

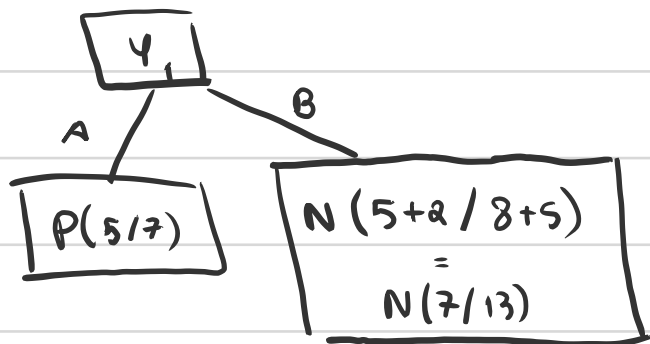
1)

	real	
	P	N
P	5+3	2+2
N	3	5

 $=$

	real	
	P	N
P	8	4
N	3	5

2) Pruning (depth = 1)



CM:

	real	
	P	N
P	5 ^{TP}	2 ^{FP}
N	0 ^{FN}	7 ^{TN}

$$F1 = \frac{2 \text{Prec} \cdot \text{Sum}}{\text{Prec} + \text{Sum}} = \frac{2 \cdot \frac{5}{7} \cdot \frac{5}{11}}{\frac{5}{7} + \frac{5}{11}} = \frac{5}{9}$$

$$\text{Sum} = \frac{TP}{TP+FN} = \frac{5}{5+0} = \frac{5}{5}$$

$$\text{Prec} = \frac{TP}{TP+FP} = \frac{5}{5+2} = \frac{5}{7}$$

3) Two reasons that can justify why the left path was not further decomposed are:

- To avoid overfitting, because exploring the left path would make the model adapted to the training data.
- All the observations of $y_1 = A$ lead to $y_{out} = P$.

$$4) IG(y_{out} | y_1) = I(y_{out}) - E(y_{out} | y_1)$$

	P	N
y_{out}	$5+3+(8-5) = 11$	$5+(7-5)+(5-3) = 9$

 $\Rightarrow P(y_{out} = P) = 11/20$
 $P(y_{out} = N) = 9/20$

$$I(y_{out}) = -\left[\frac{11}{20} \log_2\left(\frac{11}{20}\right) + \frac{9}{20} \log_2\left(\frac{9}{20}\right)\right] \approx 0.992774454$$

$$E(y_{out} | y_1) = \frac{7}{20} I(y_{out} | y_1 = A) + \frac{13}{20} I(y_{out} | y_1 = B)$$

$$= -\frac{7}{20} \left(\frac{5}{7} \log_2 \frac{5}{7} + \frac{2}{7} \log_2 \frac{2}{7}\right) - \frac{13}{20} \left(\frac{7}{13} \log_2 \frac{7}{13} + \frac{6}{13} \log_2 \frac{6}{13}\right) \approx 0.949315$$

$$IG(y_{out} | y_1) = I(y_{out}) - E(y_{out} | y_1) \approx 0.992774454 - 0.949315 = 0.043459$$

Pig. de test

* Caso 3) este vine bene *

- The information gain on the right path was greater than on the left one;

Testul "nimic" Tabelă
Nu există a doua

y_1	y_2	y_{out}
A	1	P
B	4	N
A	3	P
B	5	N
B	2	P
A	3	N
B	4	N
A	1	P

$$IG_{\text{left}} = 0.043594...$$

$$E_{\text{before}} = 0.948746$$

$$E_{\text{after}} = 0.949353$$