

EOSC 410/510 Assignment 1

Problem 1:

The following ranking were derived:

Graph	Pearson	Spearman
x-y	0.580098	0.572420
x2-y2	0.339721	0.572420
x3-y3	-0.901029	0.431895

Table 1: Pearson and Spearman ranking for 3 pair of datasets (1. x and y, x2 and y2, x3 and y3)

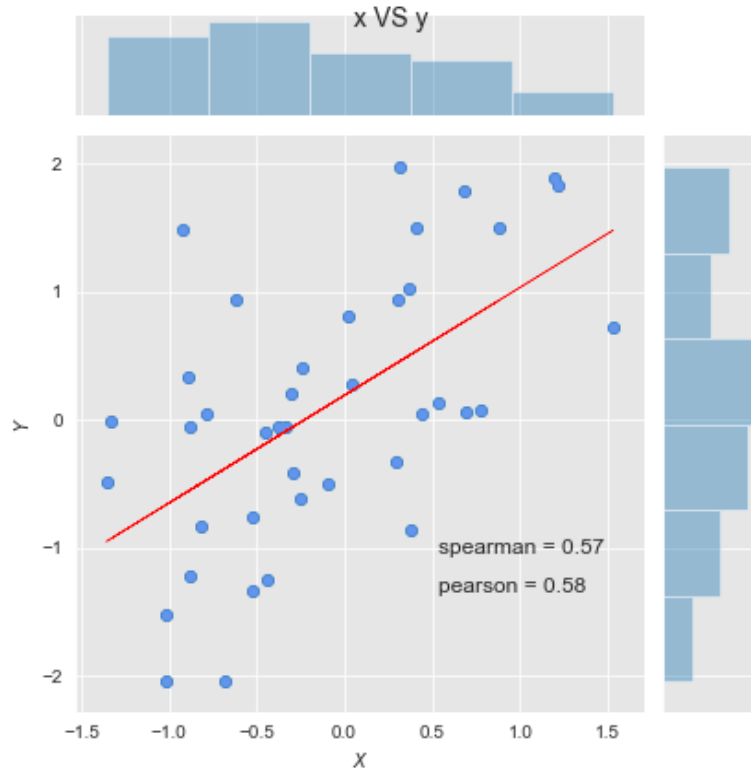


Figure 1: Regression between the x and y datasets. The Spearman and Pearson ranking is given on the graph.

When there is a linear relationship and no outliers the Pearson and Spearman rank are almost the same. As seen in the first graph for x vs y (Figure 1), this is true for distributions that are generally normal. However, the Pearson correlation scored 0.01 higher than the Spearman in this example for Figure 1.

