, Winograd convolutions)**
- **Large numbers of parameters: significant interest in reducing size of networks for both training and evaluation**
  - **Pruning: remove least important network links**
  - **Quantization: low-precision parameter representations often suffice**
- **Many ongoing studies of specialized hardware architectures for efficient evaluation**
  - **Future CPUs/GPUs, ASICs, FPGS, ...**
  - **Specialization will be important to achieving “always on” applications**



# Two Distinct Issues with Deep Networks

- **Evaluation/Inference**
  - often takes milliseconds
- **Training**
  - often takes hours, days, weeks

# **“Training a network”**

- **Training a network is the process of learning the value of network parameters so that output of the network provides the desired result for a task**
  - **[Krizhevsky12] task = object classification**
    - **input 224 x 224 x 3 RGB image**
    - **output probability of 1000 ImageNet object classes: “dog”, “cat”, etc...**
    - **~ 60M weights**

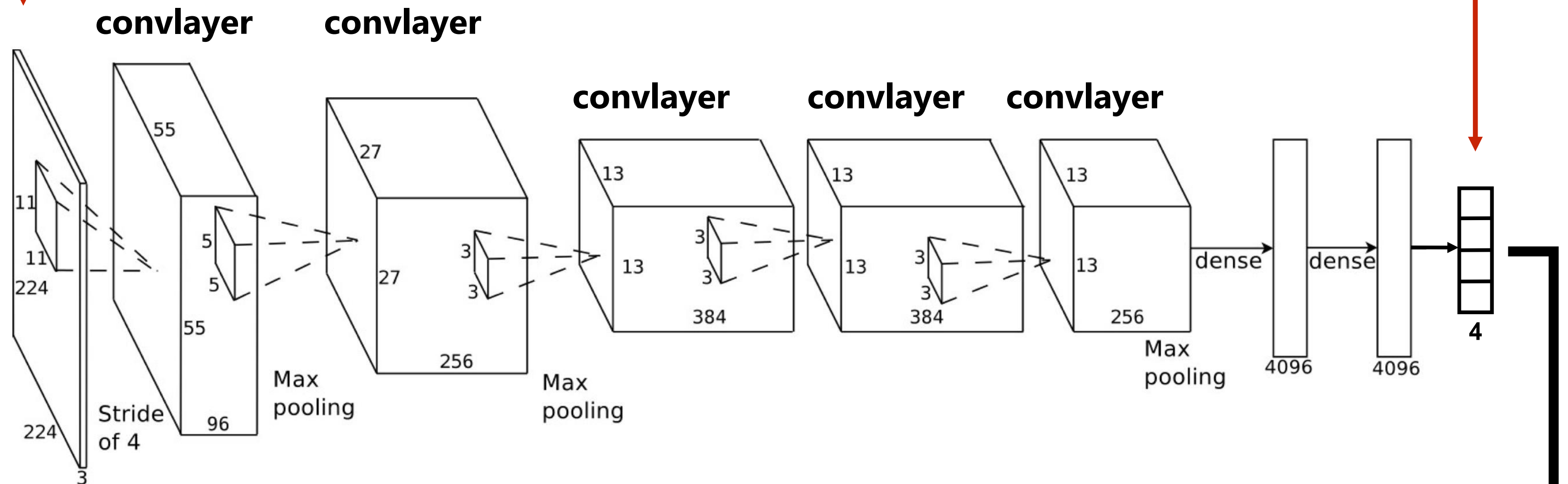


# Professor classification network

Classifies professors as easy, mean, boring, or nerdy based on their appearance.

Input:  
image of a  
professor

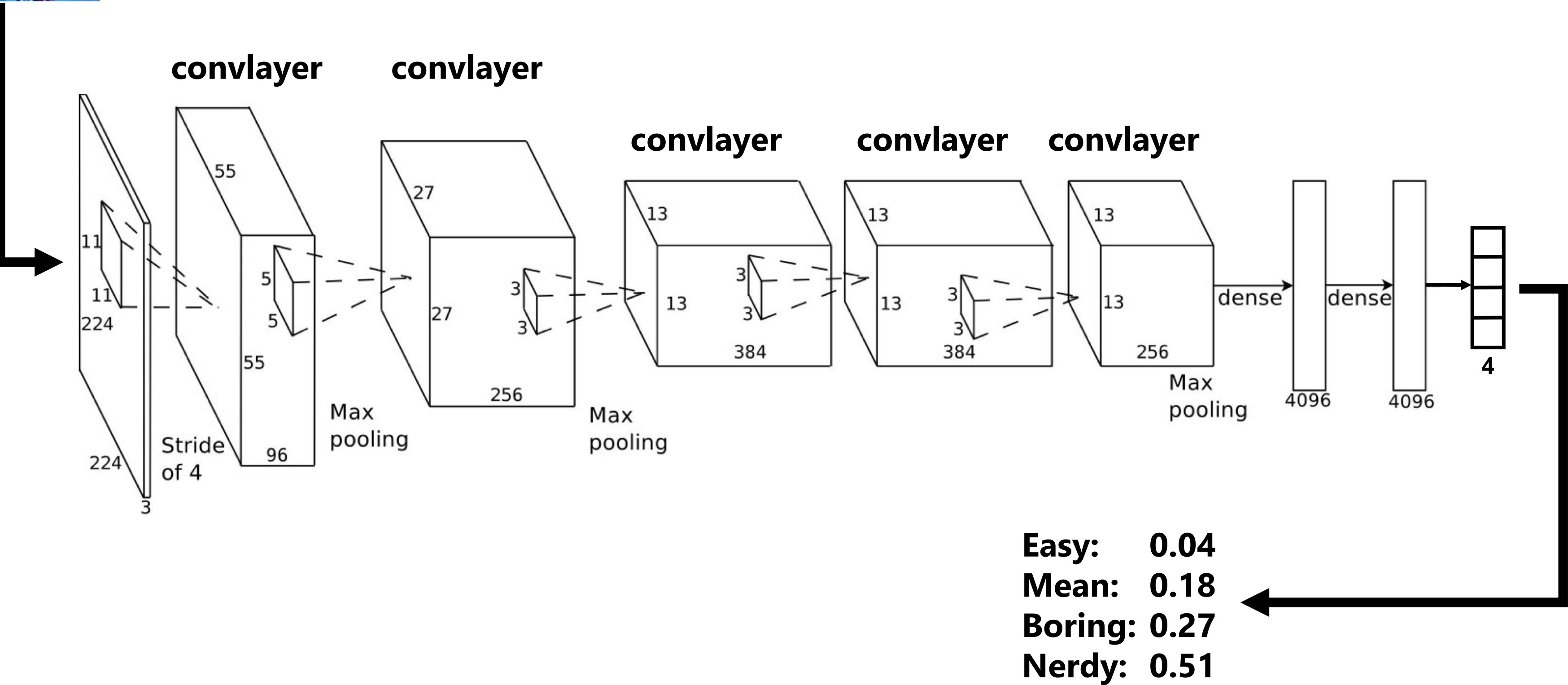
Output:  
probability of  
label



Recall from last time:  
10's-100's of millions of  
parameters

Easy: ??  
Mean: ??  
Boring: ??  
Nerdy: ??

