

## 1. Create dummy variables for categorical data before including in the model.

JASP automatically does this e.g. Feature\_name (Feature\_category) Sex(Male)

Coefficients ▼

Model		Estimate	Standard Error	Standardized*	Odds Ratio	z	Wald Test			95% Confidence interval	
							Wald Statistic	df	p	Lower bound	Upper bound
M <sub>0</sub>	(Intercept)	0.053	0.062	0.053	1.054	0.843	0.711	1	0.399	-0.070	0.175
M <sub>1</sub>	(Intercept)	6.678	2.428	6.310	794.340	2.750	7.561	1	0.006	1.918	11.437
	age	0.027	0.014	0.244	1.027	1.924	3.704	1	0.054	-0.000	0.054
	resting_blood_pressure	-0.025	0.007	-0.438	0.975	-3.821	14.600	1	< .001	-0.038	-0.012
	cholesterol	-0.005	0.002	-0.282	0.995	-2.367	5.604	1	0.018	-0.010	-0.001
	Max_heart_rate	0.022	0.007	0.499	1.022	3.324	11.051	1	< .001	0.009	0.034
	oldpeak	-0.403	0.132	-0.474	0.668	-3.053	9.318	1	0.002	-0.662	-0.144
	sex (Male)	-1.992	0.314	-1.992	0.136	-6.341	40.208	1	< .001	-2.608	-1.377

## 2. Generate and discuss the following:

-Table of coefficients with odds ratios and associated p-values.

Backward pass and Forward pass give high p value (fail to reject H<sub>0</sub>) while Enter method reject H<sub>0</sub>

H<sub>0</sub>: Fits the data just as well as the more complex model

H<sub>1</sub>: M<sub>1</sub> is better model

## Backward

Model Summary - target ▼

Model	Deviance	AIC	BIC	df	$\Delta X^2$	p	McFadden R <sup>2</sup>	Nagelkerke R <sup>2</sup>	Tjur R <sup>2</sup>	Cox & Snell R <sup>2</sup>
M <sub>0</sub>	606.815	652.815	766.261	1002			0.000	0.000	0.641	0.000
M <sub>1</sub>	608.244	652.244	760.758	1003	1.429	0.232	-0.002	-0.003	0.640	-0.001
M <sub>2</sub>	612.009	652.009	750.658	1005	3.765	0.152	-0.008	-0.011	0.638	-0.005

## Forward

Model Summary - target ▼

Model	Deviance	AIC	BIC	df	$\Delta X^2$	p	McFadden R <sup>2</sup>	Nagelkerke R <sup>2</sup>	Tjur R <sup>2</sup>	Cox & Snell R <sup>2</sup>
M <sub>0</sub>	1420.240	1422.240	1427.173	1024			0.000		0.000	
M <sub>1</sub>	1123.995	1131.995	1151.724	1021	296.246	< .001	0.209	0.335	0.274	0.251
M <sub>2</sub>	933.739	949.739	989.199	1017	190.255	< .001	0.343	0.504	0.410	0.378
M <sub>3</sub>	777.967	799.967	854.224	1014	155.773	< .001	0.452	0.621	0.530	0.466
M <sub>4</sub>	714.041	740.041	804.162	1012	63.926	< .001	0.497	0.664	0.575	0.498
M <sub>5</sub>	678.727	706.727	775.781	1011	35.314	< .001	0.522	0.687	0.595	0.515
M <sub>6</sub>	655.001	685.001	758.988	1010	23.725	< .001	0.539	0.702	0.612	0.526
M <sub>7</sub>	640.753	672.753	751.672	1009	14.248	< .001	0.549	0.710	0.621	0.533
M <sub>8</sub>	628.941	662.941	746.792	1008	11.813	< .001	0.557	0.717	0.629	0.538
M <sub>9</sub>	621.017	657.017	745.801	1007	7.923	0.005	0.563	0.722	0.633	0.541
M <sub>10</sub>	615.217	653.217	746.934	1006	5.800	0.016	0.567	0.726	0.635	0.544
M <sub>11</sub>	612.009	652.009	750.658	1005	3.208	0.073	0.569	0.727	0.638	0.545

## Enter

Model Summary - target ▼

Model	Deviance	AIC	BIC	df	$\Delta X^2$	p	McFadden R <sup>2</sup>	Nagelkerke R <sup>2</sup>	Tjur R <sup>2</sup>	Cox & Snell R <sup>2</sup>
M <sub>0</sub>	1420.240	1422.240	1427.173	1024			0.000		0.000	
M <sub>1</sub>	606.815	652.815	766.261	1002	813.425	< .001	0.573	0.731	0.641	0.548

Note. M<sub>1</sub> includes age, resting\_blood\_pressure, cholesterol, Max\_heart\_rate, oldpeak, sex, chest\_pain\_type, fasting\_blood\_sugar, rest\_ecg, exercise\_induced\_angina, slope, vessels\_colored\_by\_flourosopy, thalassemia

