

VE 320 Summer 2019

Introduction to Semiconductor Devices

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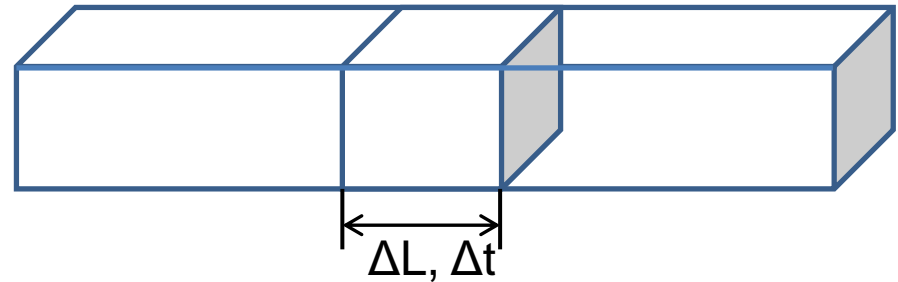
Lecture 5

Carrier Transport (Chapter 5)

Carrier transport

n type semiconductor

$$I = \frac{\Delta Q}{\Delta t} = \frac{neA_c\Delta L}{\Delta t} = neA_cv$$



Current density

$$J = \frac{I}{A_c} = nev$$

v : average drift velocity, e : electron charge, n : electron density

$$F = -eE = m^*a \rightarrow a = -\frac{eE}{m^*} \rightarrow v = at \quad m^*: \text{conductivity effective mass of electrons}$$

$$v = -\frac{et}{m^*}E$$

If effective mass and t are constant, then will v linearly increase with E ?

True for low electric field

$$v = -\mu_n E$$

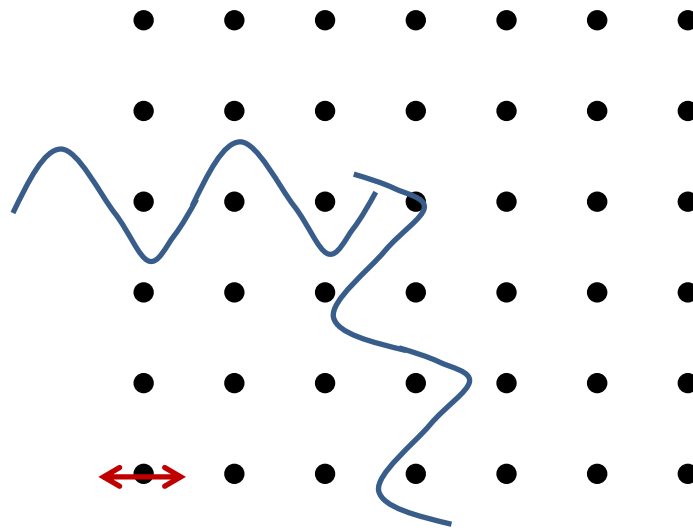
μ_n is the electron mobility – Very important for semiconductors! Unit: $\text{cm}^2/(\text{V}\cdot\text{s})$

Drift current density due to electrons $J_{n|drf} = (-en)(-\mu_n E) = e\mu_n nE$

Total drift current density: $J_{drf} = e(\mu_n n + \mu_p p)E$

Carrier transport

Electron:



Resistor heating
up by current

Thermal vibration \longleftrightarrow phonon

Ionized impurity

scattering \rightarrow average $\langle v \rangle$ does not increase as time

$$\mu_n = \frac{et}{m^*}$$

What is t here? Time? Give more time, then the mobility increases?

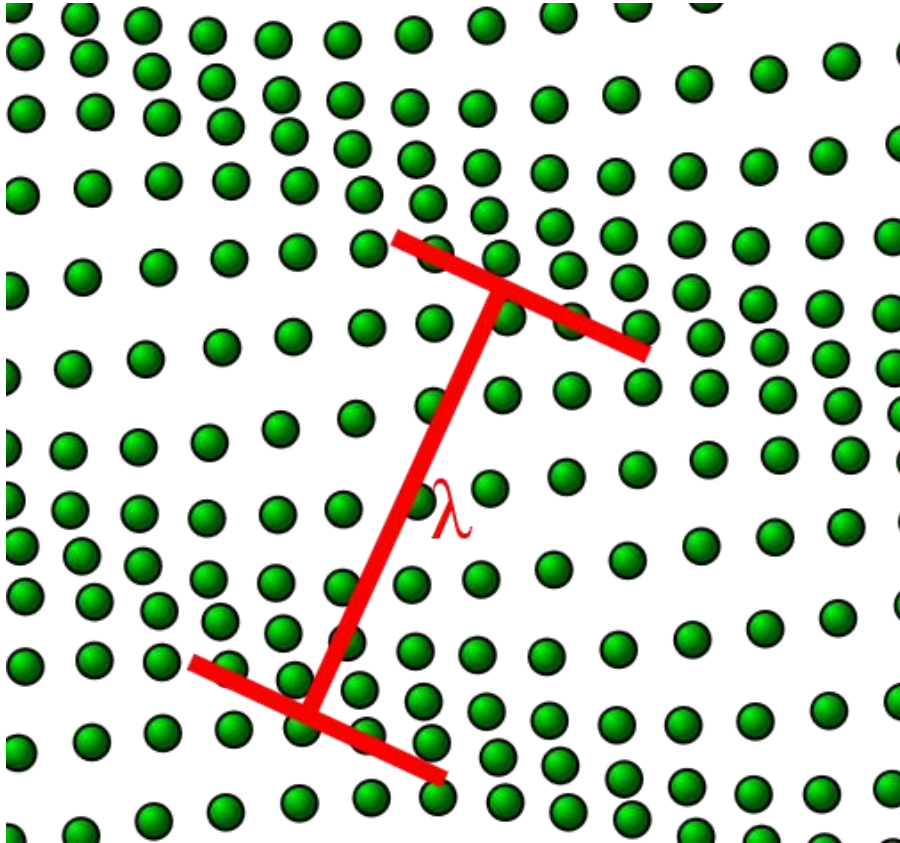
$$\mu_n = \frac{e\tau_{cn}}{m_{cn}^*}$$

τ_{cn} is the mean time between collisions for electron

Hole:
$$\mu_p = \frac{e\tau_{cp}}{m_{cp}^*}$$

Phonons

Basic facts:



Atom displacement
exaggerated.