# Professor classification network





**Where did the parameters come from?**



# Training data (ground truth answers)



[label  
omitted]



[label  
omitted]



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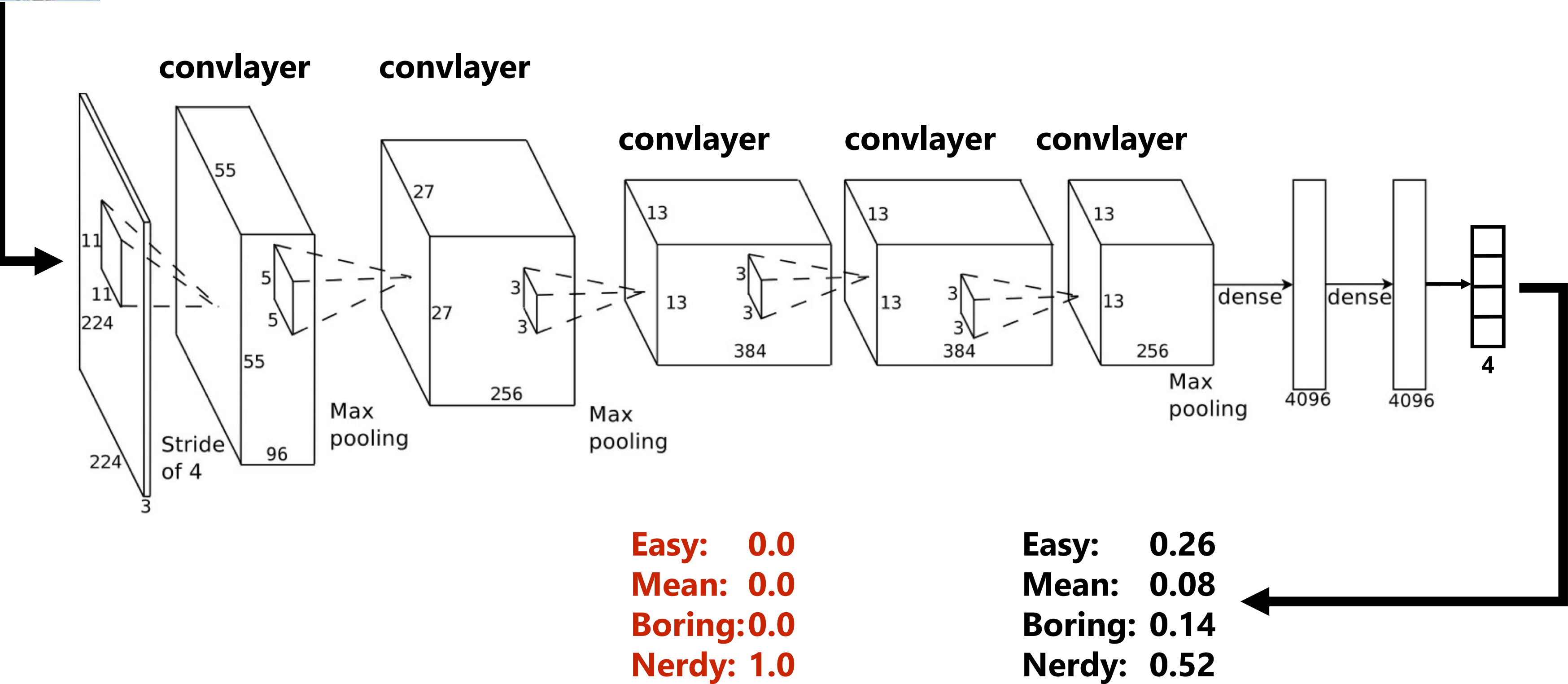


[label  
omitted]



# Professor classification network

New image of Bryant  
(not in training set)



Ground truth  
(what the answer should be)

Network output

# Error (loss)

**Ground truth:**  
**(what the answer should be)**

**Easy: 0.0**

**Mean: 0.0**

**Boring: 0.0**

**Nerdy: 1.0**

**Network output: \***

**Easy: 0.26**

**Mean: 0.08**

**Boring: 0.14**

**Nerdy: 0.52**

**Common example:**  
**softmax loss:**

$$L = -\log \left( \frac{e^{f_c}}{\sum_j e^{f_j}} \right)$$

Output of network for correct category

Output of network for all categories

\* In practice a network using a softmax classifier outputs unnormalized, log probabilities ( $f_j$ ), but I'm showing a probability distribution above for clarity



# Training

**Goal of training: learning good values of network parameters so that network outputs the correct classification result for any input image**

**Idea: minimize loss for all the training examples (for which the correct answer is known)**

$$L = \sum_i L_i \quad \text{(total loss for entire training set is sum of losses } L_i \text{ for each training example } x_i)$$

**Intuition: if the network gets the answer correct for a wide range of training examples, then hopefully it has learned parameter values that yield the correct answer for future images as well.**

# Intuition: gradient descent

Say you had a function  $f$  that contained a hidden parameters  $f(x_i)$   $p_1$  and  $p_2$ :

And for some input  $x_i$ , your training data says the function should output 0.

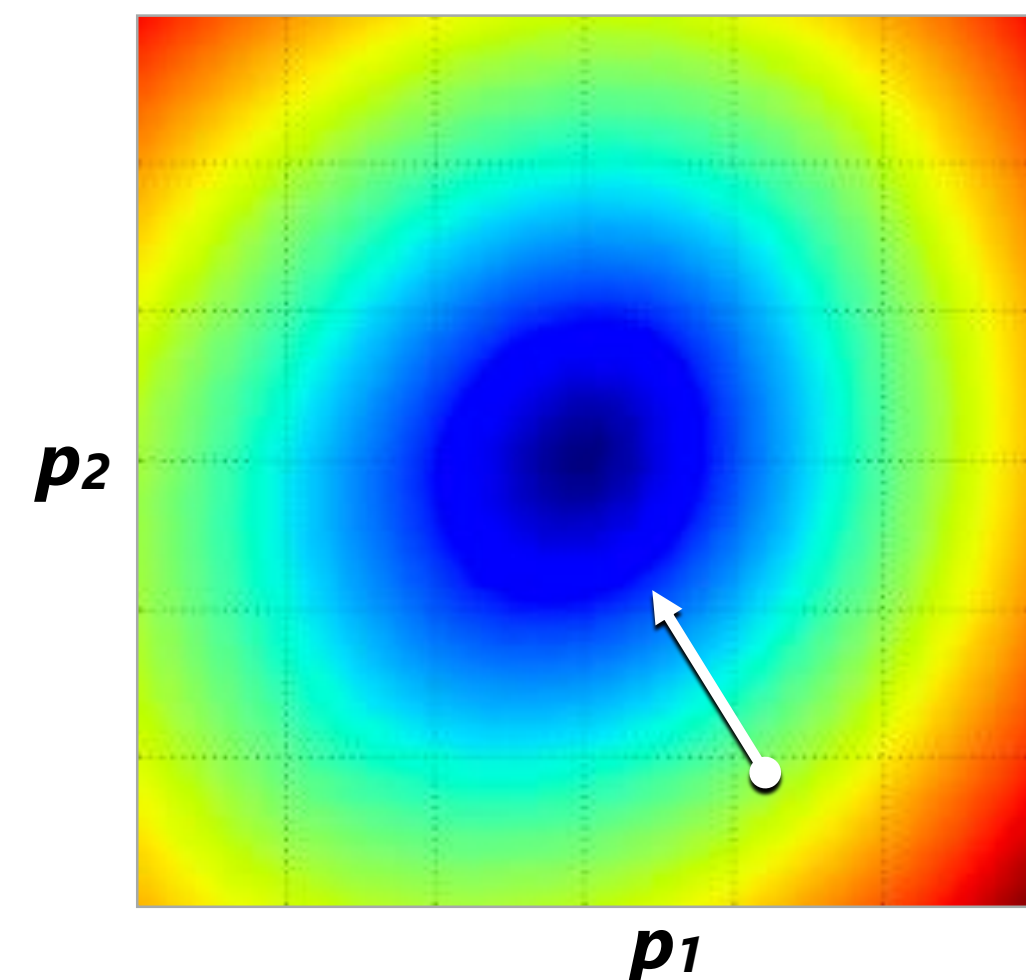
But for the current values of  $p_1$  and  $p_2$ , it currently outputs 10.

$$f(x_i, p_1, p_2) = 10$$

And say I also gave you expressions for the derivative of  $f$  with respect to  $p_1$  and  $p_2$  so you could compute their value at  $x_i$ .

$$\frac{df}{dp_1} = 2 \quad \frac{df}{dp_2} = -5 \quad \nabla f = [2, -5]$$

red = high values of  $f$   
blue = low values



How might you adjust the values  $p_1$  and  $p_2$  to reduce the error for this training example?

