

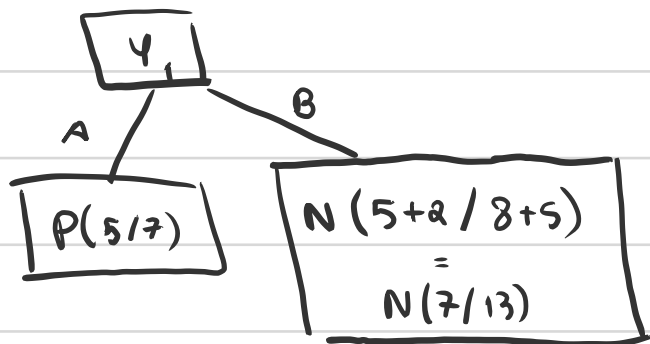
1)

	real	
	P	N
P	5+3	2+2
N	3	5

=

	real	
	P	N
P	8	4
N	3	5

2) Pruning (depth = 1)



CM:

	real	
	P	N
P	5 <sup>TP</sup>	2 <sup>FP</sup>
N	0 <sup>FN</sup>	7 <sup>TN</sup>

$$F1 = \frac{2 P_{rec} S_{em}}{P_{rec} + S_{em}} = \frac{2 \cdot \frac{5}{7} \cdot \frac{5}{11}}{\frac{5}{7} + \frac{5}{11}} = \frac{5}{9}$$

$$S_{em} = \frac{TP}{TP+FN} = \frac{5}{5+0} = \frac{5}{5}$$

$$P_{rec} = \frac{TP}{TP+FP} = \frac{5}{5+2} = \frac{5}{7}$$

3) Two reasons that can justify why the left path was not further decomposed are:

- To avoid overfitting, because exploring the left path would make the model adapted to the training data.
- All the observations of  $y_1 = A$  lead to  $y_{out} = P$ .

$$4) IG(y_{out} | y_1) = I(y_{out}) - E(y_{out} | y_1)$$

	P	N
$y_{out}$	12	8

= 20  $\Rightarrow P(y_{out} = P) = \frac{3}{5}$   
 $P(y_{out} = N) = \frac{2}{5}$

$$I(y_{out}) = -\left[\frac{3}{5} \log\left(\frac{3}{5}\right) + \frac{2}{5} \log\left(\frac{2}{5}\right)\right] \approx 0.97$$

$$E(y_{out} | y_1) = \frac{7}{20} I(y_{out} | y_1 = A) + \frac{13}{20} I(y_{out} | y_1 = B)$$

$$= \frac{7}{20} (0) + \frac{13}{20} \cdot \left(\frac{8}{13} \log\left(\frac{8}{13}\right) + \frac{5}{13} \log\left(\frac{5}{13}\right)\right)$$

$$\approx \frac{13}{20} \cdot -0.9612 \approx -0.6248$$

$$IG(y_{out} | y_1) = I(y_{out}) - E(y_{out} | y_1) = 0.97 + 0.6248 = 1.5948$$

## Pig. de testes

\* Caso 3) estive bem #

- The information gain on the right path was greater than on the left one;

Testes "simulados" Tabela  
Não vai ser a ideia

$y_1$	$y_2$	$y_{out}$
A	1	P
B	4	N
A	3	P
B	5	N
B	2	P
A	3	N
B	4	N
A	1	P