Lattice scattering, or phonon scattering

- Perfect periodic lattice: no scattering
- Thermal vibration: potential function disruption, scattering

$$\mu_L \propto T^{-3/2}$$

μ_L : mobility only due to phonon scattering

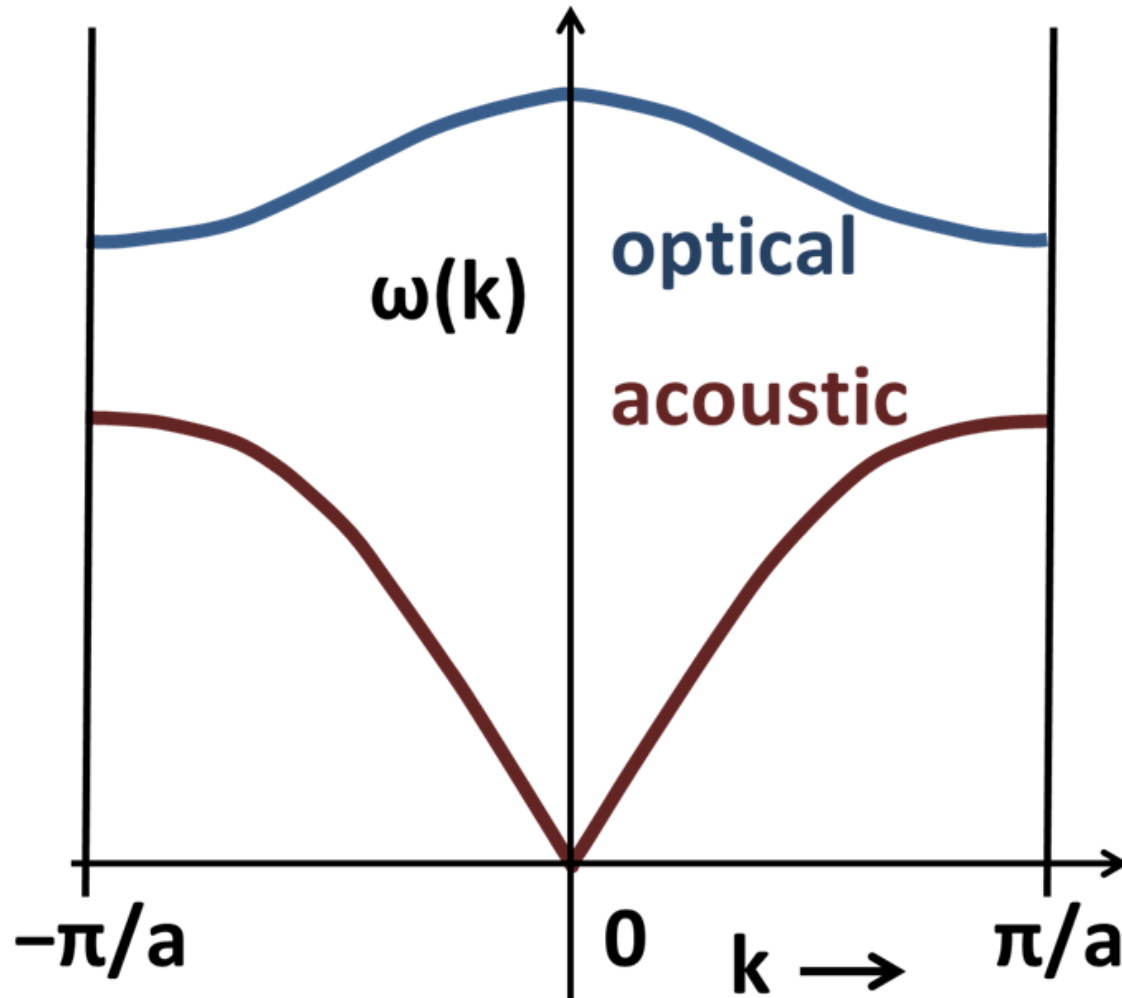
Phonon scattering

Basic facts:

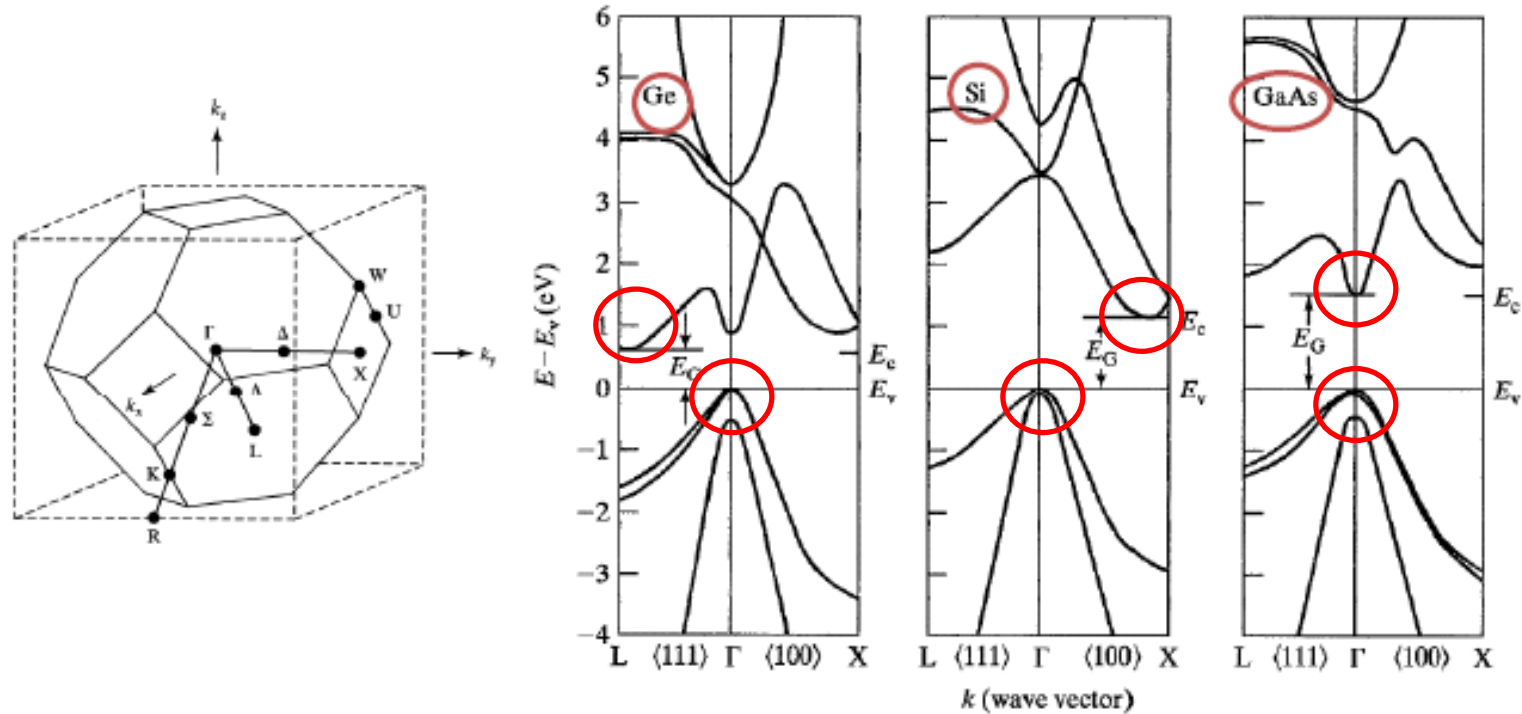
- Quantum mechanic description of atom vibration at a frequency
- A wave and also a particle
- Two kinds: optical phonons and acoustic phonons
- Optical phonons:
short wavelength \rightarrow high energy
electron-phonon collision: inelastic scattering (energy E change)
- Acoustic phonons:
long wavelength (tens of lattice constant) \rightarrow low energy
electron-phonon collision: elastic scattering (momentum k change)
- Acoustic: coherent movement of atoms, like sound wave
- Optical: out-of-phase movements of atoms, lattice basis consists of two or more atoms, can be excited by infrared light. Raman scattering \rightarrow useful

