# **LEC005** Demand Forecasting

#### VG441 SS2020

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#### F0 = Initial Model = Taking the mean

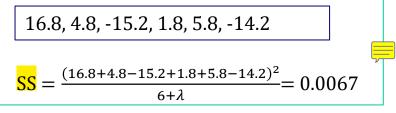
Height (m)	Favorite Color	Gender	Weight (kg)
1.6	Blue	Male	88
1.6	Green	Female	76
1.5	Blue	Female	56
1.8	Red	Male	73
1.5	Green	Male	77
1.4	Blue	Female	57

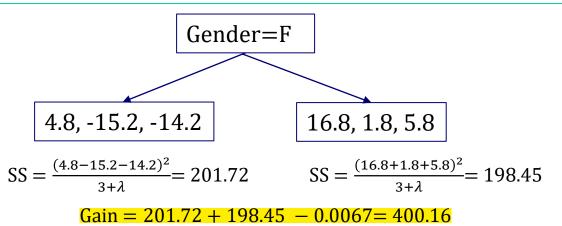


Height (m)	Favorite Color	Gender	Weight (kg)	F0	PR0
1.6	Blue	Male	88	71.2	16.8
1.6	Green	Female	76	71.2	4.8
1.5	Blue	Female	56	71.2	-15.2
1.8	Red	Male	73	71.2	1.8
1.5	Green	Male	77	71.2	5.8
1.4	Blue	Female	57	71.2	-14.2

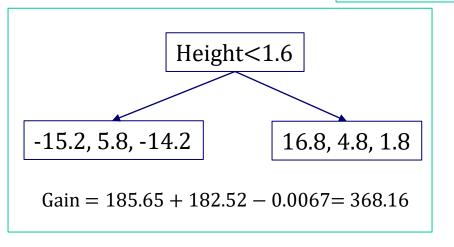
Pseudo Residual (PR) = True Value - Predicted Value

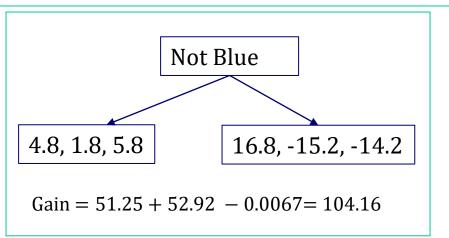
Height (m)	Favorite Color	Gender	PR0
1.6	Blue	Male	16.8
1.6	Green	Female	4.8
1.5	Blue	Female	-15.2
1.8	Red	Male	1.8
1.5	Green	Male	5.8
1.4	Blue	Female	-14.2



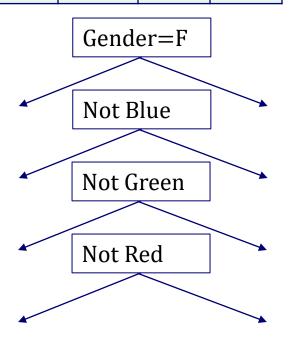


Regularization term  $\lambda = 0$ 

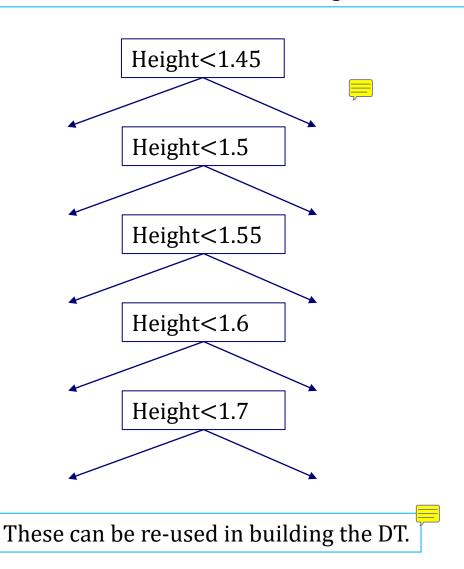




Height (m)	Favorite Color	Gender	PR0
1.6	Blue	Male	16.8
1.6	Green	Female	4.8
1.5	Blue	Female	-15.2
1.8	Red	Male	1.8
1.5	Green	Male	5.8
1.4	Blue	Female	-14.2

