

HW4 P5

#2

File "rv2.dat" has radial velocities with a period of

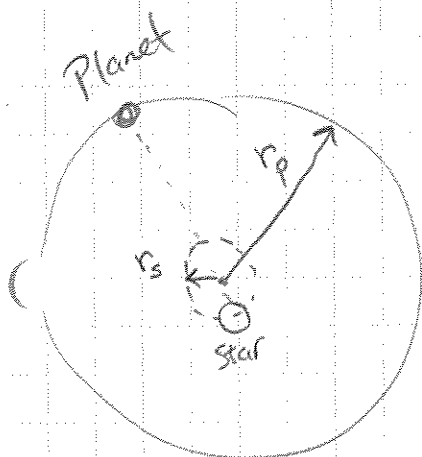
$$P = 4.627669 \text{ days}$$

See Fig 6, and Winn et al., AJ 141, 63 (2011). If we assume the star has mass $1 M_{\odot}$, and also assume

$$M_p \ll M_s = 1 M_{\odot}$$

then we can find orbital radius like so.

- first, use maximum speed of star to compute radius of star's motion around center of mass



$$r_s = \frac{v_{\max} \cdot P}{2\pi} = \frac{(210 \frac{\text{m}}{\text{s}})(399,800 \text{ s})}{2\pi} = 1.336 \times 10^7 \text{ m}$$

- next, use Kepler's 3rd Law to find separation a

$$P^2 = a^3 \quad \text{since we assume } M_s = M_{\odot}$$

in years in AU

$$\rightarrow a = 8.13 \times 10^9 \text{ m} = 0.054 \text{ AU}$$

$$\text{- now, } a = r_s + r_p \rightarrow r_p = a - r_s$$

and center of mass tells us

$$\frac{M_p}{M_s} = \frac{r_s}{r_p} = \frac{r_s}{a - r_s}$$

Pb
HW 4
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So

$$\begin{aligned} M_p &= M_s \left(\frac{r_s}{a - r_s} \right) \\ &= 1 M_\odot \left(\frac{1.336 \times 10^7 \text{ m}}{8.13 \times 10^9 \text{ m} - 1.336 \times 10^7 \text{ m}} \right) \\ &= 1.65 \times 10^{-3} M_\odot \end{aligned}$$

$$M_p = 1.7 M_J$$

and

$$\begin{aligned} a &= 8.13 \times 10^9 \text{ m} \\ r_p &= 8.12 \times 10^9 \text{ m} \end{aligned}$$

Bonus: HAT P-14b

HAT P14 with period 4.627669 days; Winn et al., AJ 141, 63 (2011)

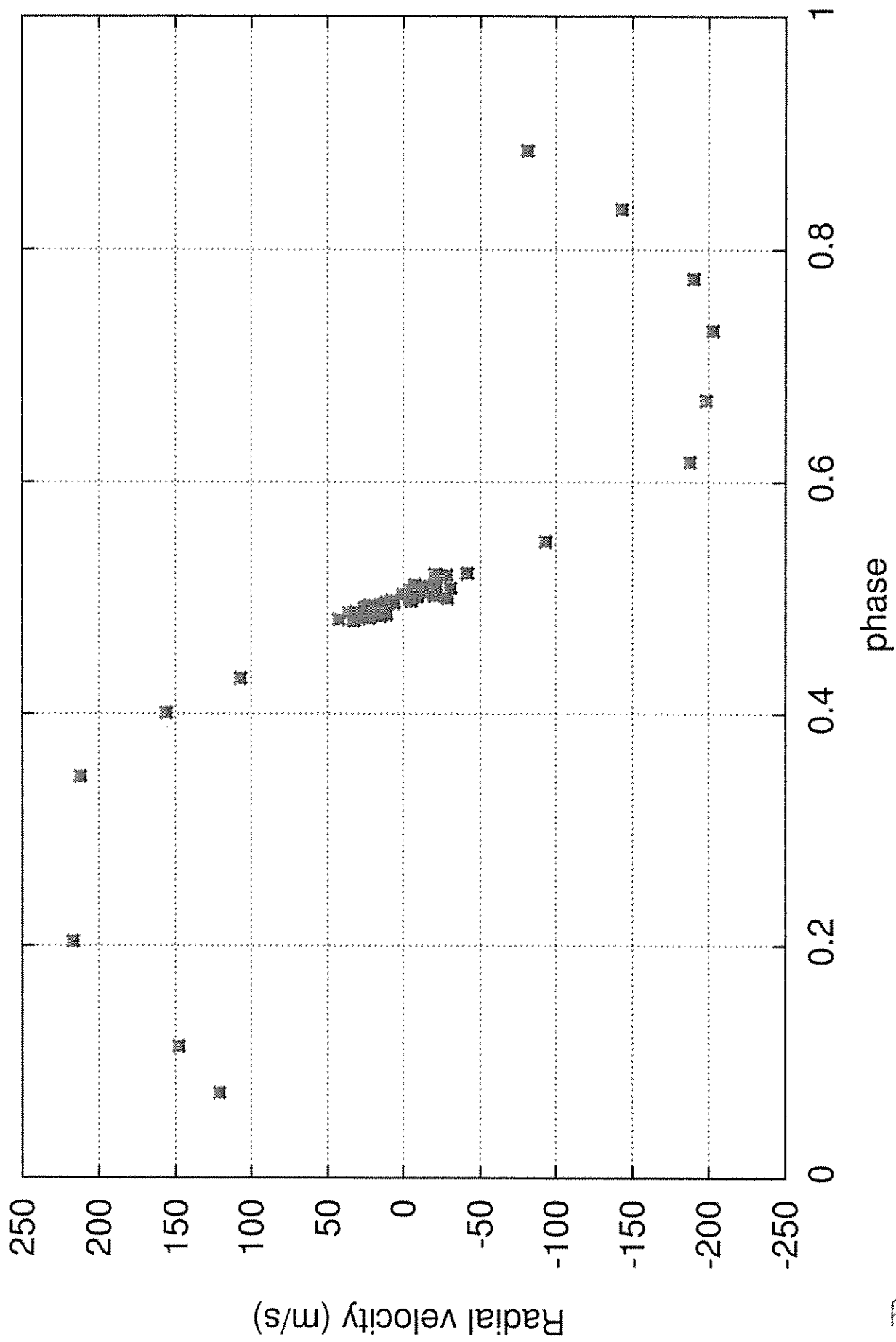


Fig 6
4/4(2015)