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CS5100 - Introduction to Artificial Intelligence

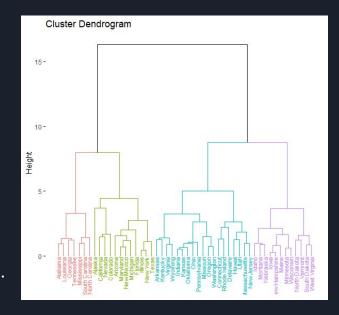
GitHub Repository: https://github.com/PdAlbedo/Al Final Project

Project Aim

Agglomerative Hierarchical Clustering is a bottom up approach to clustering data. There are two primary variables that can affect the clusters that are generated. Different combinations of these variables will generate different clusters.

- Linkage A method for building the clusters based on how close the observations are.
- Affinity The distance metric used to determine how close the elements are to each other.

The aim of this project is to see if the dimension of the dataset affects which affinity should be used in the clustering algorithm.



Project Objectives

- Are there any affinities consistently better as the dimensions increase or decrease?
- Are there any affinities that are relatively consistent across dimensions?
- Are there any combinations of linkage and affinity that perform better as the dimension increases?

We will use a combination of existing measures and observations to explore these questions.

Literature Review

- In 2010, Erisoglu and Sakallioglu explored different combinations of distance metrics and linkages in hierarchical clustering, and determined that the distance metric is impactful.
- In 2011, Rajalingam and Ranjini explored clustering with different data types, and determined that the run time for datasets of the same type of data, and with comparable record counts is relatively equal. The used a single distance metric for each data type.
- In 2014, Kumar, Chhabra, and Kumar explored 10 distance measures against 8 clustering algorithms, and determined that the performance and quality of the clusters varied based on the distance, clustering technique, and the nature of the data.
- In 2016, Irani, Pise, and Phatak explored distance metrics further, and determined that the metrics can tell you the distance between points, but do not consider the behavior of the data. They also note that negative data can be a challenge to clustering.
- In 2018, Ogbuabor, and Ugwoke explored a healthcare dataset using K-Means and DBSCAN with varying distance metrics, and evaluated the results using the Silhouette Score value.

Project Requirements

- Obtain Clean Datasets
- Vary the Dimensions of the Datasets
- Vary the Linkage Parameter
- Vary the Affinity Parameter (Including Standard and PreComputed)
- Calculate the Measures
- Analyze the Results

Datasets

Dataset	Description	Attributes	Records
CC General *	Credit Card Data	16	8,950
COVID *	COVID Statistics by Country	7	225
Credit Card Customer Data **	Credit Card Summary Data	6	660
Mall Customers *	Mall Customer Summary Data	5	200
Sales Transaction **	Sales Transaction Information	53	811
Wholesale **	Sales Summary Information	8	440

^{*} https://www.kaggle.com/

^{**} https://archive.ics.uci.edu/ml/index.php

Variables Part 1

Dimensions: 2, 3, 4

Linkage	Definition
Average	Average inter-cluster distance
Complete	The farthest distance between elements in each cluster
Single	The smallest distance between elements in each cluster
Ward	Creates new clusters that minimize the variance

Variables Part 2

Affinity	Definition	Formula *
Euclidean	Straight Line Distance	sqrt(sum((x-y)^2))
Manhattan	City Block Distance	sum(x -y)
Cosine	1 - Cosine Similarity	1 - (x * y)/(x y)
Chebyshev	The maximum distance between vectors	max(x - y)
Minkowski	A generalization of the Euclidean and Manhattan distance	sum(w * x-y ^p)^(1/p)
Mahalanobis	A measure of the number of standard deviations a point is from the mean distribution	sqrt((x-y)' V^-1 (x-y)

 $^{^*\} https://scikit-learn.org/stable/modules/generated/sklearn.metrics. Distance Metric.html$

Measures

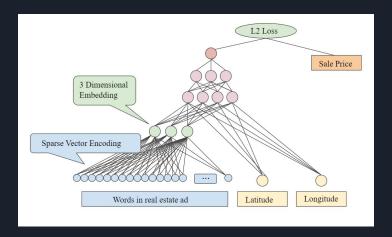
Measure	Definition	Interpretation
Silhouette Score	A measure of similarity between items in the same cluster	-1 to 1 0 means overlap Higher values are better
Calinski Harabasz Score	A measure of the variance in cluster dispersion	Higher values are better
Davies-Bouldin Index	A measure of the average similarity between clusters focusing on the size of the clusters and the distance between the clusters	0 and above Closer to 0 is better