Phonons

Basic facts:



Previously: band structure in 3D k-space



- Direct bandgap
(electron excited, k constant, $E \uparrow \rightarrow f \uparrow, v = f \lambda \uparrow$)
- Indirect bandgap ($P(\text{absorbing photon}) * P(\text{phonon scattering})$)

Ionized impurity scattering

Coulomb interaction

$$\mu_I \propto \frac{T^{+3/2}}{N_I}$$

μ_I : mobility only due to ionized impurity scattering

$N_I = N_d^+ + N_a^-$ is the total ionized impurity concentration

If the number of ionized impurity centers increases, then the probability of a carrier encountering an ionized impurity center increases, implying a smaller value of μ_I

Total scattering and mobility

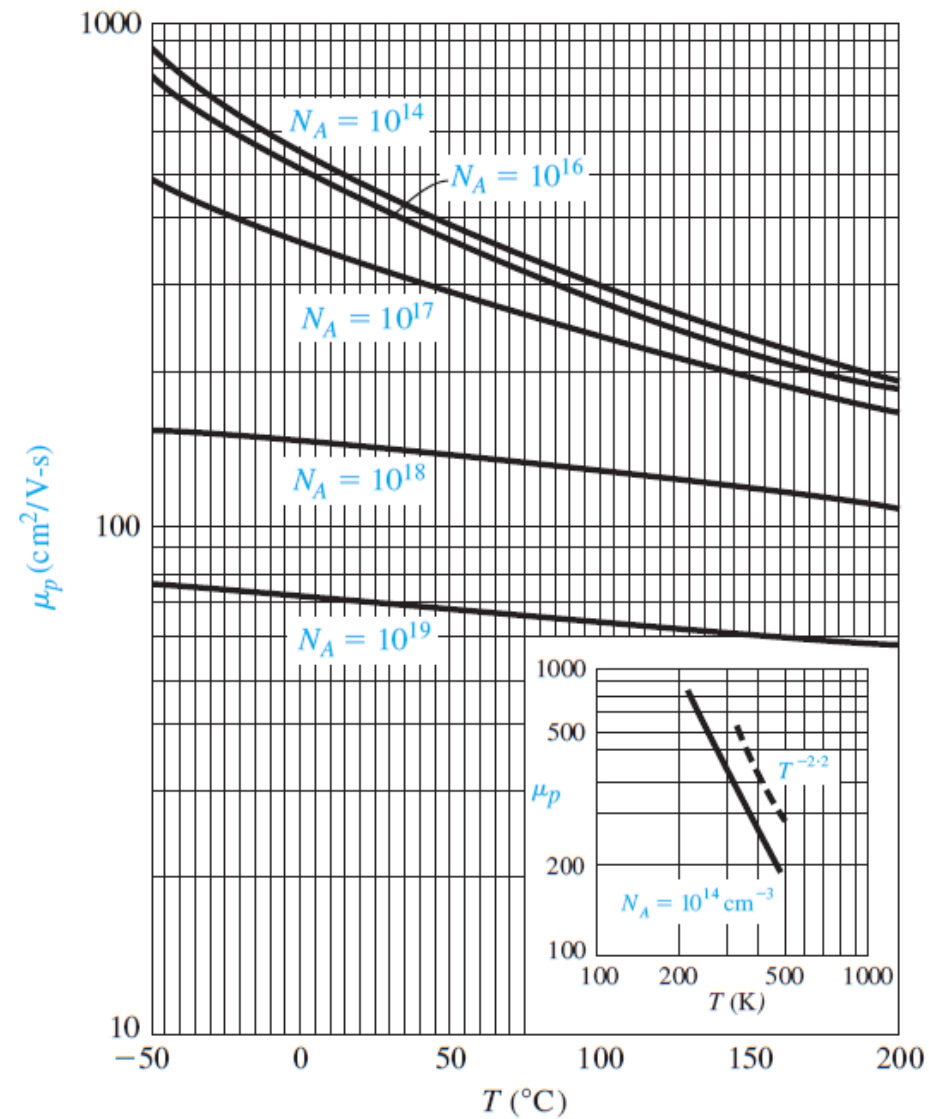
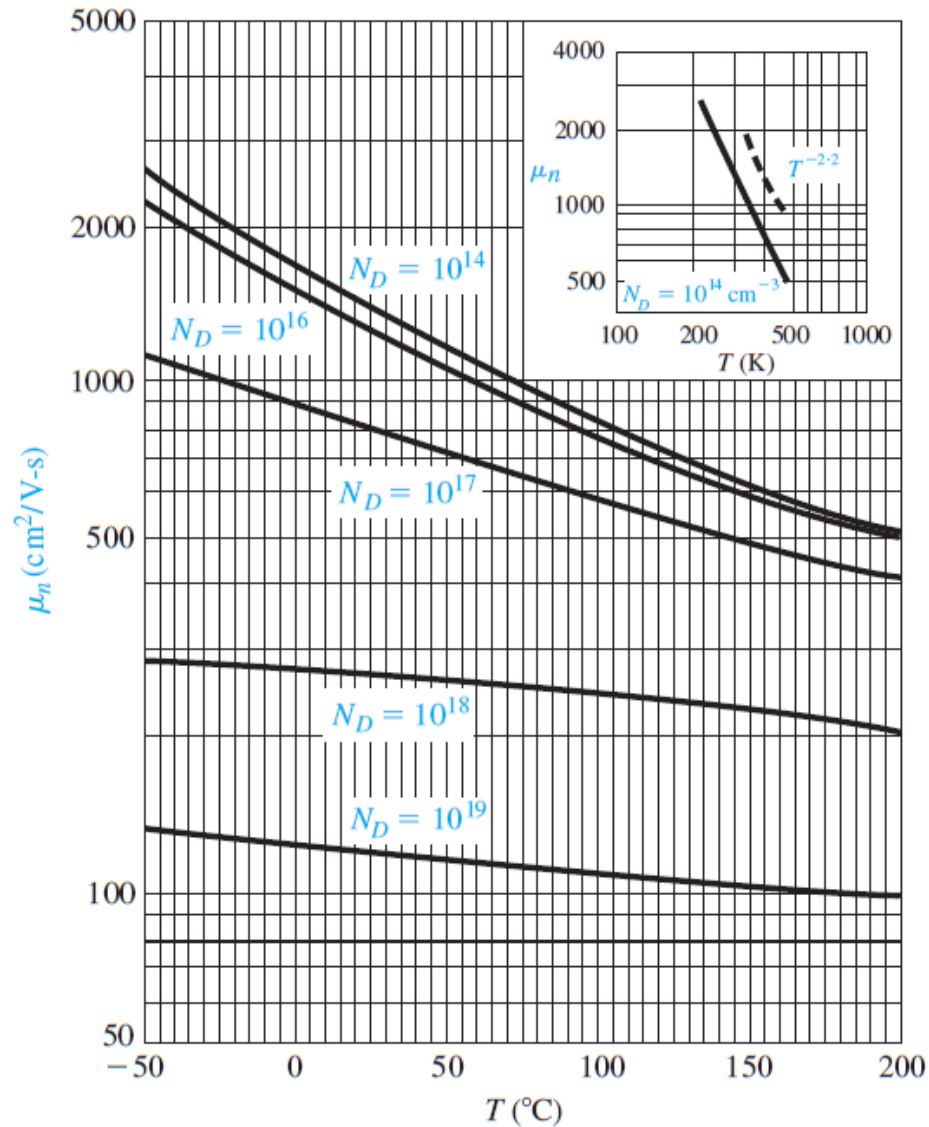
Total probability of a scattering event occurring in the differential time dt