# Basic gradient descent

```
while (loss too high):  
    for each item x_i in training set:  
        grad += evaluate_loss_gradient(f, loss_func, params, x_i)  
  
    params += -grad * step_size;
```

**Mini-batch stochastic gradient descent (mini-batch SGD): choose a random (small) subset of the training examples to compute gradient in each iteration of the while loop**

**How to compute  $df/dp$  for a complex neural network with millions of parameters?**



# Derivatives using the chain rule

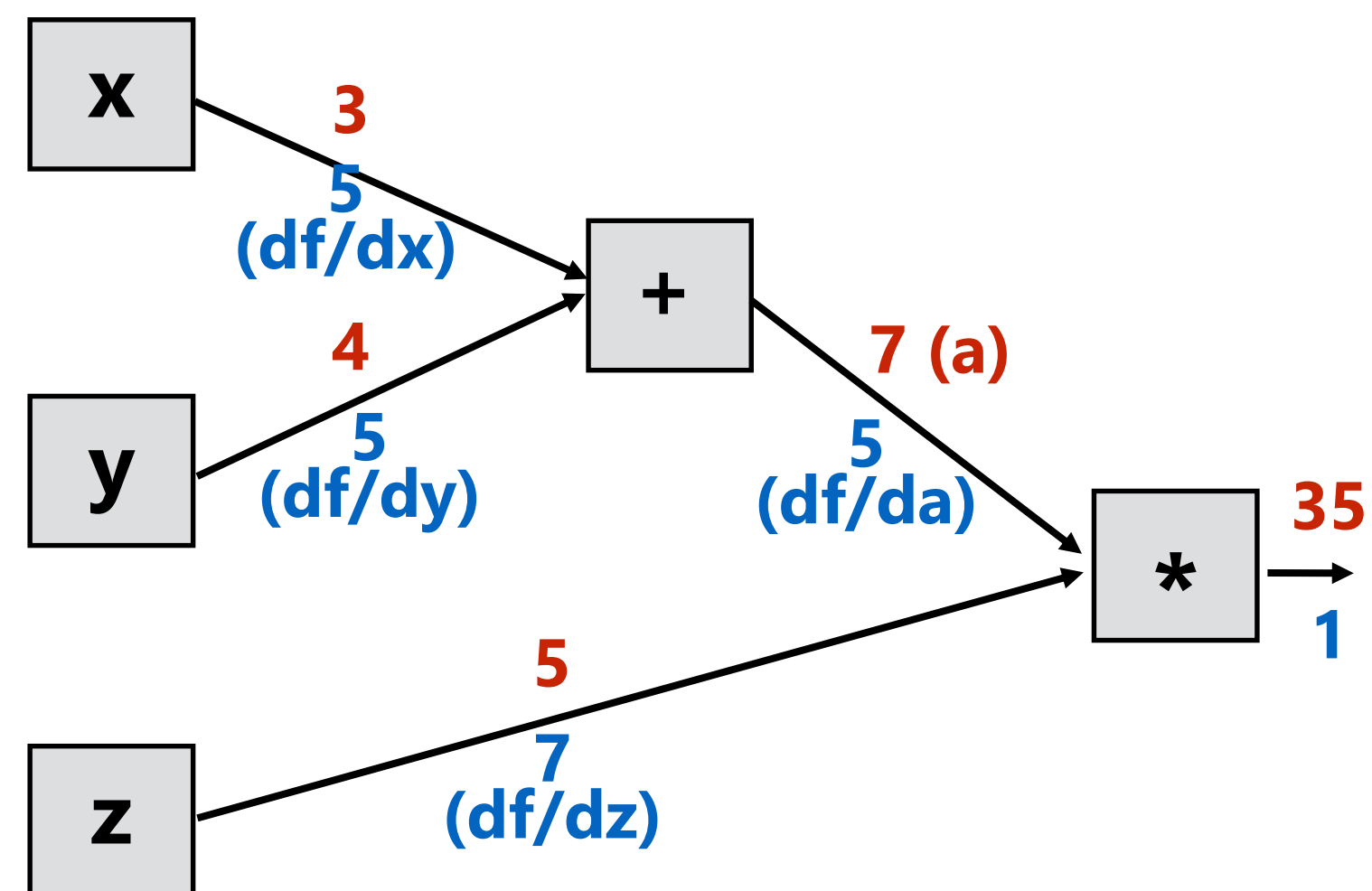
$$f(x, y, z) = (x + y)z = az$$

**Where:**  $a = x + y$

$$\frac{df}{da} = z \quad \frac{da}{dx} = 1 \quad \frac{da}{dy} = 1$$

**So, by the derivative chain rule:**

$$\frac{df}{dx} = \frac{df}{da} \frac{da}{dx} = z$$



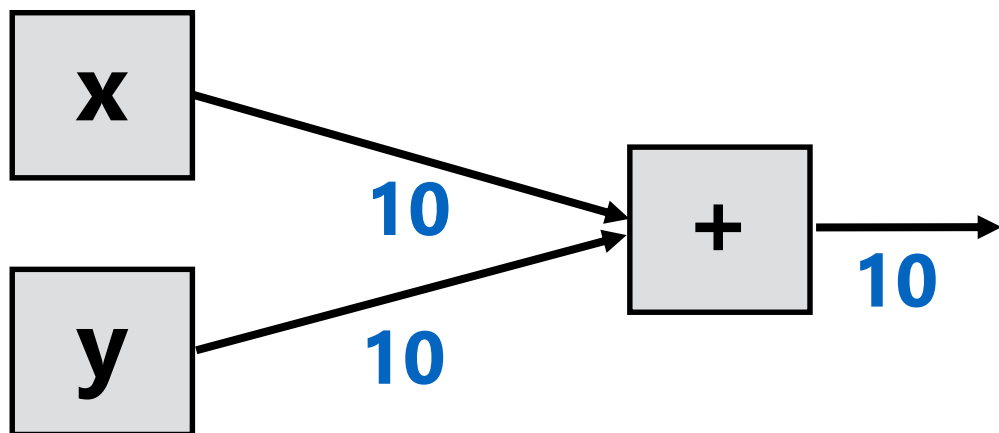