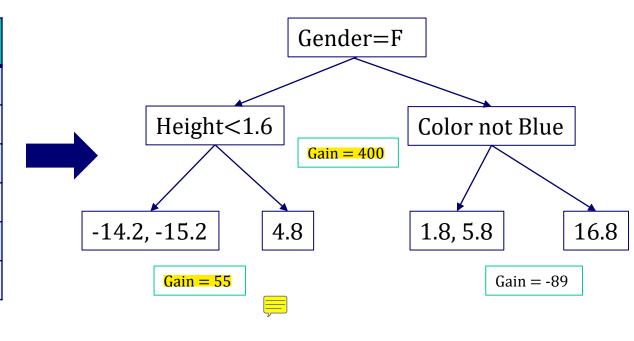


If numerical, sort and take average between adjacent



#### Fit PR0 into an XGBoost tree (up to four leaves)

Height (m)	Favorite Color	Gender	PR0
1.6	Blue	Male	16.8
1.6	Green	Female	4.8
1.5	Blue	Female	-15.2
1.8	Red	Male	1.8
1.5	Green	Male	5.8
1.4	Blue	Female	-14.2



- 1) Pruning
- 2) Regularization

# Pruning Term $\gamma$

If the gain  $< \gamma$ , then we prune the tree!



The tree could be pruned even if we set  $\gamma = 0$ .

# Regularization Term $\lambda$

If the regularization term grows large, then the gain will be decreased, and thus the node becomes harder to split and easier to prune. This is used to prevent overfitting (of the training data).

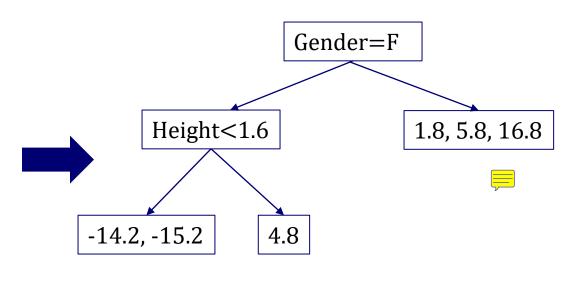
The regularization affects children nodes more than their parent node.

$$SS = \frac{SPR}{4PRS + \lambda}$$

Fit PR0 into an XGBoost tree (up to four leaves)

$$\lambda = 0, \gamma = 0$$

Height (m)	Favorite Color	Gender	PR0
1.6	Blue	Male	16.8
1.6	Green	Female	4.8
1.5	Blue	Female	-15.2
1.8	Red	Male	1.8
1.5	Green	Male	5.8
1.4	Blue	Female	-14.2



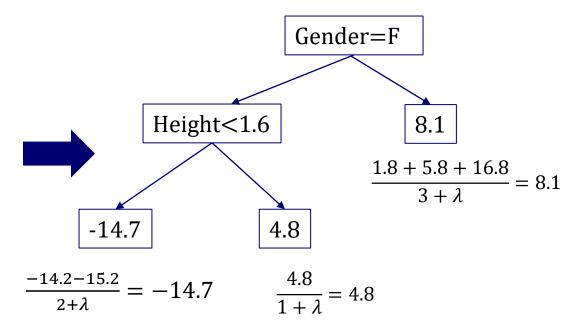
Pseudo Residual (PR) = True Value - Predicted Value

# **XGBoost Output**

Output Value = Sum of PR / (#PRs + regularization term)