For this model we'll use the following as reference for each feature (will be dropped to avoid collinearity)

Feature	Reference (to be drop)
Sex	Female
Chest_pain	Asymptomatic
Fasting	Greater than 120mg
Rest_ecg	Normal
Exercise_induced	No
Slope	Flat
Flouroscopy	Four
Thalassemia	Normal

Coefficients

Model		Estimate	Standard Error	Standardized*	Odds Ratio	z	Wald Test		
							Wald Statistic	df	p
M <sub>0</sub>	(Intercept)	0.053	0.062	0.053	1.054	0.843	0.711	1	0.399
M <sub>1</sub>	(Intercept)	6.475	1.891	6.107	648.582	3.424	11.724	1	< .001
	age	0.027	0.014	0.244	1.027	1.924	3.704	1	0.054
	resting_blood_pressure	-0.025	0.007	-0.438	0.975	-3.821	14.600	1	< .001
	cholesterol	-0.005	0.002	-0.282	0.995	-2.367	5.604	1	0.018
	Max_heart_rate	0.022	0.007	0.499	1.022	3.324	11.051	1	< .001
	oldpeak	-0.403	0.132	-0.474	0.668	-3.053	9.318	1	0.002
	sex (Male)	-1.992	0.314	-1.992	0.136	-6.341	40.208	1	< .001
	chest_pain_type (Atypical angina)	-1.523	0.442	-1.523	0.218	-3.450	11.903	1	< .001
	chest_pain_type (Non-anginal pain)	-0.403	0.383	-0.403	0.668	-1.052	1.106	1	0.293
	chest_pain_type (Typical angina)	-2.410	0.392	-2.410	0.090	-6.148	37.795	1	< .001
	fasting_blood_sugar (Lower than 120 mg/ml)	-0.380	0.320	-0.380	0.684	-1.189	1.414	1	0.234
	rest_ecg (Left ventricular hypertrophy)	-0.800	1.537	-0.800	0.449	-0.521	0.271	1	0.603
	rest_ecg (ST-T wave abnormality)	0.397	0.218	0.397	1.488	1.823	3.322	1	0.068
	exercise_induced_angina (Yes)	-0.750	0.249	-0.750	0.472	-3.016	9.099	1	0.003
	slope (Downsloping)	1.395	0.272	1.395	4.036	5.133	26.345	1	< .001
	slope (Upsloping)	0.596	0.472	0.596	1.814	1.262	1.592	1	0.207
	vessels_colored_by_flourosopy (One)	-3.900	0.966	-3.900	0.020	-4.036	16.288	1	< .001
	vessels_colored_by_flourosopy (Three)	-3.854	1.055	-3.854	0.021	-3.651	13.333	1	< .001
	vessels_colored_by_flourosopy (Two)	-5.163	1.052	-5.163	0.006	-4.908	24.092	1	< .001
	vessels_colored_by_flourosopy (Zero)	-1.566	0.930	-1.566	0.209	-1.683	2.833	1	0.092
	thalassemia (Fixed Defect)	-0.392	0.442	-0.392	0.676	-0.888	0.788	1	0.375
	thalassemia (No)	-2.797	1.466	-2.797	0.061	-1.908	3.639	1	0.056
	thalassemia (Reversible Defect)	-1.806	0.436	-1.806	0.164	-4.145	17.182	1	< .001

Note. target level '1' coded as class 1.

\* Standardized estimates represent estimates where the continuous predictors are standardized (X-standardization).

Based from the Coefficients

**H0: Feature has no effect on the outcome**

**H1: Feature does have effect**

Feature	Insights
age	Age has 2.7% increase in odds of having disease although Age has 0.054 p value, we'll consider it due medical field where age has positive correlation with heart diseases
resting_blood_pressure	is associated with a 2.5% decrease in odds of disease
cholesterol	Higher cholesterol slightly decreases odds by 0.5% per unit this should be reviewed since it does not make sense that a high cholesterol is better hence greater than 5% p value
Max_heart_rate	Each additional unit increases the odds by 2.2%. With a p value less than 5% means this feature have an effect in determining if a patient have disease
oldpeak	Higher oldpeak slightly decreases odds by 33% per unit this should be reviewed since it