**Red = output of node**

**Blue = df/dnode**

# Backpropagation

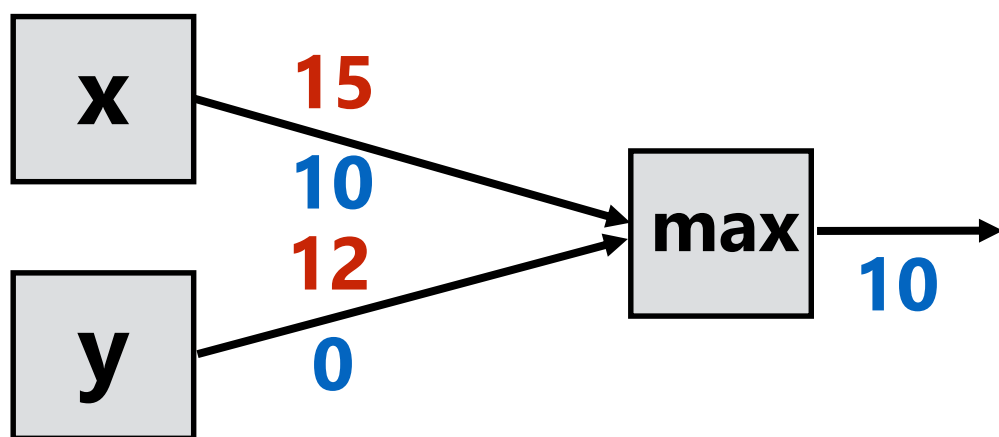
Red = output of node  
Blue = df/dnode

Recall:  $\frac{df}{dx} = \frac{df}{dg} \frac{dg}{dx}$



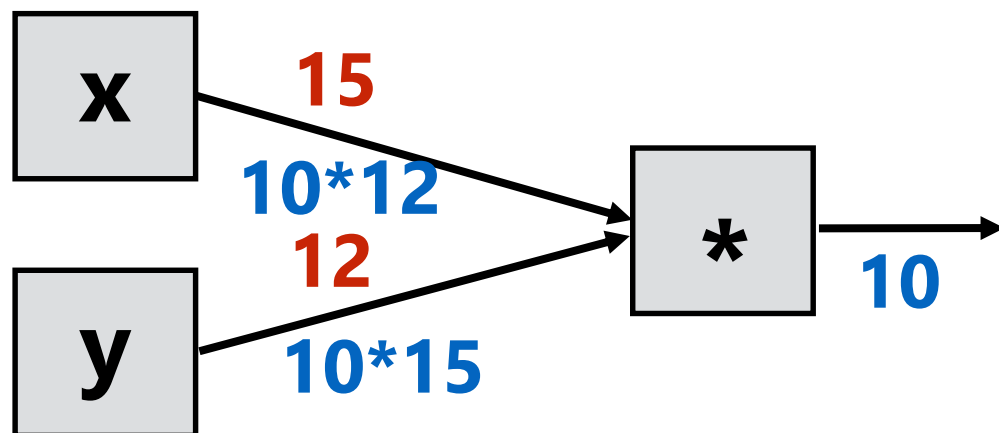
$$g(x, y) = x + y$$

$$\frac{dg}{dx} = 1, \frac{dg}{dy} = 1$$



$$g(x, y) = \max(x, y)$$

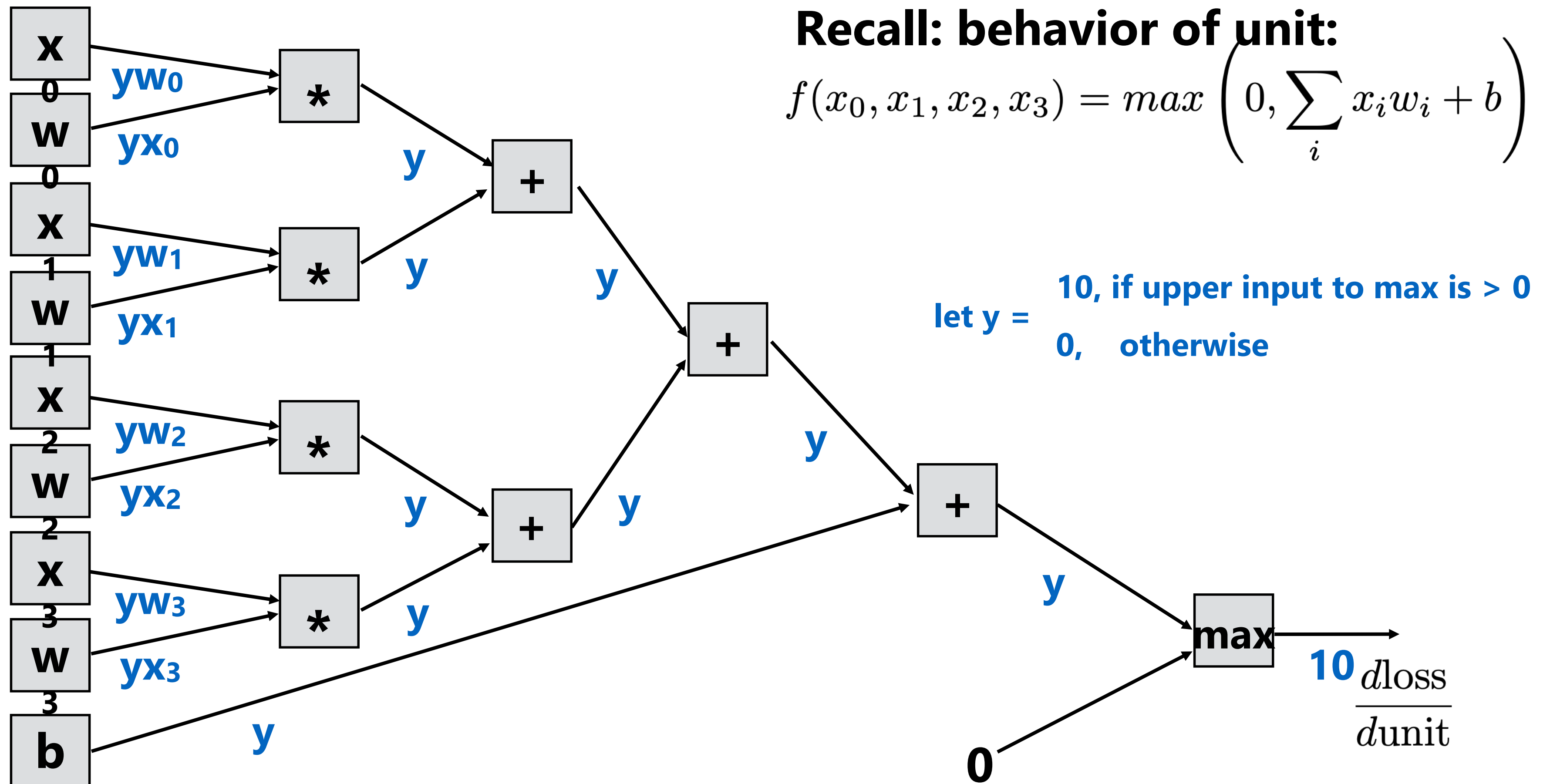
$$\frac{dg}{dx} = \begin{cases} 1, & \text{if } x > y \\ 0, & \text{otherwise} \end{cases}$$



$$g(x, y) = xy$$

$$\frac{dg}{dx} = y, \frac{dg}{dy} = x$$

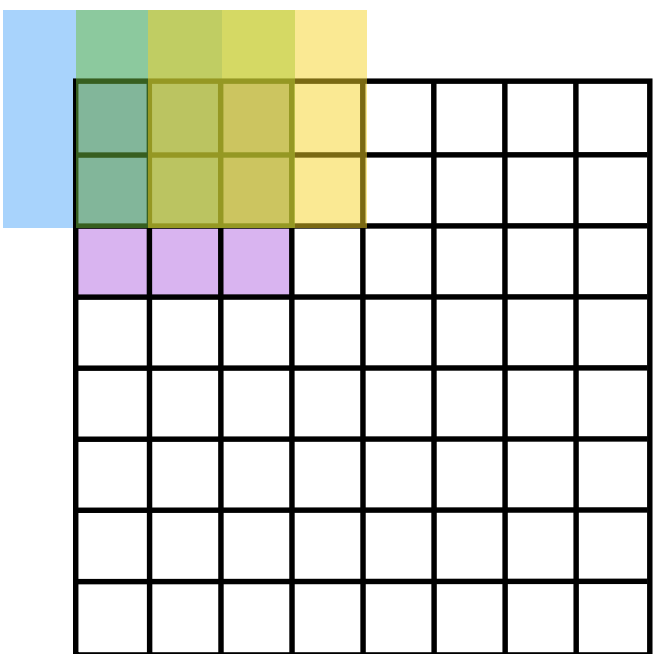
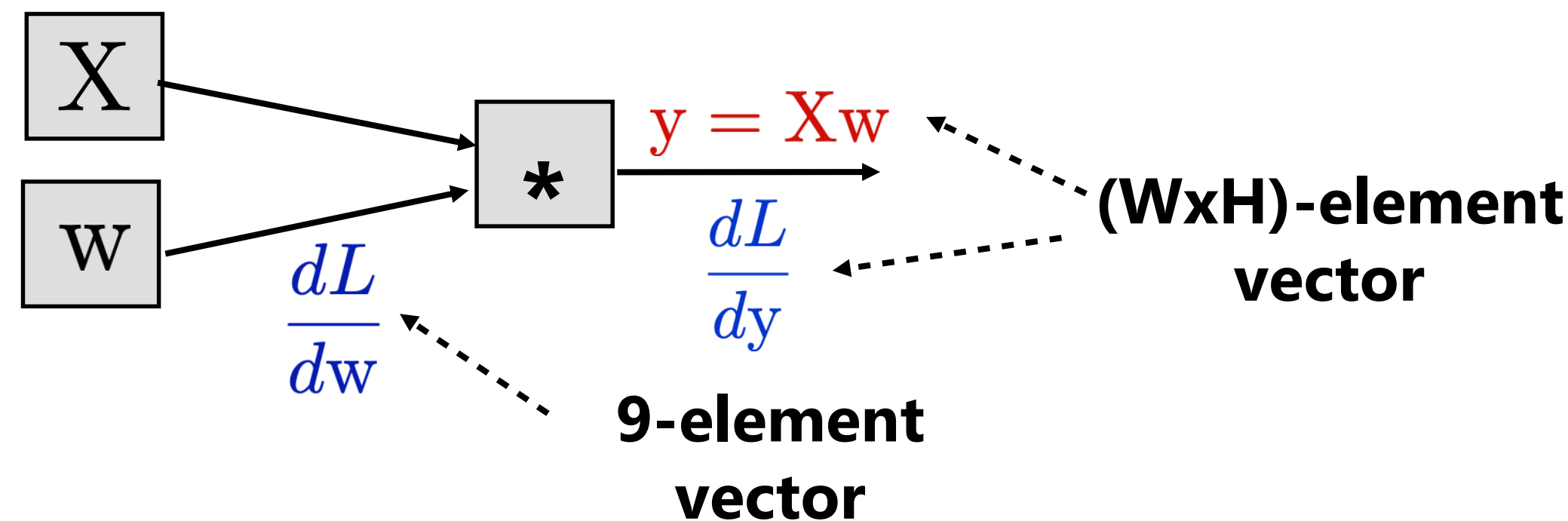
# Backpropagating through single unit



Observe: output of prior layer ( $x_i$ 's) and output of this unit must be retained in order to compute weight gradients for this unit during backprop.