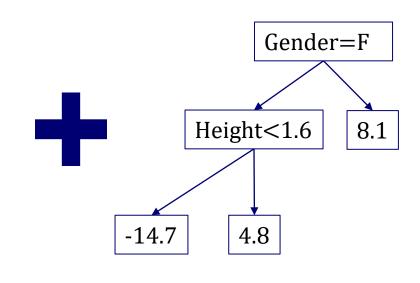
$$\lambda = 0, \gamma = 0$$

Height (m)	Favorite Color	Gender	PR0
1.6	Blue	Male	16.8
1.6	Green	Female	4.8
1.5	Blue	Female	-15.2
1.8	Red	Male	1.8
1.5	Green	Male	5.8
1.4	Blue	Female	-14.2



F1(x) = F0(x) +  $\nu_1$  × Output of DT(x)

Height (m)	Favorite Color	Gender	Weight (kg)	F0
1.6	Blue	Male	88	71.2
1.6	Green	Female	76	71.2
1.5	Blue	Female	56	71.2
1.8	Red	Male	73	71.2
1.5	Green	Male	77	71.2
1.4	Blue	Female	57	71.2



F1((1.6, Blue, Male)) =  $71.2 + 0.1 \times 8.1 = 72.0$ F1((1.6, Green, Female)) =  $71.2 + 0.1 \times 4.8 = 71.7$ F1((1.5, Blue, Female)) =  $71.2 + 0.1 \times -14.7 = 69.7$ F1((1.8, Red, Male)) =  $71.2 + 0.1 \times 8.1 = 72.0$ F1((1.5, Green, Male)) =  $71.2 + 0.1 \times 8.1 = 72.0$ F1((1.4, Blue, Female)) =  $71.2 + 0.1 \times -14.7 = 69.7$ 

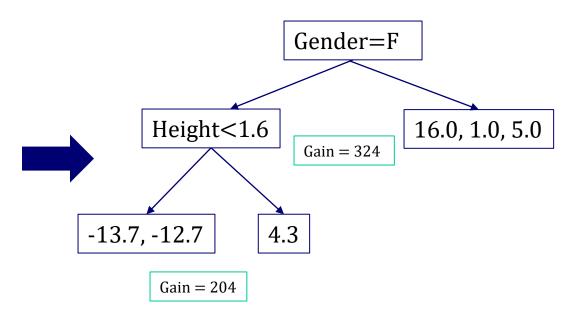
So after building the first DT, we obtain...

Height (m)	Favorite Color	Gender	Weight (kg)	F0	PR0	F1	PR1
1.6	Blue	Male	88	71.2	16.8	72.0	16.0
1.6	Green	Female	76	71.2	4.8	71.7	4.3
1.5	Blue	Female	56	71.2	-15.2	69.7	-13.7
1.8	Red	Male	73	71.2	1.8	72.0	1.0
1.5	Green	Male	77	71.2	5.8	72.0	5.0
1.4	Blue	Female	57	71.2	-14.2	69.7	-12.7

Fit PR1 into an XGBoost tree (up to four leaves)

$$\lambda = 0, \gamma = 0$$

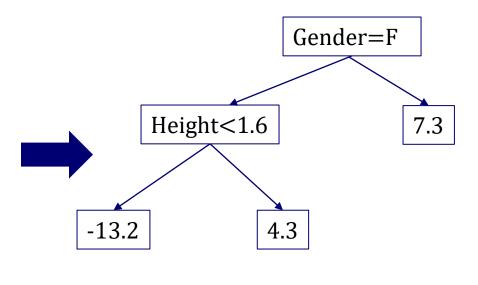
Height (m)	Favorite Color	Gender	PR1
1.6	Blue	Male	16.0
1.6	Green	Female	4.3
1.5	Blue	Female	-13.7
1.8	Red	Male	1.0
1.5	Green	Male	5.0
1.4	Blue	Female	-12.7



Output Value = Sum of PR / (#PRs + regularization term)