• https://scikit-learn.org/stable/modules/classes.html#module-sklearn.metrics

Prior Works

- Datasets
 - Numerical data
 - Clean datasets
 - Normalization
- Number of dimensions
 - Embedding space

Embedding space



- Embedding is a kind of dimension reduction technique
 - Neural network
 - Generally, it means to project the higher dimension values into lower dimension space
 - Proportionally

Demo of projection in to Embedding space

```
class MyNetwork(nn.Module):
```



Code Demo

Analysis Approach

- Generated 342 records that included the dataset name, linkage, affinity, dimension,
 Silhouette Score, Calinkski Harabasz Score, Davies-Bouldin Index and the number of clusters
- Discarded any records with a single cluster
- Calculated the range between the fourth and second dimension for each measure for each linkage and affinity combination
- Averaged the results across the datasets
- Tabulated the data in separate tables for each measure for interpretation

Results - Change in Silhouette Score

Linkage	Chebyshev	Cosine	Euclidean	Mahalanobis	Manhattan	Minkowski
Average	0.07	0.18	0.31		0.42	0.07
Complete	0.30	0.08	0.36	-0.24	0.25	0.11
Single	-0.10	-0.17	0.91	-0.10	0.47	0.37
Ward	-	-	0.19	-	-	-

The dimension changed from 2 to 4

Average change in Silhouette Score was 0.18 Largest increase in Silhouette Score was 0.91 Largest decrease in Silhouette Score was -0.24

Results - Change in Calinski Harabasz Score

Linkage	Chebyshev	Cosine	Euclidean	Mahalanobis	Manhattan	Minkowski
Average	210.69	-362.5	109.18	15199.21	284.02	-5.77
Complete	379.27	172.63	296.97	642.46	-3407.30	55.20
Single	-159.80	-102.41	90.21	7519.38	90.59	-10770.77
Ward	-	-	716.52	-	-	-

The dimension changed from 2 to 4

Average change in Calinski Harabasz Score was 576.73 Largest increase in Calinski Harabasz Score was 15199.21 Largest decrease in Calinski Harabasz Score was -10770.77

Results - Change in Davies-Bouldin Index

Linkage	Chebyshev	Cosine	Euclidean	Mahalanobis	Manhattan	Minkowski
Average	0.11	0.16	-0.19	-0.08	0.44	-0.05
Complete	0.33	-0.27	0.51	-0.32	0.53	-0.10
Single	0.90	0	-0.91	-0.04	1.09	1.02
Ward	-	-	0.16	-	-	-

The dimension changed from 2 to 4

Average change in Davies-Bouldin Index was 0.17 Largest increase in Davies-Bouldin Index was 1.09 Largest decrease in Davies-Bouldin Index was -0.91

Results Summary

- Are there any affinities consistently better as the dimensions increase or decrease?
 - Euclidean, Manhattan, and Minkowski improved the Silhouette Score across linkages
 - Euclidean and Mahalanobis improved the Calinski Harabasz Score across linkages
 - Mahalanobis improved the Davies-Bouldin index across linkages
- Are there any affinities that are relatively consistent across dimensions?
 - We saw fluctuations in all measures as the dimension changed across all affinities
- Are there any combinations of linkage and affinity that perform better as the dimension increases?
 - Single Linkage with Euclidean improved by 0.91 in Silhouette Score
 - Average Linkage with Mahalanobis improved by 15199.21 in Calinski Harabasz Score
 - Since with Euclidean improved by -0.91 in Davies-Bouldin Index

Future Work

- Are there other measures that give additional insight?
- Evaluating the cluster statistics against a dataset Ground Truth
- Is there an upper threshold on the number of dimensions an affinity improves with?
- Do any of the newer affinities, like Geometric Distance, perform better at higher dimensions?

Conclusion

- There appears to be some affinities that perform better as the dataset dimension increases.
- Some affinities performed better with specific linkages, while others were more universal.
- Further research and findings in this area could be very impactful to future clustering efforts.

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Questions?

Thank you!