$$\frac{dt}{\tau} = \frac{dt}{\tau_I} + \frac{dt}{\tau_L}$$

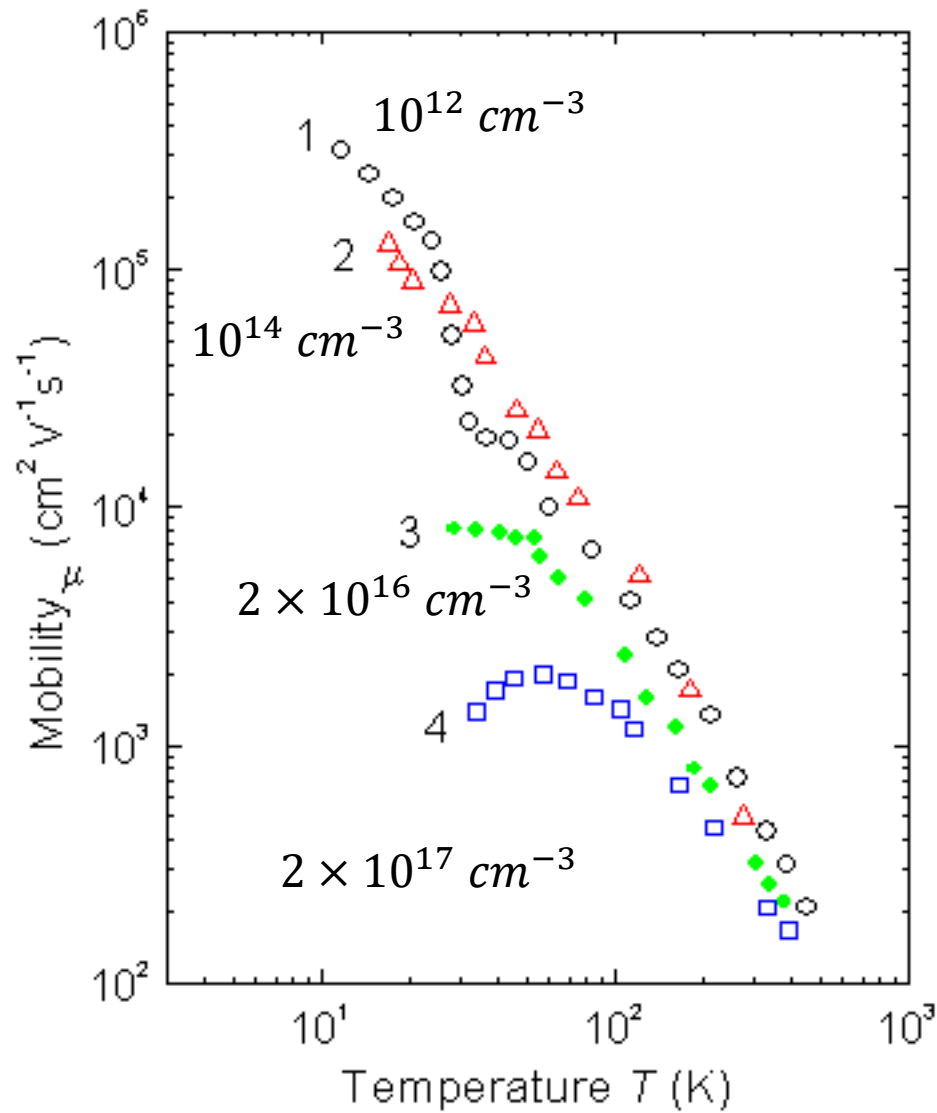
Total mobility

$$\frac{1}{\mu} = \frac{1}{\mu_I} + \frac{1}{\mu_L}$$

Mobility vs. T at different doping



Mobility vs. T



Drift current density

$$J_{drf} = e(\mu_n n + \mu_p p)E = \sigma E$$

σ is the conductivity of the semiconductor material