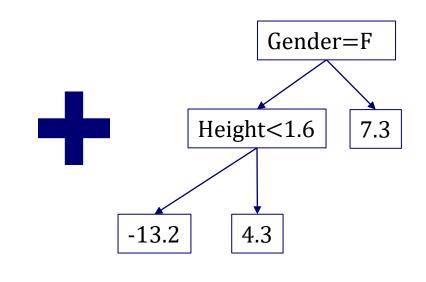
$$\lambda = 0, \gamma = 0$$

Height (m)	Favorite Color	Gender	PR1
1.6	Blue	Male	16.0
1.6	Green	Female	4.3
1.5	Blue	Female	-13.7
1.8	Red	Male	1.0
1.5	Green	Male	5.0
1.4	Blue	Female	-12.7



F2(x) = F1(x) +  $\nu_2$  × Output of DT(x)

Height (m)	Favorite Color	Gender	Weight (kg)	F1	
1.6	Blue	Male	88	72.9	
1.6	Green	Female	76	71.7	
1.5	Blue	Female	56	69.7	
1.8	Red	Male	73	71.6	
1.5	Green	Male	77	71.6	
1.4	Blue	Female	57	69.7	

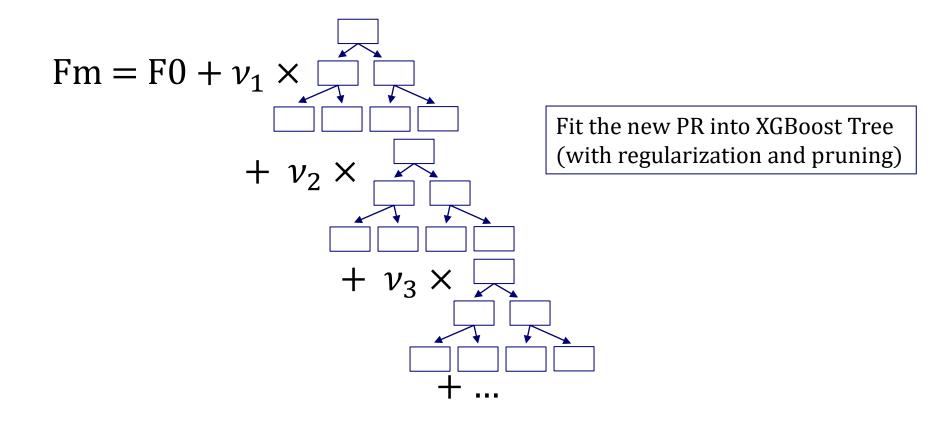


F2((1.6, Blue, Male)) =  $72.9 + 0.1 \times 7.3 = 73.6$ F2((1.6, Green, Female)) =  $71.7 + 0.1 \times 4.3 = 72.1$ F2((1.5, Blue, Female)) =  $69.7 + 0.1 \times -13.2 = 68.4$ F2((1.8, Red, Male)) =  $71.6 + 0.1 \times 7.3 = 72.3$ F2((1.5, Green, Male)) =  $71.6 + 0.1 \times 7.3 = 72.3$ F2((1.4, Blue, Female)) =  $69.7 + 0.1 \times -13.2 = 68.4$ 

#### So after building the second DT, we obtain...

Height (m)	Favorite Color	Gender	Weight (kg)	F0	PR0	F1	PR1	F2	PR2
1.6	Blue	Male	88	71.2	16.8	72.9	15.1	73.6	14.4
1.6	Green	Female	76	71.2	4.8	71.7	4.3	72.1	3.9
1.5	Blue	Female	56	71.2	-15.2	69.7	-13.7	68.4	-12.4
1.8	Red	Male	73	71.2	1.8	71.6	1.4	72.3	0.7
1.5	Green	Male	77	71.2	5.8	71.6	5.4	72.3	4.7
1.4	Blue	Female	57	71.2	-14.2	69.7	-12.7	68.4	-11.4

Notice the PR's are shrinking: Small steps towards the right direction!



Stop until the pre-specified #DTs or the PR stops improving!

# **Python Time!**

- pip install xgboost
- Import xgboost as xgb
- Install graphviz-2.38.zip for visualization



Works exceptionally well in practice

Won a series of Kaggle competitions

More robust and explainable than DNN

Comes with regularization and pruning