# Backpropagation: matrix form



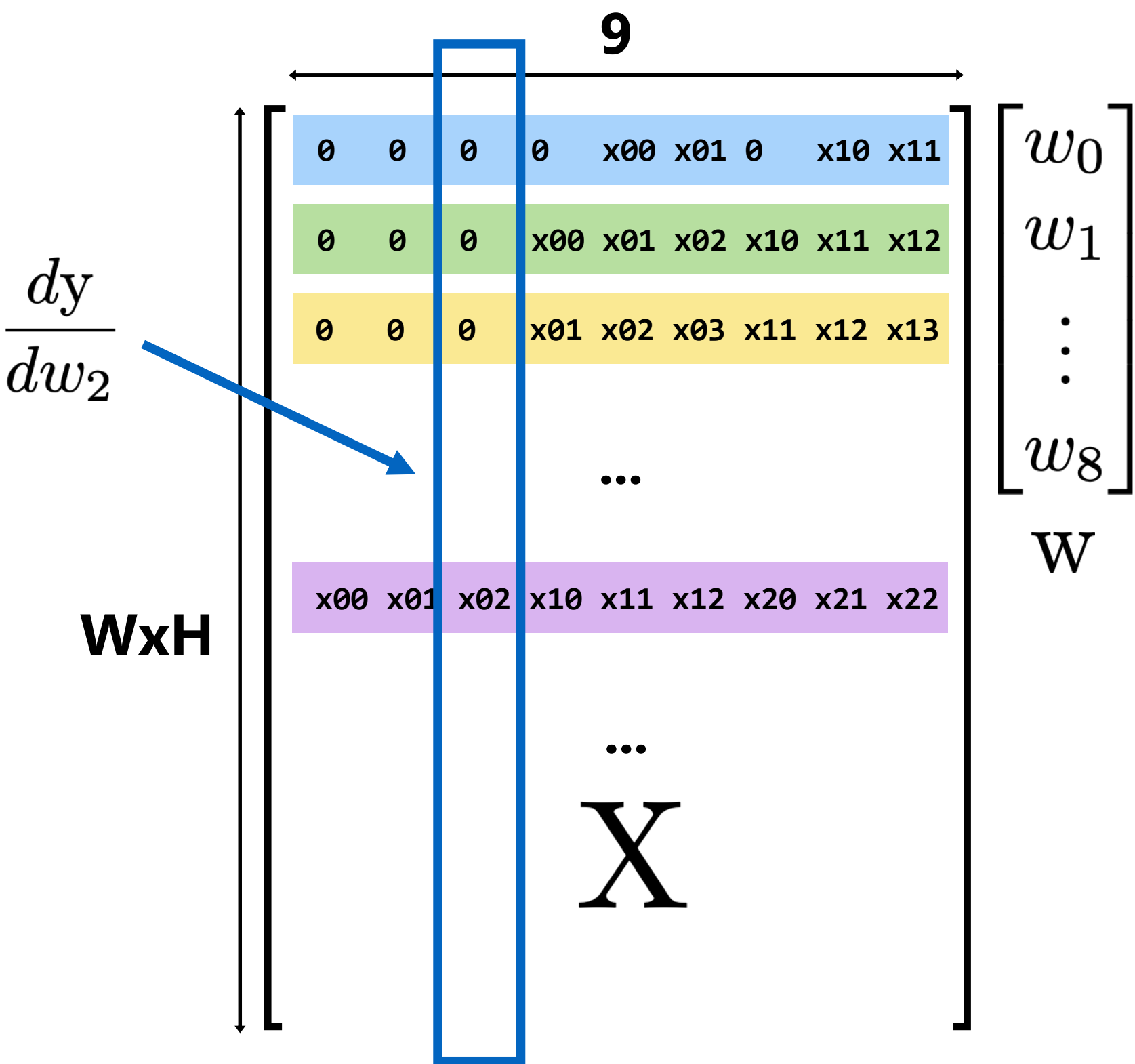
$$\frac{dy_j}{dw_i} = X_{ji}$$

$$\frac{dL}{dw_i} = \sum_j \frac{dL}{dy_j} \frac{dy_j}{dw_i}$$

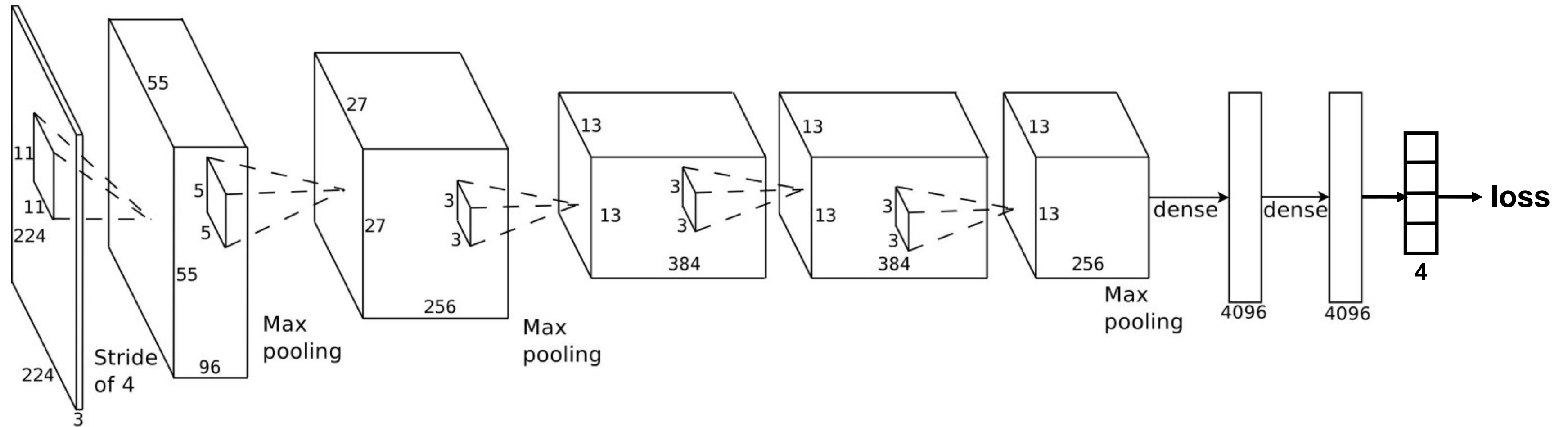
$$= \sum_j \frac{dL}{dy_j} X_{ji}$$

Therefore:

$$\frac{dL}{dw} = X^T \frac{dL}{dy}$$



# Backpropagation through the entire professor classification network



**For each training example  $x_i$  in mini-batch:**

**Perform forward evaluation to compute loss for  $x_i$**

**Note: must retain all layer outputs + output gradients (needed to compute weight gradients during backpropagation)**

**Compute gradient of loss w.r.t. final layer's outputs**

**Backpropagate gradient to compute gradient of loss w.r.t. all network parameters**

**Accumulate gradients (over all images in batch)**

**Update all parameter values:  $w_{i\_new} = w_{i\_old} - \text{step\_size} * \text{grad}_i$**

# VGG memory footprint

Calculations assume 32-bit values (image batch size = 1)

inputs/outputs  
get multiplied  
by mini- batch  
size

Unlike forward  
evaluation:

1. must store outputs and gradient of outputs
2. cannot immediately free outputs once consumed by next level of network

	weights mem:	output size (per image)	(mem)
input: 224 x 224 RGB image	—	224x224x3	150K
conv: (3x3x3) x 64	6.5 KB	224x224x64	12.3 MB
conv: (3x3x64) x 64	144 KB	224x224x64	12.3 MB
maxpool	—	112x112x64	3.1 MB
conv: (3x3x64) x 128	228 KB	112x112x128	6.2 MB
conv: (3x3x128) x 128	576 KB	112x112x128	6.2 MB
maxpool	—	56x56x128	1.5 MB
conv: (3x3x128) x 256	1.1 MB	56x56x256	3.1 MB
conv: (3x3x256) x 256	2.3 MB	56x56x256	3.1 MB
conv: (3x3x256) x 256	2.3 MB	56x56x256	3.1 MB
maxpool	—	28x28x256	766 KB
conv: (3x3x256) x 512	4.5 MB	28x28x512	1.5 MB
conv: (3x3x512) x 512	9 MB	28x28x512	1.5 MB
conv: (3x3x512) x 512	9 MB	28x28x512	1.5 MB
maxpool	—	14x14x512	383 KB
conv: (3x3x512) x 512	9 MB	14x14x512	383 KB
conv: (3x3x512) x 512	9 MB	14x14x512	383 KB
conv: (3x3x512) x 512	9 MB	14x14x512	383 KB
maxpool	—	7x7x512	98 KB
fully-connected 4096	392 MB	4096	16 KB
fully-connected 4096	64 MB	4096	16 KB
fully-connected 1000	15.6 MB	1000	4 KB
soft-max		1000	4 KB