$$\text{Resistivity } \rho = \frac{1}{\sigma} = \frac{1}{e(\mu_n n + \mu_p p)}$$

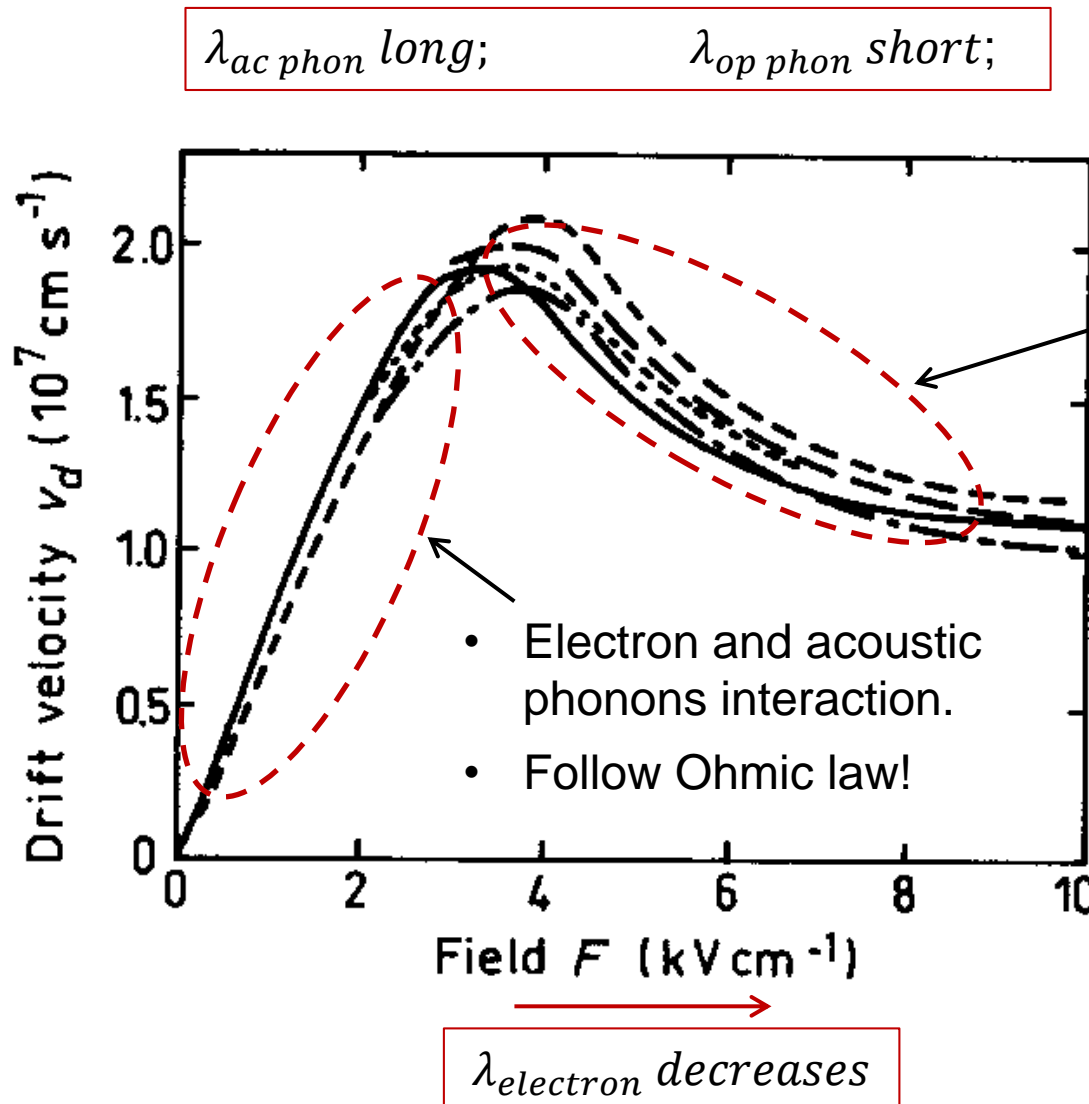
For p-type semiconductor with an acceptor doping N_a ($N_d=0$) in which $N_a \gg n_i$, and if electron and hole mobilities are similar, then

$$\sigma = e(\mu_n n + \mu_p p) \approx e\mu_p p$$

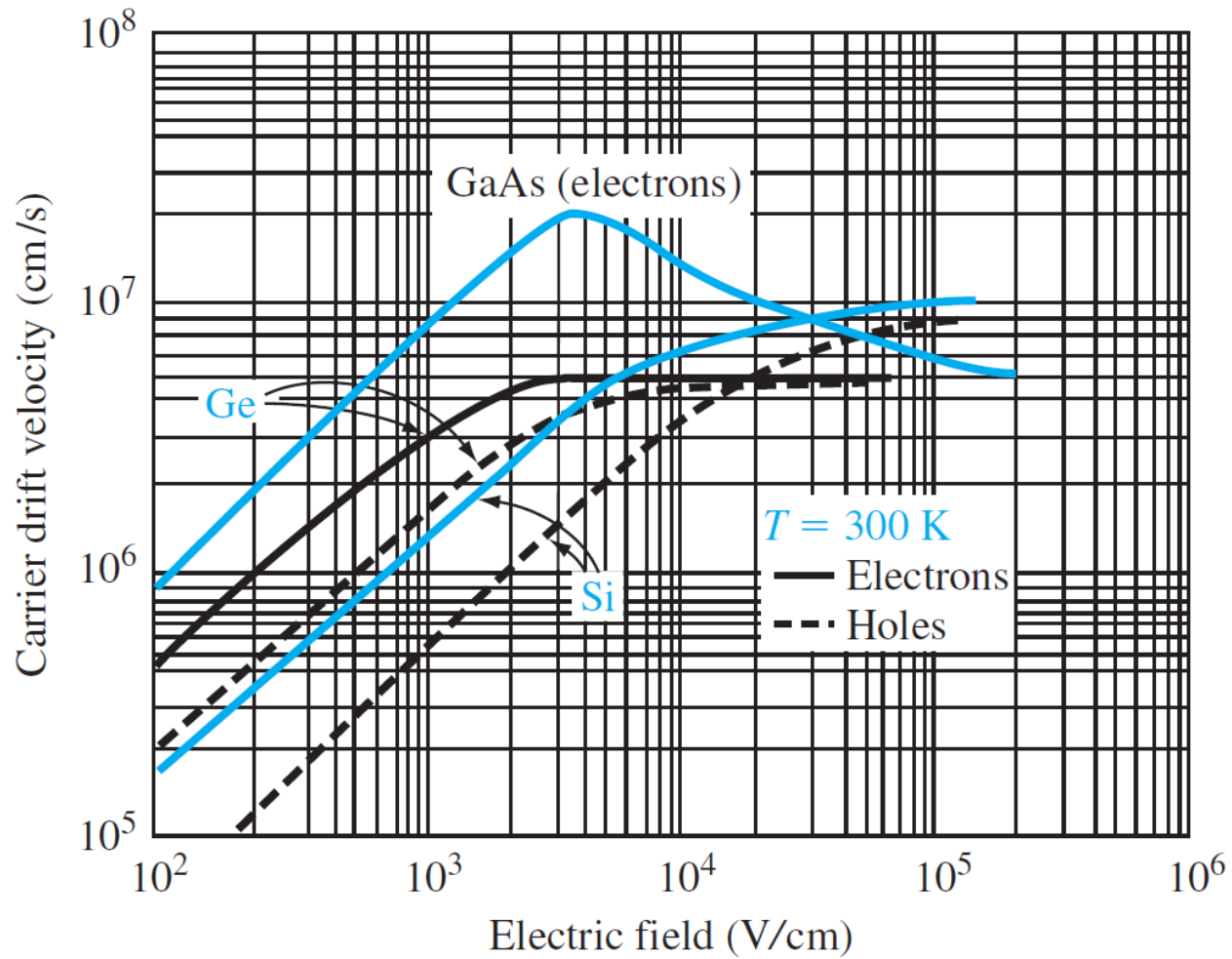
Assume complete ionization:

$$\sigma \approx e\mu_p N_a$$

Velocity saturation



Velocity saturation



Velocity saturation

Carrier drift velocity versus electric field for electrons in silicon

$$v_n = \frac{v_s}{\left[1 + \left(\frac{E_{\text{on}}}{E}\right)^2\right]^{1/2}}$$

v_s : saturation velocity $\sim 10^7$ cm/s at 300K, $E_{\text{on}} = 7 \times 10^3$ V/cm

Small electric field:

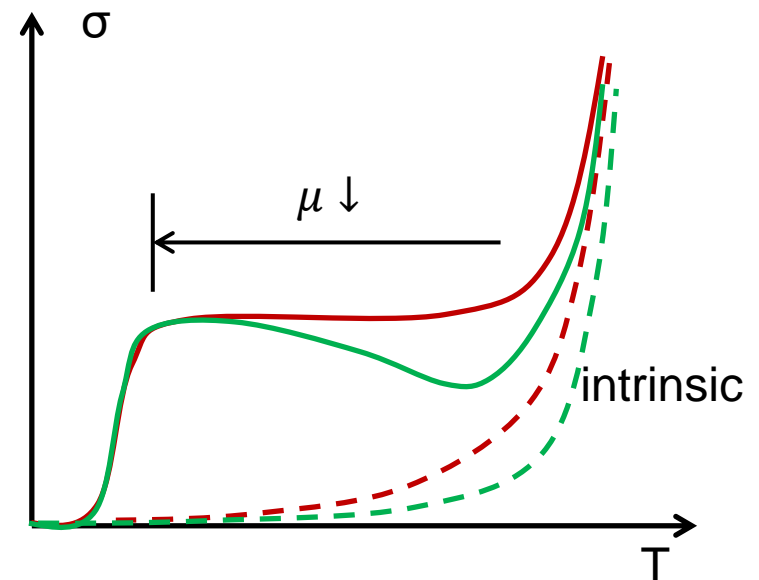
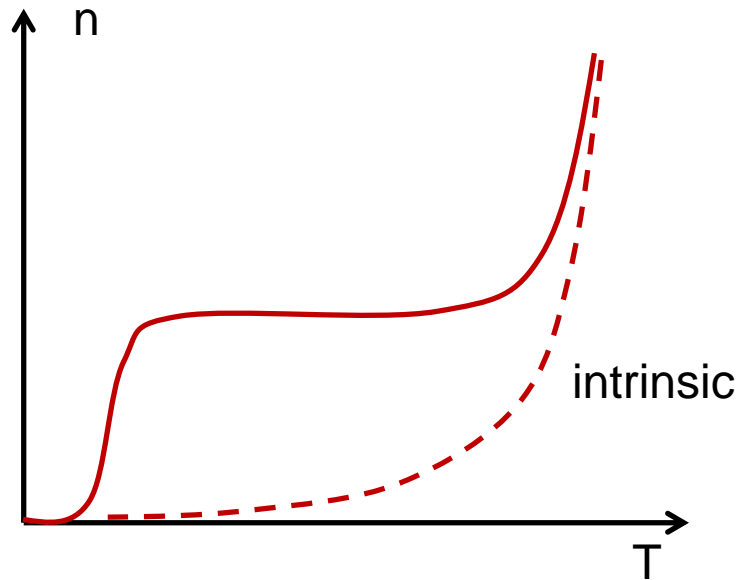
$$v_n \cong \left(\frac{E}{E_{\text{on}}}\right) \cdot v_s$$

Holes, small electric field:

$$v_p \cong \left(\frac{E}{E_{\text{op}}}\right) \cdot v_s$$

Mobility vs T

Semiconductor:

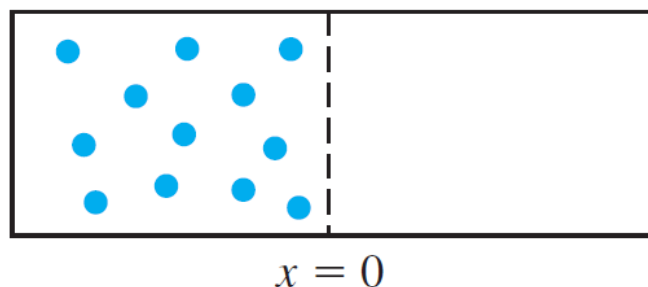


metal: conductivity \downarrow

Carrier diffusion

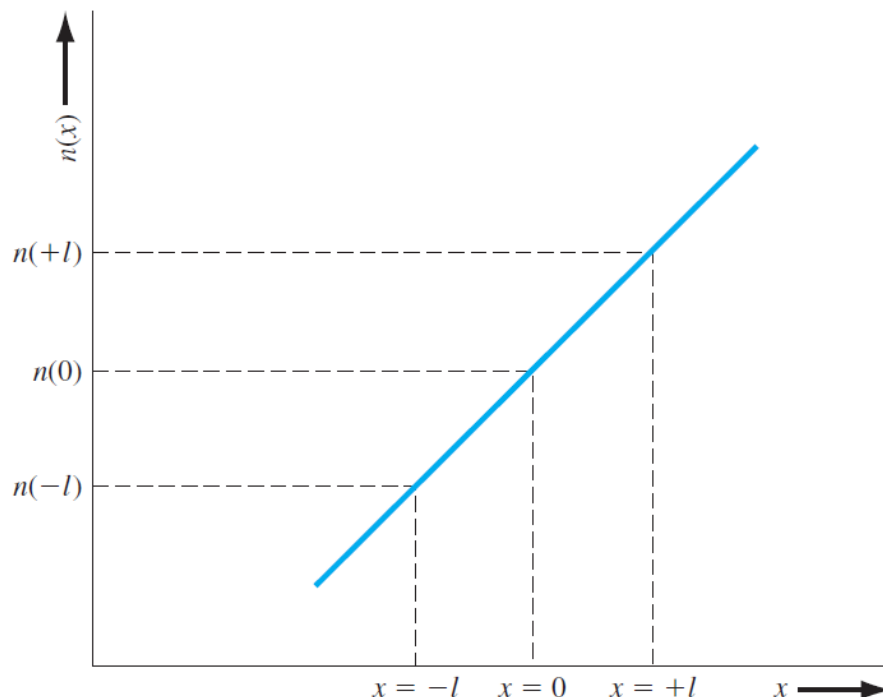
2 mechanisms that can induce current in a semiconductor: drift, diffusion

Diffusion is the process whereby particles flow from a region of high concentration toward a region of low concentration.