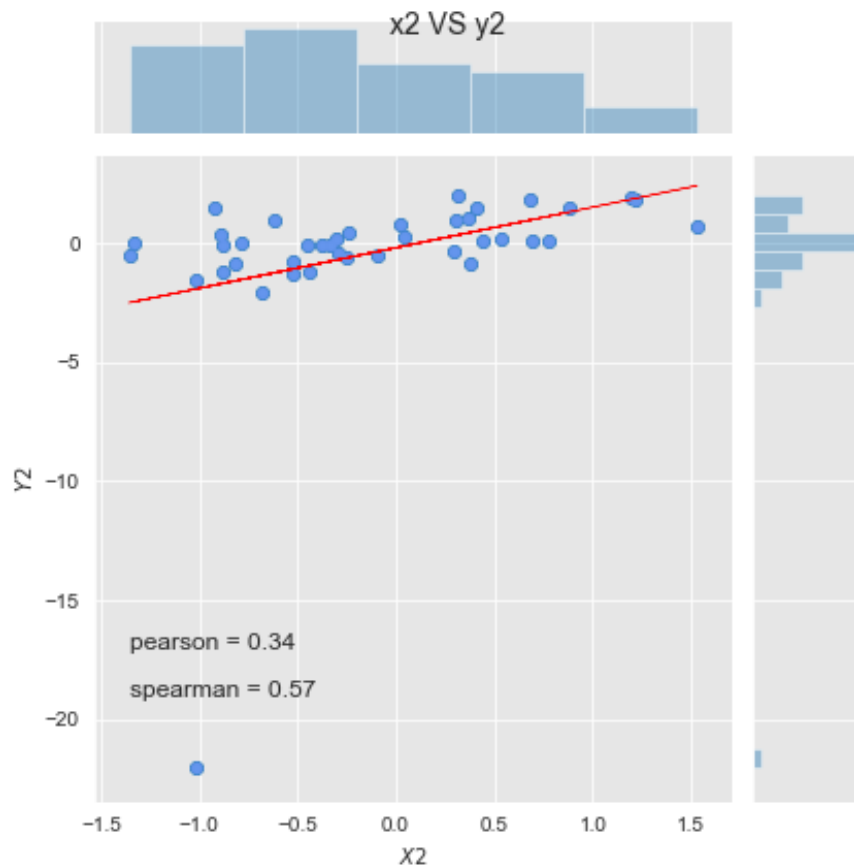


Figure 2: Regression between the x2 and y2 datasets. The Spearman and Pearson ranking is given on the graph.

In Figure 2 we notice that an outlier is added in the y2 dataset. This seems to throw off the Pearson correlation more than the Spearman. The Spearman raking was the same as that in Figure 1 (0.57 in both cases) whereas the Pearson ranking drops from 0.58 in Figure 1 to 0.34 in Figure 2 when an outlier in y2 is introduced. This would suggest that the Spearman ranking performs better when there is an outlier in the dependant variable; that is the Spearman is more robust to outliers.

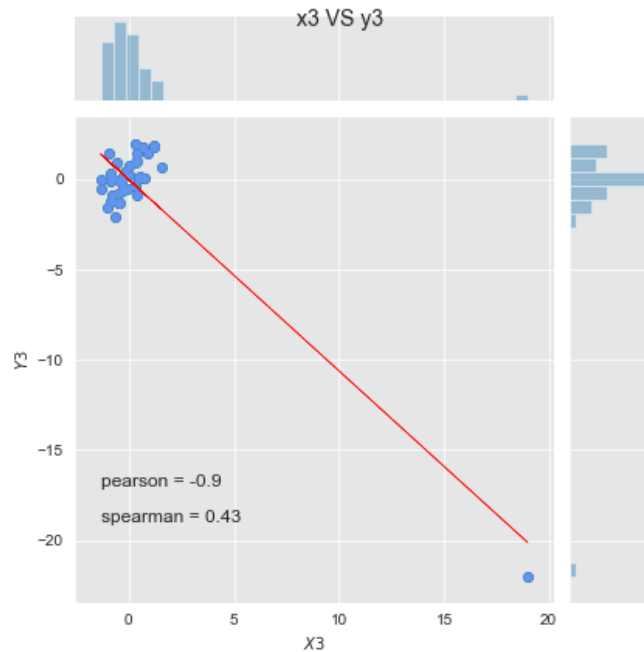


Figure 3: Regression between the x3 and y3 datasets. The Spearman and Pearson ranking is given on the graph.

In Figure 3, outliers exist in both the x3 and y3 datasets. In this case both rankings show lower correlation, the Spearman still showing one stronger than the Pearson. The Spearman ranking only fell from 0.57 in Figure 1 to 0.43 in Figure 3. The Pearson ranking however fell from 0.58 to -0.9, suggesting that an outlier in the dependent variable greatly affects the correlation. This would mean the Spearman ranking is usually more robust to outliers overall. The Pearson correlation coefficient measures the strength of the linear relationship between normally distributed variables. When the variables are not normally distributed or the relationship between the variables is not linear, it may be more appropriate to use the Spearman rank correlation method.

Vars	MLR coeffs	Included in Step	Step coeffs
x1	0.077280	True	0.0750933
x2	0.036674	False	na
x3	-0.355149	True	-0.334674
x4	-0.570685	True	-0.570856
x5	0.019197	False	na
x6	0.465527	True	0.488096

Table 2: Regression coefficients for MLR and step-wise regression. na for predictors which were not included in the stepwise.

Problem 2:

The regression coefficients for MLR, and regression coefficients for stepwise are summarized in Table 2 below. The table shows that the step-wise model was able to eliminate 2 variables. Based on the step-wise coefficients, the importance of the predictors are x4,x6,x3 and x1 in order of most to least importance. The MLR results produced a R^2 value of 0.98 while the stepwise results produce 0.97, showing that MLR claims that all the variables account for 98% of the variance, whereas in stepwise x1,x3,x4,x6 account for 97% of the variance. The MLR could have been overfitting to noise since it was considering x2 and x5 as well, and especially since the sample size was small.