Must also store  
per-weight  
gradients

Many  
implementations  
also store  
gradient  
"momentum" as  
well  
(multiply by 3)



# SGD workload

`while (loss too high):` ← **At first glance, this loop is sequential (each step of “walking downhill” depends on previous)**

`for each item  $x_i$  in mini-batch:` ← **Parallel across images**  
`grad += evaluate_loss_gradient(f, loss_func, params,  $x_i$ )`  
↑ **sum reduction**      ↙ **large computation with its own parallelism (but working set may not fit on single machine)**

`params += -grad * step_size;`  
↙ **trivial data-parallel over parameters**

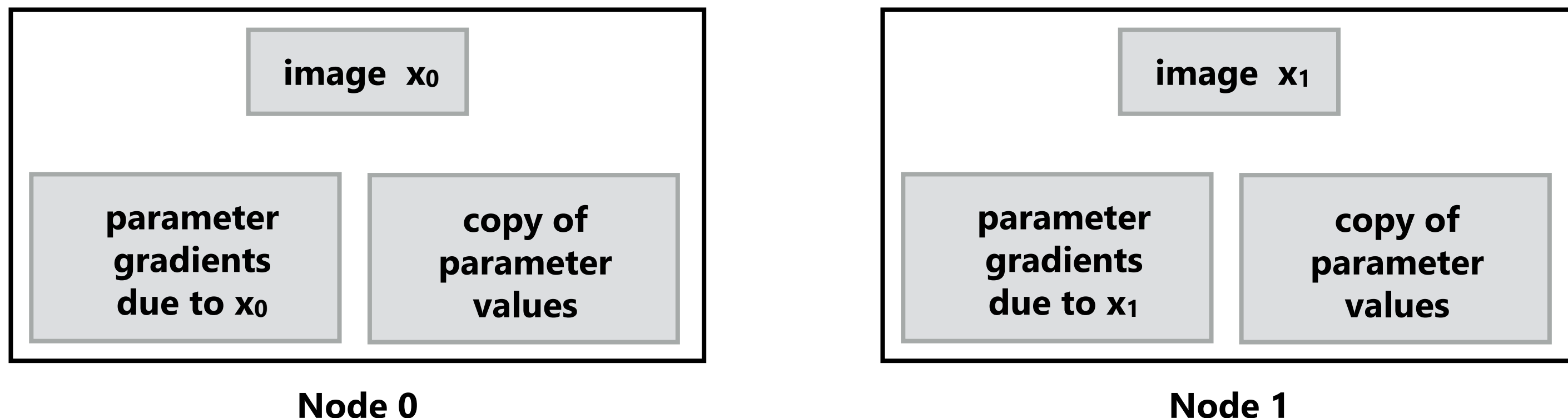
# Deep network training workload

- **Huge computational expense**
  - Must evaluate the network (forward and backward) for millions of training images
  - Must iterate for many iterations of gradient descent (100's of thousands)
  - Training modern networks takes days
- **Large memory footprint**
  - Must maintain network layer outputs from forward pass
  - Additional memory to store gradients for each parameter
  - Recall parameters for popular VGG-16 network require ~500 MB of memory (training requires GBs of memory for academic networks)
  - Scaling to larger networks requires partitioning network across nodes to keep network + intermediates in memory
- **Dependencies /synchronization (not embarrassingly parallel)**
  - Each parameter update step depends on previous
  - Many units contribute to same parameter gradients (fine-scale reduction)
  - Different images in mini batch contribute to same parameter gradients

# Data-parallel training (across images)

```
for each item  $x_i$  in mini-batch:  
    grad += evaluate_loss_gradient(f, loss_func, params,  $x_i$ )  
params += -grad * step_size;
```

Consider parallelization of the outer for loop across machines in a cluster



partition mini-batch across nodes

for each item  $x_i$  in mini-batch assigned to local node:

*// just like single node training*

```
grad += evaluate_loss_gradient(f, loss_func, params,  $x_i$ )
```

```
barrier();
```

sum reduce gradients, communicate results to all nodes

```
barrier();
```

update copy of parameter values



# Challenges of computing at cluster scale

- **Slow communication between nodes**
  - **Clusters do not feature high-performance interconnects typical of supercomputers**
- **Nodes with different performance (even if machines are the same)**
  - **Workload imbalance at barriers (sync points between nodes)**

**Modern solution: exploit characteristics of SGD using asynchronous execution!**

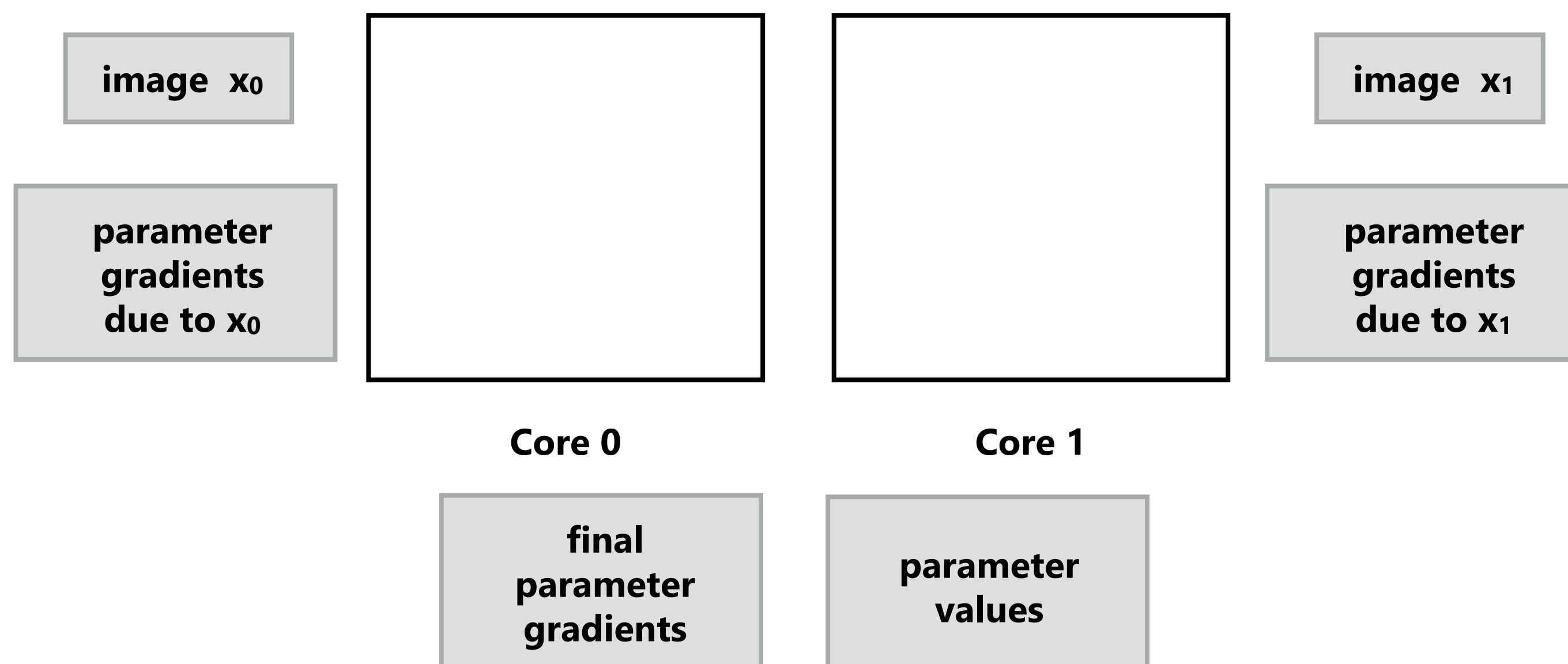
# Exploiting SGD Characteristics

- **Convergent computation**
  - **Update ordering does not matter**
  - **OK to have small errors in weight updates**
- **How used**
  - **Within machine: Don't synchronize weight updates across threads**
  - **Between machines:**
    - **OK to do some computations using stale data**
    - **Ordering of updates not critical**
    - **Incomplete or redundant coverage of data set acceptable**