One half of the electrons at $x=-l$ will be traveling to the right and one half of the electrons at $x=l$ will be traveling to the left, then the net rate of electron flow, F_n in the $+x$ direction at $x=0$ is

$$F_n = \frac{1}{2}n(-l)v_{th} - \frac{1}{2}n(+l)v_{th} = \frac{1}{2}v_{th}[n(-l) - n(+l)]$$



Carrier diffusion

Electron:
$$F_n = \frac{1}{2}n(-l)v_{th} - \frac{1}{2}n(+l)v_{th} = \frac{1}{2}v_{th}[n(-l) - n(+l)]$$

Taylor expansion of n at $x=0$ (l is very small)

$$F_n = \frac{1}{2}v_{th} \left\{ \left[n(0) - l \frac{dn}{dx} \right] - \left[n(0) + l \frac{dn}{dx} \right] \right\}$$

$$F_n = -v_{th} l \frac{dn}{dx}$$

Current density

$$J = -eF_n = +ev_{th} l \frac{dn}{dx}$$

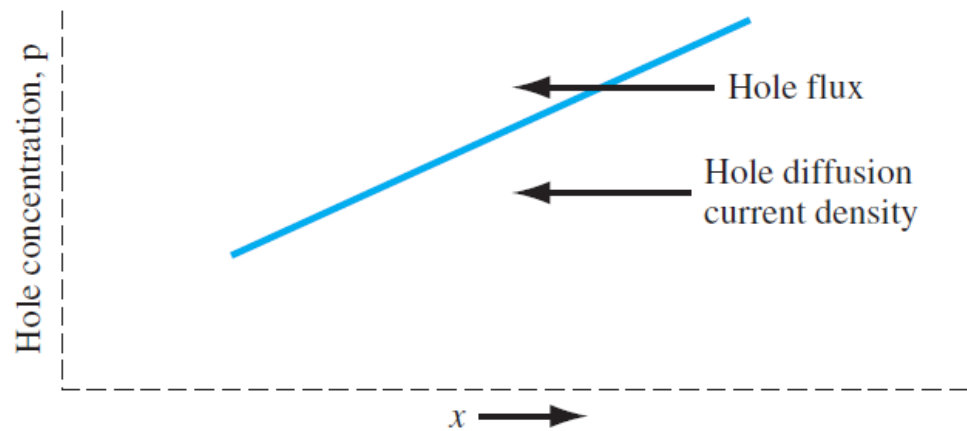
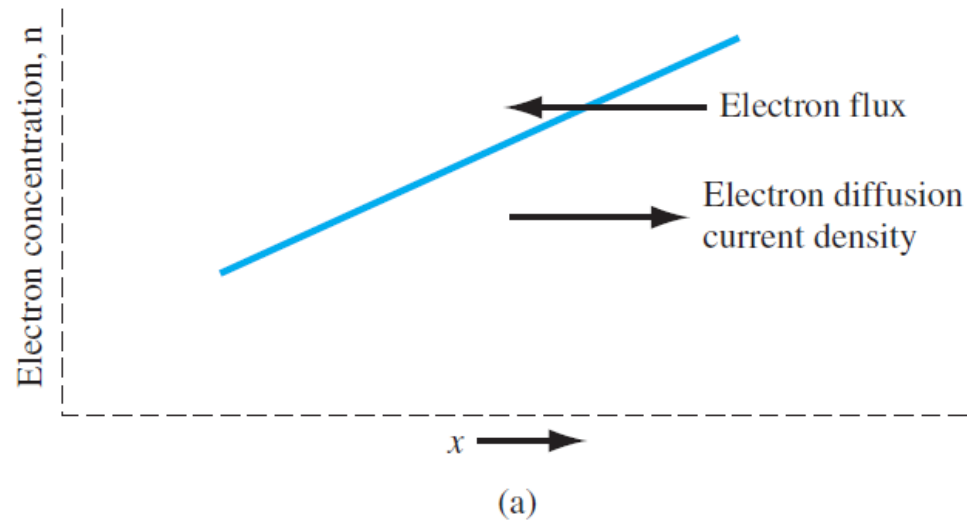
$$J_{nx|dif} = eD_n \frac{dn}{dx}$$

where $D_n = v_{th}l$ is called the electron diffusion coefficient, has units of cm^2/s

Hole:

$$J_{px|dif} = -eD_p \frac{dp}{dx}$$

Carrier diffusion



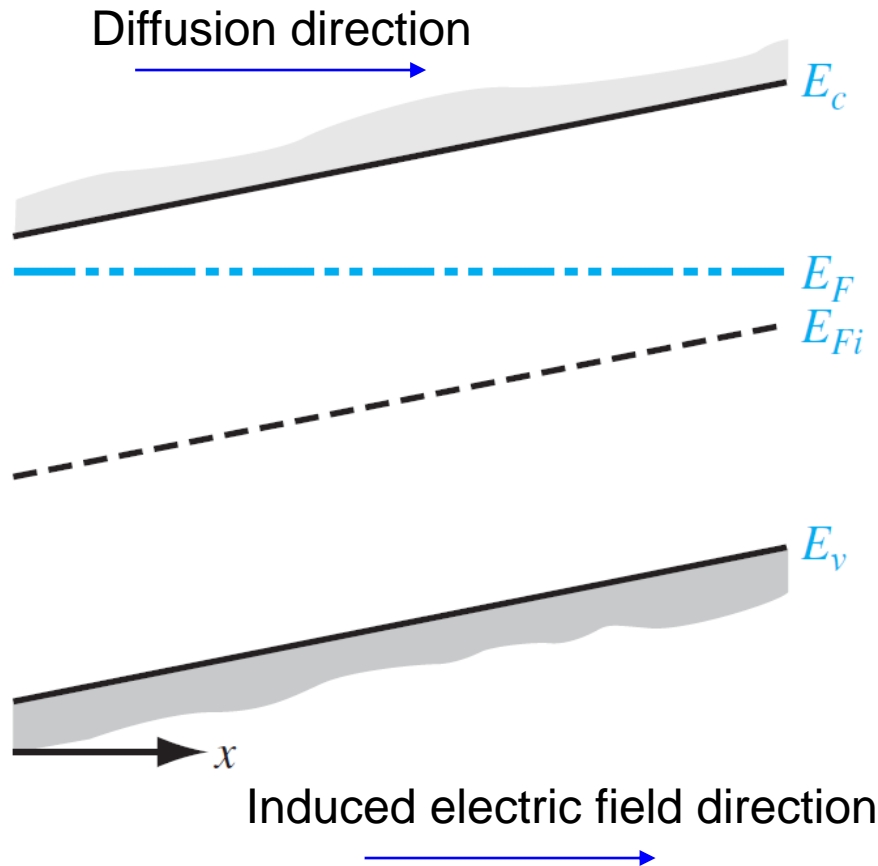
Total current density with both drift and diffusion