	does not make sense that a high oldpleak is better hence greater than 5% p value.
sex (Male)	The odds of having heart disease for Male is lower 13.6% compared to women 86.4%
chest_pain_type	Atypical and Typical angina significantly lower odds compared to Asymptomatic (Reference)
fasting_blood_sugar (Lower than 120 mg/ml)	Has lower odds of having (32%) disease vs 68% of greater than 120mg/ml fasting blood sugar. But has greater than 5% p val meaning we have weak evidence to tell if this is by chance or not (small dataset)
rest_ecg (LVH)	About 55% lower odds of heart disease compared to those with a normal ECG, but this is not statistically significant high p val. So, no strong evidence LVH is associated with heart disease risk in this model.
rest_ecg (ST-T wave abnormality)	About 49% higher odds of heart disease compared to those with a normal ECG. High p value also so no strong evidence with heart disease for this dataset
exercise_induced_angina (Yes)	About 53% lower odds of having heart disease compared to those without exercise-induced angina (No). With p val lower than 5%, exercise-induced angina is associated with lower odds of heart disease in this model.
slope (Downsloping)	odds ratio of 4.036 indicates that patients with a downsloping slope have about 4 times higher odds of having heart disease. P val less than 5% means this is significant.
slope (Upsloping)	odds ratio of 1.814 suggests these patients have about 1.8 times higher odds of heart disease relative to the reference. With high p value the evidence is not strong enough
vessels_colored_by_flourosopy vs Four	<p>having 1, 2, or 3 vessels colored is associated with much lower odds (0.006) of heart disease compared to 4 vessels.</p> <p>Zero vessels also seem to have lower odds, but this result is not quite statistically significant but is insignificant since it has high p val.</p>

thalassemia (Fixed Defect)	about 32.4% lower odds of having heart disease compared to Normal thalassemia. difference is not statistically significant high p val
thalassemia (No)	about 93.9% lower odds of heart disease compared to normal thalassemia. With p val close to 5% we can say that this is significant
thalassemia (Reversible Defect)	about 83.6% lower odds of having heart disease compared to normal thalassemia patients low p val meaning there is strong evidence in this dataset that this feature has lower odds compared to Normal thalassemia

Based from the dataset a Higher max heart rate, slop(downslaping) and rest\_ecg (ST-T wave abnormality) increases the odds of heart disease, while higher resting blood pressure, cholesterol, and oldpeak decreased the odds (might need further investigation because some metrics are inverse of real-life application). Males, those with typical or atypical angina, and patients with multiple-colored vessels and reversible thalassemia defects also had lower odds compared to female counter parts.

**-Model evaluation metrics such as accuracy, precision, recall, and other metrics.**

### Performance Diagnostics

#### Confusion matrix

Observed	Predicted		% Correct
	0	1	
0	420	79	84.168
1	42	484	92.015
Overall % Correct			88.195

Note. The cut-off value is set to 0.5

#### Performance metrics

	Value
Accuracy	0.882
AUC	0.946
Sensitivity	0.920
Specificity	0.842
Precision	0.860
F-measure	0.889
Brier score	0.087
H-measure	0.707

Since this is for medical application, the best metric here would be **sensitivity** or true positive rate it's best to capture actual positive patients.

<b>True Positives (TP) = 484</b>
<b>True Negatives (TN) = 420</b>
<b>False Positives (FP) = 79</b>
<b>False Negatives (FN) = 42</b>

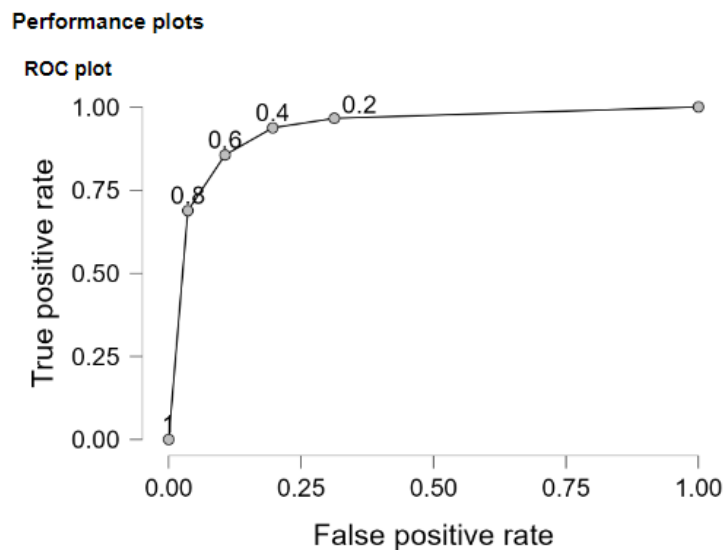
## Odds ratio

$$TP * TN / FP * FN =$$

$$484 * 420 / 79 * 42 = 61.27$$

The odds of the model correctly predict (true positive or true negative) are 61.27 times higher than the odds of an incorrect prediction (false positive or false negative).

## ROC curve.



## Thresholds

0.8 – Low false positives but will miss many positives

0.6 – trade-off between sensitivity/specificity

**0.4** – Has more positives but an increase in false positives

0.2 – highest positives detected but has more false positives

**For medical application we choose 0.4 Threshold for screening cases while 0.2 for high-risk population**

**With a AUC score of 94.6 the model distinguishes the classes well**

- High TPR (Sensitivity = 0.920)
- Low FPR (1 - Specificity = 0.158)