# Parallelizing mini-batch on one machine

```
for each item  $x_i$  in mini-batch:  
    grad += evaluate_loss_gradient(f, loss_func, params,  $x_i$ )  
params += -grad * step_size;
```

**Consider parallelization of the outer for  
loop across cores**



**Good: completely independent computations (until gradient reduction)**

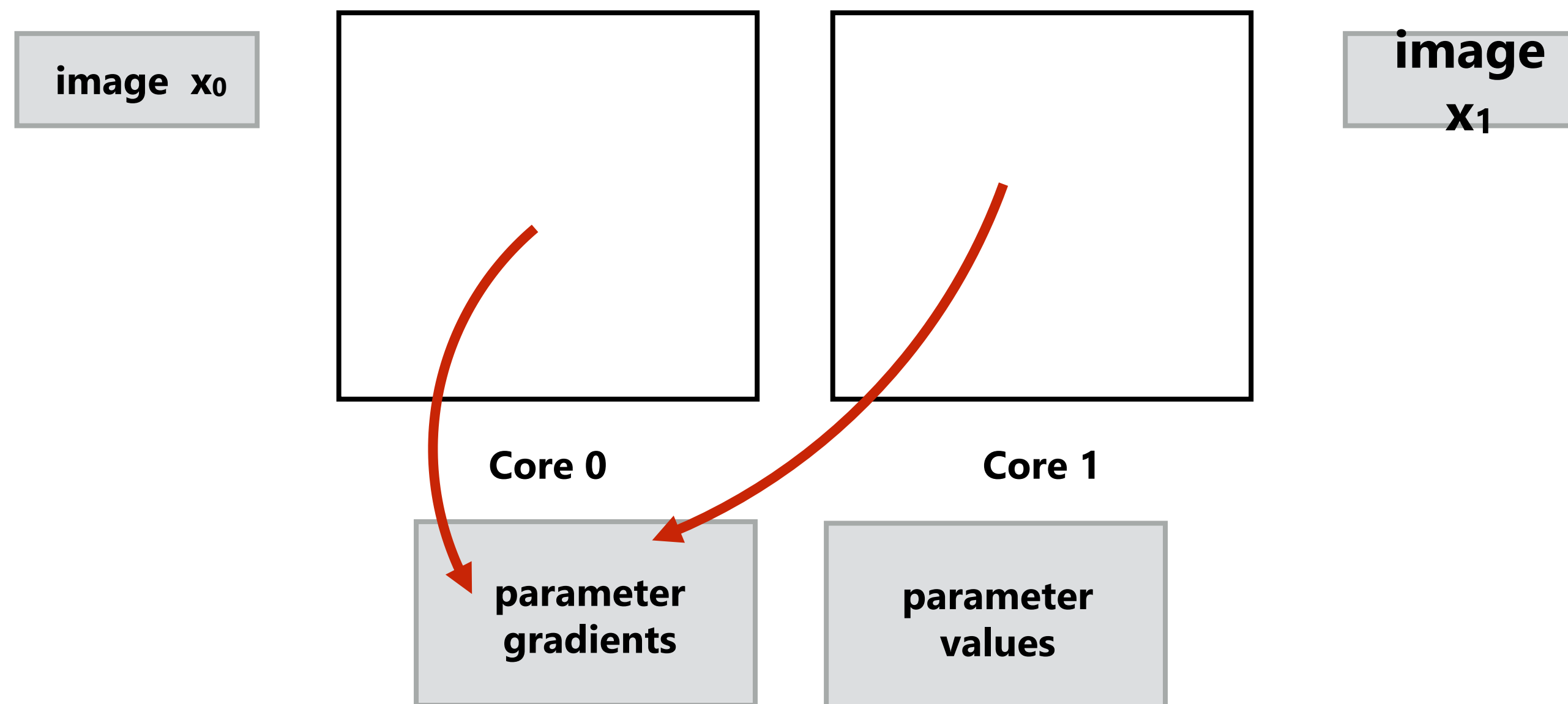
**Bad: complete duplication of parameter gradient state (100's MB per core)**



# Asynchronous update on one node

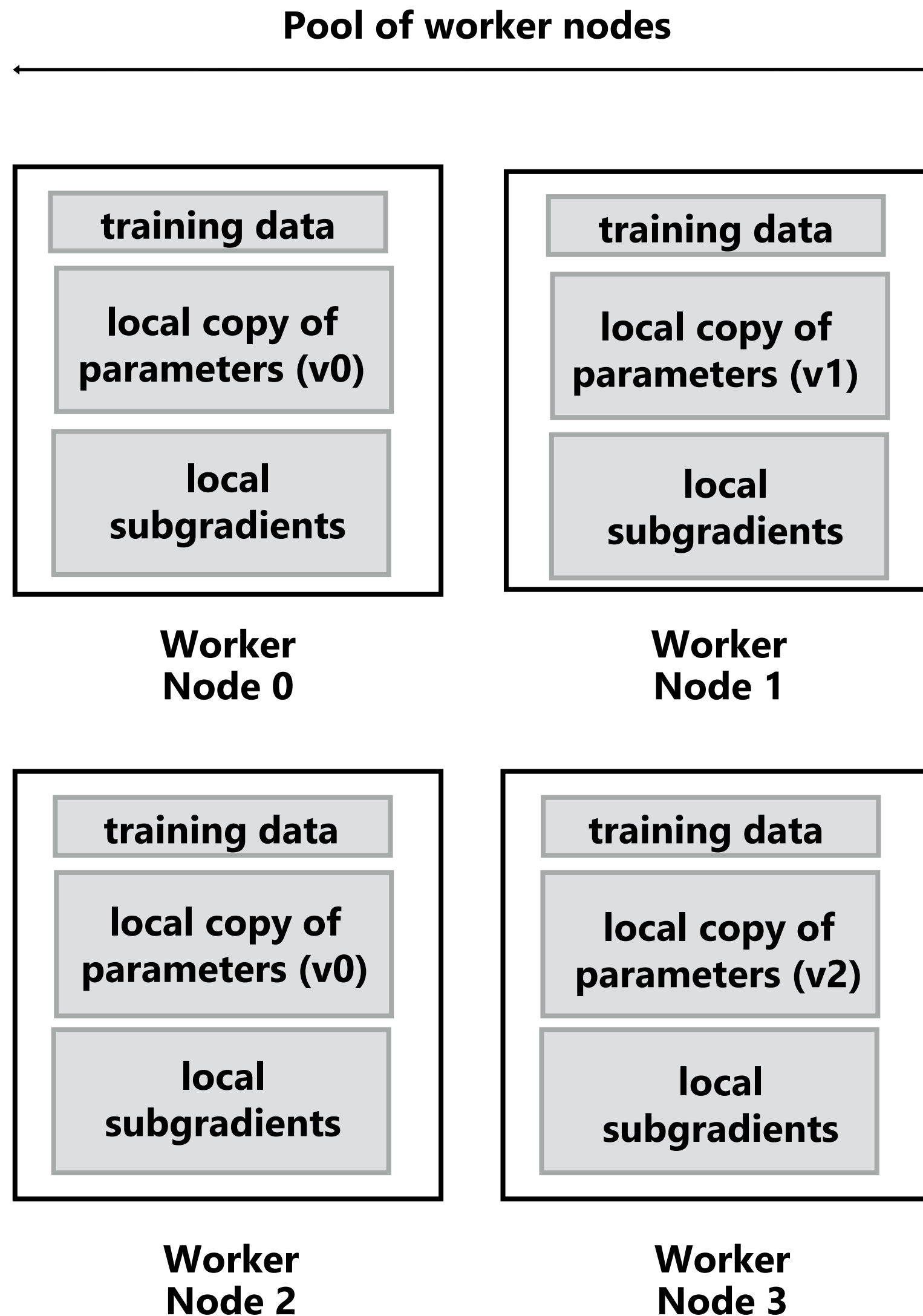
```
for each item  $x_i$  in mini-batch:  
    grad += evaluate_loss_gradient(f, loss_func, params,  $x_i$ )  
params += -grad * step_size;
```

**Cores update shared set of gradients.**  
**Skip taking locks / synchronizing across cores: perform**  
**“approximate reduction”**



# Parameter server design

Parameter Server [Li OSDI14]  
Google's DistBelief [Dean NIPS12]  
Microsoft's Project Adam [Chilimbi OSDI14]