$$J = en\mu_n E_x + ep\mu_p E_x + eD_n \frac{dn}{dx} - eD_p \frac{dp}{dx}$$

4 terms: but usually some certain term will dominate for certain cases

Nonuniform doping

Fermi level: always constant at thermal equilibrium



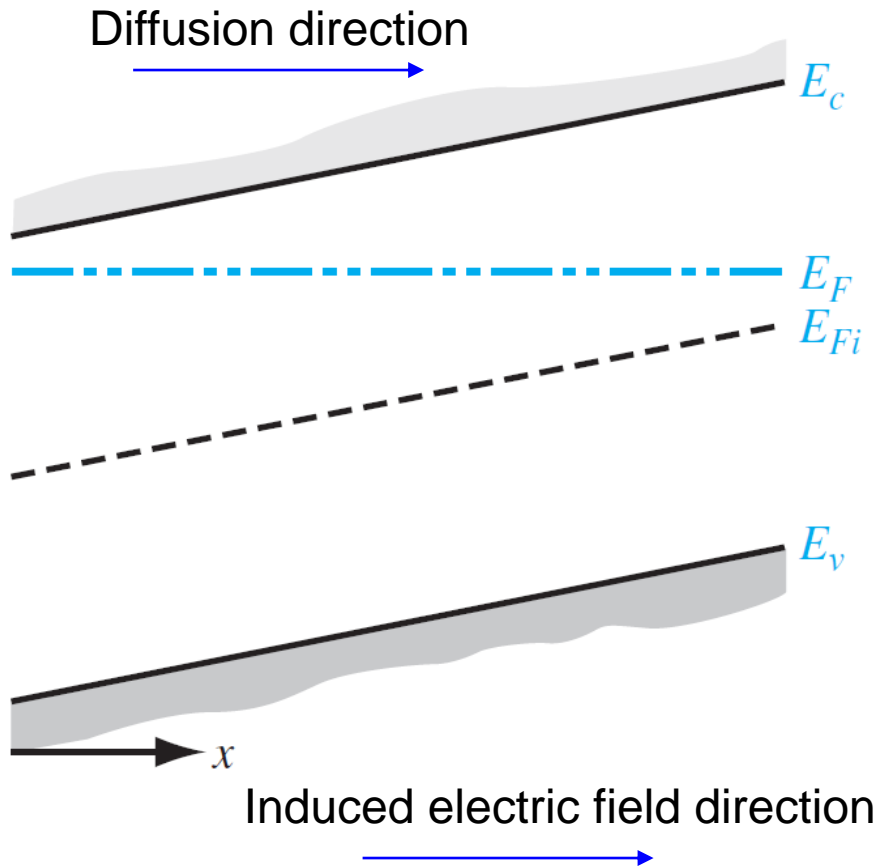
- The space charge induced by this diffusion process is a small fraction of the impurity concentration
- Induced electric field: prevents any further diffusion, counter the diffusion

$$E_x = -\frac{d\phi}{dx} = \frac{1}{e} \frac{dE_{Fi}}{dx}$$

Intrinsic Fermi-level changes->
there is an electric field

Nonuniform doping

Fermi level: always constant at thermal equilibrium



$$E_x = -\frac{d\phi}{dx} = \frac{1}{e} \frac{dE_{Fi}}{dx}$$

$$n_0 = n_i \exp\left[\frac{E_F - E_{Fi}}{kT}\right] \approx N_d(x)$$

$$E_F - E_{Fi} = kT \ln\left(\frac{N_d(x)}{n_i}\right)$$

$$-\frac{dE_{Fi}}{dx} = \frac{kT}{N_d(x)} \frac{dN_d(x)}{dx}$$

$$E_x = -\left(\frac{kT}{e}\right) \frac{1}{N_d(x)} \frac{dN_d(x)}{dx}$$

Einstein relation

Drift current = diffusion current

Nonuniformly doped semiconductor with no electrical connection

Drift from induced electric field balances the diffusion

Electrons: $J_n = 0 = en\mu_n E_x + eD_n \frac{dn}{dx}$

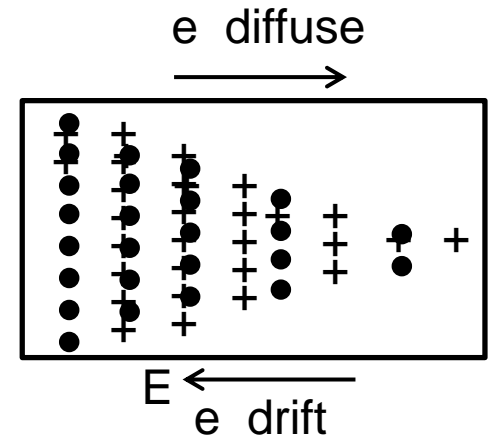
Assume $n=N_d$ $J_n = 0 = e\mu_n N_d(x)E_x + eD_n \frac{dN_d(x)}{dx}$

$$E_x = -\left(\frac{kT}{e}\right) \frac{1}{N_d(x)} \frac{dN_d(x)}{dx}$$

$$0 = -e\mu_n N_d(x) \left(\frac{kT}{e}\right) \frac{1}{N_d(x)} \frac{dN_d(x)}{dx} + eD_n \frac{dN_d(x)}{dx}$$

$$\frac{D_n}{\mu_n} = \frac{kT}{e}$$

Einstein relation $\frac{D_n}{\mu_n} = \frac{D_p}{\mu_p} = \frac{kT}{e}$



Carrier concentration

- Carrier drift & diffusion

carrier drift: electric field $E \neq 0$

driving force: electric field

flux:

of charges passing a unit area at a give unit time



carrier diffusion: electric field $E = 0$

driving force: thermal dynamics

flux:

of carriers passing a unit area at a give unit time