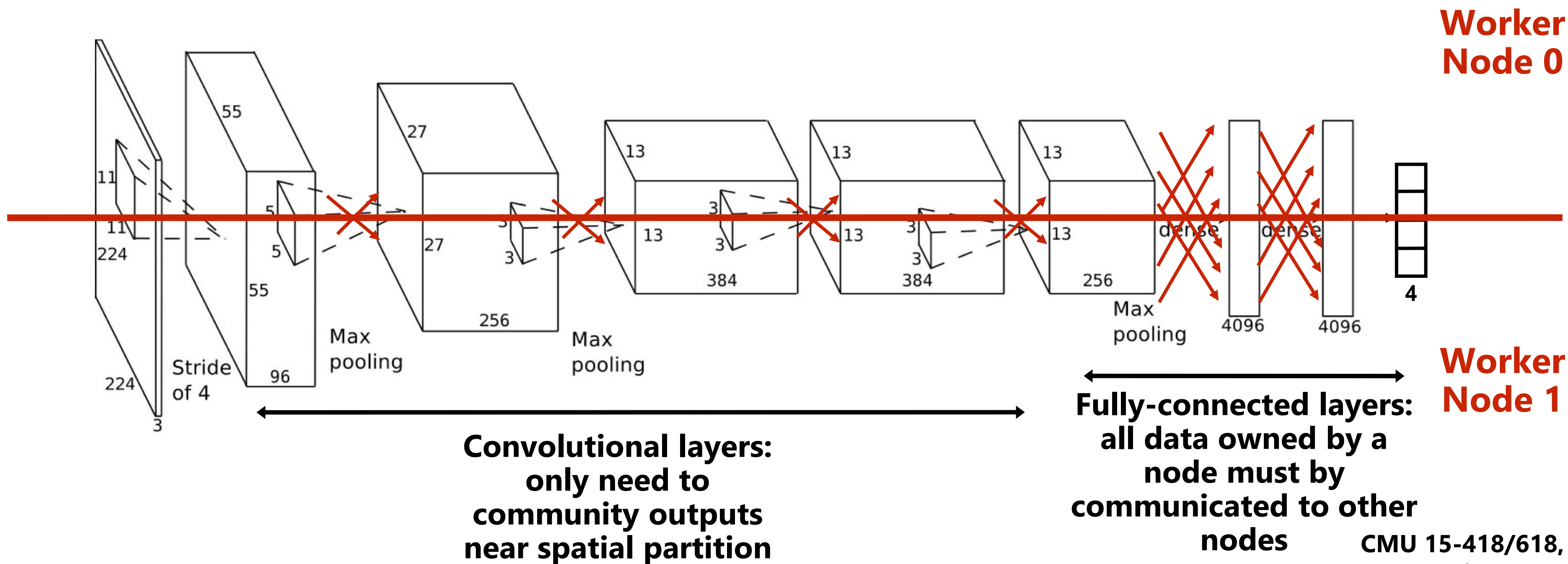
- **Separate set of machines to maintain DNN parameters**
- **Highly fault tolerant (so that worker nodes need not be reliable)**
- **Accept updates from workers asynchronously**

# Model parallelism

Partition network parameters across nodes  
(spatial partitioning to reduce communication)

Reduce internode communication through network design:

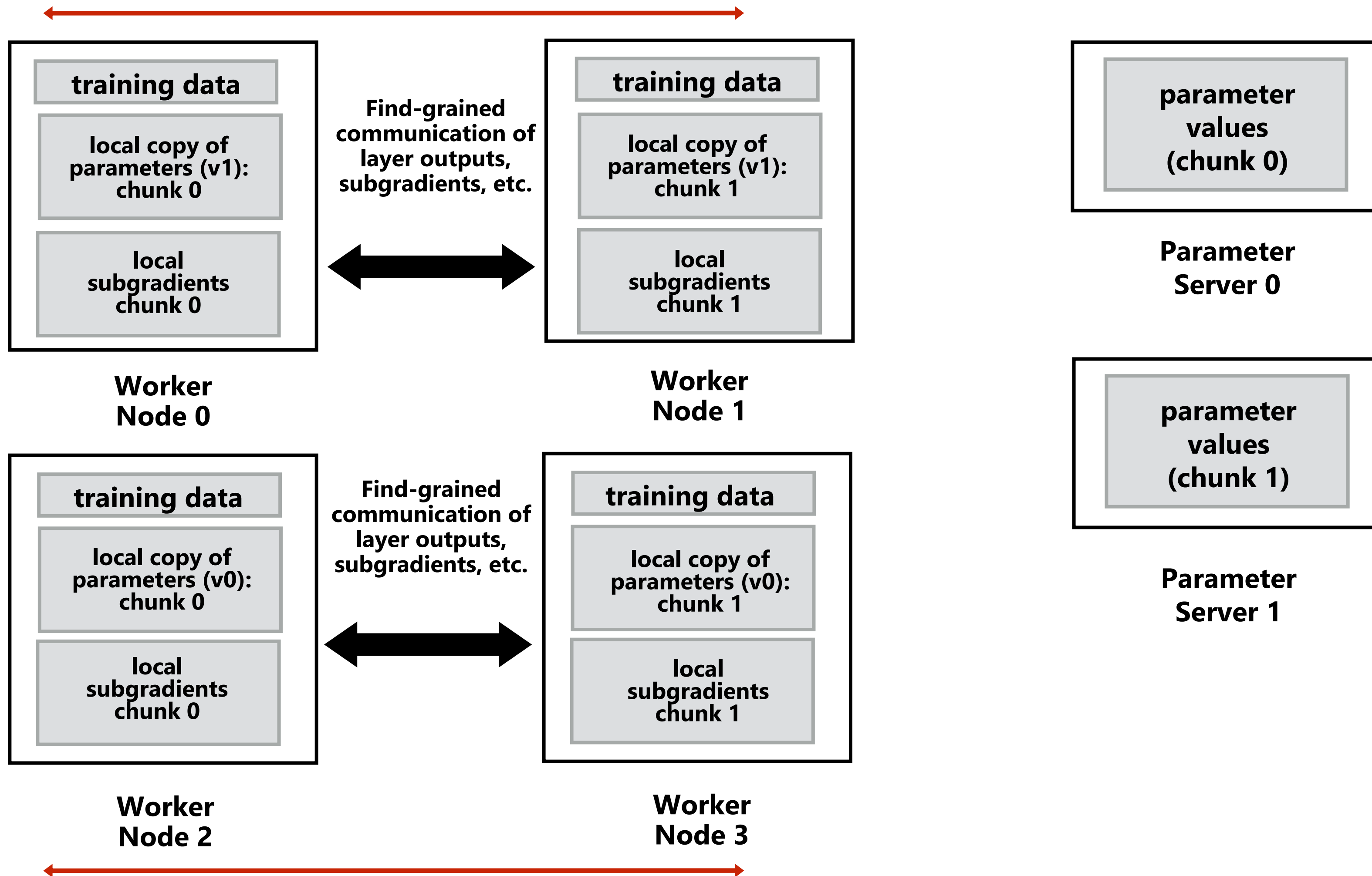
- Use small spatial convolutions (1x1 convolutions)
- Reduce/shrink fully-connected layers





# Training data-parallel and model-parallel execution

Working on subgradient computation for a single copy of the model



Working on subgradient computation for a single copy of the model



# Using supercomputers for training?

- Fast interconnects critical for model-parallel training
  - Fine-grained communication of outputs and gradients
- Fast interconnect diminishes need for async training algorithms
  - Avoid randomness in training due to computation schedule (there remains randomness due to SGD algorithm)



**OakRidge Titan  
Supercomputer**



**NVIDIA DGX-1: 8 Pascal GPUs  
connected via high speed  
NV-Link interconnect**



# Summary: training large networks in parallel

- Most systems rely on asynchronous update to efficiently used clusters of commodity machines
  - Modification of SGD algorithm to meet constraints of modern parallel systems
  - Open question: effects on convergence are problem dependent and not particularly well understood
  - Tighter integration / faster interconnects may provide alternative to these methods (facilitate tightly orchestrated solutions much like supercomputing applications)
- Open question: how big of networks are needed?
  - >90% of connections could be removed without significant impact on quality of network
  - **High-performance training of deep networks is an interesting example of constant iteration of algorithm design and parallelization strategy**

**(a key theme of this course! recall the original grid solver example!)**